

# Evergreening\*

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September 2021

## Abstract

We develop a simple model of relationship lending where lenders have an incentive to evergreen loans by offering better terms to less productive and more indebted firms. We detect such lending distortions using loan-level supervisory data for the United States. Low-capitalized banks systematically distort their risk assessments of firms to window-dress their balance sheets and extend relatively more credit to underreported borrowers. Consistent with our theoretical predictions, these effects are driven by larger outstanding loans and low-productivity firms. We incorporate the theoretical mechanism into a dynamic heterogeneous-firm model to show that evergreening can give rise to equilibria with low interest rates, high levels of debt, and factor misallocation.

**Keywords:** Evergreening, Zombie-Lending, Misallocation, COVID-19

**JEL Codes:** E32, E43, E44, E52, E60, G21, G32

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\*We thank seminar and conference participants at Stanford GSB, the University of Zurich, the Federal Reserve Bank of San Francisco, the Virtual Australian Macro Seminar, McGill University, and the Annual Meeting of the Canadian Economics Association for their questions and insights. We also thank Colton Merrill and Olivia Wilkinson for excellent research assistance. All errors are our own. The views expressed herein are solely those of the authors and do not necessarily reflect the views of the Federal Reserve Bank of San Francisco, the Federal Reserve Bank of St. Louis, or the Federal Reserve System. This paper has been screened to ensure that no confidential bank or firm level data have been revealed. Faria-e-Castro: Federal Reserve Bank of St. Louis, email: [miguel.fariaecastro@stls.frb.org](mailto:miguel.fariaecastro@stls.frb.org). Paul: Federal Reserve Bank of San Francisco, email: [pascal.paul@sf.frb.org](mailto:pascal.paul@sf.frb.org). Sánchez: Federal Reserve Bank of St. Louis, email: [juan.m.sanchez@stls.frb.org](mailto:juan.m.sanchez@stls.frb.org).

*"Owe your banker £1,000 and you are at his mercy; owe him £1 million and the position is reversed."* — J. M. Keynes (1945)

## 1 Introduction

Following the outbreak of COVID-19 in early 2020, firm profits sharply declined and governments supported businesses through a number of programs that provided firms with subsidized credit. In the short-run, such interventions can stabilize the economy since they prevent firms from laying off workers and declaring bankruptcy, mitigating adverse aggregate demand externalities during a recession. However, in the medium-run, less productive firms may be kept alive, potentially averting efficient restructuring and depressing aggregate productivity. Related to these government programs, concerns emerged that banks would "evergreen" loans, with similar short-run benefits, but potentially leading to the creation of "zombie" firms and lowering economic growth after an immediate crisis passes (Peek and Rosengren, 2005; Caballero, Hoshi and Kashyap, 2008). However, at least in the United States, such worries were frequently dismissed on the basis that such evergreening is typically associated with economies during depressions and severely under-capitalized banks—with Japan in the 1990s used as a prime example—and the U.S. economy was not thought to be in such a position (e.g., Gagnon, 2021).

To assess whether banks evergreen loans requires a general theory that formalizes such lending behavior. In this paper, we illustrate the economic mechanism that results in evergreening using a stylized model of bank lending. Equipped with this basic framework, we address the following questions. Instead of being specific to economies that resemble Japan in the 1990s, is evergreening in fact a general feature of financial intermediation? If so, can we find empirical evidence for such lending distortions even for the U.S. economy over recent years, when banks were operating with relatively high capital ratios? And last, what are the macroeconomic implications of evergreening for aggregate productivity and economic growth?

To begin our analysis, we modify a benchmark model of bank-firm lending along two realistic dimensions. First, we assume that a bank owns a firm's legacy debt, resulting in bank losses in the case of firm default. Second, we posit that the bank has market power and internalizes how the offered lending terms influence a firm's decision to default and therefore the likelihood of repayment of existing liabilities. In the presence of such relationship banking and market power, typical lending incentives can be reversed. In contrast to standard intuition, lenders may offer *better* terms to less productive and more indebted firms. That is because such firms are closer to the default boundary. By offering more attractive conditions on a new loan contract, a bank can raise the continuation value for a firm, thereby reduce the likelihood of default, and increase the chance of repayment of existing debt. Within our static framework, firms with "worse" fundamentals—more debt and lower productivity—pay lower interest rates and invest relatively more. As a result, these firms have lower marginal products of capital, leading to capital misallocation across firms.

With these theoretical predictions, we turn to the data to test whether such lending behavior can be found in practice. To this end, we use the Federal Reserve's Y-14 data set that provides us

with detailed loan-level information for the United States. For our analysis, we make use of the fact that the data include banks' risk assessments for each individual loan and that banks have an incentive to assess similar loans differently due to the regulator design. Specifically, we show that banks with low capital buffers systematically understate their credit risk exposure, confirming previous findings by [Plosser and Santos \(2018\)](#). Such "window-dressing" can arise because the loan risk assessments either directly or indirectly affect bank capital positions. Banks with low buffers above the minimum requirements therefore have an incentive to avoid further declines in their capital ratios and regulatory penalties. Exploiting these differential risk assessments, we test whether the underreporting by low capitalized banks also affects their lending decisions, in a way that is consistent with our theoretical predictions. Using the approach by [Khwaja and Mian \(2008\)](#), we find that low capitalized banks lend relatively more to underreported borrowers, avoiding further losses and reconciling their reporting. However, we show that these results are only present for larger preexisting debt and for low productivity firms, confirming our theoretical mechanism. Illustrating the generality of the theoretical incentives, these effects are found even outside of a recession when U.S. banks were thought to be well capitalized, operating with relatively high capital ratios but smaller capital buffers above regulatory requirements.

Building on this empirical evidence, we embed the mechanism into a dynamic model to study the macroeconomic implications of evergreening. We augment the frameworks developed by [Hopenhayn \(1992\)](#), [Hennessy and Whited \(2005\)](#), and [Gomes and Schmid \(2010\)](#) with the mechanism that we describe in the static, two-period model. We use the model to show that a stationary equilibrium with relationship lending features larger firms, lower interest rates, more debt, and lower total factor productivity than the stationary equilibrium in an economy with anonymous, competitive lenders. In our baseline calibration, which targets moments related to U.S. firms, we find that the relationship lending equilibrium is associated with a drop in aggregate TFP of about 0.3%. Unlike the static model, the dynamic model endogenizes the joint distribution of firm productivity, debt, and capital. It therefore shows that the basic mechanism behind evergreening is not merely a theoretical curiosity but that it may arise in the equilibrium of a calibrated dynamic model. One important insight from our dynamic model is that it shows that most evergreening done in equilibrium seems to be done for riskier firms that are paying relatively high interest rates. This suggests that attempts to empirically identify zombies by comparing measures of funding costs to benchmark risk-free rates may severely underestimate the dimension of this phenomenon.

**Related Literature.** Our paper relates to the literature on evergreening and zombie lending that emerged from Japan's "lost decade," which started with the collapse of stock and real estate markets in the early 1990s. For this period, [Peek and Rosengren \(2005\)](#) provide evidence of evergreening by showing that poor-performing firms typically experienced an increase in their credit. Lending surges were also associated with banks that were weakly capitalized or if banks and firms had strong corporate affiliations.<sup>1</sup> Similarly, [Caballero, Hoshi and Kashyap \(2008\)](#) document a rise

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<sup>1</sup>Within the bank, loan officers may engage in evergreening if they face a lower likelihood of being exposed (e.g., [Hertzberg, Liberti and Paravisini, 2010](#)). Related to this explanation, banks are found to reduce zombie-lending after

in the share of zombie firms, which they define as businesses that pay interest rates below comparable prime rates. Consistent with a model of creative destruction, they show that in industries that experienced an increase in the share of zombie firms, job creation and destruction declined and productivity growth stalled. The presence of zombie firms also spilled over to other firms. In industries with a higher share of zombies, healthy firms experienced a fall in their investment and employment, while their productivity relative to zombies increased.

Building on these seminal contributions, a number of papers have documented similar evidence of evergreening and real economy effects of zombie firms subsequently.<sup>2</sup> These studies span several countries with varying economic conditions, but they generally share the findings that evergreening is more prevalent among weakly capitalized banks during severe recessions, and that zombie firms adversely impact healthy firms and impede firm exit and entry, hindering productivity growth within industries. Throughout, this literature faces two key identification challenges. First, identifying the credit supply effects of evergreening. Second, quantifying the spillover effects of zombie firms onto other firms and broader economic indicators. We contribute to the literature by addressing these two challenges with the following two approaches.

We isolate the credit supply effects with the described empirical strategy that exploits the regulatory environment in the United States.<sup>3</sup> Low capitalized banks have incentives to underreport their credit risk exposure and we use this setting to test for the existence of lending distortions.<sup>4</sup> To assess the real effects of zombie lending, the common approach follows Caballero, Hoshi and Kashyap (2008) in defining a zombie firm and, based on this definition, testing for spillover effects within industries or beyond. This approach isolates only extreme forms of evergreening by design—those that lead to the creation of zombie firms—and has led to a number of distinct zombie-firm definitions that may affect the identification of the spillover effects as pointed out by Schivardi, Sette and Tabellini (2020).<sup>5</sup> Given these empirical challenges, we depart from the common practice and take a theoretical approach instead, embedding our mechanism into a dynamic model which allows us to investigate the spillover effects and also study the aggregate implications of evergreening.

The theoretical mechanism is distinct from existing models of zombie-lending, though it shares similarities with some mechanisms in distantly related literatures. Thus far, relatively few papers formalize the idea of zombie-lending theoretically. Previous theories have relied on information

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on-site inspections (e.g., Bonfim et al., 2020; Angelini et al., 2021).

<sup>2</sup>Among others, examples are Giannetti and Simonov (2013), Storz et al. (2017), McGowan, Andrews and Millot (2018), Banerjee and Hofmann (2018), Acharya et al. (2019), Andrews and Petroulakis (2019), Acharya et al. (2020), Blattner, Farinha and Rebelo (2020), Acharya et al. (2021), Bittner, Fecht and Georg (2021), Chari, Jain and Kulkarni (2021) and Schivardi, Sette and Tabellini (2021).

<sup>3</sup>In this regard, we connect to an extensive body of work that measures how bank health affects the allocation of firm credit (e.g., Khwaja and Mian, 2008) and firm outcomes (e.g., Chodorow-Reich, 2014). Related to our application, Berrospide and Edge (2019), Favara, Ivanov and Rezende (2021), and Ma, Paligorova and Peydro (2021) have used the Y-14 data in this context to investigate the effects of bank capitalization and lender expectations.

<sup>4</sup>Underreporting of risk has been found for various bank assets and to be linked to bank capital positions (see, e.g., Behn, Haselmann and Vig, 2016; Begley, Purnanandam and Zheng, 2017; and Plosser and Santos, 2018).

<sup>5</sup>For example, zombie firms have been defined according to their interest expenses, profitability, age, investment rates, leverage, ratings, and often based on a combination of several measures (see, e.g., Caballero, Hoshi and Kashyap, 2008; Storz et al., 2017; McGowan, Andrews and Millot, 2018; Banerjee and Hofmann, 2018; Acharya et al., 2019; Acharya et al., 2020; and Schivardi, Sette and Tabellini, 2021).

asymmetries (Rajan, 1994; Puri, 1999; Hu and Varas, 2021) or on the premise that banks gamble for resurrection (Bruche and Llobet, 2013). In contrast, our model assumes full information and excludes the possibility of bank default. Closer to our dynamic model, Tracey (2021) considers a heterogeneous-firm setting, in which firms have the option to enter a loan forbearance state, which results in a larger number of less productive firms in equilibrium compared with an economy without this option. In contrast, in our model, lenders choose to offer better loan conditions to less productive firms to keep them alive and recover their outstanding debt.

The mechanism is also different from the classic problem of debt overhang (Myers, 1977). This theory posits that equity holders are reluctant to invest in profitable investment projects since the benefits could be reaped by existing debt holders, hindering further borrowing. In our static framework, more indebted firms receive better loan conditions, enabling them to borrow and invest relatively more, yielding strikingly different predictions than the debt overhang theory. In the sovereign debt literature, related mechanisms illustrate similar results, showing that more indebted governments are able to obtain more favorable conditions once they restructure their debt (e.g., Dvorkin et al., 2021).

Last, our paper relates to an extensive literature that studies factor misallocation (e.g., Restuccia and Rogerson, 2008; Hsieh and Klenow, 2009). For Spain around the early 2000s, Gopinath et al. (2017) show that the dispersion of the return to capital increased, at the same time as real interest rates declined and aggregate productivity growth stalled.<sup>6</sup> Using a heterogeneous firm model, they show that these facts can be explained by a misallocation of capital inflows towards less productive firms. Our model shares the feature that lower interest rates lead to an increase of the capital stock of less productive firms, resulting in capital misallocation. However, such a decline in interest rates is the result of evergreening in our framework, and constrained to the set of indebted and less productive firms.

**Overview.** The next section illustrates the economic mechanism of evergreening using a static two-period model. Section 3 contains the empirical analysis and provides evidence for the mechanism. Section 4 embeds the static two-period framework to a dynamic infinite-horizon model and studies the macroeconomic consequences of evergreening.

## 2 Static Model

In this section, we develop a simple static model of relationship lending. In the model, lenders internalize the existence of an ongoing relationship with the borrower. This means, in particular, that they internalize the effects of pre-existing outstanding debt when determining the terms for new lending contracts. In equilibrium, this leads lenders to potentially offer better terms to firms that are more indebted and less productive, which in turn may induce capital misallocation and lower aggregate TFP for the economy.

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<sup>6</sup>The connection between the secular decline in interest rates and aggregate productivity and output has also recently been studied by Liu, Mian and Sufi (2021), Asriyan et al. (2021), and López-Salido, Goldberg and Chikis (2021).

