SIO 207A: Fundamentals of Digital Signal Processing Class 10

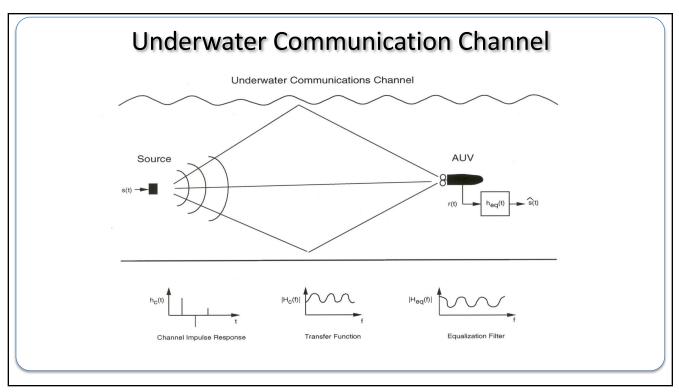
Florian Meyer

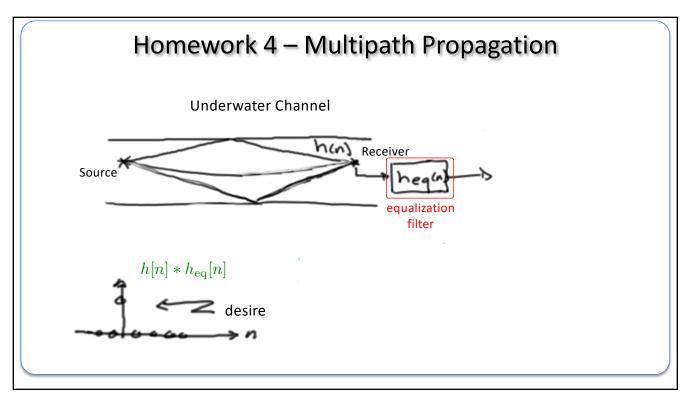
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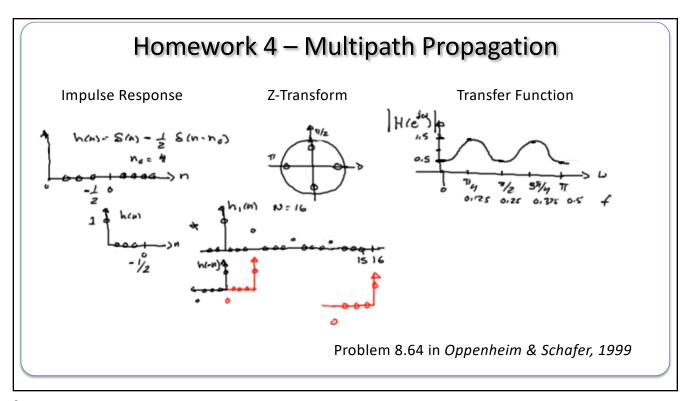


