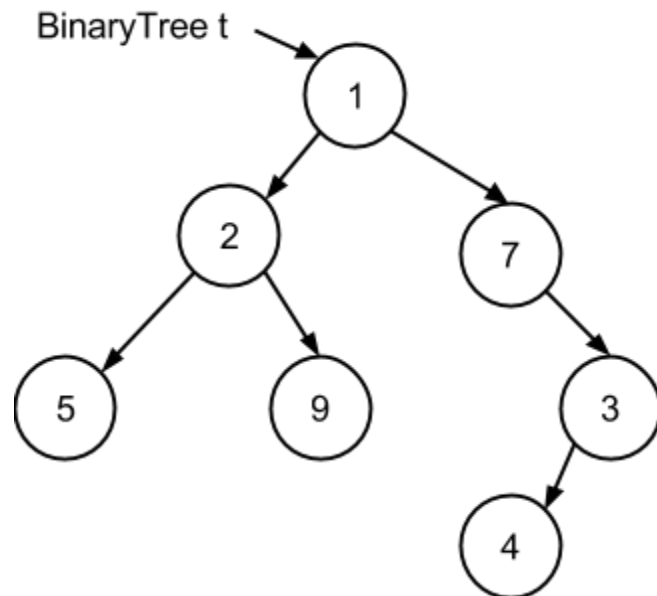


Consider these classes/methods and the following BinaryTree t:

```
class BinaryTree<V> {
    BinaryTree<V> right;
    BinaryTree<V> left;
    V val;
}

interface Fringe<V> {
    public void add(V item);
    public V removeNext();
    public boolean isEmpty();
}
```



```
public static <V> void printTraversal(BinaryTree<V> t,
                                     Fringe<BinaryTree<V>> f) {

    f.add(t);
    while (!f.isEmpty()) {
        BinaryTree curr = f.removeNext();
        if (curr.left != null) f.add(curr.left);
        if (curr.right != null) f.add(curr.right);
        System.out.println(curr.val);
    }
}

class Queue<V> implements Fringe<V> {
    private LinkedList<V> data = new LinkedList<V>();
    public void add(V item) {
        data.addFirst(item);
    }
    public V removeNext() {
        return data.removeLast();
    }
    public boolean isEmpty() {
        return data.isEmpty();
    }
}
```

```
class Stack<V> implements Fringe<V> {
    private LinkedList<V> data = new LinkedList<V>();
    public void add(V item) {
        data.addLast(item);
    }
    public V removeNext() {
        return data.removeLast();
    }
    public boolean isEmpty() {
        return data.isEmpty();
    }
}
```

1. What will Java output?

```
printTraversal(t, new Queue<BinaryTree>());
```

```
printTraversal(t, new Stack<BinaryTree>());
```

2. Height

Write *height*, which takes in a `BinaryTree` and outputs the height of the tree. Assume that a tree with just the root node is of height 1.

height(*t*) => 4

height(*t.left*) => 2

height(*t.right*) => 3

```
public static int height(BinaryTree node) {
```

```
}
```

What's the runtime of *height*?

3. Is it balanced?

Given the above, write *isBalanced*, which takes a *BinaryTree* and outputs whether or not the tree is balanced. A Tree is balanced if the left and right branches differ in height by at most one, and are themselves balanced.

```
isBalanced(t) => false  
isBalanced(t.left) => true  
isBalanced(t.right) => false  
isBalanced(t.right.right) => true
```

```
public static boolean isBalanced(BinaryTree tree) {
```

```
}
```

How long does your method take:
in general?
on balanced trees?

[Extra Exercises] Can you do better? How much better? Outline the algorithm, come up with a runtime, *then* write the code.

Hint: What part of the previous algorithm was expensive?

How can you make it less expensive?