We begin by presenting the problem of a borrower firm that decides how much to borrow and invest, taking the borrowing interest rate as given. That firm has some legacy/pre-existing liabilities and may decide to exit instead of investing and producing. We then analyze the equilibrium in an economy with competitive lenders and where there is no relationship banking. Finally, we analyze the equilibrium in an economy with relationship banking, where lenders have market power and internalize the effects of lending terms on the likelihood of repayment of legacy debt.

**Environment** Time is discrete and finite: there are two periods  $t = 0, 1$ . There are two types of agents in the economy: firms, which are indexed by their pre-determined states  $(b, z)$ , where  $b$  are pre-existing liabilities and  $z$  is productivity, and lenders. In the competitive lending economy, there is a continuum of lenders for each firm. In the relationship banking economy, there is a single lender for each firm.

## 2.1 Firm Problem

Firms are characterized by their level of pre-existing liabilities  $b$  and productivity  $z$ . At the beginning of  $t = 0$ , the firm may choose to default and obtain zero value, or continue and obtain value equal to  $V(z, b; Q)$ , where  $Q$  is the price of debt that is offered by the lender at  $t = 0$ , and which the firm takes as a given. For simplicity, there is no default at  $t = 1$ . The firm defaults if and only if  $V(z, b; Q) < 0$ .

If the firm does not default, it has to repay its existing liabilities  $b$ , borrows  $Qb'$ , and invests  $k$  at  $t = 0$ . At  $t = 1$ , the firm produces according to a decreasing returns to scale technology  $zk^\alpha$ ,  $\alpha \in (0, 1)$ , and repays debt borrowed at  $t = 0$ ,  $b'$ . Additionally, the firm faces a borrowing constraint at  $t = 0$  that states that borrowing cannot exceed the investment in capital,  $Qb' \leq k$ . The firm's value, conditional on not defaulting, is then given by

$$\begin{aligned} V(z, b; Q) &= \max_{b', k \geq 0} -b - k + Qb' + \beta^f (zk^\alpha - b') \\ \text{s.t.} \\ Qb' &\leq k \end{aligned} \tag{2.1}$$

where  $\beta^f$  is the firm's discount factor.<sup>7</sup> The firm's first-order condition with respect to  $b'$  is simply

$$Q - \beta^f - \lambda Q \leq 0$$

where  $\lambda \geq 0$  is the Lagrange multiplier on the borrowing constraint. Clearly, the constraint is binding as long as  $Q \geq \beta^f$ , implying that  $\lambda = 1 - \beta^f / Q$ . We assume this for now, and later impose restrictions on the model's parameters that ensure that this will be the case. The FOC for

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<sup>7</sup>We assume that the firm owns no pre-existing stock of capital that would allow it to produce at  $t = 0$  and faces no costs of issuing equity. These assumptions are made without loss of generality, and to keep the framework as simple as possible. The model can easily be extended to accommodate both of these features.

capital investment is

$$-1 + \beta^f z \alpha k^{\alpha-1} + \lambda \leq 0$$

Replacing for  $\lambda = 1 - \beta^f / Q$ , we obtain a closed-form solution for the optimal capital stock

$$k(z; Q) = (Q z \alpha)^{\frac{1}{1-\alpha}} \quad (2.2)$$

From the binding constraint, this implies that

$$b'(z; Q) = k(z; Q) / Q = (z \alpha)^{\frac{1}{1-\alpha}} Q^{\frac{\alpha}{1-\alpha}} \quad (2.3)$$

and, finally, this also allows us to write the value function in closed-form

$$V(z, b; Q) = -b + \beta^f (z \alpha)^{\frac{1}{1-\alpha}} Q^{\frac{\alpha}{1-\alpha}} (1/\alpha - 1) \quad (2.4)$$

**Proposition 1** *Given states  $(z, b)$  and an interest rate  $Q$ , the firm's policies  $(k, b')$  are:*

1. *Strictly increasing in productivity  $z$*
2. *Strictly increasing in the price of debt  $Q$*

*The firm's value  $V$  is:*

1. *Strictly increasing in productivity  $z$*
2. *Strictly increasing in the price of debt  $Q$*
3. *Strictly decreasing in legacy debt  $b$*

Proposition 1 also allows us to characterize the firm's default decision. In particular, we can show that there exists  $Q^{\min}(z, b)$  such that the firm chooses to default if it is offered a  $Q$  that is lower than this threshold, using the closed-form expression for the firm's value in 2.4.

**Proposition 2** *There exists a  $Q^{\min}(z, b)$  such that the firm defaults if and only if  $Q < Q^{\min}(z, b)$ . This threshold is given by*

$$Q^{\min}(z, b) = \left[ \frac{b}{\beta^f (z \alpha)^{\frac{1}{1-\alpha}} \left( \frac{1}{\alpha} - 1 \right)} \right]^{\frac{1-\alpha}{\alpha}} \quad (2.5)$$

*This threshold is:*

1. *Strictly increasing in  $b$*
2. *Strictly decreasing in  $z$*

This completes the characterization of the firm's problem given a lending contract  $Q$ . We now proceed to study two different forms of determining  $Q$ , and characterize the equilibria that result from each of them.



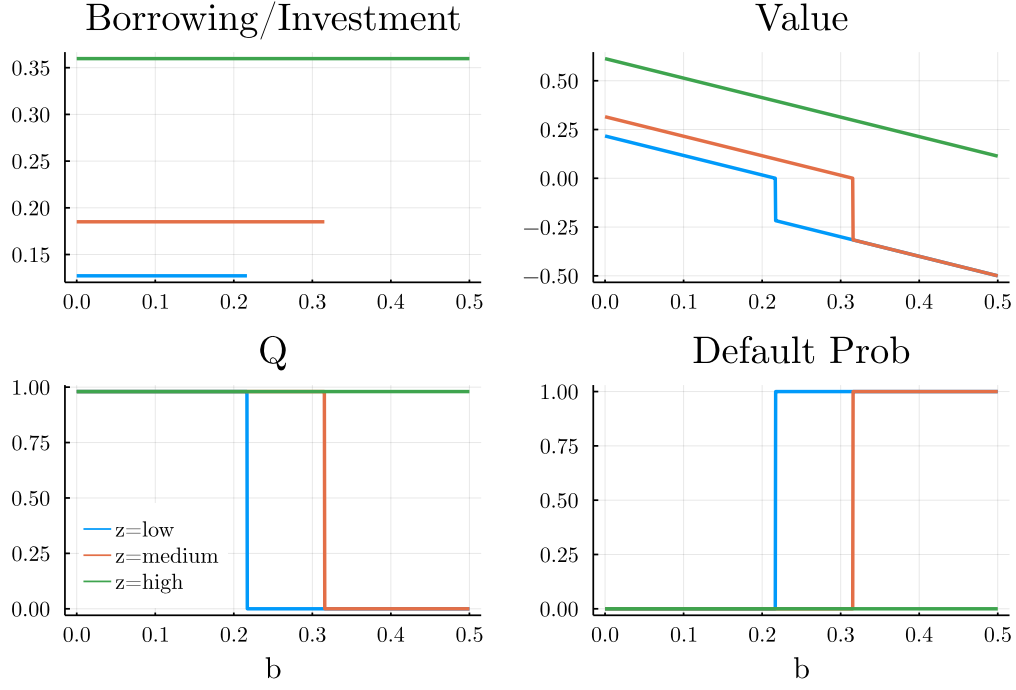


Figure 2.1: Equilibrium policies and prices for the competitive lending economy as a function of  $b$ , for different levels of  $z$ .

## 2.2 Competitive Lending

In the first economy that we consider, there is a continuum of lenders that are available to lend to the firm. These lenders are risk-neutral, have deep pockets, and discount payoffs with factor  $\beta^k > \beta^f$ . Since we assume that there is no default at  $t = 1$ , no arbitrage in the lending market imposes that the offered contract, conditional on no default at  $t = 0$ , satisfies

$$Q = \begin{cases} \beta^k & \text{if } \beta^k \geq Q^{\min}(z, b) \\ 0 & \text{otherwise} \end{cases} \quad (2.6)$$

The equilibrium allocation is then obtained by evaluating 2.2, 2.3, and 2.4 at  $Q = \beta^k$ .<sup>8</sup> In particular, note that the firm's first-order condition for capital can be rewritten as

$$z\alpha k^{\alpha-1} \equiv MPK = \frac{1}{\beta^k}, \forall (z, b)$$

This implies that all firms borrow at the same interest rate, regardless of their initial states  $(z, b)$ , and as long as they do not default at  $t = 0$ . Thus the marginal product of capital is equalized for all surviving firms, and there is no misallocation in this economy.

The equilibrium policies and prices are plotted in Figure 2.1, as a function of the pre-existing liability  $b$  and for different levels of productivity  $z$ .<sup>9</sup> The bottom left panel shows that all firms

<sup>8</sup>Since  $\beta^k = Q > \beta^f$ , our conjecture that the constraint is always binding is confirmed.

<sup>9</sup>All plots are based on the model parametrization described in Appendix E.



borrow at the same  $Q$ , up to the point where  $b$  becomes sufficiently large that the firm decides to instead exit and default. This happens for lower values of  $b$  for less productive firms, which reflects the shape of the  $Q^{\min}(z, b)$  function. The top left panel shows that, predictably, more productive firms borrow and invest more, as marginal productivities of capital are equalized. Furthermore, investment and borrowing policies, as well as prices, are independent of  $b$  up to default.

### 2.3 Relationship Lending

We now proceed to analyze the equilibrium under a different institutional setting, in which a single lender offers the contract  $Q$  to the firm, and internalizes the effects that  $Q$  may have on the firm's policies and values. In short, there are two key differences with respect to the previous arrangement: first, the lender has market power, and behaves as a Stackelberg leader, internalizing  $(b', k, V)(z, b; Q)$  in its choice of  $Q$ . Second, lending is non-anonymous in the sense that the lender owns the pre-existing debt  $b$  and understands that this debt will be lost in the case of default. In the context of relationship lending, we use the terms "lender" and "bank" interchangeably.

The lender's problem is now given by

$$W = \max_{Q \geq \beta^k} \mathbb{I}[V(z, b; Q) \geq 0] \times [-Qb'(z; Q) + b + \beta^k b'(z; Q)] \quad (2.7)$$

where  $\mathbb{I}$  is the indicator function. If the firm defaults at  $t = 0$ , the lender earns zero. Otherwise, the lender recovers  $b$ , lends  $Qb'$  and gets back  $b'$  next period, which is discounted at the factor  $\beta^k$ . Finally, the lender's choice of  $Q$  is constrained to be above  $\beta^k$ , as we assume that the firm may access a competitive debt market similar to the one previously described if the lender tries to offer terms that are worse than those.

Note that we can equivalently write the bank's problem as

$$W = \max_{Q \geq \max\{\beta^k, Q^{\min}(z, b)\}} [b + b'(z; Q)(\beta^k - Q)] \quad (2.8)$$

From this formulation, and the fact that  $\frac{\partial b'(z; Q)}{\partial Q} > 0$ , it is evident that the bank's objective function is strictly decreasing in  $Q$  (ignoring the constraint). For this reason, the optimal policy for the bank consist of offering the lowest possible  $Q$  as long as  $W \geq 0$ . The next propositions characterize the bank's optimal lending policy:

**Proposition 3** Let  $Q^{\max}(z, b)$  denote the maximum  $Q$  at which the bank is willing to lend,

$$Q^{\max}(z, b) : W(z, b; Q^{\max}) = 0 \quad (2.9)$$

$Q^{\max}(z, b)$  solves the following implicit equation

$$b + [\beta^k - Q^{\max}(z, b)](z\alpha)^{\frac{1}{1-\alpha}} Q^{\max}(z, b)^{\frac{\alpha}{1-\alpha}} = 0 \quad (2.10)$$

and satisfies the following properties:

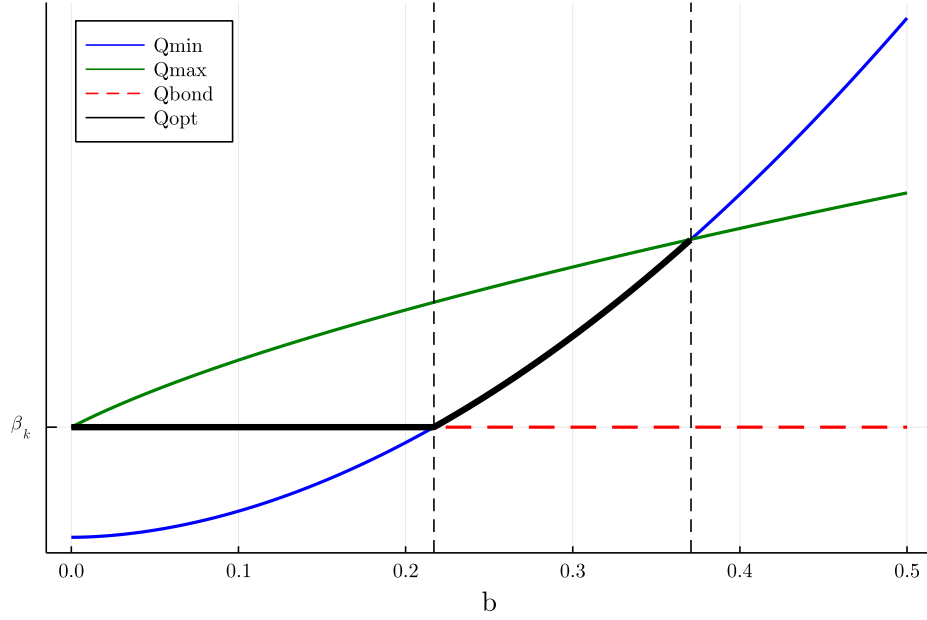


Figure 2.2: Equilibrium allocation as a function of  $b$ , for low  $z$ . The solid blue line is  $Q^{\min}(z, b)$ , the solid green line is  $Q^{\max}(z, b)$ , the dashed red line is  $\beta^k$ , and the thick black line is the bank's chosen policy  $Q^*$ .

