The Parma Polyhedra Library C Language Interface User's Manual* (version 0.10)

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CONTENTS

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Contents

1	Main I	cage control of the c	J
2	GNU (General Public License	2
3	GNU I	Free Documentation License	12
4	Modul	e Index	17
	4.1 N	Modules	17
5	Class I	[ndex	17
	5.1 C	Class List	17
6	Modul	e Documentation	18
	6.1 C	C Language Interface	18
	6.2 L	ibrary Initialization and Finalization	18
	6.3 V	Version Checking	19
	6.4 E	Error Handling	21
	6.5 L	aibrary Datatypes	22
7	Class I	Documentation	27
	7.1 p	pl_Coefficient_tag Interface Reference	27
	7.2 p	pl_Congruence_System_const_iterator_tag Interface Reference	29
	7.3 p	pl_Congruence_System_tag Interface Reference	30
	7.4 p	pl_Congruence_tag Interface Reference	31

1 Main Page

7.5	ppl_Constraint_System_const_iterator_tag Interface Reference	33
7.6	ppl_Constraint_System_tag Interface Reference	34
7.7	ppl_Constraint_tag Interface Reference	36
7.8	ppl_Generator_System_const_iterator_tag Interface Reference	37
7.9	ppl_Generator_System_tag Interface Reference	38
7.10	ppl_Generator_tag Interface Reference	40
7.11	ppl_Grid_Generator_System_const_iterator_tag Interface Reference	42
7.12	ppl_Grid_Generator_System_tag Interface Reference	43
7.13	ppl_Grid_Generator_tag Interface Reference	44
7.14	ppl_Linear_Expression_tag Interface Reference	46
7.15	ppl_MIP_Problem_tag Interface Reference	48
7.16	ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag Interface Reference	52
7.17	ppl_Pointset_Powerset_C_Polyhedron_iterator_tag Interface Reference	54
7.18	ppl_Pointset_Powerset_C_Polyhedron_tag Interface Reference	55
7.19	ppl Polyhedron tag Interface Reference	57

1 Main Page

All the declarations needed for using the PPL's C interface (preprocessor symbols, data types, variables and functions) are collected in the header file ppl_c.h. This file, which is designed to work with pre-ANSI and ANSI C compilers as well as C99 and C++ compilers, should be included, either directly or via some other header file, with the directive

```
#include <ppl_c.h>
```

If this directive does not work, then your compiler is unable to find the file ppl_c.h. So check that the library is installed (if it is not installed, you may want to make install, perhaps with root privileges) in the right place (if not you may want to reconfigure the library using the appropriate pathname for the -prefix option); and that your compiler knows where it is installed (if not you should add the path to the directory where ppl_c.h is located to the compiler's include file search path; this is usually done with the -I option).

The name space of the PPL's C interface is PPL_* for preprocessor symbols, enumeration values and variables; and ppl_* for data types and function names. The interface systematically uses *opaque data types* (generic pointers that completely hide the internal representations from the client code) and provides all required access functions. By using just the interface, the client code can exploit all the functionalities of the library yet avoid directly manipulating the library's data structures. The advantages are that (1) applications do not depend on the internals of the library (these may change from release to release), and (2) the interface invariants can be thoroughly checked (by the access functions).

The PPL's C interface is initialized by means of the ppl_initialize function. This function must be called *before using any other interface of the library*. The application can release the resources allocated by the library by calling the ppl_finalize function. After this function is called *no other interface of the library may be used* until the interface is re-initialized using ppl_initialize.

Any application using the PPL should make sure that only the intended version(s) of the library are ever used. The version used can be checked at compile-time thanks to the macros PPL_VERSION_MAJOR,

PPL_VERSION_MINOR, PPL_VERSION_REVISION and PPL_VERSION_BETA, which give, respectively major, minor, revision and beta numbers of the PPL version. This is an example of their use:

```
#if PPL_VERSION_MAJOR == 0 && PPL_VERSION_MINOR < 6
# error "PPL version 0.6 or following is required"
#endif</pre>
```

Compile-time checking, however, is not normally enough, particularly in an environment where there is dynamic linking. Run-time checking can be performed by means of the functions ppl_version_major, ppl_version_minor, ppl_version_revision, and ppl_version_beta. The PPL's C interface also provides functions ppl_version, returning character string containing the full version number, and ppl_banner, returning a string that, in addition, provides (pointers to) other useful information for the library user.

All programs using the PPL's C interface must link with the following libraries: <code>libppl_c</code> (PPL's C interface), <code>libppl</code> (PPL's core), <code>libgmpxx</code> (GMP's C++ interface), and <code>libgmp</code> (GMP's library core). On most Unix-like systems, this is done by adding <code>-lppl_c</code>, <code>-lppl</code>, <code>-lgmpxx</code>, and <code>-lgmp</code> to the compiler's or linker's command line. For example:

```
gcc myprogram.o -lppl_c -lppl -lgmpxx -lgmp
```

If this does not work, it means that your compiler/linker is not finding the libraries where it expects. Again, this could be because you forgot to install the library or you installed it in a non-standard location. In the latter case you will need to use the appropriate options (usually -L) and, if you use shared libraries, some sort of run-time path selection mechanisms. Consult your compiler's documentation for details. Notice that the PPL is built using Libtool and an application can exploit this fact to significantly simplify the linking phase. See Libtool's documentation for details. Those working under Linux can find a lot of useful information on how to use program libraries (including static, shared, and dynamically loaded libraries) in the Program Library HOWTO.

For examples on how to use the functions provided by the C interface, you are referred to the directory demos/ppl_lpsol/ in the source distribution. It contains a *Mixed Integer (Linear) Programming* solver written in C. In order to use this solver you will need to install GLPK (the GNU Linear Programming Kit): this is used to read linear programs in MPS format.

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4 Module Index 17

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4 Module Index

4.1 Modules

Here is a list of all modules:

C Language Interface	
Library Initialization and Finalization	18
Version Checking	19
Error Handling	21
Library Datatypes	22

5 Class Index

5.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

```
ppl_Coefficient_tag (Types and functions for coefficients )
                                                                                          27
ppl_Congruence_System_const_iterator_tag (Types and functions for iterating on congru-
   ence systems)
                                                                                          29
ppl_Congruence_System_tag (Types and functions for congruence systems )
                                                                                          30
ppl_Congruence_tag (Types and functions for congruences )
                                                                                          31
ppl_Constraint_System_const_iterator_tag (Types and functions for iterating on constraint
   systems)
                                                                                          33
ppl_Constraint_System_tag (Types and functions for constraint systems )
                                                                                          34
ppl_Constraint_tag (Types and functions for constraints )
                                                                                          36
```

6 Module Documentation 18

<pre>ppl_Generator_System_const_iterator_tag (Types and functions for iterating on generator systems)</pre>	37
ppl_Generator_System_tag (Types and functions for generator systems)	38
<pre>ppl_Generator_tag (Types and functions for generators)</pre>	40
<pre>ppl_Grid_Generator_System_const_iterator_tag (Types and functions for iterating on grid generator systems)</pre>	42
ppl_Grid_Generator_System_tag (Types and functions for grid generator systems)	43
<pre>ppl_Grid_Generator_tag (Types and functions for grid generators)</pre>	44
ppl_Linear_Expression_tag (Types and functions for linear expressions)	46
ppl_MIP_Problem_tag (Types and functions for MIP problems)	48
$\begin{array}{c} ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag \ (Types \ and \ functions \ for \ iterating \\ on \ the \ disjuncts \ of \ a \ const \ ppl_Pointset_Powerset_C_Polyhedron_tag \) \end{array}$	52
$\label{lem:ppl_Pointset_Powerset_C_Polyhedron_iterator_tag} \ (Types \ and \ functions \ for \ iterating \ on \ the \ disjuncts \ of \ a \ ppl_Pointset_Powerset_C_Polyhedron_tag \)$	54
$\begin{array}{c} \textbf{ppl_Pointset_Powerset_C_Polyhedron_tag} \ (Types \ and \ functions \ for \ the \ Pointset_Powerset \ of \\ C_Polyhedron \ objects \) \end{array}$	55
ppl_Polyhedron_tag (Types and functions for the domains of C and NNC convex polyhedra)	57

6 Module Documentation

6.1 C Language Interface

The Parma Polyhedra Library comes equipped with an interface for the C language.

6.2 Library Initialization and Finalization

Functions

- int ppl_initialize (void)

 Initializes the Parma Polyhedra Library. This function must be called before any other function.
- int ppl_finalize (void)

 Finalizes the Parma Polyhedra Library. This function must be called after any other function.
- int ppl_set_rounding_for_PPL (void)

 Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.
- int ppl_restore_pre_PPL_rounding (void)

 Sets the FPU rounding mode as it was before initialization of the PPL.

6.2.1 Detailed Description

Functions for initialization/finalization of the library, as well as setting/resetting of floating-point rounding mode.

6.2.2 Function Documentation

6.2.2.1 int ppl_initialize (void)

Initializes the Parma Polyhedra Library. This function must be called before any other function.

Returns:

PPL ERROR INVALID ARGUMENT if the library was already initialized.

6.2.2.2 int ppl_finalize (void)

Finalizes the Parma Polyhedra Library. This function must be called after any other function.

Returns:

PPL_ERROR_INVALID_ARGUMENT if the library was already finalized.

6.2.2.3 int ppl_set_rounding_for_PPL (void)

Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.

This is performed automatically at initialization-time. Calling this function is needed only if restore_pre_-PPL_rounding() has been previously called.

6.2.2.4 int ppl_restore_pre_PPL_rounding (void)

Sets the FPU rounding mode as it was before initialization of the PPL.

After calling this function it is absolutely necessary to call set_rounding_for_PPL() before using any PPL abstractions based on floating point numbers. This is performed automatically at finalization-time.

6.3 Version Checking

Defines

- #define PPL_VERSION "0.10"
 A string containing the PPL version.
- #define PPL_VERSION_MAJOR 0
 The major number of the PPL version.
- #define PPL_VERSION_MINOR 10

 The minor number of the PPL version.
- #define PPL_VERSION_REVISION 0
 The revision number of the PPL version.

• #define PPL_VERSION_BETA 0

The beta number of the PPL version. This is zero for official releases and nonzero for development snapshots.

Functions

- int ppl_version_major (void)

 Returns the major number of the PPL version.
- int ppl_version_minor (void)

 Returns the minor number of the PPL version.
- int ppl_version_revision (void)

 Returns the revision number of the PPL version.
- int ppl_version_beta (void)

 Returns the beta number of the PPL version.
- int ppl_version (const char **p)

 Writes to *p a pointer to a character string containing the PPL version.
- int ppl_banner (const char **p)

 Writes to *p a pointer to a character string containing the PPL banner.

6.3.1 Detailed Description

Symbolic constants and functions related to library version checking.

6.3.2 Define Documentation

6.3.2.1 #define PPL_VERSION "0.10"

A string containing the PPL version.

Let M and m denote the numbers associated to PPL_VERSION_MAJOR and PPL_VERSION_MINOR, respectively. The format of PPL_VERSION is M "." m if both PPL_VERSION_REVISION (r) and PPL_VERSION_BETA (b)are zero, M "." m "pre" b if PPL_VERSION_REVISION is zero and PPL_VERSION_BETA is not zero, M "." m "." r if PPL_VERSION_REVISION is not zero and PPL_VERSION_BETA is zero, M "." m "." r "pre" b if neither PPL_VERSION_REVISION nor PPL_VERSION_BETA are zero.

6.3.3 Function Documentation

6.3.3.1 int ppl_banner (const char **p)

Writes to *p a pointer to a character string containing the PPL banner.

The banner provides information about the PPL version, the licensing, the lack of any warranty whatsoever, the C++ compiler used to build the library, where to report bugs and where to look for further information.

6.4 Error Handling 21

6.4 Error Handling

Enumerations

• enum ppl_enum_error_code {

PPL_ERROR_OUT_OF_MEMORY, PPL_ERROR_INVALID_ARGUMENT, PPL_ERROR_DOMAIN_ERROR, PPL_ERROR_LENGTH_ERROR,

PPL_ARITHMETIC_OVERFLOW, PPL_STDIO_ERROR, PPL_ERROR_INTERNAL_ERROR, PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION,

PPL_ERROR_UNEXPECTED_ERROR }

Defines the error codes that any function may return.

Functions

• int ppl_set_error_handler (void(*h)(enum ppl_enum_error_code code, const char *description))

Installs the user-defined error handler pointed at by h.

6.4.1 Detailed Description

Symbolic constants and functions related to error reporting/handling.

6.4.2 Enumeration Type Documentation

6.4.2.1 enum ppl_enum_error_code

Defines the error codes that any function may return.

Enumerator:

- PPL_ERROR_OUT_OF_MEMORY The virtual memory available to the process has been exhausted
- PPL ERROR INVALID ARGUMENT A function has been invoked with an invalid argument.
- PPL_ERROR_DOMAIN_ERROR A function has been invoked outside its domain of definition.
- **PPL_ERROR_LENGTH_ERROR** The construction of an object that would exceed its maximum permitted size was attempted.
- **PPL_ARITHMETIC_OVERFLOW** An arithmetic overflow occurred and the computation was consequently interrupted. This can *only* happen in library's incarnations using bounded integers as coefficients.
- **PPL_STDIO_ERROR** An error occurred during a C input/output operation. A more precise indication of what went wrong is available via erro.
- **PPL_ERROR_INTERNAL_ERROR** An internal error that was diagnosed by the PPL itself. This indicates a bug in the PPL.
- **PPL_ERROR_UNKNOWN_STANDARD_EXCEPTION** A standard exception has been raised by the C++ run-time environment. This indicates a bug in the PPL.
- **PPL_ERROR_UNEXPECTED_ERROR** A totally unknown, totally unexpected error happened. This indicates a bug in the PPL.

6.4.3 Function Documentation

6.4.3.1 int ppl_set_error_handler (void(*)(enum ppl_enum_error_code code, const char *description) h)

Installs the user-defined error handler pointed at by h.

The error handler takes an error code and a textual description that gives further information about the actual error. The C string containing the textual description is read-only and its existence is not guaranteed after the handler has returned.

6.5 Library Datatypes

Typedefs for the library datatypes and related symbolic constants.

Typedefs

- typedef size_t ppl_dimension_type

 An unsigned integral type for representing space dimensions.
- typedef const char * ppl_io_variable_output_function_type (ppl_dimension_type var)

 The type of output functions used for printing variables.
- typedef struct ppl_Coefficient_tag * ppl_Coefficient_t
 Opaque pointer.
- typedef struct ppl_Coefficient_tag const * ppl_const_Coefficient_t
 Opaque pointer to const object.
- typedef struct ppl_Linear_Expression_tag const * ppl_const_Linear_Expression_t
 Opaque pointer to const object.
- typedef struct ppl_Constraint_tag * ppl_Constraint_t
 Opaque pointer.
- typedef struct ppl_Constraint_tag const * ppl_const_Constraint_t
 Opaque pointer to const object.

typedef struct ppl_Constraint_System_const_iterator_tag const * ppl_const_Constraint_System_const_iterator_t

Opaque pointer to const object.