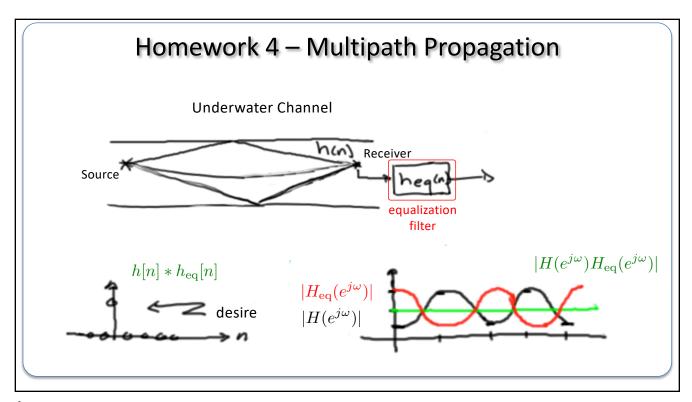


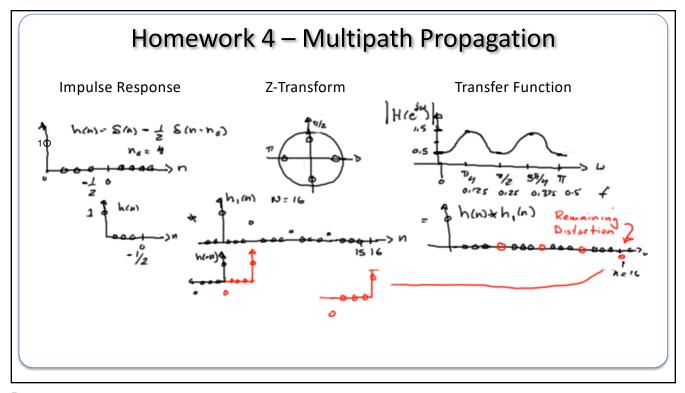
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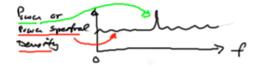








Recovering Sinusoid Amplitude and Power from FFT



Power of Sinusoid: $A^2/2$

$$x[n] = A \sin \omega n$$
$$= A \left\{ \frac{e^{j\omega n} - e^{-j\omega n}}{2j} \right\}$$

$$\text{let } \omega = \frac{2\pi}{N} k'$$

 ${\cal N}$ length of FFT

$$\begin{split} X(k) &= \sum_{n=0}^{N-1} w[n] x[n] e^{-j\frac{2\pi}{N}nk} \\ &= A \sum_{n=0}^{N-1} w[n] \bigg\{ \frac{e^{j\frac{2\pi}{N}nk'} - e^{-j\frac{2\pi}{N}nk'}}{2j} \bigg\} e^{-j\frac{2\pi}{N}nk} \\ &= \frac{A}{2j} \sum_{n=0}^{N-1} w[n] \text{ for } k = k' \text{ (sinusoid is bin centered)} \end{split}$$

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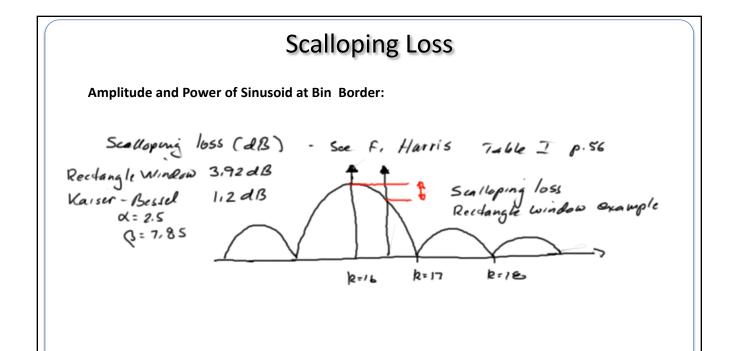
Calibration

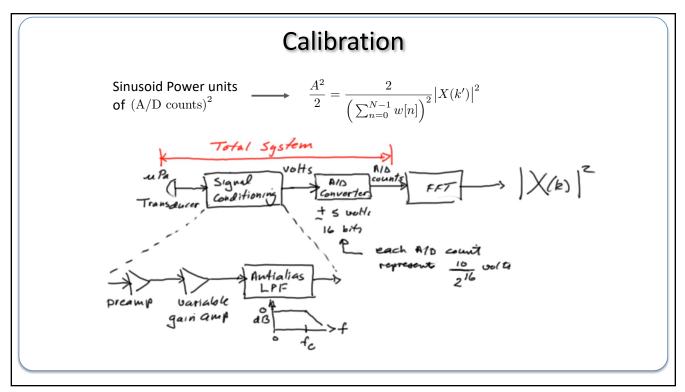
Amplitude and Power of Bin-Centered Sinusoid:

$$X(k) = \frac{A}{2j} \sum_{n=0}^{N-1} w[n] \qquad k = k'$$

sinusoid amplitude
$$A = \frac{2}{\sum_{n=0}^{N-1} w[n]} |X(k')| \qquad \text{True regardless of phase of sinusoid}$$

$$\begin{array}{ll} \text{sinusoid} & \frac{A^2}{2} = \frac{2}{\left(\sum_{n=0}^{N-1} w[n]\right)^2} \big| X(k') \big|^2 \end{array}$$





Calibration