1.  $Q^{\max}(z, b) > \beta^k$  iff  $b > 0$
2. It is increasing in  $b$
3. It is decreasing in  $z$

**Proposition 4** *The bank's optimal policy can be written as follows*

$$Q^*(b, z) = \begin{cases} \beta^k & \text{if } Q^{\min}(z, b) < \beta^k < Q^{\max}(z, b) \\ Q^{\min}(z, b) & \text{if } \beta^k < Q^{\min}(z, b) < Q^{\max}(z, b) \\ 0 & \text{otherwise} \end{cases} \quad (2.11)$$

Let  $\bar{b}(z)$  be such that  $Q^{\min}(\bar{b}(z), z) = \beta^k$  and  $\hat{b}(z)$  such that  $Q^{\min}(\hat{b}(z), z) = Q^{\max}(\hat{b}(z), z)$ , then:

1.  $Q^*(b, z)$  is increasing in  $b$ , strictly if  $b \in [\bar{b}(z), \hat{b}(z)]$
2.  $Q^*(b, z)$  is decreasing in  $z$ , strictly if  $b \in [\bar{b}(z), \hat{b}(z)]$

Essentially, the proposition states that as long as  $b > 0$ , legacy debt is nonzero, the bank is willing to offer terms that are better than those in the competitive market to the firm, so as to recover  $b$  by preventing the firm from defaulting. As long as  $Q^{\min}(z, b) < \beta^k$ , the bank can offer  $Q^* = \beta^k$  and guarantee that the firm does not default. In this case, the allocation in the relationship economy is the same as in the competitive lending economy. From 2, we know that  $Q^{\min}(z, b)$  is increasing in  $b$  and decreasing in  $z$ . Therefore, for sufficiently high  $b$  or low  $z$ , we may have that

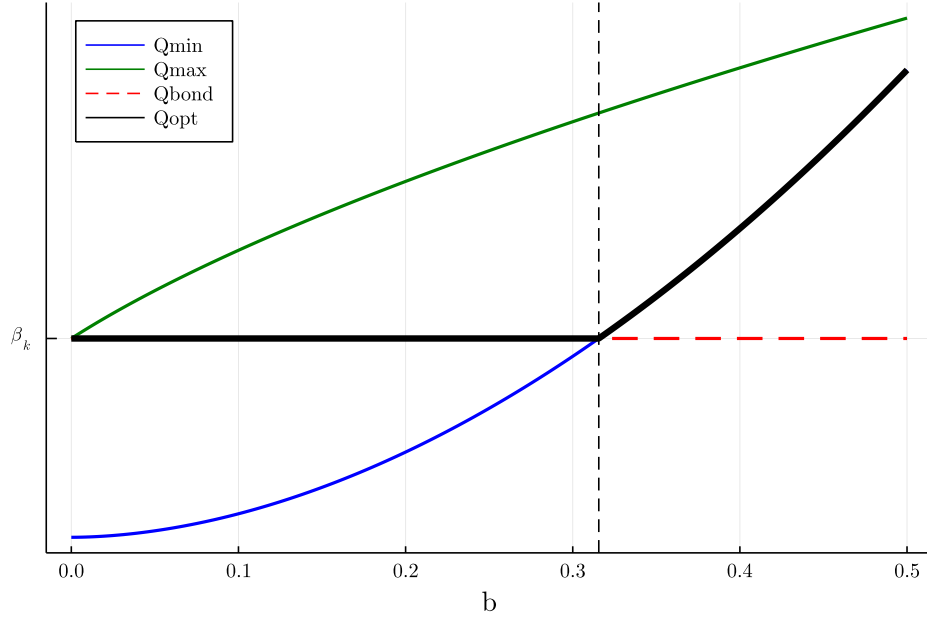


Figure 2.3: Equilibrium allocation as a function of  $b$ , for high  $z$ . The solid blue line is  $Q^{\min}(z, b)$ , the solid green line is  $Q^{\max}(z, b)$ , the dashed red line is  $\beta^k$ , and the thick black line is the bank's chosen policy  $Q^*$ .

$Q^{\min}(z, b) > \beta^k$ . At this point, the firm would simply exit in the competitive economy. In the relationship economy, however, and as long as  $Q^{\min}(z, b)$  is lower than the maximum price the bank is willing to offer,  $Q^{\max}(z, b)$ , the bank will be willing to keep the firm alive by offering  $Q^* = Q^{\min}(z, b) > \beta^k$ . These terms are strictly better than those that the firm could obtain in the competitive market, and become better as  $b$  increases and  $z$  falls. At some point, however,  $Q^{\min}(z, b)$  exceeds the maximum price the bank is willing to offer in order to break-even, and the bank decides to simply liquidate the firm.

This is illustrated in Figure 2.2, which plots the  $Q^{\min}(z, b)$ ,  $Q^{\max}(z, b)$ ,  $Q^*(z, b)$  functions as a function of  $b$ , for a low level of productivity  $z$ . For low enough  $b$ , we have  $Q^{\min}(z, b) < \beta^k < Q^{\max}(z, b)$  and thus the bank's optimal policy is to offer  $Q^* = \beta^k$ . From a certain level of  $b$  onwards,  $Q^{\min}(z, b) > \beta^k$  and the bank is forced to offer  $Q^* = Q^{\min}(z, b)$ . Finally, for sufficiently high  $b$ , it is no longer profitable to lend as this would require the bank to transfer surplus to the firm in excess of the legacy debt that is owed. At this point, the bank decides to liquidate the firm. Figure 2.3 corresponds to the same plot, but for a higher value of productivity  $z$ . In this case, it is clear that  $Q^{\min}(z, b)$  only starts exceeding  $\beta^k$  at a higher level of  $b$ , and the bank always decides to support the firm. Since firm value is increasing in productivity, the amount of surplus that the bank needs to transfer to the firm to prevent it from defaulting is lower, for the same level of legacy debt  $b$ .

**Misallocation** Recall that the firm's FOC implies that

$$z\alpha k^{\alpha-1} \equiv MPK = \frac{1}{Q^*(z, b)}$$

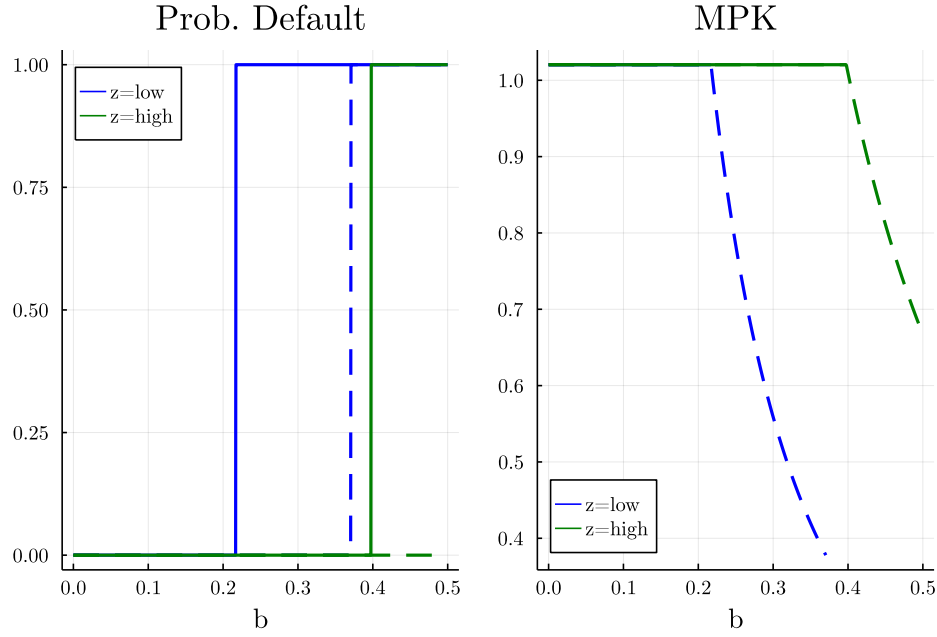


Figure 2.4: Probability of Default (left panel) and marginal product of capital (right panel) as a function of  $b$  for different levels of  $z$ . Solid lines correspond to the competitive lending economy, while dashed lines correspond to the relationship lending economy.

The results in Proposition 4 establish that  $Q^*(b, z)$  is weakly increasing in  $b$  and decreasing in  $z$ . This means that more indebted firms and less productive firms are offered better lending terms  $Q^*(z, b)$  and therefore choose larger levels of capital, consistent with lower marginal productivities of capital. Unlike in the competitive lending case, where MPKs are equalized conditional on no default, the relationship lending economy features MPK dispersion, with more capital flowing to firms that are more indebted and/or less productive.

This is illustrated in Figure 2.4, which plots probabilities of default and MPKs as a function of  $b$  for different levels of  $z$  in the two economies, competitive lending (solid lines) and relationship lending (dashed lines). Consistent with what we have seen above, lenders have an extra incentive to keep firms alive in the relationship lending. Thus default only occurs for higher levels of  $b$ , in the case of the lowest productivity firms. While all firms have the same MPK in the competitive lending economy, regardless of the level of  $b$ , that is not the case in the relationship lending economy, where the MPK is now a function of  $b$ . In particular, and as the figure shows, there are levels of  $b$  for which medium and high productivity firms have the same MPK as in the competitive lending case, but low productivity firms have a lower MPK, which means that they are borrowing and investing relatively more.

## 2.4 Aggregate Effects

In this section, we focused only on the contracting problem between an individual lender and a borrower. Additionally, we perform comparative statics with respect to  $b$ , the amount of pre-existing debt, while fixing the amount of pre-existing capital to zero. In practice, the pre-existing

stocks of debt and capital should be correlated, which affects the value of the firm and therefore the decision to default or not at  $t = 0$ . The extent to which the default decision is affected, and how this affected the contract that is optimally offered by the lender, are important to determine the extent of evergreening in the aggregate economy, and how it affects total output and productivity. In section 4, we present a dynamic equilibrium extension of this 2-period model, which allows us to address some of these issues.

### 3 Empirical Analysis

In this section, we investigate whether the described mechanism plays a role in banks' lending behavior. Identifying such lending practices empirically poses some well-known, as well as some more subtle identification challenges. To begin with, we are interested in isolating the credit supply effects of evergreening. To this end, we apply the common approach of using a "credit registry" and a sample of firms that borrow from multiple banks, which allows us to control for a firm's common credit demand across lenders using firm-time fixed effects (Khwaja and Mian, 2008). To test our theory, we could distinguish banks according to the share of a firm's debt that they hold, with more indebted banks having a stronger incentive to evergreen loans. However, separating bank-firm pairs by their ex-ante lending intensity would likely violate the common credit demand assumption of the Khwaja and Mian (2008)-approach. Further, the effects of any firm-specific characteristics, like measures of firm productivity, could not be estimated separately in the presence of firm-time fixed effects, rendering any empirical design that builds on such differences infeasible to test our theory.

We therefore pursue a different empirical strategy. Due to the regulatory environment in the United States, the incentives to report their credit risk exposure correctly differs in the cross-section of banks. As we document, low capitalized banks systematically underreport their risk exposure relative to better capitalized banks for similar loans to the same firm. We exploit these differential risk assessments stemming from regulatory rules and test whether they also influence banks' lending decisions in a way that is consistent with the predictions of our theory. We find that low capitalized banks lend relatively more to underreported borrowers to avoid potential losses and to reconcile their reporting. However, such lending behavior is only observed in the subset of larger legacy debt and for low productivity firms, providing evidence in support of our theoretical mechanism.

#### 3.1 Data

The main data set of our analysis is the corporate loan schedule H.1 of the Federal Reserve's Y-14Q collection (Y14 for short). These data were introduced as part of the Dodd-Frank Act following the 2007-09 financial crisis. They are typically used for stress-testing and cover large bank holding companies (BHCs).<sup>10</sup> For the BHCs within our sample, the data contain quarterly updates on the

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<sup>10</sup>Until 2019, BHCs with more than \$50 billion in assets were required to participate in the collection, and the size threshold was changed to \$100 billion subsequently.

universe of loan facilities with commitments in excess of \$1 million, and include detailed information about the credit arrangements. Important for our analysis, the data cover risk assessments for each individual loan, allowing us to compare evaluations for the same borrower across banks, as explained in the next section.

We identify a firm using the Taxpayer Identification Number (TIN). The vast majority of firms within our data are private ones. For these firms, we rely on the banks' own collections of firm balance sheet and income statements that are also part of the Y14 data. To reduce measurement error and to increase the number of observations, we take the median of firm financial variables across all banks and loans for a particular firm-date observation since these data are firm-specific. For the public firms, we instead use information from Compustat on firm financials. We further apply several sample restrictions. First, we exclude lending to financial and real estate firms. Second, we restrict the start of the sample to 2012:Q3 to allow for a short phase-in period, though most of our analysis is constrained to begin in 2014:Q4, when loan risk assessments were required for all banks. We include information up until 2020:Q4. Over this sample, we cover 4,904,321 loan facility observations, 216,661 distinct firms, and we identify 3,217 of those as public ones, since they can be matched to Compustat. Last, we apply a number of filtering steps that are left to Appendix A, which also includes an overview of the variables that are used from the various sources.