- typedef struct ppl_Generator_System_const_iterator_tag * ppl_Generator_System_const_iterator_t Opaque pointer.
- typedef struct ppl_Generator_System_const_iterator_tag const * ppl_const_Generator_System_-const_iterator_t

Opaque pointer to const object.

- typedef struct ppl_Congruence_System_const_iterator_tag * ppl_Congruence_System_const_iterator_t

Opaque pointer.

• typedef struct ppl_Congruence_System_const_iterator_tag const * ppl_const_Congruence_-System_const_iterator_t

Opaque pointer to const object.

- typedef struct ppl_Grid_Generator_System_tag * ppl_Grid_Generator_System_t

Opaque pointer.

- typedef struct ppl_Grid_Generator_System_const_iterator_tag * ppl_Grid_Generator_System_const_iterator_t

Opaque pointer.

• typedef struct ppl_Grid_Generator_System_const_iterator_tag const * ppl_const_Grid_Generator_ System_const_iterator_t

Opaque pointer to const object.

- typedef struct ppl_MIP_Problem_tag * ppl_MIP_Problem_t Opaque pointer.

- typedef struct ppl_Polyhedron_tag const * ppl_const_Polyhedron_t

 Opaque pointer to const object.
- $\bullet \ \ typedef \ struct \ ppl_Pointset_Powerset_C_Polyhedron_tag * ppl_Pointset_Powerset_C_Polyhedron_t$

Opaque pointer.

• typedef struct ppl_Pointset_Powerset_C_Polyhedron_tag const * ppl_const_Pointset_Powerset_C_-Polyhedron_t

Opaque pointer to const object.

• typedef struct ppl_Pointset_Powerset_C_Polyhedron_iterator_tag * ppl_Pointset_Powerset_C_-Polyhedron_iterator_t

Opaque pointer.

• typedef struct ppl_Pointset_Powerset_C_Polyhedron_iterator_tag const * ppl_const_Pointset_-Powerset_C_Polyhedron_iterator_t

Opaque pointer to const object.

• typedef struct ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag * ppl_Pointset_Powerset_-C_Polyhedron_const_iterator_t

Opaque pointer.

• typedef struct ppl_Pointset_Powerset_C_Polyhedron_const_iterator_tag const * ppl_const_-Pointset_Powerset_C_Polyhedron_const_iterator_t

Opaque pointer to const object.

Enumerations

enum ppl_enum_Constraint_Type {
 PPL_CONSTRAINT_TYPE_LESS_THAN, PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL,
 PPL_CONSTRAINT_TYPE_EQUAL, PPL_CONSTRAINT_TYPE_GREATER_OR_EQUAL,
 PPL_CONSTRAINT_TYPE_GREATER_THAN }

Describes the relations represented by a constraint.

enum ppl_enum_Generator_Type { PPL_GENERATOR_TYPE_LINE, PPL_GENERATOR_TYPE_RAY, PPL_GENERATOR_TYPE_POINT, PPL_GENERATOR_TYPE_CLOSURE_POINT }

Describes the different kinds of generators.

enum ppl_enum_Grid_Generator_Type { PPL_GRID_GENERATOR_TYPE_LINE, PPL_GRID_GENERATOR_TYPE_PARAMETER, PPL_GRID_GENERATOR_TYPE_POINT }

Describes the different kinds of grid generators.

Functions

- int ppl_max_space_dimension (ppl_dimension_type *m)

 Writes to m the maximum space dimension this library can handle.
- int ppl_not_a_dimension (ppl_dimension_type *m)

 Writes to m a value that does not designate a valid dimension.
- int ppl_io_print_variable (ppl_dimension_type var)

 Pretty-prints var to stdout.
- int ppl_io_fprint_variable (FILE *stream, ppl_dimension_type var)

 Pretty-prints var to the given output stream.
- int ppl_io_set_variable_output_function (ppl_io_variable_output_function_type *p)

 Sets the output function to be used for printing variables to p.
- int ppl_io_get_variable_output_function (ppl_io_variable_output_function_type **pp)

 Writes a pointer to the current variable output function to pp.

Variables

- unsigned int PPL_COMPLEXITY_CLASS_POLYNOMIAL Code of the worst-case polynomial complexity class.
- unsigned int PPL_COMPLEXITY_CLASS_SIMPLEX
 Code of the worst-case exponential but typically polynomial complexity class.
- unsigned int PPL_COMPLEXITY_CLASS_ANY
 Code of the universal complexity class.

- unsigned int PPL_POLY_CON_RELATION_IS_DISJOINT
 - Individual bit saying that the polyhedron and the set of points satisfying the constraint are disjoint.
- unsigned int PPL_POLY_CON_RELATION_STRICTLY_INTERSECTS

Individual bit saying that the polyhedron intersects the set of points satisfying the constraint, but it is not included in it.

• unsigned int PPL POLY CON RELATION IS INCLUDED

Individual bit saying that the polyhedron is included in the set of points satisfying the constraint.

• unsigned int PPL_POLY_CON_RELATION_SATURATES

Individual bit saying that the polyhedron is included in the set of points saturating the constraint.

unsigned int PPL POLY GEN RELATION SUBSUMES

Individual bit saying that adding the generator would not change the polyhedron.

6.5.1 Detailed Description

Typedefs for the library datatypes and related symbolic constants.

The datatypes provided by the library should be manipulated by means of the corresponding opaque pointer types and the functions working on them.

Note:

To simplify the detection of common programming mistakes, we provide both pointer-to-const and pointer-to-nonconst opaque pointers, with implicit conversions mapping each pointer-to-nonconst to the corresponding pointer-to-const when needed. The user of the C interface is therefore recommended to adopt the pointer-to-const type whenever read-only access is meant.

6.5.2 Typedef Documentation

6.5.2.1 typedef const char* ppl_io_variable_output_function_type(ppl_dimension_type var)

The type of output functions used for printing variables.

An output function for variables must write a textual representation for var to a character buffer, null-terminate it, and return a pointer to the beginning of the buffer. In case the operation fails, 0 should be returned and perhaps errno should be set in a meaningful way. The library does nothing with the buffer, besides printing its contents.

6.5.3 Enumeration Type Documentation

6.5.3.1 enum ppl_enum_Constraint_Type

Describes the relations represented by a constraint.

Enumerator:

 $PPL_CONSTRAINT_TYPE_LESS_THAN$ The constraint is of the form e < 0. $PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL$ The constraint is of the form $e \le 0$.

7 Class Documentation 27

```
PPL\_CONSTRAINT\_TYPE\_EQUAL The constraint is of the form e=0. PPL\_CONSTRAINT\_TYPE\_GREATER\_OR\_EQUAL The constraint is of the form e\geq 0. PPL\_CONSTRAINT\_TYPE\_GREATER\_THAN The constraint is of the form e>0.
```

6.5.3.2 enum ppl_enum_Generator_Type

Describes the different kinds of generators.

Enumerator:

```
PPL_GENERATOR_TYPE_LINE The generator is a line.
PPL_GENERATOR_TYPE_RAY The generator is a ray.
PPL_GENERATOR_TYPE_POINT The generator is a point.
PPL_GENERATOR_TYPE_CLOSURE_POINT The generator is a closure point.
```

6.5.3.3 enum ppl_enum_Grid_Generator_Type

Describes the different kinds of grid generators.

Enumerator:

```
PPL_GRID_GENERATOR_TYPE_LINE The grid generator is a line.
PPL_GRID_GENERATOR_TYPE_PARAMETER The grid generator is a parameter.
PPL_GRID_GENERATOR_TYPE_POINT The grid generator is a point.
```

7 Class Documentation

7.1 ppl_Coefficient_tag Interface Reference

Types and functions for coefficients.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Coefficient (ppl_Coefficient_t *pc)

 Creates a new coefficient with value 0 and writes a handle for the newly created coefficient at address
 pc.
- int ppl_new_Coefficient_from_mpz_t (ppl_Coefficient_t *pc, mpz_t z)

 Creates a new coefficient with the value given by the GMP integer z and writes a handle for the newly created coefficient at address pc.
- int ppl_new_Coefficient_from_Coefficient (ppl_Coefficient_t *pc, ppl_const_Coefficient_t c)

Builds a coefficient that is a copy of c; writes a handle for the newly created coefficient at address pc.

- int ppl_assign_Coefficient_from_mpz_t (ppl_Coefficient_t dst, mpz_t z)

 Assign to dst the value given by the GMP integer z.
- int ppl_assign_Coefficient_from_Coefficient (ppl_Coefficient_t dst, ppl_const_Coefficient_t src)

 Assigns a copy of the coefficient src to dst.
- int ppl_delete_Coefficient (ppl_const_Coefficient_t c)

Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

Read-Only Accessor Functions

- int ppl_Coefficient_to_mpz_t (ppl_const_Coefficient_t c, mpz_t z)

 Sets the value of the GMP integer z to the value of c.
- int ppl_Coefficient_OK (ppl_const_Coefficient_t c)

Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

• int ppl_Coefficient_is_bounded (void)

Returns a positive integer if coefficients are bounded; returns 0 otherwise.

• int ppl_Coefficient_min (mpz_t min)

Returns a positive integer if coefficients are bounded, in which case min is set to their minimum value; returns 0 otherwise.

• int ppl_Coefficient_max (mpz_t max)

Returns a positive integer if coefficients are bounded, in which case max is set to their maximum value; returns 0 otherwise.

I/O Functions

- int ppl_io_print_Coefficient (ppl_const_Coefficient_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Coefficient (FILE *stream, ppl_const_Coefficient_t x)

 Prints x to the given output stream.

7.1.1 Detailed Description

Types and functions for coefficients.

The types and functions for coefficients provide an interface towards *Coefficient*. Depending on configuration, the PPL coefficients may be implemented by the unbounded precision integers provided by GMP (default), or by bounded precision integers (with checks for overflows).

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.2 ppl_Congruence_System_const_iterator_tag Interface Reference

Types and functions for iterating on congruence systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t *pcit)

Builds a new 'const iterator' and writes a handle to it at address poit.

• int ppl_new_Congruence_System_const_iterator_from_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t *pcit, ppl_const_Congruence_System_const_iterator_t cit)

Builds a const iterator that is a copy of cit; writes an handle for the newly created const iterator at address pcit.

• int ppl_assign_Congruence_System_const_iterator_from_Congruence_System_const_iterator (ppl_Congruence_System_const_iterator_t dst, ppl_const_Congruence_System_const_iterator_t src)

Assigns a copy of the const iterator src to dst.

• int ppl_delete_Congruence_System_const_iterator (ppl_const_Congruence_System_const_iterator_t cit)

Invalidates the handle cit: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

• int ppl_Congruence_System_const_iterator_dereference (ppl_const_Congruence_System_const_iterator_t cit, ppl_const_Congruence_t *pc)

Dereference cit writing a const handle to the resulting congruence at address pc.

• int ppl_Congruence_System_const_iterator_increment (ppl_Congruence_System_const_iterator_t cit)

Increment cit so that it "points" to the next congruence.

• int ppl_Congruence_System_const_iterator_equal_test (ppl_const_Congruence_System_const_iterator_t x, ppl_const_Congruence_System_const_iterator_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.2.1 Detailed Description

Types and functions for iterating on congruence systems.

The types and functions for congruence systems iterators provide read-only access to the elements of a congruence system by interfacing *Congruence_System::const_iterator*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.3 ppl_Congruence_System_tag Interface Reference

Types and functions for congruence systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Congruence_System (ppl_Congruence_System_t *pcs)

 Builds an empty system of congruences and writes a handle to it at address pcs.
- int ppl_new_Congruence_System_zero_dim_empty (ppl_Congruence_System_t *pcs)

 Builds a zero-dimensional, unsatisfiable congruence system and writes a handle to it at address pcs.
- int ppl_new_Congruence_System_from_Congruence (ppl_Congruence_System_t *pcs, ppl_const Congruence t c)

Builds the singleton congruence system containing only a copy of congruence c; writes a handle for the newly created system at address pcs.

- int ppl_new_Congruence_System_from_Congruence_System (ppl_Congruence_System_t *pcs, ppl_const_Congruence_System_t cs)
 - Builds a congruence system that is a copy of cs; writes a handle for the newly created system at address pcs.
- int ppl_assign_Congruence_System_from_Congruence_System (ppl_Congruence_System_t dst, ppl_const_Congruence_System_t src)

Assigns a copy of the congruence system src to dst.

• int ppl_delete_Congruence_System (ppl_const_Congruence_System_t cs)

Invalidates the handle cs: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Congruence System

• int ppl_Congruence_System_space_dimension (ppl_const_Congruence_System_t cs, ppl_dimension_type *m)

Writes to m the dimension of the vector space enclosing cs.

- int ppl_Congruence_System_empty (ppl_const_Congruence_System_t cs)

 Returns a positive integer if cs contains no (non-trivial) congruence; returns 0 otherwise.
- int ppl_Congruence_System_begin (ppl_const_Congruence_System_t cs, ppl_Congruence_System_const_iterator_t cit)

Assigns to cit a const iterator "pointing" to the beginning of the congruence system cs.

• int ppl_Congruence_System_end (ppl_const_Congruence_System_t cs, ppl_Congruence_System_const_iterator_t cit)

Assigns to cit a const iterator "pointing" past the end of the congruence system cs.

• int ppl_Congruence_System_OK (ppl_const_Congruence_System_t cs)

Returns a positive integer if cs is well formed, i.e., if it satisfies all its implementation invariants; returns

0 and perhaps makes some noise if cs is broken. Useful for debugging purposes.

Functions that May Modify the Congruence System

- int ppl_Congruence_System_clear (ppl_Congruence_System_t cs)

 Removes all the congruences from the congruence system cs and sets its space dimension to 0.
- int ppl_Congruence_System_insert_Congruence (ppl_Congruence_System_t cs, ppl_const_-Congruence_t c)

Inserts a copy of the congruence c into cs; the space dimension is increased, if necessary.

Input/Output Functions

- int ppl_io_print_Congruence_System (ppl_const_Congruence_System_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Congruence_System (FILE *stream, ppl_const_Congruence_System_t x)

 *Prints x to the given output stream.
- int ppl_Congruence_System_ascii_dump (ppl_const_Congruence_System_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Congruence_System_ascii_load (ppl_Congruence_System_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.3.1 Detailed Description

Types and functions for congruence systems.

The types and functions for congruence systems provide an interface towards Congruence_System.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.4 ppl_Congruence_tag Interface Reference

Types and functions for congruences.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Congruence (ppl_Congruence_t *pc, ppl_const_Linear_Expression_t le, ppl_const_-Coefficient_t m)

Creates the new congruence $le = 0 \pmod{m}$ and writes a handle for it at address pc. The space dimension of the new congruence is equal to the space dimension of le.

- int ppl_new_Congruence_zero_dim_false (ppl_Congruence_t *pc)

 Creates the unsatisfiable (zero-dimension space) congruence 0 = 1 (mod 0) and writes a handle for it at address pc.
- int ppl_new_Congruence_zero_dim_integrality (ppl_Congruence_t *pc)

 Creates the true (zero-dimension space) congruence 0 = 1 (mod 1), also known as integrality congruence. A handle for the newly created congruence is written at address pc.
- int ppl_new_Congruence_from_Congruence (ppl_Congruence_t *pc, ppl_const_Congruence_t c)

Builds a congruence that is a copy of c; writes a handle for the newly created congruence at address pc.

• int ppl_assign_Congruence_from_Congruence (ppl_Congruence_t dst, ppl_const_Congruence_t src)

Assigns a copy of the congruence src to dst.

• int ppl_delete_Congruence (ppl_const_Congruence_t c)

Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Congruence

- int ppl_Congruence_space_dimension (ppl_const_Congruence_t c, ppl_dimension_type *m)

 Writes to m the space dimension of c.
- int ppl_Congruence_coefficient (ppl_const_Congruence_t c, ppl_dimension_type var, ppl_-Coefficient t n)

Copies into n the coefficient of variable var in congruence c.

- int ppl_Congruence_inhomogeneous_term (ppl_const_Congruence_t c, ppl_Coefficient_t n)

 Copies into n the inhomogeneous term of congruence c.
- int ppl_Congruence_modulus (ppl_const_Congruence_t c, ppl_Coefficient_t m)

 Copies into m the modulus of congruence c.
- int ppl_Congruence_OK (ppl_const_Congruence_t c)

Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

Input/Output Functions

- int ppl_io_print_Congruence (ppl_const_Congruence_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Congruence (FILE *stream, ppl_const_Congruence_t x)

 Prints x to the given output stream.

- int ppl_Congruence_ascii_dump (ppl_const_Congruence_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Congruence_ascii_load (ppl_Congruence_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.4.1 Detailed Description

Types and functions for congruences.

The types and functions for congruences provide an interface towards Congruence.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.5 ppl_Constraint_System_const_iterator_tag Interface Reference

Types and functions for iterating on constraint systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t *pcit)

 Builds a new 'const iterator' and writes a handle to it at address poit.
- int ppl_new_Constraint_System_const_iterator_from_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t *pcit, ppl_const_Constraint_System_const_iterator_t cit)

 Builds a const iterator that is a copy of cit; writes an handle for the newly created const iterator at address pcit.
- int ppl_assign_Constraint_System_const_iterator_from_Constraint_System_const_iterator (ppl_Constraint_System_const_iterator_t dst, ppl_const_Constraint_System_const_iterator_t src)

 Assigns a copy of the const iterator src to dst.
- int ppl_delete_Constraint_System_const_iterator (ppl_const_Constraint_System_const_iterator t cit)

Invalidates the handle cit: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

• int ppl_Constraint_System_const_iterator_dereference (ppl_const_Constraint_System_const_iterator_t cit, ppl_const_Constraint_t *pc)

Dereference cit writing a const handle to the resulting constraint at address pc.

• int ppl_Constraint_System_const_iterator_increment (ppl_Constraint_System_const_iterator_t cit)

Increment cit so that it "points" to the next constraint.

• int ppl_Constraint_System_const_iterator_equal_test (ppl_const_Constraint_System_const_iterator_t x, ppl_const_Constraint_System_const_iterator_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.5.1 Detailed Description

Types and functions for iterating on constraint systems.

The types and functions for constraint systems iterators provide read-only access to the elements of a constraint system by interfacing *Constraint_System::const_iterator*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.6 ppl_Constraint_System_tag Interface Reference

Types and functions for constraint systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Constraint_System (ppl_Constraint_System_t *pcs)

 Builds an empty system of constraints and writes a handle to it at address pcs.
- int ppl_new_Constraint_System_zero_dim_empty (ppl_Constraint_System_t *pcs)

 Builds a zero-dimensional, unsatisfiable constraint system and writes a handle to it at address pcs.
- int ppl_new_Constraint_System_from_Constraint (ppl_Constraint_System_t *pcs, ppl_const_-Constraint_t c)

Builds the singleton constraint system containing only a copy of constraint c; writes a handle for the newly created system at address pcs.

• int ppl_new_Constraint_System_from_Constraint_System (ppl_Constraint_System_t *pcs, ppl_const Constraint System t cs)

Builds a constraint system that is a copy of cs; writes a handle for the newly created system at address pcs.

• int ppl_assign_Constraint_System_from_Constraint_System (ppl_Constraint_System_t dst, ppl_const_Constraint_System_t src)

Assigns a copy of the constraint system src to dst.

• int ppl_delete_Constraint_System (ppl_const_Constraint_System_t cs)

Invalidates the handle cs: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Constraint System

• int ppl_Constraint_System_space_dimension (ppl_const_Constraint_System_t cs, ppl_dimension_type *m)

Writes to m the dimension of the vector space enclosing cs.

- int ppl_Constraint_System_empty (ppl_const_Constraint_System_t cs)

 Returns a positive integer if cs contains no (non-trivial) constraint; returns 0 otherwise.
- int ppl_Constraint_System_has_strict_inequalities (ppl_const_Constraint_System_t cs)

 Returns a positive integer if cs contains any (non-trivial) strict inequality; returns 0 otherwise.
- int ppl_Constraint_System_begin (ppl_const_Constraint_System_t cs, ppl_Constraint_System_const_iterator_t cit)

Assigns to cit a const iterator "pointing" to the beginning of the constraint system cs.

 int ppl_Constraint_System_end (ppl_const_Constraint_System_t cs, ppl_Constraint_System_const_iterator_t cit)

Assigns to cit a const iterator "pointing" past the end of the constraint system cs.

• int ppl_Constraint_System_OK (ppl_const_Constraint_System_t cs)

Returns a positive integer if cs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if cs is broken. Useful for debugging purposes.

Functions that May Modify the Constraint System

- int ppl_Constraint_System_clear (ppl_Constraint_System_t cs)

 Removes all the constraints from the constraint system cs and sets its space dimension to 0.
- int ppl_Constraint_System_insert_Constraint (ppl_Constraint_System_t cs, ppl_const_-Constraint_t c)

Inserts a copy of the constraint c *into* cs; *the space dimension is increased, if necessary.*

Input/Output Functions

- int ppl_io_print_Constraint_System (ppl_const_Constraint_System_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Constraint_System (FILE *stream, ppl_const_Constraint_System_t x)

 Prints x to the given output stream.
- int ppl_Constraint_System_ascii_dump (ppl_const_Constraint_System_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Constraint_System_ascii_load (ppl_Constraint_System_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.6.1 Detailed Description

Types and functions for constraint systems.

The types and functions for constraint systems provide an interface towards Constraint_System.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.7 ppl_Constraint_tag Interface Reference

Types and functions for constraints.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Constraint (ppl_Constraint_t *pc, ppl_const_Linear_Expression_t le, enum ppl_enum_Constraint_Type rel)

Creates the new constraint 'le rel 0' and writes a handle for it at address pc. The space dimension of the new constraint is equal to the space dimension of le.

- int ppl_new_Constraint_zero_dim_false (ppl_Constraint_t *pc)

 Creates the unsatisfiable (zero-dimension space) constraint 0 = 1 and writes a handle for it at address
 pc.
- int ppl_new_Constraint_zero_dim_positivity (ppl_Constraint_t *pc)
 Creates the true (zero-dimension space) constraint 0 ≤ 1, also known as positivity constraint. A handle for the newly created constraint is written at address pc.
- int ppl_new_Constraint_from_Constraint (ppl_Constraint_t *pc, ppl_const_Constraint_t c)

 Builds a constraint that is a copy of c; writes a handle for the newly created constraint at address pc.
- int ppl_assign_Constraint_from_Constraint (ppl_Constraint_t dst, ppl_const_Constraint_t src)

 Assigns a copy of the constraint src to dst.
- int ppl_delete_Constraint (ppl_const_Constraint_t c)

 Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Constraint

- int ppl_Constraint_space_dimension (ppl_const_Constraint_t c, ppl_dimension_type *m)

 Writes to m the space dimension of c.
- int ppl_Constraint_type (ppl_const_Constraint_t c)

 Returns the type of constraint c.

• int ppl_Constraint_coefficient (ppl_const_Constraint_t c, ppl_dimension_type var, ppl_Coefficient_t n)

Copies into n the coefficient of variable var in constraint c.

- int ppl_Constraint_inhomogeneous_term (ppl_const_Constraint_t c, ppl_Coefficient_t n)

 Copies into n the inhomogeneous term of constraint c.
- int ppl_Constraint_OK (ppl_const_Constraint_t c)

Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

Input/Output Functions

- int ppl_io_print_Constraint (ppl_const_Constraint_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Constraint (FILE *stream, ppl_const_Constraint_t x)

 Prints x to the given output stream.
- int ppl_Constraint_ascii_dump (ppl_const_Constraint_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Constraint_ascii_load (ppl_Constraint_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.7.1 Detailed Description

Types and functions for constraints.

The types and functions for constraints provide an interface towards Constraint.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.8 ppl_Generator_System_const_iterator_tag Interface Reference

Types and functions for iterating on generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Generator_System_const_iterator (ppl_Generator_System_const_iterator_t *pgit)

Builds a new 'const iterator' and writes a handle to it at address pgit.

- int ppl_new_Generator_System_const_iterator_from_Generator_System_const_iterator (ppl_Generator_System_const_iterator_t *pgit, ppl_const_Generator_System_const_iterator_t git)

 Builds a const iterator that is a copy of git; writes an handle for the newly created const iterator at address pgit.
- int ppl_assign_Generator_System_const_iterator_from_Generator_System_const_iterator (ppl_Generator_System_const_iterator_t dst, ppl_const_Generator_System_const_iterator_t src)

 Assigns a copy of the const iterator src to dst.
- int ppl_delete_Generator_System_const_iterator (ppl_const_Generator_System_const_iterator_t git)

Invalidates the handle git: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

• int ppl_Generator_System_const_iterator_dereference (ppl_const_Generator_System_const_iterator_t git, ppl_const_Generator_t *pg)

Dereference git writing a const handle to the resulting generator at address pg.

• int ppl_Generator_System_const_iterator_increment (ppl_Generator_System_const_iterator_t git)

Increment git so that it "points" to the next generator.

• int ppl_Generator_System_const_iterator_equal_test (ppl_const_Generator_System_const_iterator_t x, ppl_const_Generator_System_const_iterator_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.8.1 Detailed Description

Types and functions for iterating on generator systems.

The types and functions for generator systems iterators provide read-only access to the elements of a generator system by interfacing *Generator_System::const_iterator*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.9 ppl_Generator_System_tag Interface Reference

Types and functions for generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Generator_System (ppl_Generator_System_t *pgs)

 Builds an empty system of generators and writes a handle to it at address pgs.
- int ppl_new_Generator_System_from_Generator (ppl_Generator_System_t *pgs, ppl_const_-Generator_t g)

Builds the singleton generator system containing only a copy of generator g; writes a handle for the newly created system at address pgs.

• int ppl_new_Generator_System_from_Generator_System (ppl_Generator_System_t *pgs, ppl_const_Generator_System_t gs)

Builds a generator system that is a copy of gs; writes a handle for the newly created system at address pgs.

• int ppl_assign_Generator_System_from_Generator_System (ppl_Generator_System_t dst, ppl_const_Generator_System_t src)

Assigns a copy of the generator system src to dst.

• int ppl_delete_Generator_System (ppl_const_Generator_System_t gs)

Invalidates the handle gs: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Generator System

• int ppl_Generator_System_space_dimension (ppl_const_Generator_System_t gs, ppl_dimension_type *m)

Writes to m the dimension of the vector space enclosing gs.

- int ppl_Generator_System_empty (ppl_const_Generator_System_t gs)

 Returns a positive integer if gs contains no generators; returns 0 otherwise.
- int ppl_Generator_System_begin (ppl_const_Generator_System_t gs, ppl_Generator_System_const_iterator_t git)

Assigns to git a const iterator "pointing" to the beginning of the generator system gs.

• int ppl_Generator_System_end (ppl_const_Generator_System_t gs, ppl_Generator_System_const_iterator_t git)

Assigns to git a const iterator "pointing" past the end of the generator system gs.

• int ppl_Generator_System_OK (ppl_const_Generator_System_t gs)

Returns a positive integer if gs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if gs is broken. Useful for debugging purposes.

Functions that May Modify the Generator System

- int ppl_Generator_System_clear (ppl_Generator_System_t gs)

 Removes all the generators from the generator system qs and sets its space dimension to 0.
- int ppl_Generator_System_insert_Generator (ppl_Generator_System_t gs, ppl_const_-Generator_t g)

Inserts a copy of the generator g *into* gs; *the space dimension is increased, if necessary.*

Input/Output Functions

- int ppl_io_print_Generator_System (ppl_const_Generator_System_t x)

 Prints x to stdout.
- int ppl_io_fprint_Generator_System (FILE *stream, ppl_const_Generator_System_t x)

 Prints x to the given output stream.
- int ppl_Generator_System_ascii_dump (ppl_const_Generator_System_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Generator_System_ascii_load (ppl_Generator_System_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.9.1 Detailed Description

Types and functions for generator systems.

The types and functions for generator systems provide an interface towards Generator_System.

The documentation for this interface was generated from the following file:

• ppl c header.h

7.10 ppl_Generator_tag Interface Reference

Types and functions for generators.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Generator (ppl_Generator_t *pg, ppl_const_Linear_Expression_t le, enum ppl_enum_Generator_Type t, ppl_const_Coefficient_t d)

Creates a new generator of direction le and type t. If the generator to be created is a point or a closure point, the divisor d is applied to le. For other types of generators d is simply disregarded. A handle for the new generator is written at address pg. The space dimension of the new generator is equal to the space dimension of le.

- int ppl_new_Generator_zero_dim_point (ppl_Generator_t *pg)

 Creates the point that is the origin of the zero-dimensional space \mathbb{R}^0 . Writes a handle for the new generator at address pg.
- int ppl_new_Generator_zero_dim_closure_point (ppl_Generator_t *pg)

 Creates, as a closure point, the point that is the origin of the zero-dimensional space \mathbb{R}^0 . Writes a handle for the new generator at address pg.
- int ppl_new_Generator_from_Generator (ppl_Generator_t *pg, ppl_const_Generator_t g)

 Builds a generator that is a copy of g; writes a handle for the newly created generator at address pg.