### 3.2 Risk-Reporting and Bank Capital

For each loan, banks have to report several risk measures: the probability of default (PD), a loan rating, the loss given default, and the exposure at default. Among those, we use the PD for our analysis, since it is a continuous measure and approximately borrower- rather than loan-specific.<sup>11</sup> That is, a borrower is typically late on several outstanding payments or defaults on a number of loans at the same time. In support of this approximation, Appendix Figure B.1 shows that individual banks assign virtually the same PD across multiple loans to the same firm, even if those loans have distinct characteristics. In contrast, there is substantial dispersion of PDs across banks, even when considering loans with similar characteristics to the same firm.

To understand the origin of the dispersion across banks, we conduct a similar analysis as Plosser and Santos (2018). Weighted by all outstanding loans, we denote the probability of default that bank  $j$  reports for firm  $i$  at time  $t$  by  $PD_{i,j,t}$ . To compare risk-reporting across banks, we further define the difference between this variable and the average reported PD by all other banks as  $PD\text{-}Gap_{i,j,t} = PD_{i,j,t} - \overline{PD}_{i,t}$  where  $\overline{PD}_{i,t} = (1/M) \sum_m PD_{i,m,t}$  for all  $m \neq j$ . In practice, there are many reasons why banks differ in their risk assessments. For example, some banks may possess private information about a borrower, resulting in a more accurate and potentially different forecast relative to other banks. To assess whether bank capital positions can explain the dispersion

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<sup>11</sup>The PD measures whether a loan is non-performing over the course of the next year. According to the Basel Committee, a loan is in default, if either one or both of the following events have taken place: (1) the bank considers that the obligor is unlikely to pay its credit obligations to the banking group in full, without recourse by the bank to actions such as realizing security (if held); and (2) the obligor is past due more than 90 days on any material credit obligation to the banking group. Source: [https://www.bis.org/basel\\_framework/chapter/CRE/36.htm](https://www.bis.org/basel_framework/chapter/CRE/36.htm)

across banks, we estimate different versions of the regression

$$PD_{i,j,t} = \beta Capital_{j,t-1} + \gamma X_{j,t-1} + \alpha_{i,t} + \kappa_j + u_{i,j,t} \quad , \quad (3.1)$$

where  $X_{j,t-1}$  is a vector of bank characteristics,  $\alpha_{i,t}$  is a firm-time fixed effect, and  $\kappa_j$  is a bank fixed effect. The variable of interest is  $Capital_{j,t-1}$  and we use the buffer over the common equity Tier 1 (CET1) requirement to measure bank capital positions.<sup>12</sup>

Before estimating the regression, it is useful to consider various explanations for different values of  $\beta$ . First, assume that some banks possess private information and therefore have more accurate forecasts than others. All else equal, such an explanation should not result in a systematic relation between bank capital and reported PDs but rather give  $\beta \approx 0$ . Second, assume that a bank has downward-biased PDs. If that bank's risk-weighted assets (RWAs) are computed according to the internal ratings-based approach (IRB), then such a bank would assign relatively lower risk-weights and therefore lower RWAs. The ratio of capital-to-RWAs should therefore be higher, resulting in  $\beta < 0$ . Similarly, imagine that a bank learns that its loan portfolio is riskier than previously anticipated. This should raise PDs, risk-weights, and RWAs, and therefore lower the ratio of capital to RWAs, again giving  $\beta < 0$ . And third, there are two relevant explanations that can instead result in  $\beta > 0$ . Assume that a bank's overall risk-perception is low or its risk-taking is high. Such a bank may assign low PDs but also operate with a high leverage (or low capital buffers). Similarly, if banks specialize in risky lending, they may assign high PDs but also operate with high capital buffers to support potential losses. To account for this "business-model" explanation, we include bank fixed effects and total portfolio risk variables into our regressions, controlling for time-invariant and time-varying factors, respectively.

The final explanation why we should find  $\beta > 0$  is that low-capitalized banks systematically underreport their credit risk exposure due to regulatory incentives. In the United States, banks may have such incentives for the following three reasons. First, around half of the banks in our sample were subject to the IRB approach, which allows banks to use their own risk measures to compute loan-specific risk weights.<sup>13</sup> The PDs that we use directly enter those calculations, and banks with low capital buffers may underreport PDs to avoid further declines in their capital ratios and potential penalties for violating capital requirements.<sup>14</sup> Second, the Federal Reserve's

<sup>12</sup>Throughout our analysis, we use the CET1 buffer since CET1 is the most "costly" type of capital for banks. It covers common stock, stock surplus, retained earnings, minority interest, and accumulated other comprehensive income. We define the capital buffer as the difference between the capital ratio and the required capital, consisting of a minimum and a capital conservation buffer requirement (GSIB surcharge + stress capital buffer + countercyclical capital buffer). In addition to the CET1 requirement, banks face requirements on their Tier 1 and their total capital.

<sup>13</sup>According to the advanced IRB approach, banks' own risk measures determine risk weights (PD, exposure at default, loss given default, expected credit loss, and loan maturities). Pre-2020, banks with >\$250 billion assets or >\$10 billion in foreign exposure were required to use the advanced IRB approach. Post-2020, the requirement changed to cover all GSIBs or firms with >\$700 billion assets or >\$75 billion cross-jurisdictional activity. In the United States, banks that are subject to the advanced IRB approach also have to compute their capital ratios based on the standardized approach and must comply with the capital requirements under both approaches. Source: <https://www.federalreserve.gov/aboutthefed/boardmeetings/files/board-memo-20181031.pdf>

<sup>14</sup>When bridging the capital conservation buffer requirement, banks may face limitations such as restrictions on dividend payouts, retained earnings, and share buybacks. When violating the minimum requirement, regulators may, for example, force a bank to issue capital or restrict asset growth ("prompt corrective action"). Sources: [https://www.bis.org/basel\\_framework/chapter/RBC/30.htm](https://www.bis.org/basel_framework/chapter/RBC/30.htm) and <https://www.occ.gov/news->



Table 3.1: Reported PDs and Bank Capital.

	(i) PD	(ii) PD	(iii) PD-Gap	(iv) PD-Gap
Capital	0.10*** (0.04)	0.06** (0.03)	0.10** (0.04)	0.08*** (0.02)
Fixed Effects				
Firm $\times$ Time	✓	✓		
Time			✓	✓
Bank		✓		✓
Bank Controls	✓	✓	✓	✓
Portfolio Risk Controls		✓		✓
R-squared	0.80	0.80	0.00	0.01
Observations	412,537	401,790	419,060	407,362
Number of Firms	12,189	12,065	12,489	12,347
Number of Banks	32	32	32	32

**Notes:** Estimation results for regression (3.1), where the dependent variable is either given by  $PD_{i,j,t}$  in columns (i) and (ii) or by  $PD\text{-}Gap_{i,j,t}$  in columns (iii) and (iv). Bank controls: bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), and banks' income gap (see Table A.3 in Appendix A for details on the data). Portfolio risk controls: RWA/total assets, weighted portfolio PD. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2014:Q4-2020:Q4. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

stress tests also make use of the banks' own risk measures.<sup>15</sup> Institutions with low capital buffers may therefore have an incentive to underreport their credit risk exposure to increase the chance of passing the tests. And third, low-capitalized banks attract supervisory attention and may therefore window-dress their balance sheets to avoid further regulatory scrutiny (e.g., through on-site inspections). With these explanations in mind, we expect to find that  $\beta \leq 0$  when accounting for the business-model explanation and absent any regulatory incentives.

Table 3.1 reports the estimation results for various setups of regression (3.1). Columns (i) and (ii) use  $PD_{i,j,t}$  as a dependent variable, whereas columns (iii) and (iv) show the results for  $PD\text{-}Gap_{i,j,t}$  instead. To account for the business-model explanation, we include bank fixed effects and total portfolio risk controls into the regressions reported in columns (ii) and (iv).<sup>16</sup> Across the various specifications, we find that  $\beta$  is positive and statistically significant at either the 1 percent or the 5 percent confidence level. These results are also economically sizable. A 1 percentage point higher capital buffer is related to a 6-10 basis points higher PD of a bank's entire loan portfolio, a

issuances/bulletins/2018/bulletin-2018-33.html

<sup>15</sup>Specifically, banks' corporate loan ratings are one of the inputs that are used to compute potential losses under the various scenarios. These ratings are directly related to the PDs (see the Y14 data description, Appendix Table A.2). Starting in 2020:Q4, the bank-specific stress capital buffer requirement is also based on the outcome of the stress tests, providing an additional incentive for low-capitalized banks to underreport their credit risk exposures. Source: <https://www.federalreserve.gov/publications/files/2019-march-supervisory-stress-test-methodology.pdf>

<sup>16</sup>Following Plosser and Santos (2018), we use the ratio of risk-weighted assets to total assets and the PD of the total loan portfolio based on the average reported PDs of other banks, given by  $PD_{j,t} = \sum_i \bar{PD}_{i,t} Loan_{i,j,t} / \sum_i Loan_{i,j,t}$  where  $\bar{PD}_{i,t} = (1/K) \sum_k PD_{i,k,t}$  where  $k \neq j$ .

substantial effect given that the average PD across all loans is around 2.5 percent. The magnitude of the effects are also comparable to the ones by [Plosser and Santos \(2018\)](#) who estimate similar regressions for syndicated loans.

We interpret these findings as providing evidence that low-capitalized banks systematically underreport their credit risk exposure. The quantitative magnitude of our results are likely a lower bound for two reasons. First, the described alternative explanations may push  $\beta$  in the opposite direction, such that the effect originating from regulatory incentives may be even larger. Second, our findings are conservative if all banks are misreporting, even the ones with the largest capital buffers in our sample.<sup>17</sup>

### 3.3 PDs, Bank Capital, and Credit Supply

Next, we exploit these differential risk assessments and test whether they also result in lending distortions. Specifically, we are interested in whether low-capitalized banks not only understate their credit risk exposure, but also lend relatively more to underreported borrowers to reconcile their reporting and avoid losses. At a first pass, we analyze credit movements following the outbreak of COVID-19 in 2020:Q1, an adverse macroeconomic shock that was largely unexpected. For firm  $i$ , bank  $j$ , and loan type  $k$ , we estimate

$$\frac{L_{i,j,t+2}^k - L_{i,j,t}^k}{0.5 \cdot (L_{i,j,t+2}^k + L_{i,j,t}^k)} = \alpha_{i,t}^k + \beta_1 \text{Capital}_{j,t} + \beta_2 \text{Low-PD}_{i,j,t}^k + \beta_3 \text{Low-PD}_{i,j,t}^k \times \text{Capital}_{j,t} + \gamma X_{j,t} + u_{i,j,t}^k \quad (3.2)$$

where  $t$  denotes 2019:Q4 and we consider movements in credit  $L_{i,j,t}^k$  over two quarters. As a dependent variable, we use the symmetric growth rate as an approximation of a percentage change in credit.<sup>18</sup> Following [Khwaja and Mian \(2008\)](#), we include firm-time fixed effects  $\alpha_{i,t}^k$  into our regressions, therefore the sample is restricted to firms that borrow from multiple banks. This approach accounts for potential links between bank-firm selection and firm demand. The fixed effects control for credit demand under the assumption that firms have a common demand across their lenders.

The coefficients of interest  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  therefore capture credit supply effects, conditional on other bank-specific controls that are collected in the vector  $X_{j,t}$ . The variable  $\text{Capital}_{j,t}$  again denotes bank  $j$ 's CET1 capital buffer in period  $t$ .  $\text{Low-PD}_{i,j,t}^k$  is a binary indicator variable that takes the value of one if  $\text{PD}_{i,j,t}^k$  is lower than the average reported PDs by other banks for the same firm and zero otherwise.<sup>19</sup> The interpretation of  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  is as follows. If  $\beta_1 > 0$ , banks that are better capitalized lend relatively more to firms to which they assign high PDs. If  $\beta_2 > 0$ , banks with zero-capital buffers extend relatively more credit to firms if they also consider those firms to have relatively low PDs. Last, if  $\beta_3 < 0$ , lowering capital predicts a relative increase in lending

<sup>17</sup>Appendix B collects additional evidence. Table B.1 shows that our results extend to local projections that consider how PDs adjust following changes in bank capital buffers. Table B.2 illustrates that the positive relation between bank capital and PDs is driven by riskier credit types, such as loans with higher PDs, that are syndicated, and held by private firms.

<sup>18</sup>The symmetric growth rate is the second-order approximation of the log-difference for growth rates around zero. It is bounded in the range  $[-2,2]$ , robust to outliers, and is able to include changes in credit from a starting level of zero.

<sup>19</sup>That is,  $\text{Low-PD}_{i,j,t}^k$  is one if  $\text{PD}_{i,j,t}^k < \overline{\text{PD}}_{i,t}$ . After excluding credit lines as described in the text,  $\overline{\text{PD}}_{i,t} = (1/M)(1/K) \sum_m^M \sum_k^K \text{PD}_{i,m,t}^k$  is the average PD for firm  $i$  at time  $t$  across all non- $j$  lenders and loan types.

from low-PD banks in comparison with high-PD banks.

We restrict the sample in three additional ways. First, we exclude loans that are guaranteed by a third party since the associated PD may not be representative of the firm itself. Second, we consider only term loans and omit credit lines which were largely demand-driven after the COVID outbreak (Greenwald, Krainer and Paul, 2020). To account for the variation of credit line drawdowns across banks at the time, we also include the bank-specific ratio of unused credit lines to total assets before the outbreak into  $X_{j,t}$ . Third, we consider adjustable- and fixed-rate loans as separate types  $k$  since the demand for these loans may differ when short-term rates adjust suddenly and may be correlated with the bank-specific variables of interest.<sup>20</sup>

The estimation results for regression (3.2) are shown in Table 3.2. The first three columns introduce the regressors of interest sequentially. In column (iii),  $\beta_1$  and  $\beta_2$  are estimated to be positive, while  $\beta_3$  is negative, corresponding to the interpretation of the coefficients above.<sup>21</sup> The three coefficients are statistically different from zero at either the 5 percent or the 10 percent level. In comparison with columns (i) and (ii),  $\beta_1$  increases in magnitude and statistical significance, highlighting the importance of the interaction term that is included in column (iii).

Columns (iv)-(vi) consider alternative specifications that address several identification concerns. First, the demand for syndicated and non-syndicated loans may have changed during the COVID crisis as some firms may have chosen to borrow from their main relationship lender. In turn, the supply of these different types of credit may depend on bank capitalization and potentially relative risk assessments, leading us to interpret shifts in credit demand as supply effects. To account for this possibility, we extend  $\alpha_{i,t}^k$  by a loan's syndication type in column (iv). Similarly, if banks specialize in certain types of lending and firm demand across the lending types differs, then  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  may again capture demand rather than supply effects if such bank specialization is correlated with  $\text{Capital}_{j,t}$  or  $\text{Low-PD}_{i,j,t}^k$  (Paravisini, Rappoport and Schnabl, 2020). To address this possibility, we extend  $\alpha_{i,t}^k$  by categories of loan purposes that firms report in column (v).<sup>22</sup> The estimation results show that the findings actually strengthen in magnitude and statistical significance with the more granular fixed effects. Last, in column (vi), we include a bank fixed effect. While the impact of other bank characteristics cannot be estimated separately in the presence of such a fixed effect, our findings with respect to  $\beta_2$  and  $\beta_3$  remain intact. Taken together, our results show that bank capitalization and relative risk assessments jointly determine credit availability. Low-capitalized banks not only underreport their credit risk exposure but they also lend relatively more to underreported borrowers.

While the outbreak of COVID-19 represents a unique setting with a sharp adverse macroeconomic shock, the mechanism that we identify may not be specific to this episode but can also be present during other periods. To explore this possibility, we exploit the historical evolution of bank capital buffers that is specific to the sample for which our data are available. As shown in Figure

<sup>20</sup>To avoid that our results are explained by a possible switching effect between credit lines and term loans, as well as between loans that differ in the flexibility of interest rates, we exclude bank-firm pairs that cover multiple types. If a bank issues multiple loans of a single type to the same firm, then we aggregate these loans at each date.

<sup>21</sup>Appendix Figure C.1 provides a graphical illustration of the estimates in column (iv) of Table 3.2 over the range of the observed capital buffers in 2019:Q4 among the Y14-banks.

<sup>22</sup>Specifically, we consider the categories "Mergers and Acquisition," "Working Capital (permanent or short-term)," "Real estate investment or acquisition," and "All other purposes" as separate types (see also Appendix Table A.2).

Table 3.2: COVID-19 – Credit Supply.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	0.78 (0.59)	0.96 (0.70)	1.77* (0.86)	2.27** (0.92)	3.80*** (1.04)	
Low-PD		2.63* (1.51)	6.51** (2.74)	9.86*** (2.93)	11.56*** (2.70)	8.29** (3.44)
Capital $\times$ Low-PD			-1.23* (0.63)	-2.16*** (0.68)	-2.19** (0.78)	-1.43** (0.68)
Fixed Effects						
Firm $\times$ Rate	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn.				✓		
Firm $\times$ Rate $\times$ Pur.					✓	
Bank						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.53	0.53	0.53	0.53	0.55	0.55
Observations	892	667	667	612	510	663
Number of Firms	412	309	309	286	240	307
Number of Banks	24	23	23	21	23	21

**Notes:** Estimation results for regression (3.2). All specifications include firm fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls for 2019:Q4: bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2019:Q4 - 2020:Q2. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

3.1, the typical bank in our sample operates with a capital buffer of 3 percent or more in "normal times" such as during the early 2000s until the financial crisis of 2007-09, during which bank capital buffers sharply increased. In the following years, capital buffers remained elevated, possibly in anticipation of the higher capital requirements, which increased step-by-step from 2013:Q1 until the end of our sample, while bank capital ratios stayed high (see Appendix Figures C.2 and C.3). This allows us to split our sample into two parts: one running from 2014:Q4 to 2017:Q4 when typical capital buffers were relatively high (marked by the two vertical lines in Figure 3.1), and one starting in 2018:Q1 with typical capital buffers close to the ones in the early 2000s.<sup>23</sup>

For these two subsamples, we reestimate regression (3.2) and the results are shown in Tables 3.3 and 3.4. For the earlier sample with high capital buffers, the estimated coefficients are relatively small compared with the ones in Table 3.2, sometimes with opposite signs, and largely statistically insignificant. In contrast, for the later sample with low capital buffers, the estimated coefficients are slightly smaller in absolute magnitude but close to the ones in Table 3.2 and highly statistically significant. In comparison, Table 3.4 covers a substantially larger sample with close to

<sup>23</sup>We end the low capital buffer sample in 2020:Q2, such that the latest capital ratios that enter the estimations are the ones in 2019:Q4. This avoids that the capital ratios during the COVID crisis enter our analysis, which were subject to a number of regulatory changes to make it easier for banks to meet the requirements.

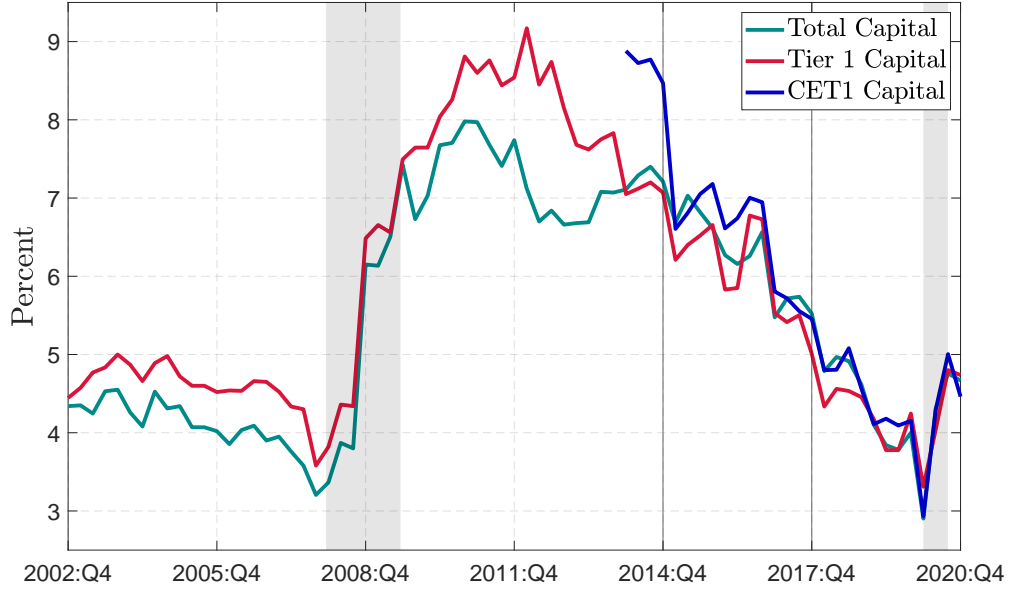


Figure 3.1: Bank Capital Buffers.

**Notes:** For each date, the figure shows the median of the CET1, Tier 1, and total capital buffer across the Y14-banks. Capital buffers are defined as the difference between capital ratios and requirements. Gray bars denote NBER recessions.

7,000 observations.<sup>24</sup> Overall, these results suggest that economies may be more prone to the documented lending distortions when the banking sector has relatively low *capital buffers*, but may be present even when banks have high *capital ratios*, such as the banks in our sample that were generally perceived to be "well-capitalized" around the onset of the COVID crisis.

Appendix C collects additional evidence and robustness checks of our findings for the extended "low-capital-buffer" sample. First, Table C.2 shows that the effects are not only present for loan quantities but also for interest rates. Second, we test whether our findings depend on the inclusion of the firm fixed effects. Table C.3 omits the firm-specific component of the fixed effect and Table C.4 uses time, location, industry, and firm-size fixed effects instead. Across the various alternative specifications, our results remain largely unchanged.<sup>25</sup> Third, we investigate whether our findings can be explained by an alternative channel, as opposed to the mechanism working through underreporting and lending distortions. For example, it may be the case that low-capitalized banks favor safer borrowers. To test for this hypothesis, we replace  $\text{Low-PD}_{i,j,t}^k$  with  $\text{PD}_{i,j,t}^k$  itself in regression (3.2). As shown in Table C.5, we do not find evidence that low-capitalized banks favor safer borrowers since the coefficient  $\beta_3$  is statistically not distinguishable from zero across the various regressions. Alternatively, it may be the case that lending supply is jointly determined by  $\text{Low-PD}_{i,j,t}^k$  and another bank characteristic. To account for this possibility, we include various interaction terms between  $\text{Low-PD}_{i,j,t}^k$  and the bank controls into regression (3.2). The estimation results in Table C.6 show that the original size and significance of the coefficient  $\beta_3$  remains much

<sup>24</sup>The results in Table 3.4 do not depend on the inclusion of the COVID episode but also hold for a shorter sample that excludes this period and ends in 2019:Q4 (see Appendix Table C.1).

<sup>25</sup>Even though these regressions increase the sample size in comparison with Table 3.4, they do not include firms that borrow from a single lender in our data. That is because we require a multi-bank sample to compute relative risk assessments and the variable  $\text{Low-PD}_{i,j,t}^k$ .

Table 3.3: High Capital Buffers – Credit Supply.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	-0.17 (0.29)	0.09 (0.25)	0.10 (0.32)	-0.19 (0.36)	0.40 (0.52)	
Low-PD		0.88 (0.80)	0.92 (1.87)	-1.22 (2.37)	-1.16 (4.12)	5.22** (2.18)
Capital $\times$ Low-PD			-0.01 (0.38)	0.26 (0.44)	0.27 (0.71)	-0.62 (0.39)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.54	0.55	0.55	0.56	0.55	0.58
Observations	10,309	6,606	6,606	6,135	3,160	6,535
Number of Firms	835	581	581	551	307	574
Number of Banks	32	26	26	26	25	23

**Notes:** Estimation results for regression (3.2). All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2014:Q4 - 2017:Q4. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

the same. Last, we include credit lines into our regressions. However, we consider loan commitments rather than used credit amounts to minimize the possibility that we pick up demand rather than supply effects. The estimated coefficients reported in Table C.7 are similar to our baseline results.

**Sample Splits.** Next, we return to the theoretical predictions based on the "Static Model" in Section 2. Accordingly, the lending distortions should be stronger for low-productivity firms with larger preexisting debt since relationship lenders have stronger incentives to keep such firms alive. To test whether that is the case, we split the sample in Table 3.4 into high- and low productivity firms and small and large loans. We use several measures of firm productivity: (i) return on assets (net income to total assets), (ii) an approximation of firm marginal revenue product of capital (MRPK, see Appendix D for details), and (iii) the average interest rate that firms pay on their total debt as a proxy for MRPK based on a typical optimality condition. The results are shown in Table 3.5. Consistent with our theory, we find that the results are explained by low-productivity firms and larger legacy debt. In contrast, the regression estimates for high-productivity firms and small loans are largely statistically insignificant.



Table 3.4: Low Capital Buffers – Credit Supply.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	0.18 (0.30)	0.17 (0.34)	0.95** (0.40)	1.13*** (0.40)	1.68** (0.64)	
Low-PD		0.63 (1.30)	5.46*** (1.89)	5.92*** (1.86)	6.82** (2.58)	5.24** (2.25)
Capital $\times$ Low-PD			-1.29*** (0.36)	-1.64*** (0.35)	-1.63** (0.63)	-1.14** (0.41)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.51	0.54	0.54	0.54	0.54	0.57
Observations	6,977	4,674	4,674	4,188	3,617	4,649
Number of Firms	683	495	495	455	396	491
Number of Banks	29	27	27	26	27	24

**Notes:** Estimation results for regression (3.2). All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2020:Q2. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

**Effects at the Firm Level.** In a last exercise, we test whether the lending distortions also persist at the firm level, affecting total firm debt and investment. To this end, we estimate

$$\frac{y_{i,t+2} - y_{i,t}}{0.5 \cdot (y_{i,t+2} + y_{i,t})} = \alpha_i + \tau_{m,t} + \beta_1 \widetilde{\text{Capital}}_{i,t} + \beta_2 \widetilde{\text{Low-PD}}_{i,t} + \beta_3 \widetilde{\text{Low-PD} \times \text{Capital}}_{i,t} + \gamma X_{i,t} + u_{i,t} \quad (3.3)$$

where  $y_{i,t}$  denotes an outcome for firm  $i$ ,  $\alpha_i$  is a firm fixed effect,  $\tau_{m,t}$  is an industry-time fixed effect, and  $X_{i,t}$  is a vector of firm controls. As dependent variables, we consider changes in total firm debt and fixed assets as an approximation for investment. The regressors associated with  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  represent exposures to bank capitalization and risk assessments that firms have through their term borrowing. That is, each regressor is defined as  $\tilde{R}_{i,t} = \sum_j R_{i,j,t} \times \text{Term Loan}_{i,j,t} / \text{Debt}_{i,t}$  where  $R_{i,j,t}$  is given by  $\text{Capital}_{j,t}$ ,  $\text{Low-PD}_{i,j,t}^k$ , or the interaction of the two, and firms' term-loan-to-debt ratios are used as weights to aggregate the exposures across lenders.<sup>26</sup>

<sup>26</sup>We note three details about regression (3.3). First, we include firm fixed effects to capture time-invariant firm-specific changes of debt and investment, and to estimate these effects consistently, we extend the estimation back to 2016:Q3 to allow for a sufficiently long sample covering four years of data. Second, the variable  $\text{Low-PD}_{i,j,t}^k$  takes either values of zero or one and the associated coefficients are only identified because of the relative size shares of term borrowing across lenders. Third, apart from the exclusion of credit lines, we lift all other sample restrictions in comparison with regression (3.2), such as the exclusion of bank-firm observations with multiple credit types.