- int ppl_assign_Generator_from_Generator (ppl_Generator_t dst, ppl_const_Generator_t src)

 Assigns a copy of the generator src to dst.
- int ppl_delete_Generator (ppl_const_Generator_t g)

Invalidates the handle g: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Generator

- int ppl_Generator_space_dimension (ppl_const_Generator_t g, ppl_dimension_type *m)

 Writes to m the space dimension of g.
- int ppl_Generator_type (ppl_const_Generator_t g)

 Returns the type of generator g.
- int ppl_Generator_coefficient (ppl_const_Generator_t g, ppl_dimension_type var, ppl_Coefficient_t n)

Copies into n the coefficient of variable var in generator q.

- int ppl_Generator_divisor (ppl_const_Generator_t g, ppl_Coefficient_t n)

 If g is a point or a closure point assigns its divisor to n.
- int ppl_Generator_OK (ppl_const_Generator_t g)

Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if g is broken. Useful for debugging purposes.

Input/Output Functions

- int ppl_io_print_Generator (ppl_const_Generator_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Generator (FILE *stream, ppl_const_Generator_t x)

 Prints x to the given output stream.
- int ppl_Generator_ascii_dump (ppl_const_Generator_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Generator_ascii_load (ppl_Generator_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.10.1 Detailed Description

Types and functions for generators.

The types and functions for generators provide an interface towards Generator.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.11 ppl_Grid_Generator_System_const_iterator_tag Interface Reference

Types and functions for iterating on grid generator systems.

#include <ppl_c_header.h>

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t *pgit)

Builds a new 'const iterator' and writes a handle to it at address pgit.

• int ppl_new_Grid_Generator_System_const_iterator_from_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t *pgit, ppl_const_Grid_Generator_System_const_iterator_t git)

Builds a const iterator that is a copy of git; writes an handle for the newly created const iterator at address pgit.

• int ppl_assign_Grid_Generator_System_const_iterator_from_Grid_Generator_System_const_iterator (ppl_Grid_Generator_System_const_iterator_t dst, ppl_const_Grid_Generator_System_const_iterator_t src)

Assigns a copy of the const iterator src to dst.

• int ppl_delete_Grid_Generator_System_const_iterator (ppl_const_Grid_Generator_System_const_iterator_t git)

Invalidates the handle git: this makes sure the corresponding resources will eventually be released.

Dereferencing, Incrementing and Equality Testing

Dereference git writing a const handle to the resulting grid generator at address pg.

• int ppl_Grid_Generator_System_const_iterator_increment (ppl_Grid_Generator_System_const_iterator_t git)

Increment git so that it "points" to the next grid generator.

• int ppl_Grid_Generator_System_const_iterator_equal_test (ppl_const_Grid_Generator_-System_const_iterator_t x, ppl_const_Grid_Generator_System_const_iterator_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.11.1 Detailed Description

Types and functions for iterating on grid generator systems.

The types and functions for grid generator systems iterators provide read-only access to the elements of a grid generator system by interfacing *Grid_Generator_System::const_iterator*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.12 ppl_Grid_Generator_System_tag Interface Reference

Types and functions for grid generator systems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Grid_Generator_System (ppl_Grid_Generator_System_t *pgs)

 Builds an empty system of grid generators and writes a handle to it at address pgs.
- int ppl_new_Grid_Generator_System_from_Grid_Generator (ppl_Grid_Generator_System_t *pgs, ppl_const_Grid_Generator_t g)

Builds the singleton grid generator system containing only a copy of generator g; writes a handle for the newly created system at address pgs.

- int ppl_new_Grid_Generator_System_from_Grid_Generator_System (ppl_Grid_Generator_System_t *pgs, ppl_const_Grid_Generator_System_t gs)
 - Builds a grid generator system that is a copy of gs; writes a handle for the newly created system at address pgs.
- int ppl_assign_Grid_Generator_System_from_Grid_Generator_System (ppl_Grid_Generator_System_t dst, ppl_const_Grid_Generator_System_t src)

Assigns a copy of the grid generator system src to dst.

• int ppl_delete_Grid_Generator_System (ppl_const_Grid_Generator_System_t gs)

Invalidates the handle gs: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Grid Generator System

• int ppl_Grid_Generator_System_space_dimension (ppl_const_Grid_Generator_System_t gs, ppl_dimension_type *m)

Writes to m the dimension of the vector space enclosing gs.

- int ppl_Grid_Generator_System_empty (ppl_const_Grid_Generator_System_t gs)

 Returns a positive integer if qs contains no generator; returns 0 otherwise.
- int ppl_Grid_Generator_System_begin (ppl_const_Grid_Generator_System_t gs, ppl_Grid_-Generator System const iterator t git)

Assigns to git a const iterator "pointing" to the beginning of the grid generator system gs.

• int ppl_Grid_Generator_System_end (ppl_const_Grid_Generator_System_t gs, ppl_Grid_-Generator_System_const_iterator_t git)

Assigns to git a const iterator "pointing" past the end of the grid generator system gs.

• int ppl_Grid_Generator_System_OK (ppl_const_Grid_Generator_System_t gs)

Returns a positive integer if gs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if gs is broken. Useful for debugging purposes.

Functions that May Modify the Grid Generator System

- int ppl_Grid_Generator_System_clear (ppl_Grid_Generator_System_t gs)

 Removes all the generators from the grid generator system gs and sets its space dimension to 0.
- int ppl_Grid_Generator_System_insert_Grid_Generator (ppl_Grid_Generator_System_t gs, ppl_const_Grid_Generator_t g)

Inserts a copy of the grid generator g into gs; the space dimension is increased, if necessary.

Input/Output Functions

- int ppl_io_print_Grid_Generator_System (ppl_const_Grid_Generator_System_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Grid_Generator_System (FILE *stream, ppl_const_Grid_Generator_System_t x)

Prints x *to the given output* stream.

• int ppl_Grid_Generator_System_ascii_dump (ppl_const_Grid_Generator_System_t x, FILE *stream)

Dumps an ascii representation of x on stream.

• int ppl_Grid_Generator_System_ascii_load (ppl_Grid_Generator_System_t x, FILE *stream)

Loads an ascii representation of x from stream.

7.12.1 Detailed Description

Types and functions for grid generator systems.

The types and functions for grid generator systems provide an interface towards *Grid_Generator_System*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.13 ppl_Grid_Generator_tag Interface Reference

Types and functions for grid generators.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

• int ppl_new_Grid_Generator (ppl_Grid_Generator_t *pg, ppl_const_Linear_Expression_t le, enum ppl_enum_Grid_Generator_Type t, ppl_const_Coefficient_t d)

Creates a new grid generator of direction le and type t. If the grid generator to be created is a point or a parameter, the divisor d is applied to le. If it is a line, d is simply disregarded. A handle for the new grid generator is written at address pg. The space dimension of the new grid generator is equal to the space dimension of le.

• int ppl_new_Grid_Generator_zero_dim_point (ppl_Grid_Generator_t *pg)

Creates the point that is the origin of the zero-dimensional space \mathbb{R}^0 . Writes a handle for the new grid generator at address pg.

• int ppl_new_Grid_Generator_from_Grid_Generator (ppl_Grid_Generator_t *pg, ppl_const_-Grid_Generator_t g)

Builds a grid generator that is a copy of g; writes a handle for the newly created grid generator at address pg.

• int ppl_assign_Grid_Generator_from_Grid_Generator (ppl_Grid_Generator_t dst, ppl_const_-Grid_Generator_t src)

Assigns a copy of the grid generator src to dst.

• int ppl_delete_Grid_Generator (ppl_const_Grid_Generator_t g)

Invalidates the handle g: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Grid Generator

int ppl_Grid_Generator_space_dimension (ppl_const_Grid_Generator_t g, ppl_dimension_type *m)

Writes to m the space dimension of g.

• int ppl_Grid_Generator_type (ppl_const_Grid_Generator_t g)

*Returns the type of grid generator g.

• int ppl_Grid_Generator_coefficient (ppl_const_Grid_Generator_t g, ppl_dimension_type var, ppl_Coefficient_t n)

Copies into n the coefficient of variable var in grid generator g.

- int ppl_Grid_Generator_divisor (ppl_const_Grid_Generator_t g, ppl_Coefficient_t n)

 If g is a point or a parameter assigns its divisor to n.
- int ppl_Grid_Generator_OK (ppl_const_Grid_Generator_t g)

Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if g is broken. Useful for debugging purposes.

Input/Output Functions

• int ppl_io_print_Grid_Generator (ppl_const_Grid_Generator_t x)

*Prints x to stdout.

- int ppl_io_fprint_Grid_Generator (FILE *stream, ppl_const_Grid_Generator_t x)

 Prints x to the given output stream.
- int ppl_Grid_Generator_ascii_dump (ppl_const_Grid_Generator_t x, FILE *stream)

Dumps an ascii representation of x on stream.

• int ppl_Grid_Generator_ascii_load (ppl_Grid_Generator_t x, FILE *stream)

Loads an ascii representation of x from stream.

7.13.1 Detailed Description

Types and functions for grid generators.

The types and functions for grid generators provide an interface towards *Grid_Generator*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.14 ppl_Linear_Expression_tag Interface Reference

Types and functions for linear expressions.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Constructors, Assignment and Destructor

- int ppl_new_Linear_Expression (ppl_Linear_Expression_t *ple)

 Creates a new linear expression corresponding to the constant 0 in a zero-dimensional space; writes a handle for the new linear expression at address ple.
- int ppl_new_Linear_Expression_with_dimension (ppl_Linear_Expression_t *ple, ppl_dimension_type d)

Creates a new linear expression corresponding to the constant 0 in a d-dimensional space; writes a handle for the new linear expression at address ple.

• int ppl_new_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t *ple, ppl_const_Linear_Expression_t le)

Builds a linear expression that is a copy of le; writes a handle for the newly created linear expression at address ple.

• int ppl_new_Linear_Expression_from_Constraint (ppl_Linear_Expression_t *ple, ppl_const_-Constraint t c)

Builds a linear expression corresponding to constraint c; writes a handle for the newly created linear expression at address ple.

• int ppl_new_Linear_Expression_from_Generator (ppl_Linear_Expression_t *ple, ppl_const_-Generator_t g)

Builds a linear expression corresponding to generator g; writes a handle for the newly created linear expression at address ple.

• int ppl_new_Linear_Expression_from_Congruence (ppl_Linear_Expression_t *ple, ppl_const_-Congruence_t c) Builds a linear expression corresponding to congruence c; writes a handle for the newly created linear expression at address ple.

• int ppl_new_Linear_Expression_from_Grid_Generator (ppl_Linear_Expression_t *ple, ppl_const_Grid_Generator_t g)

Builds a linear expression corresponding to grid generator g; writes a handle for the newly created linear expression at address ple.

• int ppl_assign_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)

Assigns a copy of the linear expression src to dst.

• int ppl_delete_Linear_Expression (ppl_const_Linear_Expression_t le)

Invalidates the handle le: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Linear Expression

• int ppl_Linear_Expression_space_dimension (ppl_const_Linear_Expression_t le, ppl_dimension_type *m)

Writes to m the space dimension of le.

• int ppl_Linear_Expression_coefficient (ppl_const_Linear_Expression_t le, ppl_dimension_type var, ppl_Coefficient_t n)

Copies into n the coefficient of variable var in the linear expression le.

• int ppl_Linear_Expression_inhomogeneous_term (ppl_const_Linear_Expression_t le, ppl_-Coefficient_t n)

Copies into n the inhomogeneous term of linear expression le.

• int ppl_Linear_Expression_OK (ppl_const_Linear_Expression_t le)

Returns a positive integer if $l \in is$ well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if $l \in is$ broken. Useful for debugging purposes.

Functions that May Modify the Linear Expression

• int ppl_Linear_Expression_add_to_coefficient (ppl_Linear_Expression_t le, ppl_dimension_type var, ppl_const_Coefficient_t n)

Adds n to the coefficient of variable var in the linear expression le. The space dimension is set to be the maximum between var + 1 and the old space dimension.

• int ppl_Linear_Expression_add_to_inhomogeneous (ppl_Linear_Expression_t le, ppl_const_-Coefficient_t n)

Adds n to the inhomogeneous term of the linear expression le.

int ppl_add_Linear_Expression_to_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)

Adds the linear expression src to dst.

• int ppl_subtract_Linear_Expression_from_Linear_Expression (ppl_Linear_Expression_t dst, ppl_const_Linear_Expression_t src)

Subtracts the linear expression src from dst.

• int ppl_multiply_Linear_Expression_by_Coefficient (ppl_Linear_Expression_t le, ppl_const_-Coefficient_t n)

Multiply the linear expression dst by n.

Input/Output Functions

- int ppl_io_print_Linear_Expression (ppl_const_Linear_Expression_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Linear_Expression (FILE *stream, ppl_const_Linear_Expression_t x)

 Prints x to the given output stream.
- int ppl_Linear_Expression_ascii_dump (ppl_const_Linear_Expression_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Linear_Expression_ascii_load (ppl_Linear_Expression_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.14.1 Detailed Description

Types and functions for linear expressions.

The types and functions for linear expression provide an interface towards *Linear_Expression*.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

7.15 ppl_MIP_Problem_tag Interface Reference

Types and functions for MIP problems.

```
#include <ppl_c_header.h>
```

Related Functions

(Note that these are not member functions.)

Symbolic Constants

- int PPL_OPTIMIZATION_MODE_MAXIMIZATION Code of the "maximization" optimization mode.
- int PPL_OPTIMIZATION_MODE_MINIMIZATION Code of the "minimization" optimization mode.
- int PPL_MIP_PROBLEM_STATUS_UNFEASIBLE Code of the "unfeasible MIP problem" status.
- int PPL_MIP_PROBLEM_STATUS_UNBOUNDED Code of the "unbounded MIP problem" status.

- int PPL_MIP_PROBLEM_STATUS_OPTIMIZED Code of the "optimized MIP problem" status.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_NAME_PRICING Code for the MIP problem's "pricing" control parameter name.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_TEXTBOOK Code of MIP problem's "textbook" pricing method.
- int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_STEEPEST_EDGE_EXACT

Code of MIP problem's "exact steepest-edge" pricing method.

• int PPL_MIP_PROBLEM_CONTROL_PARAMETER_PRICING_STEEPEST_EDGE_FLOAT Code of MIP problem's "float steepest-edge" pricing method.

Constructors, Assignment and Destructor

• int ppl_new_MIP_Problem_from_space_dimension (ppl_MIP_Problem_t *pmip, ppl_dimension_type d)

Builds a trivial MIP problem of dimension d and writes an handle to it at address pmip.