Table 3.5: Low Capital Buffers – Sample Splits.

	(i) Low ROA	(ii) High ROA	(iii) Low MRPK	(iv) High MRPK	(v) Low Rate	(vi) High Rate	(vii) Large Loans	(viii) Small Loans
Capital	3.39*** (1.06)	0.54 (0.73)	3.51*** (1.02)	0.77 (0.83)	2.33** (0.98)	0.76 (0.90)	1.77 (1.08)	1.22 (0.96)
Low-PD	15.23** (6.57)	8.83* (4.46)	19.04*** (3.86)	9.29 (6.60)	17.18*** (5.06)	4.49 (4.03)	13.61*** (4.30)	8.49 (8.31)
Capital $\times$ Low-PD	-3.20*** (1.02)	-0.81 (1.06)	-3.87*** (0.97)	-1.25 (0.96)	-3.01*** (0.78)	-0.33 (0.75)	-2.77*** (0.85)	-1.02 (1.22)
Fixed Effects								
Firm $\times$ Rate $\times$ Time	✓	✓	✓	✓	✓	✓	✓	✓
Bank Controls	✓	✓	✓	✓	✓	✓	✓	✓
R-squared	0.56	0.64	0.56	0.67	0.61	0.56	0.51	0.69
Observations	632	618	674	653	640	633	549	547
Number of Firms	116	103	111	107	132	110	104	88
Number of Banks	24	20	24	23	24	23	22	20

**Notes:** Estimation results for regression (3.2). The samples are split at the median at time  $t$  according to the return on assets (ROA) in columns (i) & (ii), the MRPK in columns (iii) & (iv), the average interest rate in columns (v) & (vi), and the size of the loan relative to total firm debt in columns (vii) & (viii). All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2020:Q2. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

The estimation results for regression (3.3) are reported in Appendix Table C.8. Columns (ii) and (iv) show that the credit supply effects persist at the firm level and firms do not alter their credit across pre-existing or new lenders, such that their total debt adjusts by a similar amount as for the regressions reported in Table (3.4). These debt changes also translate into investment adjustments, indicating that firms do not alter other resources like their cash-holdings in response.

Taken together, our empirical results show that large U.S. banks with low capital buffers systematically underreport their credit risk exposure. To avoid potential losses and to reconcile their reporting, such banks favor underreported borrowers in their credit decisions, affecting real firm outcomes like investment. Consistent with the theoretical mechanism in Section 2, the lending distortions are only present among low-productivity firms and larger outstanding debt. Building on this empirical validation, we next embed the mechanism into a dynamic model to study whether such lending incentives also affect aggregate capital allocation, productivity, and output.

## 4 Dynamic Model

While the static model presented in section 2 is useful to understand the incentives of a non-anonymous lender in shaping the contract that is offered to a firm with pre-existing debt, that model is too simple to analyze the aggregate and equilibrium consequences of these lending incentives. In particular, we are interested in studying whether these lending incentives affect aggregate productivity through misallocation. To this end, we embed the basic mechanisms of the static model in a dynamic model with an endogenous distribution of firms that are heterogeneous

with respect to their productivity, holdings of physical capital, and debt. Importantly, the dynamic model model endogenizes firm entry and exit, as well as the joint distribution of physical and debt, which is essential to study misallocation in this context.

The structure of the dynamic model is based on the model developed by [Hopenhayn \(1992\)](#), augmented with debt and default. We first present the model set up and the problem of the firm. We then define a stationary industry equilibrium (SIE) for an arbitrary debt price function. We then proceed to describe two potential institutional arrangements, as in the static model, that give rise to different debt price functions and therefore to different SIE. Finally, we calibrate the model and compare equilibria under the two arrangements.

## 4.1 Set-up

**Environment.** Time is discrete and infinite,  $t = 0, 1, 2, \dots$ . The economy is populated by a continuum of firms whose mass is endogenous. The distribution of firms is denoted by  $\lambda(z, b, k)$ , where  $z$  denotes productivity,  $b$  is debt, and  $k$  is capital. There is endogenous firm entry and exit, with the mass of entrants being denoted by  $m$ . For now, we simply assume that the price of debt is described by some arbitrary function  $Q(z, b, k)$  that firms take as given. In the following sections, we present alternative institutional arrangements that provide microfoundations for this function. There is a fixed and constant supply of labor equal to  $\bar{N}$ , and the supply of physical capital is perfectly elastic. The wage rate  $w$  is endogenous, and the price of capital is constant and equal to 1.

**Timing.** The timing within each period is as follows:

1. Firm productivity  $z$  is realized
2. The lending contract  $Q$  is determined
3. Firm draws i.i.d. extreme value preference shocks  $\epsilon^P, \epsilon^D$ , choosing to default or not
4. Non-defaulting firms and new entrants invest, produce, repay, and borrow

Besides endogenous entry, a new feature with respect to the static model is the introduction of the i.i.d. preference shocks for the firm. This is done primarily for computational tractability as it smoothes the default/repayment decision.

## 4.2 Firm Problem

As in the static model, we assume that firms take the terms of the contract  $Q$  as given, and decide to repay, how much to borrow, and how much to invest. The firm has access to a decreasing returns to scale production technology with production function given by  $z^{1-\eta}(k^\alpha n^{1-\alpha})^\eta$ , where  $z, k$  are current productivity and capital, and  $n$  is labor.  $\alpha$  is the capital share and  $\eta$  is the degree of returns to scale. The firm hires labor at wage rate  $w$ , and can invest in new capital  $k'$  at a constant unit cost. Capital depreciates at rate  $\delta$ . Additionally, the firm pays a fixed cost of operation equal to  $c$ .

The firm's value, after receiving an offer  $Q$  and upon realizing the extreme value shocks  $\varepsilon^P, \varepsilon^D$  can be written as

$$V_0(z, b, k, \varepsilon^P, \varepsilon^D; Q) = \max \left\{ V^P(z, b, k; Q) + \varepsilon^P, 0 + \varepsilon^D \right\} \quad (4.1)$$

where  $V^P(z, b, k)$  is the value of repaying (net of the preference shock), and we normalize the value of default to zero. One way to motivate these preference shocks is as a stochastic outside option for the entrepreneur who runs the firm. We assume that these shocks follow a type I extreme value distribution (Gumbel), which implies that the difference between the two  $\varepsilon = \varepsilon^P - \varepsilon^D$  follows a logistic distribution with scale parameter  $\kappa$ . This has the following implications:

1. Conditional on today's states and the offered contract  $(z, b, k; Q)$ , we can write the probability of repayment as

$$\mathcal{P}(z, b, k; Q) = \frac{\exp \left[ \frac{V^P(z, b, k; Q)}{\kappa} \right]}{1 + \exp \left[ \frac{V^P(z, b, k; Q)}{\kappa} \right]} \quad (4.2)$$

2. Conditional on today's states and the offered contract  $(z, b, k; Q)$ , we can write the expected value as

$$\mathcal{V}(z, b, k; Q) = \mathbb{E}_{\varepsilon^P, \varepsilon^D} V_0(z, b, k, \varepsilon^P, \varepsilon^D; Q) = \kappa \log \left\{ 1 + \exp \left[ \frac{V^P(z, b, k; Q)}{\kappa} \right] \right\} \quad (4.3)$$

The value of repaying conditional on today's state  $s = (z, b, k)$  and offered contract  $Q$  is given by

$$V^P(z, b, k; Q) = \max_{b', k', n} \text{div} - \mathbb{I}[\text{div} < 0][e_{con} + e_{slo} \times \text{div}^2] + \beta^f \mathbb{E}_{z'}[\mathcal{V}(z', b', k')|z] \quad (4.4)$$

s.t.

$$\text{div} = z^{1-\eta}(k^\alpha n^{1-\alpha})^\eta - wn - k' + (1 - \delta)k + Qb' - b - c \quad (4.5)$$

$$b' \leq \theta k' \quad (4.6)$$

$$k', b', n \geq 0 \quad (4.7)$$

The value of repayment is equal to current dividends  $\text{div}$  plus the continuation value, which is given by the expectation of 4.3 over productivity in the next period  $z'$ , conditional on productivity today  $z$ . Additionally, the firm is subject to equity issuance costs, which consist of a fixed cost component  $e_{con}$  and a quadratic cost scaled by  $e_{slo}$ . Equation 4.5 defines the firm dividend: it is equal to the value of production, minus the wage bill, minus new investment net of undepreciated capital, plus new borrowings, minus debt repayments and minus the fixed cost. Equation 4.6 is the borrowing constraint, which states that repayments on newly borrowed debt may not exceed a fraction of newly chosen capital. Finally, 4.7 is a non-negativity constraint on the choices of debt, capital, and labor.

**Characterizing the Firm's Problem.** For simplicity and tractability, let us ignore for now the fixed cost of equity issuance, which introduces a non-differentiability in the firm's problem,  $e_{con} = 0$ . Let  $\mu(div) \equiv 1 + 2e_{slo} \max\{0, -div\}$  denote the marginal value of equity for the firm, and let  $\lambda$  denote the Lagrange multiplier on the borrowing constraint. Let  $\pi(z, k)$  denote the profit function at the optimal labor choice:

$$\pi(z, k) = \max_n z^{1-\eta} (k^\alpha n^{1-\alpha})^\eta - wn. \quad (4.8)$$

Then, the firm's FOC are

$$\begin{aligned} k' : \beta^f \mathbb{E}_{z'} \{ \mathcal{P}(z', b', k') \pi_k(z', k') [1 + \mu(div')] \} - [1 + \mu(div)] + \lambda \theta &\leq 0, \\ b' : -\beta^f \mathbb{E}_{z'} \{ \mathcal{P}(z', b', k') [1 + \mu(div')] \} + Q[1 + \mu(div)] - \lambda &\leq 0. \end{aligned}$$

When the borrowing constraint binds, we can write the FOC for capital as

$$\mathbb{E}_{z'} \left\{ \mathcal{P}(z', b', k') \left( \beta^f \frac{1 + \mu(div')}{1 + \mu(div)} \right) [\pi_k(z', k') - \theta] \right\} = 1 - \theta Q. \quad (4.9)$$

This condition establishes a relationship between the choice of capital  $k'$  and the price of debt  $Q$ . In particular,  $\pi_k(z', k')$  is related to the marginal product of capital next period and is decreasing in  $k'$ . This means that, as long as the constraint binds, firms that receive better lending terms (higher  $Q$ ) will tend to choose more capital  $k'$ , everything else constant. This is the dynamic version of the expression that established a tight link between the MPK and  $Q$  in the static model. As long as the constraint is binding, this also means that such firms will borrow more, since  $b' = \theta k'$ .

Now, when does the constraint bind? Rewrite the FOC for  $b'$  as

$$\lambda \geq Q[1 + \mu(div)] - \beta^f \mathbb{E}_{z'} \{ \mathcal{P}(z', b', k') [1 + \mu(div')] \}. \quad (4.10)$$

This condition states that the constraint will tend to bind when the offered price of debt  $Q$ , adjusted by the marginal value of equity today, is relatively high compared to the cost of repayment, which is adjusted by the probability of repayment and by the marginal value of equity tomorrow. Thus the constraint is also more likely to bind when the marginal value of equity is high today relative to tomorrow.

### 4.3 Entry and Industry Equilibrium

**Firm Entry** Let  $\Gamma(z)$  denote the exogenous distribution from which potential entrants draw their starting productivity level. New entrants have to pay a fixed cost  $\omega$  to take a productivity draw and start operating. The free-entry condition for firms reads

$$\mathbb{E}_\Gamma [\mathcal{V}(z', 0, 0)] = \omega \quad (4.11)$$

**Firm Distribution and Law of Motion** Let  $\lambda(z, b, k)$  be the distribution of firms after entry and exit have taken place. Then, the law of motion for the distribution is given by

$$\lambda(z', b', k') = \int_{z, b, k} \Pr(z'|z) \mathbb{I}[b'(z, b, k) = b'] \mathbb{I}[k'(z, b, k) = k'] \mathcal{P}(z, b, k) d\lambda(z, b, k) + m \int_z \Gamma(z) \Pr(z'|z) \mathbb{I}[b'(z, 0, 0) = b'] \mathbb{I}[k'(z, 0, 0) = k'] \mathcal{P}(z, 0, 0) dz, \quad (4.12)$$

where  $\mathbb{I}$  is the indicator function, equal to 1 if the condition in brackets is satisfied and 0 otherwise, and  $m$  is the mass of new entrants.

**Labor Market Equilibrium** The mass of entrants in each period must be such that the total amount of labor that is demanded by active firms equals the exogenous labor supply:

$$\bar{N} = \int_{z, b, k} \mathcal{P}(z, b, k) n(z, b, k) d\lambda(z, b, k) \quad (4.13)$$

**Stationary Industry Equilibrium** Given a contract function  $Q(z, b, k)$ , a stationary industry equilibrium (SIE) is a collection of policy and value functions  $(k^p, b^p, V^p)$  as well as an equilibrium wage  $w$  and a stationary distribution  $\lambda(z, b, k)$  as well as a mass of entrants  $m$  such that:

1. The policy and value functions solve the firm's problem in 4.4 given the lending function  $Q$  and the wage rate  $w$
2. The wage rate  $w$  ensures that the free-entry condition 4.11 is satisfied.
3.  $\lambda$  satisfies the law of motion in 4.12.
4. The mass of entrants is such that the labor market clears as in 4.13.