- int ppl_new_MIP_Problem (ppl_MIP_Problem_t *pmip, ppl_dimension_type d, ppl_const_-Constraint_System_t cs, ppl_const_Linear_Expression_t le, int m)
 - Builds an MIP problem of space dimension d having feasible region cs, objective function le and optimization mode m; writes a handle to it at address pmip.
- int ppl_new_MIP_Problem_from_MIP_Problem (ppl_MIP_Problem_t *pmip, ppl_const_MIP_-Problem_t mip)

Builds an MIP problem that is a copy of mip; writes a handle for the newly created system at address pmip.

• int ppl_assign_MIP_Problem_from_MIP_Problem (ppl_MIP_Problem_t dst, ppl_const_MIP_Problem_t src)

Assigns a copy of the MIP problem src to dst.

• int ppl_delete_MIP_Problem (ppl_const_MIP_Problem_t mip)

Invalidates the handle mip: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the MIP Problem

• int ppl_MIP_Problem_space_dimension (ppl_const_MIP_Problem_t mip, ppl_dimension_type *m)

Writes to m the dimension of the vector space enclosing mip.

• int ppl_MIP_Problem_number_of_integer_space_dimensions (ppl_const_MIP_Problem_t mip, ppl_dimension_type *m)

Writes to m the number of integer space dimensions of mip.

• int ppl_MIP_Problem_integer_space_dimensions (ppl_const_MIP_Problem_t mip, ppl_dimension_type ds[])

Writes in the first positions of the array ds all the integer space dimensions of problem mip. If the array is not big enough to hold all of the integer space dimensions, the behavior is undefined.

• int ppl_MIP_Problem_number_of_constraints (ppl_const_MIP_Problem_t mip, ppl_dimension_type *m)

Writes to m the number of constraints defining the feasible region of mip.

• int ppl_MIP_Problem_constraint_at_index (ppl_const_MIP_Problem_t mip, ppl_dimension_type i, ppl_const_Constraint_t *pc)

Writes at address pc a const handle to the i-th constraint defining the feasible region of the MIP problem mip.

• int ppl_MIP_Problem_objective_function (ppl_const_MIP_Problem_t mip, ppl_const_Linear_-Expression_t *ple)

Writes a const handle to the linear expression defining the objective function of the MIP problem mip at address ple.

- int ppl_MIP_Problem_optimization_mode (ppl_const_MIP_Problem_t mip)

 Returns the optimization mode of the MIP problem mip.
- int ppl_MIP_Problem_OK (ppl_const_MIP_Problem_t mip)

Returns a positive integer if mip is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if mip is broken. Useful for debugging purposes.

Functions that May Modify the MIP_Problem

- int ppl_MIP_Problem_clear (ppl_MIP_Problem_t mip)

 Resets the MIP problem to be a trivial problem of space dimension 0.
- int ppl_MIP_Problem_add_space_dimensions_and_embed (ppl_MIP_Problem_t mip, ppl_dimension_type d)

Adds d new dimensions to the space enclosing the MIP problem mip and to mip itself.

• int ppl_MIP_Problem_add_to_integer_space_dimensions (ppl_MIP_Problem_t mip, ppl_dimension_type ds[], size_t n)

Sets the space dimensions that are specified in first n positions of the array ds to be integer dimensions of problem mip. The presence of duplicates in ds is a waste but an innocuous one.

- int ppl_MIP_Problem_add_constraint (ppl_MIP_Problem_t mip, ppl_const_Constraint_t c)

 Modifies the feasible region of the MIP problem mip by adding a copy of the constraint c.
- int ppl_MIP_Problem_add_constraints (ppl_MIP_Problem_t mip, ppl_const_Constraint_-System_t cs)

Modifies the feasible region of the MIP problem mip by adding a copy of the constraints in cs.

• int ppl_MIP_Problem_set_objective_function (ppl_MIP_Problem_t mip, ppl_const_Linear_-Expression_t le)

Sets the objective function of the MIP problem mip to a copy of le.

• int ppl_MIP_Problem_set_optimization_mode (ppl_MIP_Problem_t mip, int mode)

Sets the optimization mode of the MIP problem mip to mode.

Computing the Solution of the MIP_Problem

- int ppl_MIP_Problem_is_satisfiable (ppl_const_MIP_Problem_t mip)

 Returns a positive integer if mip is satisfiable; returns 0 otherwise.
- int ppl_MIP_Problem_solve (ppl_const_MIP_Problem_t mip)

 Solves the MIP problem mip, returning an exit status.
- int ppl_MIP_Problem_evaluate_objective_function (ppl_const_MIP_Problem_t mip, ppl_const_-Generator_t g, ppl_Coefficient_t num, ppl_Coefficient_t den)

 Evaluates the objective function of mip on point g.
- int ppl_MIP_Problem_feasible_point (ppl_const_MIP_Problem_t mip, ppl_const_Generator_t *pg)

Writes a const handle to a feasible point for the MIP problem mip at address pg.

 int ppl_MIP_Problem_optimizing_point (ppl_const_MIP_Problem_t mip, ppl_const_-Generator_t *pg)

Writes a const handle to an optimizing point for the MIP problem mip at address pg.

• int ppl_MIP_Problem_optimal_value (ppl_const_MIP_Problem_t mip, ppl_Coefficient_t num, ppl_Coefficient_t den)

Returns the optimal value for mip.

Querying/Setting Control Parameters

- int ppl_MIP_Problem_get_control_parameter (ppl_const_MIP_Problem_t mip, int name)

 Returns the value of control parameter name in problem mip.
- int ppl_MIP_Problem_set_control_parameter (ppl_MIP_Problem_t mip, int value)

 Sets control parameter value in problem mip.

Input/Output Functions

- int ppl_io_print_MIP_Problem (ppl_const_MIP_Problem_t x)

 *Prints x to stdout.
- int ppl_io_fprint_MIP_Problem (FILE *stream, ppl_const_MIP_Problem_t x)

 Prints x to the given output stream.
- int ppl_MIP_Problem_ascii_dump (ppl_const_MIP_Problem_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_MIP_Problem_ascii_load (ppl_MIP_Problem_t x, FILE *stream)

 Loads an ascii representation of x from stream.

7.15.1 Detailed Description

Types and functions for MIP problems.

The types and functions for MIP problems provide an interface towards MIP_Problem.

7.15.2 Friends And Related Function Documentation

7.15.2.1 int ppl MIP Problem solve (ppl const MIP Problem t mip) [related]

Solves the MIP problem mip, returning an exit status.

Returns:

PPL_MIP_PROBLEM_STATUS_UNFEASIBLE if the MIP problem is not satisfiable; PPL_MIP_PROBLEM_STATUS_UNBOUNDED if the MIP problem is satisfiable but there is no finite bound to the value of the objective function; PPL_MIP_PROBLEM_STATUS_OPTIMIZED if the MIP problem admits an optimal solution.

7.15.2.2 int ppl_MIP_Problem_evaluate_objective_function (ppl_const_MIP_Problem_t mip, ppl_const_Generator_t g, ppl_Coefficient_t num, ppl_Coefficient_t den) [related]

Evaluates the objective function of mip on point g.

Parameters:

```
mip The MIP problem defining the objective function;
```

g The generator on which the objective function will be evaluated;

num Will be assigned the numerator of the objective function value;

den Will be assigned the denominator of the objective function value;

7.15.2.3 int ppl_MIP_Problem_optimal_value (ppl_const_MIP_Problem_t mip, ppl_Coefficient_t num, ppl_Coefficient_t den) [related]

Returns the optimal value for mip.

Parameters:

mip The MIP problem;

num Will be assigned the numerator of the optimal value;

den Will be assigned the denominator of the optimal value.

The documentation for this interface was generated from the following file:

• ppl_c_header.h

Types and functions for iterating on the disjuncts of a const ppl_Pointset_Powerset_C_Polyhedron_tag.

Related Functions

(Note that these are not member functions.)

Construction, Initialization and Destruction

• int __ppl_new_Pointset_Powerset_C_Polyhedron_const_iterator (ppl_Pointset_Powerset_C_-Polyhedron_const_iterator_t *pit)

Builds a new 'const iterator' and writes a handle to it at address pit.

• int ppl_new_Pointset_Powerset_C_Polyhedron_const_iterator_from_const_iterator (ppl_-Pointset_Powerset_C_Polyhedron_const_iterator_t *pit, ppl_const_Pointset_Powerset_C_-Polyhedron_const_iterator_t y)

Builds a copy of y and writes a handle to it at address pit.

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_begin (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t psit)

 Assigns to psit a const iterator "pointing" to the beginning of the sequence of disjuncts of ps.
- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_end (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t psit)

 Assigns to psit a const iterator "pointing" past the end of the sequence of disjuncts of ps.
- int ppl_delete_Pointset_Powerset_C_Polyhedron_const_iterator (ppl_const_Pointset_Powerset_-C_Polyhedron_const_iterator_t it)

Invalidates the handle it: this makes sure the corresponding resources will eventually be released.

Dereferencing, Increment, Decrement and Equality Testing

- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_dereference (ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t it, ppl_const_Polyhedron_t *d)

 Dereferences it writing a const handle to the resulting disjunct at address d.
- int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_increment (ppl_Pointset_Powerset_C_Polyhedron_const_iterator_t it)

Increments it so that it "points" to the next disjunct.

• int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_decrement (ppl_Pointset_Powerset_-C_Polyhedron_const_iterator_t it)

Decrements it so that it "points" to the previous disjunct.

• int _ppl_Pointset_Powerset_C_Polyhedron_const_iterator_equal_test _(ppl_const_Pointset_-Powerset_C_Polyhedron_const_iterator_t _x, _ppl_const_Pointset_Powerset_C_Polyhedron_const_iterator_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.16.1 Detailed Description

Types and functions for iterating on the disjuncts of a const ppl_Pointset_Powerset_C_Polyhedron_tag.

7.16.2 Friends And Related Function Documentation

7.16.2.1 int ppl_Pointset_Powerset_C_Polyhedron_const_iterator_dereference (ppl_const_-Pointset_Powerset_C_Polyhedron_const_iterator_t it, ppl_const_Polyhedron_t * d) [related]

Dereferences it writing a const handle to the resulting disjunct at address d.

Warning:

On exit, the disjunct d is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, d should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

· C interface.dox

7.17 ppl_Pointset_Powerset_C_Polyhedron_iterator_tag Interface Reference

Types and functions for iterating on the disjuncts of a ppl_Pointset_Powerset_C_Polyhedron_tag.

Related Functions

(Note that these are not member functions.)

Construction, Initialization and Destruction

- - Builds a new 'iterator' and writes a handle to it at address pit.
- int ppl_new_Pointset_Powerset_C_Polyhedron_iterator_from_iterator (ppl_Pointset_Powerset_C_Polyhedron_iterator_t *pit, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)

 Builds a copy of y and writes a handle to it at address pit.
- int ppl_Pointset_Powerset_C_Polyhedron_iterator_begin (ppl_Pointset_Powerset_C_-Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_iterator_t psit)

 Assigns to psit an iterator "pointing" to the beginning of the sequence of disjuncts of ps.
- int ppl_Pointset_Powerset_C_Polyhedron_iterator_end (ppl_Pointset_Powerset_C_Polyhedron_t ps, ppl_Pointset_Powerset_C_Polyhedron_iterator_t psit)

 Assigns to psit an iterator "pointing" past the end of the sequence of disjuncts of ps.
- int ppl_delete_Pointset_Powerset_C_Polyhedron_iterator (ppl_const_Pointset_Powerset_C_-Polyhedron_iterator_t it)

Invalidates the handle it: this makes sure the corresponding resources will eventually be released.

Dereferencing, Increment, Decrement and Equality Testing

- int ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference (ppl_const_Pointset_Powerset_-C_Polyhedron_iterator_t it, ppl_const_Polyhedron_t *d)

 Dereferences it writing a const handle to the resulting disjunct at address d.
- int __ppl_Pointset_Powerset_C_Polyhedron_iterator_increment __(ppl_Pointset_Powerset_C_-Polyhedron_iterator_t it)

Increments it so that it "points" to the next disjunct.

• int __ppl_Pointset_Powerset_C_Polyhedron_iterator_decrement __(ppl_Pointset_Powerset_C_-Polyhedron_iterator_t it) Decrements it so that it "points" to the previous disjunct.

• int ppl_Pointset_Powerset_C_Polyhedron_iterator_equal_test (ppl_const_Pointset_Powerset_-C_Polyhedron_iterator_t x, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

7.17.1 Detailed Description

Types and functions for iterating on the disjuncts of a ppl_Pointset_Powerset_C_Polyhedron_tag.

7.17.2 Friends And Related Function Documentation

7.17.2.1 int ppl_Pointset_Powerset_C_Polyhedron_iterator_dereference (ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t it, ppl_const_Polyhedron_t *d) [related]

Dereferences it writing a const handle to the resulting disjunct at address d.

Note:

Even though it is an non-const iterator, dereferencing it results in a handle to a **const** disjunct. This is because mutable iterators are meant to allow for the modification of the sequence of disjuncts (e.g., by dropping elements), while preventing direct modifications of the disjuncts they point to.

Warning:

On exit, the disjunct d is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, d should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

• C_interface.dox

7.18 ppl_Pointset_Powerset_C_Polyhedron_tag Interface Reference

Types and functions for the Pointset_Powerset of C_Polyhedron objects.

Related Functions

(Note that these are not member functions.)

Ad Hoc Functions for Pointset Powerset domains

• int ppl_Pointset_Powerset_C_Polyhedron_omega_reduce (ppl_const_Pointset_Powerset_C_-Polyhedron t ps)

Drops from the sequence of disjuncts in ps all the non-maximal elements so that ps is non-redundant.

• int ppl_Pointset_Powerset_C_Polyhedron_size (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, size_t *sz)

Writes to sz the number of disjuncts in ps.

• int ppl_Pointset_Powerset_C_Polyhedron_geometrically_covers_Pointset_Powerset_C_-Polyhedron (ppl_const_Pointset_Powerset_C_Polyhedron_t x, ppl_const_Pointset_Powerset_-C_Polyhedron_t y)

Returns a positive integer if powerset x geometrically covers powerset y; returns 0 otherwise.

• int ppl_Pointset_Powerset_C_Polyhedron_geometrically_equals_Pointset_Powerset_C_-Polyhedron (ppl_const_Pointset_Powerset_C_Polyhedron_t x, ppl_const_Pointset_Powerset_-C_Polyhedron_t y)

Returns a positive integer if powerset x is geometrically equal to powerset y; returns 0 otherwise.

- int ppl_Pointset_Powerset_C_Polyhedron_add_disjunct (ppl_Pointset_Powerset_C_-Polyhedron_t ps, ppl_const_Polyhedron_t d)

 Adds to ps a copy of disjunct d.
- int ppl_Pointset_Powerset_C_Polyhedron_drop_disjunct (ppl_Pointset_Powerset_C_-Polyhedron_t ps, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t cit, ppl_Pointset_-Powerset_C_Polyhedron_iterator_t it)

Drops from ps the disjunct pointed to by cit, assigning to it an iterator to the disjunct following cit.

• int ppl_Pointset_Powerset_C_Polyhedron_drop_disjuncts (ppl_Pointset_Powerset_C_-Polyhedron_t ps, ppl_const_Pointset_Powerset_C_Polyhedron_iterator_t first, ppl_const_-Pointset_Powerset_C_Polyhedron_iterator_t last)

Drops from ps all the disjuncts from first to last (excluded).

• int __ppl_Pointset_Powerset_C_Polyhedron_pairwise_reduce __(ppl_Pointset_Powerset_C_-Polyhedron_t ps)

Modifies ps by (recursively) merging together the pairs of disjuncts whose upper-bound is the same as their set-theoretical union.

7.18.1 Detailed Description

Types and functions for the Pointset_Powerset of C_Polyhedron objects.

The powerset domains can be instantiated by taking as a base domain any fixed semantic geometric description (C and NNC polyhedra, BD and octagonal shapes, boxes and grids). An element of the powerset domain represents a disjunctive collection of base objects (its disjuncts), all having the same space dimension

Besides the functions that are available in all semantic geometric descriptions (whose documentation is not repeated here), the powerset domain also provides several ad hoc functions. In particular, the iterator types allow for the examination and manipulation of the collection of disjuncts.

7.18.2 Friends And Related Function Documentation

7.18.2.1 int ppl_Pointset_Powerset_C_Polyhedron_size (ppl_const_Pointset_Powerset_C_Polyhedron_t ps, size_t * sz) [related]

Writes to sz the number of disjuncts in ps.

Note:

If present, Omega-redundant elements will be counted too.

The documentation for this interface was generated from the following file:

• C_interface.dox

7.19 ppl_Polyhedron_tag Interface Reference

Types and functions for the domains of C and NNC convex polyhedra.

Related Functions

(Note that these are not member functions.)

Constructors and Assignment for C_Polyhedron

• int ppl_new_C_Polyhedron_from_space_dimension (ppl_Polyhedron_t *pph, ppl_dimension_type d, int empty)

Builds a C polyhedron of dimension d and writes an handle to it at address pph. If empty is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

• int ppl_new_C_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_-Polyhedron_t ph)

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

- int ppl_new_C_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)
 - Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.
- int ppl_new_C_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_-Constraint_System_t cs)

Builds a new C polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_C_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_-Constraint_System_t cs)

Builds a new C polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_C_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_-Congruence_System_t cs)

Builds a new C polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_C_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_Congruence_System_t cs)

Builds a new C polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_assign_C_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t dst, ppl_const_-Polyhedron_t src)

Assigns a copy of the C polyhedron src to the C polyhedron dst.

Constructors and Assignment for NNC_Polyhedron

• int ppl_new_NNC_Polyhedron_from_space_dimension (ppl_Polyhedron_t *pph, ppl_dimension_type d, int empty)

Builds an NNC polyhedron of dimension d and writes an handle to it at address pph. If empty is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

• int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_-Polyhedron_t ph)

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_-Constraint System t cs)

Builds a new NNC polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t *pph, ppl_-Constraint_System_t cs)

Builds a new NNC polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_from_Congruence_System (ppl_Polyhedron_t *pph, ppl_const_-Congruence System t cs)

Builds a new NNC polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t *pph, ppl_-Congruence_System_t cs)

Builds a new NNC polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl_assign_NNC_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t dst, ppl_const_-Polyhedron t src)

Assigns a copy of the NNC polyhedron src to the NNC polyhedron dst.

Constructors Behaving as Conversion Operators

Besides the conversions listed here below, the library also provides conversion operators that build a semantic geometric description starting from any other semantic geometric description (e.g., ppl_new_Grid_from_C_Polyhedron, ppl_new_C_Polyhedron_from_BD_Shape_mpq_class, etc.). Clearly, the conversion operators are only available if both the source and the target semantic geometric descriptions have been enabled when configuring the library. The conversions also taking as argument a complexity class sometimes provide non-trivial precision/efficiency trade-offs.

• int ppl_new_C_Polyhedron_from_NNC_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_-Polyhedron_t ph)

Builds a C polyhedron that is a copy of the topological closure of the NNC polyhedron ph; writes a handle for the newly created polyhedron at address pph.

• int ppl_new_C_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

Builds a C polyhedron that approximates NNC_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_from_C_Polyhedron (ppl_Polyhedron_t *pph, ppl_const_-Polyhedron_t ph)

Builds an NNC polyhedron that is a copy of the C polyhedron ph; writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t *pph, ppl_const_Polyhedron_t ph, int complexity)

Builds an NNC polyhedron that approximates C_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

Destructor for (C or NNC) Polyhedra

• int ppl_delete_Polyhedron (ppl_const_Polyhedron_t ph)

Invalidates the handle ph: this makes sure the corresponding resources will eventually be released.

Functions that Do Not Modify the Polyhedron

- int ppl_Polyhedron_space_dimension (ppl_const_Polyhedron_t ph, ppl_dimension_type *m)

 Writes to m the dimension of the vector space enclosing ph.
- int ppl_Polyhedron_affine_dimension (ppl_const_Polyhedron_t ph, ppl_dimension_type *m)

 Writes to m the affine dimension of ph (not to be confused with the dimension of its enclosing vector space) or 0, if ph is empty.
- int ppl_Polyhedron_relation_with_Constraint (ppl_const_Polyhedron_t ph, ppl_const_-Constraint_t c)

Checks the relation between the polyhedron ph and the constraint c.

• int ppl_Polyhedron_relation_with_Generator (ppl_const_Polyhedron_t ph, ppl_const_-Generator t g)

Checks the relation between the polyhedron ph and the generator g.

 int ppl_Polyhedron_get_constraints (ppl_const_Polyhedron_t ph, ppl_const_Constraint_-System_t *pcs)

Writes a const handle to the constraint system defining the polyhedron ph at address pcs.

• int ppl_Polyhedron_get_congruences (ppl_const_Polyhedron_t ph, ppl_const_Congruence_-System_t *pcs)

Writes at address pcs a const handle to a system of congruences approximating the polyhedron ph.

• int ppl_Polyhedron_get_minimized_constraints (ppl_const_Polyhedron_t ph, ppl_const_-Constraint_System_t *pcs)

Writes a const handle to the minimized constraint system defining the polyhedron ph at address pcs.

• int ppl_Polyhedron_get_minimized_congruences (ppl_const_Polyhedron_t ph, ppl_const_-Congruence_System_t *pcs) Writes at address pcs a const handle to a system of minimized congruences approximating the polyhedron ph.

- int ppl_Polyhedron_is_empty (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph is empty; returns 0 if ph is not empty.
- int ppl_Polyhedron_is_universe (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph is a universe polyhedron; returns 0 if it is not.
- int ppl_Polyhedron_is_bounded (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph is bounded; returns 0 if ph is unbounded.
- int ppl_Polyhedron_contains_integer_point (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph contains at least one integer point; returns 0 otherwise.
- int ppl_Polyhedron_is_topologically_closed (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph is topologically closed; returns 0 if ph is not topologically closed.
- int ppl_Polyhedron_is_discrete (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph is a discrete set; returns 0 if ph is not a discrete set.
- int ppl_Polyhedron_constrains (ppl_Polyhedron_t ph, ppl_dimension_type var)

 Returns a positive integer if ph constrains var; returns 0 if ph does not constrain var.
- int ppl_Polyhedron_bounds_from_above (ppl_const_Polyhedron_t ph, ppl_const_Linear_-Expression_t le)

Returns a positive integer if le is bounded from above in ph; returns 0 otherwise.

• int ppl_Polyhedron_bounds_from_below (ppl_const_Polyhedron_t ph, ppl_const_Linear_-Expression_t le)

Returns a positive integer if le *is bounded from below in* ph; *returns 0 otherwise.*

• int ppl_Polyhedron_maximize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_-Expression_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum, ppl_-Generator_t point)

Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

• int ppl_Polyhedron_maximize (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int *pmaximum)

The same as ppl_Polyhedron_maximize_with_point, but without the output argument for the location where the supremum value is reached.

• int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_-Expression_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum, ppl_-Generator_t point)

Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

• int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_-Expression_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int *pminimum)

The same as ppl_Polyhedron_minimize_with_point, but without the output argument for the location where the infimum value is reached.

• int ppl_Polyhedron_contains_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

Returns a positive integer if x contains or is equal to y; returns 0 if it does not.

• int ppl_Polyhedron_strictly_contains_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_-Polyhedron_t y)

Returns a positive integer if x strictly contains y; returns 0 if it does not.

• int ppl_Polyhedron_is_disjoint_from_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

Returns a positive integer if x and y are disjoint; returns 0 if they are not.

- int ppl_Polyhedron_equals_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.
- int ppl_Polyhedron_OK (ppl_const_Polyhedron_t ph)

 Returns a positive integer if ph is well formed, i.e., if it satisfies all its implementation invariants; returns

 0 and perhaps makes some noise if ph is broken. Useful for debugging purposes.
- int ppl_Polyhedron_external_memory_in_bytes (ppl_const_Polyhedron_t ph, size_t *sz)

 Writes to sz a lower bound to the size in bytes of the memory managed by ph.
- int ppl_Polyhedron_total_memory_in_bytes (ppl_const_Polyhedron_t ph, size_t *sz) Writes to sz a lower bound to the size in bytes of the memory managed by ph.

Space Dimension Preserving Functions that May Modify the Polyhedron

- int ppl_Polyhedron_add_constraint (ppl_Polyhedron_t ph, ppl_const_Constraint_t c)

 Adds a copy of the constraint c to the system of constraints of ph.
- int ppl_Polyhedron_add_congruence (ppl_Polyhedron_t ph, ppl_const_Congruence_t c)

 *Adds a copy of the congruence c to polyhedron of ph.
- int ppl_Polyhedron_add_constraints (ppl_Polyhedron_t ph, ppl_const_Constraint_System_t cs)

 Adds a copy of the system of constraints cs to the system of constraints of ph.
- int ppl_Polyhedron_add_congruences (ppl_Polyhedron_t ph, ppl_const_Congruence_System_t cs)

Adds a copy of the system of congruences cs to the polyhedron ph.

• int ppl_Polyhedron_add_recycled_constraints (ppl_Polyhedron_t ph, ppl_Constraint_System_t cs)

Adds the system of constraints cs to the system of constraints of ph.

 int ppl_Polyhedron_add_recycled_congruences (ppl_Polyhedron_t ph, ppl_Congruence_-System_t cs)

Adds the system of congruences cs to the polyhedron ph.

- int ppl_Polyhedron_refine_with_constraint (ppl_Polyhedron_t ph, ppl_const_Constraint_t c) *Refines ph using constraint c.
- int ppl_Polyhedron_refine_with_congruence (ppl_Polyhedron_t ph, ppl_const_Congruence_t c) Refines ph using congruence c.

• int ppl_Polyhedron_refine_with_constraints (ppl_Polyhedron_t ph, ppl_const_Constraint_-System_t cs)

Refines ph using the constraints in cs.

• int ppl_Polyhedron_refine_with_congruences (ppl_Polyhedron_t ph, ppl_const_Congruence_-System_t cs)

Refines ph using the congruences in cs.

- int ppl_Polyhedron_intersection_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Intersects x with polyhedron y and assigns the result to x.
- int ppl_Polyhedron_upper_bound_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Assigns to x an upper bound of x and y.
- int ppl_Polyhedron_difference_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y) Same as ppl_Polyhedron_poly_difference_assign(x, y).
- int ppl_Polyhedron_simplify_using_context_assign (ppl_Polyhedron_t x, ppl_const_-Polyhedron_t y)

Assigns to x the meet-preserving simplification of x with respect to context y. Returns a positive integer if x and y have a nonempty intersection; returns 0 if they are disjoint.

- int ppl_Polyhedron_time_elapse_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Assigns to x the time-elapse between the polyhedra x and y.
- int ppl_Polyhedron_topological_closure_assign (ppl_Polyhedron_t ph)

 Assigns to ph its topological closure.
- int ppl_Polyhedron_unconstrain_space_dimension (ppl_Polyhedron_t ph, ppl_dimension_type var)

Modifies ph by unconstraining the space dimension var.

• int ppl_Polyhedron_unconstrain_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type ds[], size_t n)

Modifies ph by unconstraining the space dimensions that are specified in the first n positions of the array ds. The presence of duplicates in ds is a waste but an innocuous one.

• int ppl_Polyhedron_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_ Linear_Expression_t le, ppl_const_Coefficient_t d)

Transforms the polyhedron ph, assigning an affine expression to the specified variable.

• int ppl_Polyhedron_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_-Linear_Expression_t le, ppl_const_Coefficient_t d)

Transforms the polyhedron ph, *substituting an affine expression to the specified variable.*

- int ppl_Polyhedron_bounded_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t lb, ppl_const_Linear_Expression_t ub, ppl_const_Coefficient_t d) Assigns to ph the image of ph with respect to the generalized affine transfer relation $\frac{\text{lb}}{\text{d}} \leq \text{var}' \leq \frac{\text{ub}}{\text{d}}$.
- int ppl_Polyhedron_bounded_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t lb, ppl_const_Linear_Expression_t ub, ppl_const_Coefficient_t d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$.

• int ppl_Polyhedron_generalized_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t le, ppl_const_Coefficient t d)

Assigns to ph the image of ph with respect to the generalized affine transfer relation $\operatorname{var}'\bowtie\frac{\operatorname{le}}{\operatorname{d}}$, where \bowtie is the relation symbol encoded by relsym.

• int ppl_Polyhedron_generalized_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t le, ppl_const_Coefficient t d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation $\operatorname{var}'\bowtie \frac{\operatorname{le}}{\operatorname{d}}$, where \bowtie is the relation symbol encoded by relsym.

• int ppl_Polyhedron_generalized_affine_image_lhs_rhs (ppl_Polyhedron_t ph, ppl_const_-Linear_Expression_t lhs, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_-Expression_t rhs)

Assigns to ph the image of ph with respect to the generalized affine transfer relation $lhs' \bowtie rhs$, where \bowtie is the relation symbol encoded by relsym.

• int ppl_Polyhedron_generalized_affine_preimage_lhs_rhs (ppl_Polyhedron_t ph, ppl_const_-Linear_Expression_t lhs, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_-Expression t rhs)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation lhs' \bowtie rhs, where \bowtie is the relation symbol encoded by relsym.

Functions that May Modify the Dimension of the Vector Space

- int ppl_Polyhedron_concatenate_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Seeing a polyhedron as a set of tuples (its points), assigns to x all the tuples that can be obtained by concatenating, in the order given, a tuple of x with a tuple of y.
- int ppl_Polyhedron_add_space_dimensions_and_embed (ppl_Polyhedron_t ph, ppl_dimension_type d)

Adds d new dimensions to the space enclosing the polyhedron ph and to ph itself.