Note that we define a SIE given an arbitrary function for the price of debt  $Q(z, b, k)$ . The exact nature of how this function is specified is not crucial for the definition of the equilibrium, as long as firms take  $Q$  as given when solving their problem. We now explore two different institutional arrangements for the credit market that give rise to two different  $Q$  functions, and study the properties of the SIE under each of those.

## 4.4 Competitive Lending

The first institutional arrangement consists of a purely competitive credit market. We assume that there is a large mass of lenders. The payoff of lending to a firm with states  $s = (z, b, k)$  at price  $Q$  is given by

$$W(z, b, k) = \mathcal{P}(z, b, k; Q) \left[ b - Qb' + \beta^k \mathbb{E}_{z'}[W(z', b', k')|z] \right], \quad (4.14)$$

where we assume that there is a zero payoff in case of default. If the firm does not default, with probability  $\mathcal{P}(z, b, k; Q)$ , the lender recovers the repayment amount  $b$ , offers new lending  $Qb'$ , and obtains the continuation value of the contract  $\beta^k \mathbb{E}_{z'}[W(z', b', k')|z]$ , appropriately discounted. With complementary probability, the firm defaults and the lender earns nothing.

In the competitive lending economy, lenders cannot optimize with respect to the price  $Q$ . This price is determined by a free-entry condition for lenders: there is a large mass of potential lenders who are willing to lend to the firm with states  $s = (z, b, k)$ . Their indifference condition pins down the competitive debt price for this firm,  $Q^{compet}(z, b, k)$ . Formally,

$$\begin{aligned} Q^{compet}(z, b, k) : W(z, 0, k) &= 0, \forall (z, b, k) \\ \Rightarrow Q^{compet}(z, b, k) &= \frac{1}{b'} \left\{ \beta^k [\mathbb{E}_{z'} W(z', b', k') | z] \right\}. \end{aligned}$$

Note that this price does not explicitly depend on the current levels of debt and capital, only through the firm's policy functions. In particular, this price of debt does not depend on the today's default decision and depends only on future default. Furthermore, by imposing the indifference condition on 4.14, we can write

$$W(z, b, k) = \mathcal{P}(z, b, k; Q) [b + W(z, 0, k)] = \mathcal{P}(z, b, k; Q) b,$$

which in turn allows us to write the competitive price as

$$Q^{compet}(z, b, k) = \frac{1}{b'} \left\{ \beta^k \mathbb{E}_{z'} [\mathcal{P}(z', b', k') b' | z] \right\} = \beta^k \mathbb{E}_{z'} [\mathcal{P}(z', b', k')]. \quad (4.15)$$

This simply states that the competitive price of debt is equal to the discounted probability of repayment.

## 4.5 Relationship Lending

The second type of credit market that we study is one where lenders internalize the possibility of default on current claims  $b$  when choosing lending terms, and have some degree of market power over  $Q$ . There is still a large mass of potential lenders that may offer alternative contracts to the firm, which limits the degree of market power that the relationship lender can exercise. The starting point for the relationship lender's problem is the same payoff function as in 4.14, where we abbreviate  $s = (z, b, k)$ :

$$W(s) = \max_Q \mathcal{P}(s; Q) \left[ b - Qb'(s; Q) + \beta^k \mathbb{E}_{z'} [W(z', b'(s; Q), k'(s; Q)) | z] \right] \quad (4.16)$$

$$\text{s.t.} \quad V^P(s; Q) \geq V^P(s; Q^{zero}(z, b', k')) \quad (4.17)$$

There are two key differences from the competitive lender case: first, the relationship lender can optimize over  $Q$ , and so takes into account the effects of changing  $Q$  on the firm's probability of default (through the firm's value) as well as on the firm's policies. Second, this choice of  $Q$  is subject to a participation constraint, given by equation 4.17. This constraint states that the value for the firm of accepting the contract offered by the relationship lenders must be at least as large as the value of borrowing the same amount from a different new lender. This value is defined as the value of the firm that borrows and invests the same amount, but is instead offered price

$Q^{zero}(z, b', k')$ , which is the price of debt that generates zero profits for a new lender

$$\begin{aligned} -Q^{zero}b' + \beta^k \mathbb{E}_{z'}[W(z', b', k')|z] &= 0 \\ \Leftrightarrow Q^{zero}(z, b', k') &= \frac{\beta^k \mathbb{E}_{z'}[W(z', b', k')|z]}{b'} \end{aligned} \quad (4.18)$$

Note that this function maps arbitrary firm policies  $(b', k')$  into a price of debt that is consistent with zero profits for a new lender, but that does not necessarily have to be an equilibrium price.<sup>27</sup> It is straightforward to show that  $\frac{\partial V^P}{\partial Q} = b' \geq 0$ , which allows us to rewrite the participation constraint as

$$Q \geq Q^{zero}(z, b'(s; Q), k'(s; Q)) \quad (4.19)$$

Combining 4.18 with 4.16, we can then rewrite the problem of the relationship lender as

$$\begin{aligned} W(s) &= \max_Q \mathcal{P}(s; Q) \{b - b'(s; Q) [Q - Q^{zero}(z, b'(s; Q), k'(s; Q))]\} \\ \text{s.t.} \quad Q &\geq Q^{zero}(z, b'(s; Q), k'(s; Q)) \end{aligned}$$

This simplified formulation of the relationship lender's problem highlights the key tradeoffs very clearly: on one hand, the lender would like to exploit its market power to extract as much surplus from the relationship as it can. This induces the lender to reduce  $Q$  by as much as possible, but the lender is constrained in its ability to do this by the outside option  $Q^{zero}$ . On the other hand, the lender also understands that  $Q$  affects the probability of survival today  $\mathcal{P}(s; Q)$  and hence the likelihood of  $b$  being repaid. This induces the lender to potentially offer a  $Q$  that is strictly higher than the one that the firm could obtain by borrowing the same amount from a new lender.

As with the static model, it may be that the solution to 4.16 yields a value that is lower than that of not lending to the firm. In this case, the firm has to borrow from a new lender at price  $Q^{out}(s)$  that solves

$$Q^{out}(s) : Q^{zero}[z, b'(s; Q^{out}), k'(s; Q^{out})] = Q^{out}$$

and the bank's payoff is  $\mathcal{P}(s; Q^{out}(s))b$ .

## 4.6 Calibration

We now discuss the calibration of the model, which we use to solve the model under the two alternative credit market arrangements. Table 4.1 presents the calibration of the model, and table 4.2 compares moments from the SIE of the model under competitive lending, which we take to be the benchmark case, to moments from the data and the literature. We assume that firm productivity follows an AR(1) process in logs,

$$\log z' = \mu_z + \rho_z \log z + \sigma_z \epsilon_z \quad (4.20)$$

Our calibration is annual. We set the firm discount factor  $\beta = 0.90$  and the borrowing con-

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<sup>27</sup>The equilibrium would be one point along the  $Q^{zero}$  schedule, where  $Q^{zero}[z, b'(s; Q), k'(s; Q)] = Q$ .



straint parameter  $\theta = 0.7$  to match average book and market leverage of 0.67 and 0.29, respectively, taken from [Gomes and Schmid \(2010\)](#). The depreciation rate is set to a standard annual value  $\delta = 0.09$ , which means that our investment rate slightly undershoots that in Compustat. The scale parameter  $\kappa$ , the fixed cost  $\mathbf{c}$ , and the distribution of new entrants  $F^e$  are chosen to match average exit rates over the last 40 years for all firms (0.09) and for new entrants (0.25), from [Hopenhayn, Neira and Singhania \(2018\)](#). This distribution is assumed to be uniform between 0 and  $\tilde{z} = 1.483$ . The equity issuance cost parameters are chosen to target the frequency and size of equity issuances, from [Gomes and Schmid \(2010\)](#) and [Hennessy and Whited \(2007\)](#), respectively. The production function parameters  $(\alpha, \eta)$  are standard and taken from the literature. The parameters for the TFP process are taken from [Gourio and Miao \(2010\)](#), with  $\mu_z = 0$ . Finally, the discount factor of lenders to target a risk-free rate of 3%, which is a standard value, and the entry cost  $\omega$  is chosen to normalize the wage to  $w = 1$  in the benchmark case of competitive lending.

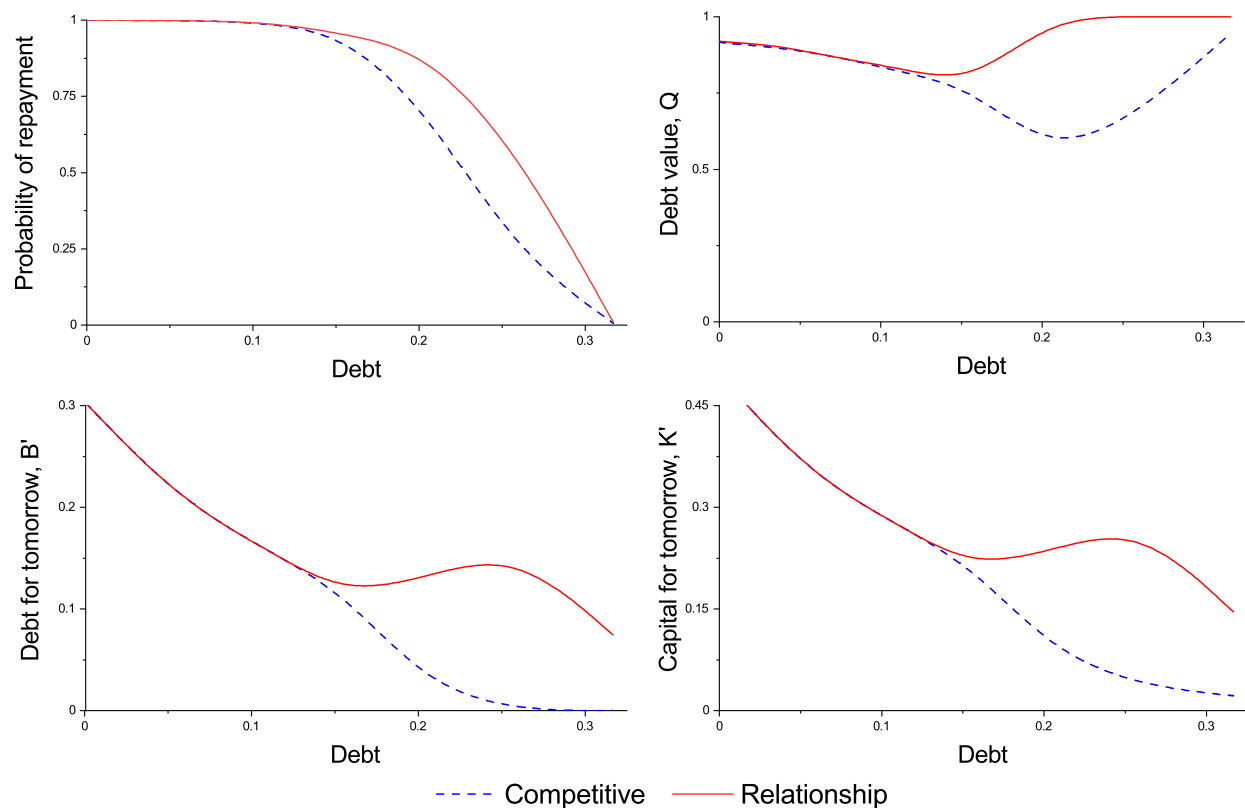
Table 4.1: Model Parameters and Values

Parameter	Value	Basis
$\beta^f$	0.900	Fit targets
$\theta$	0.700	Fit targets
$\kappa$	0.125	Fit targets
$e_{constant}$	0.100	Fit targets
$e_{slope}$	40.00	Fit targets
$\mathbf{c}$	0.125	Fit targets
$\tilde{z}$	1.483	Fit targets
$\omega$	0.344	Normalize $w = 1$
$\rho_z$	0.767	<a href="#">Gourio and Miao (2010)</a>
$\sigma_u$	0.211	<a href="#">Gourio and Miao (2010)</a>
$\eta$	0.800	<a href="#">Clementi and Palazzo (2016)</a>
$\beta^k$	0.971	Standard
$\alpha$	0.330	Standard
$\delta$	0.09	Standard

Table 4.2: Model Moments vs. Literature and Data

Moment	Data	Model	Source
Book leverage	0.67	0.54	<a href="#">Gomes and Schmid (2010)</a>
Market leverage	0.29	0.30	<a href="#">Gomes and Schmid (2010)</a>
Investment/Assets <sup>28</sup>	0.16	0.09	Compustat
Exit rate	0.09	0.09	<a href="#">Hopenhayn, Neira and Singhania (2018)</a>
Exit rate, new firms	0.25	0.25	<a href="#">Hopenhayn, Neira and Singhania (2018)</a>
Freq of equity issuance	0.09	0.10	<a href="#">Gomes and Schmid (2010)</a>
Size of equity issuance	0.09	0.17	<a href="#">Hennessy and Whited (2007)</a>

Figure 4.1: Policy functions and values for a firm with the same set of  $(z, k)$ , as a function of  $b$ , competitive lending (blue, dashed) vs. relationship lending (red, solid) economies