• int ppl_Polyhedron_add_space_dimensions_and_project (ppl_Polyhedron_t ph, ppl_dimension_type d)

Adds d new dimensions to the space enclosing the polyhedron ph.

• int ppl_Polyhedron_remove_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type ds[], size t n)

Removes from the vector space enclosing ph the space dimensions that are specified in first n positions of the array ds. The presence of duplicates in ds is a waste but an innocuous one.

• int ppl_Polyhedron_remove_higher_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type d)

Removes the higher dimensions from the vector space enclosing ph so that, upon successful return, the new space dimension is d.

• int ppl_Polyhedron_map_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type maps[], size t n)

Remaps the dimensions of the vector space according to a partial function. This function is specified by means of the maps array, which has n entries.

• int ppl_Polyhedron_expand_space_dimension (ppl_Polyhedron_t ph, ppl_dimension_type d, ppl_dimension_type m)

Expands the d-th dimension of the vector space enclosing ph to m new space dimensions.

• int ppl_Polyhedron_fold_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type ds[], size_t n, ppl_dimension_type d)

Modifies ph by folding the space dimensions contained in the first n positions of the array ds into dimension d. The presence of duplicates in ds is a waste but an innocuous one.

Input/Output Functions

- int ppl_io_print_Polyhedron (ppl_const_Polyhedron_t x)

 *Prints x to stdout.
- int ppl_io_fprint_Polyhedron (FILE *stream, ppl_const_Polyhedron_t x)

 Prints x to the given output stream.
- int ppl_Polyhedron_ascii_dump (ppl_const_Polyhedron_t x, FILE *stream)

 Dumps an ascii representation of x on stream.
- int ppl_Polyhedron_ascii_load (ppl_Polyhedron_t x, FILE *stream)

 Loads an ascii representation of x from stream.

Ad Hoc Functions for (C or NNC) Polyhedra

The functions listed here below, being specific of the polyhedron domains, do not have a correspondence in other semantic geometric descriptions.

• int ppl_new_C_Polyhedron_from_Generator_System (ppl_Polyhedron_t *pph, ppl_const_-Generator_System_t gs)

Builds a new C polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_C_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t *pph, ppl_-Generator_System_t gs)

Builds a new C polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_from_Generator_System (ppl_Polyhedron_t *pph, ppl_const_-Generator System t gs)

Builds a new NNC polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl_new_NNC_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t *pph, ppl_-Generator_System_t gs)

Builds a new NNC polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl_Polyhedron_get_generators (ppl_const_Polyhedron_t ph, ppl_const_Generator_System_t *pgs)

Writes a const handle to the generator system defining the polyhedron ph at address pgs.

• int ppl_Polyhedron_get_minimized_generators (ppl_const_Polyhedron_t ph, ppl_const_-Generator_System_t *pgs)

Writes a const handle to the minimized generator system defining the polyhedron ph at address pgs.

- int ppl_Polyhedron_add_generator (ppl_Polyhedron_t ph, ppl_const_Generator_t g)

 Adds a copy of the generator g to the system of generators of ph.
- int ppl_Polyhedron_add_generators (ppl_Polyhedron_t ph, ppl_const_Generator_System_t gs)

 Adds a copy of the system of generators gs to the system of generators of ph.
- int ppl_Polyhedron_add_recycled_generators (ppl_Polyhedron_t ph, ppl_Generator_System_t gs)

Adds the system of generators gs to the system of generators of ph.

- int ppl_Polyhedron_poly_hull_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Assigns to x the poly-hull of x and y.
- int ppl_Polyhedron_poly_difference_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 Assigns to x the poly-difference of x and y.
- int ppl_Polyhedron_BHRZ03_widening_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_-Polyhedron_t y, unsigned *tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y. If tp is not the null pointer, the widening with tokens delay technique is applied with *tp available tokens.

• int ppl_Polyhedron_H79_widening_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron t y, unsigned *tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y. If tp is not the null pointer, the widening with tokens delay technique is applied with *tp available tokens.

int ppl_Polyhedron_BHRZ03_widening_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y.

- int ppl_Polyhedron_H79_widening_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y)

 If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y.
- int ppl_Polyhedron_limited_BHRZ03_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl_Polyhedron_limited_H79_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl_Polyhedron_limited_BHRZ03_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x.

• int ppl_Polyhedron_limited_H79_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_-Polyhedron t y, ppl const Constraint System t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x.

• int ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl_Polyhedron_bounded_H79_extrapolation_assign_with_tokens (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs, unsigned *tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form $\pm v \le r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl_Polyhedron_bounded_BHRZ03_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of x.

• int ppl_Polyhedron_bounded_H79_extrapolation_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y, ppl_const_Constraint_System_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form $\pm v \leq r$ and $\pm v < r$, with $r \in \mathbb{Q}$, that are satisfied by all the points of x.

7.19.1 Detailed Description

Types and functions for the domains of C and NNC convex polyhedra.

The types and functions for convex polyhedra provide a single interface for accessing both topologically closed (C) and not necessarily closed (NNC) convex polyhedra. The distinction between C and NNC polyhedra need only be explicitly stated when *creating* or *assigning* a polyhedron object, by means of one of the functions ppl_new_* and ppl_assign_*.

Having a single datatype does not mean that C and NNC polyhedra can be freely interchanged: as specified in the main manual, most library functions require their arguments to be topologically and/or space-dimension compatible.

7.19.2 Friends And Related Function Documentation

7.19.2.1 int ppl_new_C_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t * pph, ppl_const_Polyhedron_t ph, int complexity) [related]

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

Note:

The complexity argument is ignored.

7.19.2.2 int ppl_new_C_Polyhedron_from_Constraint_System (ppl_Polyhedron_t *pph, ppl_const_Constraint_System_t cs) [related]

Builds a new C polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

7.19.2.3 int ppl_new_C_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t * pph, ppl_Constraint_System_t cs) [related]

Builds a new C polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

Warning:

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

7.19.2.4 int ppl_new_C_Polyhedron_from_Congruence_System (ppl_Polyhedron_t * pph, ppl_const_Congruence_System_t cs) [related]

Builds a new C polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

7.19.2.5 int ppl_new_C_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t * pph, ppl_Congruence_System_t cs) [related]

Builds a new C polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

Warning:

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

7.19.2.6 int ppl_new_NNC_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t * pph, ppl_const_Polyhedron_t ph, int complexity) [related]

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

Note:

The complexity argument is ignored.

7.19.2.7 int ppl_new_NNC_Polyhedron_from_Constraint_System (ppl_Polyhedron_t * pph, ppl_const_Constraint_System_t cs) [related]

Builds a new NNC polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

7.19.2.8 int ppl_new_NNC_Polyhedron_recycle_Constraint_System (ppl_Polyhedron_t * pph, ppl_Constraint_System_t cs) [related]

Builds a new NNC polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

Warning:

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

7.19.2.9 int ppl_new_NNC_Polyhedron_from_Congruence_System (ppl_Polyhedron_t * pph, ppl_const_Congruence_System_t cs) [related]

Builds a new NNC polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

7.19.2.10 int ppl_new_NNC_Polyhedron_recycle_Congruence_System (ppl_Polyhedron_t * pph, ppl_Congruence_System_t cs) [related]

Builds a new NNC polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of $\ensuremath{\texttt{cs}}.$

Warning:

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

7.19.2.11 int ppl_new_C_Polyhedron_from_NNC_Polyhedron_with_complexity (ppl_Polyhedron_t * pph, ppl_const_Polyhedron_t ph, int complexity) [related]

Builds a C polyhedron that approximates NNC_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

Note:

The complexity argument, which can take values PPL_COMPLEXITY_CLASS_POLYNOMIAL, PPL_COMPLEXITY_CLASS_SIMPLEX and PPL_COMPLEXITY_CLASS_ANY, is ignored since the exact constructor has polynomial complexity.

7.19.2.12 int ppl_new_NNC_Polyhedron_from_C_Polyhedron_with_complexity (ppl_Polyhedron_t * pph, ppl_const_Polyhedron_t ph, int complexity) [related]

Builds an NNC polyhedron that approximates C_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

Note:

The complexity argument, which can take values PPL_COMPLEXITY_CLASS_POLYNOMIAL, PPL_COMPLEXITY_CLASS_SIMPLEX and PPL_COMPLEXITY_CLASS_ANY, is ignored since the exact constructor has polynomial complexity.

7.19.2.13 int ppl_Polyhedron_relation_with_Constraint (ppl_const_Polyhedron_t ph, ppl_const_-Constraint_t c) [related]

Checks the relation between the polyhedron ph and the constraint c.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (chosen among PPL_POLY_CON_RELATION_IS_DISJOINT PPL_POLY_CON_RELATION_STRICTLY_INTERSECTS, PPL_POLY_CON_RELATION_IS_INCLUDED, and PPL_POLY_CON_RELATION_SATURATES) that describe the relation between ph and c.

7.19.2.14 int ppl_Polyhedron_relation_with_Generator (ppl_const_Polyhedron_t ph, ppl_const_Generator_t g) [related]

Checks the relation between the polyhedron ph and the generator g.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (only PPL_POLY_-GEN_RELATION_SUBSUMES, at present) that describe the relation between ph and g.

7.19.2.15 int ppl_Polyhedron_maximize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t sup_n, ppl_Coefficient_t sup_d, int * pmaximum, ppl_Generator_t point) [related]

Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

Parameters:

ph The polyhedron constraining le;

le The linear expression to be maximized subject to ph;

sup_n Will be assigned the numerator of the supremum value;

sup_d Will be assigned the denominator of the supremum value;

pmaximum Will store 1 in this location if the supremum is also the maximum, will store 0 otherwise; **point** Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from above, 0 will be returned and sup_n, sup_d, *pmaximum and point will be left untouched.

7.19.2.16 int ppl_Polyhedron_minimize_with_point (ppl_const_Polyhedron_t ph, ppl_const_Linear_Expression_t le, ppl_Coefficient_t inf_n, ppl_Coefficient_t inf_d, int * pminimum, ppl_Generator_t point) [related]

Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

Parameters:

ph The polyhedron constraining le;

le The linear expression to be minimized subject to ph;

inf_n Will be assigned the numerator of the infimum value;

inf_d Will be assigned the denominator of the infimum value;

pminimum Will store 1 in this location if the infimum is also the minimum, will store 0 otherwise;

point Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from below, 0 will be returned and sup_n, sup_d, *pmaximum and point will be left untouched.

7.19.2.17 int ppl_Polyhedron_equals_Polyhedron (ppl_const_Polyhedron_t x, ppl_const_Polyhedron_t y) [related]

Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.

Note that x and y may be topology- and/or dimension-incompatible polyhedra: in those cases, the value 0 is returned.

7.19.2.18 int ppl_Polyhedron_add_recycled_constraints (ppl_Polyhedron_t ph, ppl_Constraint_-System_t cs) [related]

Adds the system of constraints cs to the system of constraints of ph.

Warning:

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

7.19.2.19 int ppl_Polyhedron_add_recycled_congruences (ppl_Polyhedron_t ph, ppl_Congruence_System_t cs) [related]

Adds the system of congruences cs to the polyhedron ph.

Warning:

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

7.19.2.20 int ppl_Polyhedron_upper_bound_assign (ppl_Polyhedron_t x, ppl_const_Polyhedron_t y) [related]

Assigns to x an upper bound of x and y.

For the domain of polyhedra, this is the same as ppl_Polyhedron_poly_hull_assign(x, y).

7.19.2.21 int ppl_Polyhedron_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d) [related]

Transforms the polyhedron ph, assigning an affine expression to the specified variable.

Parameters:

- **ph** The polyhedron that is transformed;
- var The variable to which the affine expression is assigned;
- le The numerator of the affine expression;
- **d** The denominator of the affine expression.

7.19.2.22 int ppl_Polyhedron_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d) [related]

Transforms the polyhedron ph, substituting an affine expression to the specified variable.

Parameters:

- **ph** The polyhedron that is transformed;
- var The variable to which the affine expression is substituted;
- *le* The numerator of the affine expression;
- **d** The denominator of the affine expression.

7.19.2.23 int ppl_Polyhedron_bounded_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t lb, ppl_const_Linear_Expression_t ub, ppl_const_Coefficient_t d) [related]

Assigns to ph the image of ph with respect to the generalized affine transfer relation $\frac{\text{lb}}{\text{d}} \leq \text{var}' \leq \frac{\text{ub}}{\text{d}}$.

Parameters:

- **ph** The polyhedron that is transformed;
- var The variable bounded by the generalized affine transfer relation;
- *lb* The numerator of the lower bounding affine expression;
- **ub** The numerator of the upper bounding affine expression;
- d The (common) denominator of the lower and upper bounding affine expressions.

7.19.2.24 int ppl_Polyhedron_bounded_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, ppl_const_Linear_Expression_t lb, ppl_const_Linear_Expression_t ub, ppl_const_Coefficient_t d) [related]

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$.

Parameters:

- **ph** The polyhedron that is transformed;
- var The variable bounded by the generalized affine transfer relation;
- *lb* The numerator of the lower bounding affine expression;
- *ub* The numerator of the upper bounding affine expression;
- d The (common) denominator of the lower and upper bounding affine expressions.

7.19.2.25 int ppl_Polyhedron_generalized_affine_image (ppl_Polyhedron_t ph, ppl_dimension_type var, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d) [related]

Assigns to ph the image of ph with respect to the *generalized affine transfer relation* $\operatorname{var}' \bowtie \frac{\operatorname{le}}{\operatorname{d}}$, where \bowtie is the relation symbol encoded by relsym.

Parameters:

```
ph The polyhedron that is transformed;
```

var The left hand side variable of the generalized affine transfer relation;

relsym The relation symbol;

le The numerator of the right hand side affine expression;

d The denominator of the right hand side affine expression.

7.19.2.26 int ppl_Polyhedron_generalized_affine_preimage (ppl_Polyhedron_t ph, ppl_dimension_type var, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t le, ppl_const_Coefficient_t d) [related]

Assigns to ph the preimage of ph with respect to the *generalized affine transfer relation* $var' \bowtie \frac{le}{d}$, where \bowtie is the relation symbol encoded by relsym.

Parameters:

```
ph The polyhedron that is transformed;
```

var The left hand side variable of the generalized affine transfer relation;

relsym The relation symbol;

le The numerator of the right hand side affine expression;

d The denominator of the right hand side affine expression.

7.19.2.27 int ppl_Polyhedron_generalized_affine_image_lhs_rhs (ppl_Polyhedron_t ph, ppl_const_Linear_Expression_t lhs, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t rhs) [related]

Assigns to ph the image of ph with respect to the *generalized affine transfer relation* lhs' \bowtie rhs, where \bowtie is the relation symbol encoded by relsym.

Parameters:

```
ph The polyhedron that is transformed;
```

lhs The left hand side affine expression;

relsym The relation symbol;

rhs The right hand side affine expression.

7.19.2.28 int ppl_Polyhedron_generalized_affine_preimage_lhs_rhs (ppl_Polyhedron_t ph, ppl_const_Linear_Expression_t lhs, enum ppl_enum_Constraint_Type relsym, ppl_const_Linear_Expression_t rhs) [related]

Assigns to ph the preimage of ph with respect to the *generalized affine transfer relation* lhs' \bowtie rhs, where \bowtie is the relation symbol encoded by relsym.

Parameters:

```
ph The polyhedron that is transformed;lhs The left hand side affine expression;relsym The relation symbol;rhs The right hand side affine expression.
```

7.19.2.29 int ppl_Polyhedron_map_space_dimensions (ppl_Polyhedron_t ph, ppl_dimension_type maps[], size_t n) [related]

Remaps the dimensions of the vector space according to a *partial function*. This function is specified by means of the maps array, which has n entries.

The partial function is defined on dimension i if i < n and maps $[i] != ppl_not_a_dimension;$ otherwise it is undefined on dimension i. If the function is defined on dimension i, then dimension i is mapped onto dimension maps [i].

The result is undefined if maps does not encode a partial function with the properties described in the specification of the mapping operator.

7.19.2.30 int ppl_new_C_Polyhedron_from_Generator_System (ppl_Polyhedron_t * pph, ppl_const_Generator_System_t gs) [related]

Builds a new C polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

7.19.2.31 int ppl_new_C_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t * pph, ppl_Generator_System_t gs) [related]

Builds a new C polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

Warning:

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

7.19.2.32 int ppl_new_NNC_Polyhedron_from_Generator_System (ppl_Polyhedron_t * pph, ppl_const_Generator_System_t gs) [related]

Builds a new NNC polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

7.19.2.33 int ppl_new_NNC_Polyhedron_recycle_Generator_System (ppl_Polyhedron_t * pph, ppl_Generator_System_t gs) [related]

Builds a new NNC polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

Warning:

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

7.19.2.34 int ppl_Polyhedron_add_recycled_generators (ppl_Polyhedron_t ph, ppl_Generator_System_t gs) [related]

Adds the system of generators gs to the system of generators of ph.

Warning:

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

The documentation for this interface was generated from the following file:

• C_interface.dox

Index

C Language Interface, 18	Error, 21
Data	PPL_CONSTRAINT_TYPE_EQUAL
Datatypes PDL CONSTRAINT TYPE FOLIAL 26	Datatypes, 26
PPL_CONSTRAINT_TYPE_EQUAL, 26	PPL_CONSTRAINT_TYPE_GREATER_OR
PPL_CONSTRAINT_TYPE_GREATER	EQUAL
OR_EQUAL, 27	Datatypes, 27
PPL_CONSTRAINT_TYPE_GREATER	PPL_CONSTRAINT_TYPE_GREATER_THAN
THAN, 27	Datatypes, 27
PPL_CONSTRAINT_TYPE_LESS_OR	PPL_CONSTRAINT_TYPE_LESS_OR_EQUAL
EQUAL, 26	Datatypes, 26
PPL_CONSTRAINT_TYPE_LESS_THAN,	PPL_CONSTRAINT_TYPE_LESS_THAN
26	Datatypes, 26
PPL_GENERATOR_TYPE_CLOSURE	PPL_ERROR_DOMAIN_ERROR
POINT, 27	Error, 21
PPL_GENERATOR_TYPE_LINE, 27	PPL_ERROR_INTERNAL_ERROR
PPL_GENERATOR_TYPE_POINT, 27	Error, 21
PPL_GENERATOR_TYPE_RAY, 27	PPL_ERROR_INVALID_ARGUMENT
PPL_GRID_GENERATOR_TYPE_LINE, 27	Error, 21
PPL_GRID_GENERATOR_TYPE	PPL_ERROR_LENGTH_ERROR
PARAMETER, 27	Error, 21
PPL_GRID_GENERATOR_TYPE_POINT,	PPL_ERROR_OUT_OF_MEMORY
27	Error, 21
ppl_enum_Constraint_Type, 26	PPL_ERROR_UNEXPECTED_ERROR
ppl_enum_Generator_Type, 27	Error, 21
ppl_enum_Grid_Generator_Type, 27	PPL_ERROR_UNKNOWN_STANDARD
ppl_io_variable_output_function_type, 26	EXCEPTION
E.	Error, 21
Error	PPL_GENERATOR_TYPE_CLOSURE_POINT
PPL_ARITHMETIC_OVERFLOW, 21	Datatypes, 27
PPL_ERROR_DOMAIN_ERROR, 21	PPL_GENERATOR_TYPE_LINE
PPL_ERROR_INTERNAL_ERROR, 21	Datatypes, 27
PPL_ERROR_INVALID_ARGUMENT, 21	PPL_GENERATOR_TYPE_POINT
PPL_ERROR_LENGTH_ERROR, 21	Datatypes, 27
PPL_ERROR_OUT_OF_MEMORY, 21	PPL_GENERATOR_TYPE_RAY
PPL_ERROR_UNEXPECTED_ERROR, 21	Datatypes, 27
PPL_ERROR_UNKNOWN_STANDARD	PPL_GRID_GENERATOR_TYPE_LINE
EXCEPTION, 21	Datatypes, 27
PPL_STDIO_ERROR, 21	PPL_GRID_GENERATOR_TYPE_PARAMETER
ppl_enum_error_code, 21	Datatypes, 27
ppl_set_error_handler, 22	PPL_GRID_GENERATOR_TYPE_POINT
Error Handling, 21	Datatypes, 27
Init	PPL_STDIO_ERROR
	Error, 21
ppl_finalize, 19 ppl_initialize, 19	ppl_banner
· · ·	Version, 20
ppl_restore_pre_PPL_rounding, 19	ppl_Coefficient_tag, 27
ppl_set_rounding_for_PPL, 19	ppl_Congruence_System_const_iterator_tag, 29
Library Datatypes, 22	ppl_Congruence_System_tag, 30
Library Initialization and Finalization, 18	ppl_Congruence_tag, 31
Ziolary infiliation and I multiplicity 10	ppl_Constraint_System_const_iterator_tag, 33
PPL_ARITHMETIC_OVERFLOW	- ·

INDEX 76

ppl_Constraint_System_tag, 34	ppl_new_C_Polyhedron_recycle_Generator
ppl_Constraint_tag, 36	System
ppl_enum_Constraint_Type	ppl_Polyhedron_tag, 73
Datatypes, 26	ppl_new_NNC_Polyhedron_from_C_Polyhedron
ppl_enum_error_code	with_complexity
Error, 21	ppl_Polyhedron_tag, 69
ppl_enum_Generator_Type	ppl_new_NNC_Polyhedron_from_Congruence
Datatypes, 27	System
ppl_enum_Grid_Generator_Type	ppl_Polyhedron_tag, 68
Datatypes, 27	ppl_new_NNC_Polyhedron_from_Constraint
ppl_finalize	System
Init, 19	ppl_Polyhedron_tag, 68
ppl_Generator_System_const_iterator_tag, 37	ppl_new_NNC_Polyhedron_from_Generator
ppl_Generator_System_tag, 38	System
ppl_Generator_tag, 40	ppl_Polyhedron_tag, 73
ppl_Grid_Generator_System_const_iterator_tag, 42	ppl_new_NNC_Polyhedron_from_NNC
ppl_Grid_Generator_System_tag, 43	Polyhedron_with_complexity
ppl_Grid_Generator_tag, 44	ppl_Polyhedron_tag, 67
ppl_initialize	ppl_new_NNC_Polyhedron_recycle_Congruence
Init, 19	System
ppl_io_variable_output_function_type	ppl_Polyhedron_tag, 68
Datatypes, 26	ppl_new_NNC_Polyhedron_recycle_Constraint
ppl_Linear_Expression_tag, 46	System
ppl_MIP_Problem_evaluate_objective_function	ppl_Polyhedron_tag, 68
ppl_MIP_Problem_tag, 52	ppl_new_NNC_Polyhedron_recycle_Generator
ppl_MIP_Problem_optimal_value	System
ppl_MIP_Problem_tag, 52	ppl_Polyhedron_tag, 73
ppl_MIP_Problem_solve	ppl_Pointset_Powerset_C_Polyhedron_const
ppl_MIP_Problem_tag, 52	iterator_dereference
ppl_MIP_Problem_tag, 48	ppl_Pointset_Powerset_C_Polyhedron
ppl_MIP_Problem_evaluate_objective	const_iterator_tag, 53
function, 52	ppl_Pointset_Powerset_C_Polyhedron_const
ppl_MIP_Problem_optimal_value, 52	iterator_tag, 52
ppl_MIP_Problem_solve, 52	ppl_Pointset_Powerset_C_Polyhedron
ppl_new_C_Polyhedron_from_C_Polyhedron	const_iterator_dereference, 53
with_complexity	ppl_Pointset_Powerset_C_Polyhedron_iterator
ppl_Polyhedron_tag, 66	dereference
ppl_new_C_Polyhedron_from_Congruence	ppl_Pointset_Powerset_C_Polyhedron
System	iterator_tag, 55
ppl_Polyhedron_tag, 67	ppl_Pointset_Powerset_C_Polyhedron_iterator
ppl_new_C_Polyhedron_from_Constraint_System	tag, 54
ppl_Polyhedron_tag, 67	ppl_Pointset_Powerset_C_Polyhedron
ppl_new_C_Polyhedron_from_Generator_System	iterator_dereference, 55
ppl_Polyhedron_tag, 73	ppl_Pointset_Powerset_C_Polyhedron_size
ppl_new_C_Polyhedron_from_NNC_Polyhedron	ppl_Pointset_Powerset_C_Polyhedron_tag, 56
with_complexity	ppl_Pointset_Powerset_C_Polyhedron_tag, 55
ppl_Polyhedron_tag, 68	ppl_Pointset_Powerset_C_Polyhedron_size,
ppl_new_C_Polyhedron_recycle_Congruence	56
System	ppl_Polyhedron_add_recycled_congruences
ppl_Polyhedron_tag, 67	ppl_Polyhedron_tag, 70
ppl_roryneuron_tag, 07 ppl_new_C_Polyhedron_recycle_Constraint	ppl_Polyhedron_add_recycled_constraints
System	ppl_Polyhedron_tag, 70
ppl_Polyhedron_tag, 67	ppl_Polyhedron_add_recycled_generators
ppi_i orynouron_tag, 07	ppl_Polyhedron_tag, 74
	ppi_i orynouron_tag, /4

INDEX 77

ppl_Polyhedron_affine_image	ppl_new_NNC_Polyhedron_from_NNC
ppl_Polyhedron_tag, 70	Polyhedron_with_complexity, 67
ppl_Polyhedron_affine_preimage	ppl_new_NNC_Polyhedron_recycle
ppl_Polyhedron_tag, 71	Congruence_System, 68
ppl_Polyhedron_bounded_affine_image	ppl_new_NNC_Polyhedron_recycle
ppl_Polyhedron_tag, 71	Constraint_System, 68
ppl_Polyhedron_bounded_affine_preimage	ppl_new_NNC_Polyhedron_recycle
ppl_Polyhedron_tag, 71	Generator_System, 73
ppl_Polyhedron_equals_Polyhedron	ppl_Polyhedron_add_recycled_congruences,
ppl_Polyhedron_tag, 70	70
ppl_Polyhedron_generalized_affine_image	ppl_Polyhedron_add_recycled_constraints, 70
ppl_Polyhedron_tag, 71	ppl_Polyhedron_add_recycled_generators, 74
ppl_Polyhedron_generalized_affine_image_lhs_rhs	ppl_Polyhedron_affine_image, 70
ppl_Polyhedron_tag, 72	ppl_Polyhedron_affine_preimage, 71
ppl_Polyhedron_generalized_affine_preimage	ppl_Polyhedron_bounded_affine_image, 71
ppl_Polyhedron_tag, 72	ppl_Polyhedron_bounded_affine_preimage,
ppl_Polyhedron_generalized_affine_preimage	71
lhs_rhs	ppl_Polyhedron_equals_Polyhedron, 70
ppl_Polyhedron_tag, 72	ppl_Polyhedron_generalized_affine_image, 71
ppl_Polyhedron_map_space_dimensions	ppl_Polyhedron_generalized_affine_image
ppl_Polyhedron_tag, 73	lhs rhs, 72
ppl_Polyhedron_maximize_with_point	ppl_Polyhedron_generalized_affine_preimage.
ppl_Polyhedron_tag, 69	72
ppl_Polyhedron_minimize_with_point	ppl_Polyhedron_generalized_affine
ppl_Polyhedron_tag, 69	preimage_lhs_rhs, 72
ppl_Polyhedron_relation_with_Constraint	ppl_Polyhedron_map_space_dimensions, 73
ppl_Polyhedron_tag, 69	ppl_Polyhedron_maximize_with_point, 69
ppl_Polyhedron_relation_with_Generator	ppl_Polyhedron_minimize_with_point, 69
ppl_Polyhedron_tag, 69	ppl_Polyhedron_relation_with_Constraint, 69
ppl_Polyhedron_tag, 57	ppl_Polyhedron_relation_with_Generator, 69
ppl_new_C_Polyhedron_from_C	ppl_Polyhedron_upper_bound_assign, 70
Polyhedron_with_complexity, 66	ppl_Polyhedron_upper_bound_assign
ppl_new_C_Polyhedron_from_Congruence	ppl_Polyhedron_tag, 70
System, 67	ppl_restore_pre_PPL_rounding
ppl_new_C_Polyhedron_from_Constraint	Init, 19
System, 67	ppl_set_error_handler
ppl_new_C_Polyhedron_from_Generator	Error, 22
System, 73	ppl_set_rounding_for_PPL
ppl_new_C_Polyhedron_from_NNC	Init, 19
Polyhedron_with_complexity, 68	PPL_VERSION
ppl_new_C_Polyhedron_recycle	Version, 20
Congruence_System, 67	
ppl_new_C_Polyhedron_recycle_Constraint	Version
System, 67	ppl_banner, 20
ppl_new_C_Polyhedron_recycle_Generator	PPL_VERSION, 20
System, 73	Version Checking, 19
ppl_new_NNC_Polyhedron_from_C	
Polyhedron_with_complexity, 69	
ppl_new_NNC_Polyhedron_from	
Congruence_System, 68	
ppl_new_NNC_Polyhedron_from	
Constraint_System, 68	
ppl_new_NNC_Polyhedron_from	
Generator System, 73	