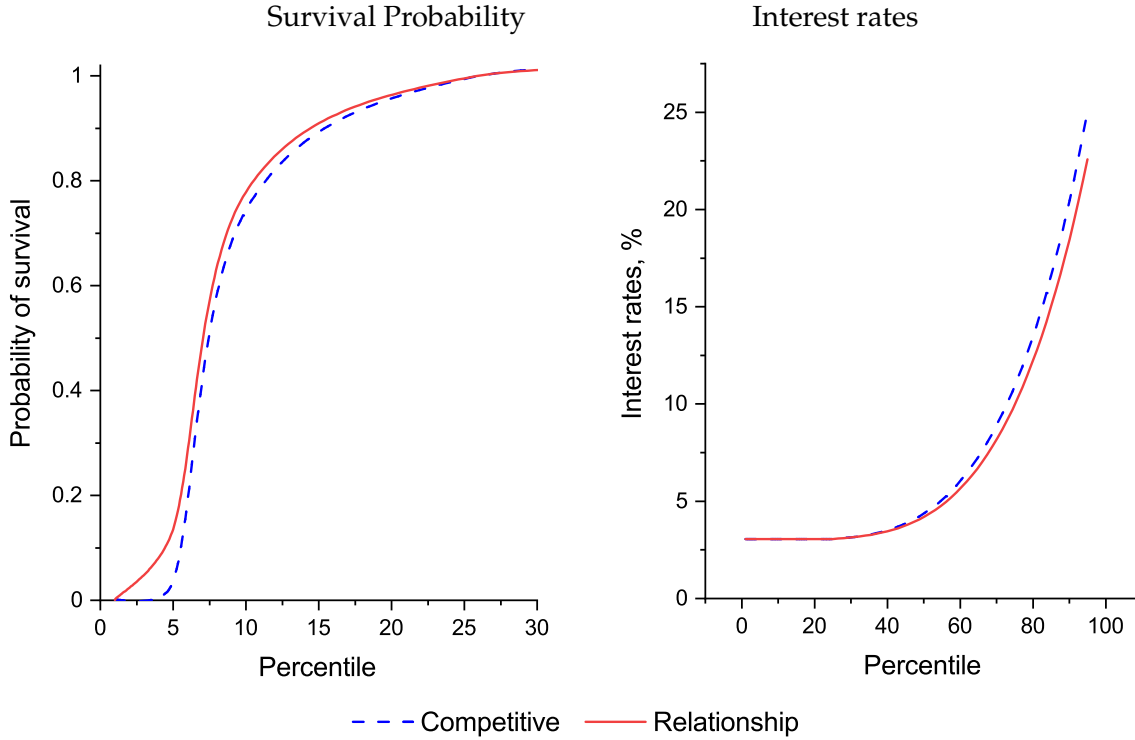


#### 4.7 Firm choices and equilibrium debt prices

Figure 4.1 plots policy and value functions for a firm with the same  $(z, k)$  in the two economies, as a function of pre-existing debt  $b$ . We begin by describing the competitive case, where results are perhaps more standard and intuitive (blue dashed lines): the firm's value is strictly decreasing in  $b$ , which means that the probability of repayment will also be strictly decreasing (first panel). Similarly,  $k'$  (fourth panel) is strictly decreasing: firms with more debt are more likely to realize negative profits, forcing them to issue equity at a cost. When the marginal value of equity is high, investment is lower, as it becomes particularly costly in that specific state. Less investment implies less borrowing too, as shown in the third panel, thanks to the borrowing constraint. Finally, the second panel plots the equilibrium price  $Q^{compet}(z, b, k)$ : as debt increases, investment falls, which raises the probability of default in the following period, making the competitive price also fall. At some point, the equilibrium price rises slightly as the firm essentially stops borrowing but is still investing (and so the forward-looking competitive price perceives the firm as relatively safe).

The red lines correspond to the same policy functions under relationship lending. For low enough debt, the policies are essentially the same, but after a certain point they begin diverging. In particular, the second panel shows that, instead of falling, the price of debt starts rising with more debt. This reflects the subsidy given by lenders who are attempting to prevent the firm from

Figure 4.2: Equilibrium CDFs for Survival Probability and Interest Rates



defaulting. The price function is discontinuous: after a certain point, the required subsidy to keep the firm alive is so high that the lender prefers to liquidate/abandon the borrower. In this case, this happens when the probability of repayment becomes zero. As the 3rd and 4th panels show, this subsidization affects firm choices of capital and debt, which are larger than in the competitive case. The effects of the subsidy are also visible in the first panel, as the firm becomes more likely to repay its debt when subsidized.

#### 4.8 Aggregate Effects

We now compare the SIE for the two economies, as described in section 4.3. The wage rate  $w$  in each economy is adjusted so that the free-entry condition 4.11 is satisfied, and the distribution for each economy is computed by solving for the stationary distribution as the fixed point of 4.12. The mass of entrants  $m$  is then computed to ensure that the stationary distribution  $\lambda$  is such that the labor market clears.

**Distributions and the Identification of Zombies** Figure 4.2 plots cumulative distribution functions for the survival probability and interest rates in the SIE for the competitive lending (CLEE) economies. The survival probability CDF for the RLE first-order stochastically dominates the CDF for the CLE. In other words, firms are uniformly less likely to exit in the RLE: this arises from the equilibrium effects of interest subsidization, and the fact that relationship lenders optimize to try to recover their pre-existing liabilities. The subsidy is visible in the second panel, where we show that the distribution of interest rates in the CLE first-order stochastically dominates that of the

RLE. That is, interest rates are uniformly lower in the RLE than in the CLE, across the firm distribution. One interesting take away from this second panel is that the interest rate subsidization appears to occur primarily for firms that are paying relatively high interest rates. In particular, we do not observe a large discrepancy between the two CDFs for low levels of interest rates. This means that the firms that are effectively being subsidized tend to be so at rates that are relatively high. We believe that this has implications for the empirical literature on zombie lending and identification of zombie firms. In our model, “zombies”, defined as firms that are receiving a subsidy from the lender, are paying interest rates that are below the fair level that would otherwise be offered in a competitive credit market. This subsidization tends to occur particularly when this benchmark is particularly high, therefore we do not really observe these firms paying negative interest rates, or interest rates that are below some risk-free rate. This suggests that attempts to identify zombies based on comparisons between measures of funding costs and aggregate interest rate benchmarks are likely to severely underestimate the number of firms that are actually being subsidized.

Table 4.3: Stationary equilibrium results for competitive and relationship economies.

Parameter	Competitive	Relationship	$\Delta\%$
<i>Averages</i>			
Market leverage	0.363	0.382	5.050
Book leverage	0.513	0.531	3.522
Interest rate	5.180	5.147	-0.643
Average capital	2.563	2.568	0.167
Average productivity	1.170	1.164	-0.486
Average output	1.467	1.456	-0.749
<i>Aggregates</i>			
Aggregate labor	1.000	1.000	0.000
Aggregate TFP	1.257	1.254	-0.273
Aggregate capital	3.257	3.288	0.975
Aggregate output	1.863	1.864	0.050
Aggregate debt	2.092	2.120	1.357
Wage	0.9995	1.000	0.048
Exit rate	0.087	0.084	-3.343

**Aggregate Moments** Table 4.3 presents some moments from the SIE in each of the economies, as well as the percentage difference between the RLE and the CLE. The first part of the table corresponds to averages across firms. It shows that the average firm in the RLE economy is more leveraged, pays a lower interest rate, is larger (in terms of capital), and less productive. On average, output is lower as the productivity decrease offsets the larger stock of capital. The second part of the table presents aggregates. By construction, aggregate labor is constant across economies. The RLE has lower aggregate TFP, more capital, and more debt. While aggregate output is slightly higher, this increase is relatively smaller than that of capital, which results in lower aggregate TFP

due to factor misallocation. Additionally, the wage rate is slightly higher in the RLE, which is a consequence of the fact that firm values are higher everything else constant, and the exit rate is lower. This last fact is another manifestation of the fact that the distribution of survival rates in the RLE first-order stochastically dominates that of the CLE.

## 5 Conclusion

In this paper we developed a simple model of relationship lending where lenders have an incentive to offer better terms to their borrowers so as to prevent default, a practice known as the evergreening of loans. We show that this phenomenon can arise in a stylized model without having to resort to traditional frictions such as asymmetric information or moral hazard, risk-shifting or gambling for resurrection on the part of the lender. More indebted and less productive firms are more likely to be subsidized through evergreening; since these subsidies affect the firm's decision to invest, this phenomenon may result in overinvestment by these firms and therefore in capital misallocation. Importantly, this phenomenon is distinct from debt overhang, which would result in underinvestment by indebted or less productive firms. We then used a loan-level supervisory dataset for the U.S. to provide empirical evidence for the existence of this phenomenon. Contrary to the rest of the literature, which has focused on crisis economies such as Japan or the Eurozone, we empirically documented that this phenomenon seems to exist in an apparently healthy and stable financial system, such as that of the U.S.. We showed that banks with lower capital buffers, who have greater incentives to evergreen, systematically underreport the probabilities of default of their borrowers, and tend to extend more credit and at better terms to these underreported borrowers. These borrowers tend to have larger outstanding loans and are less productive according to standard measures, which is in line with the predictions of the theoretical model. We then embedded the evergreening mechanism presented in the simple model in an otherwise standard model of industry dynamics augmented with corporate finance features: debt, costly equity issuance, and default. The dynamic model endogenizes the joint distribution of capital and debt, and allows us to study the effects of evergreening on macroeconomic aggregates, such as capital, debt, and productivity. We compare equilibria in two types of economies, one where lenders are competitive and have no incentives to evergreen, and another where lenders form relationships with borrowers and may have incentives to offer subsidized lending terms. We find that the equilibrium in the relationship economy features larger firms that are less productive and that borrow more at lower interest rates. Additionally, the economy is less dynamic as it features less exit and has lower aggregate TFP. This illustrates that evergreening may have macroeconomic consequences as it contributes to the misallocation of factor inputs. Finally, we use the dynamic model to argue that standard methods of identifying zombie firms based on comparing their funding costs to benchmark interest rates may underestimate the extent of this phenomenon, as much of evergreening occurs for risky firms that pay relatively high interest rates on their debt.

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# APPENDIX

## A Data

In Tables A.1-A.3, we provide names, definitions, and sources for all variables that are used in the empirical analysis. Table A.1 collects all variables that are used from Compustat, A.2 the ones from the FR Y-14Q H.1 data, and Table A.3 the variables from the FR Y-9C Filings. Section A.1 lists the sample restrictions and filtering steps that we apply.

Table A.1: Compustat Variable Definitions.

Variable Name	Description	Compustat Name
Total Assets	Total firm assets	atq
Cash and Short-Term Investments	Cash and short-term investments	cheq
Tangible Assets	Constructed from cash, fixed assets, receivables, and inventories	cheq + invtq + ppentq + rectq
Employer Identification Number	Used to match to TIN in Y14, successful merges are basis for publicly traded designation	ein
Total Liabilities	Total firm liabilities	ltq
Net Income	Firm net income (converted to 12-month trailing series)	niq
Total Debt	Debt in current liabilities + long-term debt	dlcq + dlttq
Sales	Total firm sales	saleq
Fixed Assets	Net property, plant, and equipment	ppentq

**Notes:** All data are obtained from the Wharton Research Data Services. Nominal series are converted into real series using the consumer price index for all items taken from St. Louis Fed's FRED database.

Table A.2: FR Y-14 Variable Definitions.

Variable Name	Description / Use	Field No.
Zip code	Zip code of headquarters	7
Industry	Derived 2-Digit NAICS Code	8
TIN	Taxpayer Identification Number	11
Internal Credit Facility ID	Used together with BHC and previous facility ID to construct loan histories	15
Previous Internal Credit Facility ID	Used together with BHC and facility ID to construct loan histories	16
Term Loan	Loan facility type reported as Term Loan, includes Term Loan A-C, Bridge Loans, Asset-Based, and Debtor in Possession.	20
Credit Line	Loan facility type reported as revolving or non-revolving line of credit, standby letter of credit, fronting exposure, or commitment to commit.	20
Purpose	Credit facility purpose	22
Committed Credit	Committed credit exposure	24
Used Credit	Utilized credit exposure	25
Line Reported on Y-9C	Line number reported in HC-C schedule of FR Y-9C	26
Participation Flag	Used to determine whether a loan is syndicated	34
Variable Rate	Interest rate variability reported as “Floating” or “Mixed”	37
Interest Rate	Current interest rate	38
Guarantor Flag	Used to determine whether a loan is guaranteed	44
Date Financials	Financial statement date used to match firm financials to Y-14 date	52
Net Sales Current	Firm sales over trailing 12-month period	54
Operating Income	Used for operation surplus = operating income + depreciation & amortization	56
Depreciation & Amortization	Used for operation surplus = operating income + depreciation & amortization	57
Interest Expense	Used in calculating average interest rate on all debt	58
Net Income	Current net income for trailing 12-months used to construct return on assets	59, 60
Cash and Securities	Cash and marketable securities	61
Tangible Assets	Tangible assets	68
Fixed Assets	Fixed assets	69
Total Assets	Total assets, current year and prior year	70
Short Term Debt	Used in calculating total debt	74
Long Term Debt	Used in calculating total debt	78
Total Liabilities	Total liabilities	80
Probability of Default	Probability of default for firms (corresponds to internal risk rating for non-advanced BHCs)	88
Syndicated Loan	Syndicated loan flag	100

**Notes:** Nominal series are converted into real series using the consumer price index for all items taken from St. Louis Fed’s FRED database. The corresponding “Field No.” can be found in the data dictionary (Schedule H.1, pp. 162-217): [https://www.federalreserve.gov/reportforms/forms/FR\\_Y-14Q20200331\\_i.pdf](https://www.federalreserve.gov/reportforms/forms/FR_Y-14Q20200331_i.pdf)

Table A.3: Variables from Y-9C filings.

Variable Code	Variable Label
BHCK 2170	Total Assets
BHCK 2948	Total Liabilities
BHCK 4340	Net Income
BHCK 3197	Earning assets that reprice or mature within one year
BHCK 3296	Interest-bearing deposit liabilities that reprice or mature within one year
BHCK 3298	Long-term debt that reprices within one year
BHCK 3408	Variable-rate preferred stock
BHCK 3409	Long-term debt that matures within one year
BHDM 6631	Domestic offices: noninterest-bearing deposits
BHDM 6636	Domestic offices: interest-bearing deposits
BHFN 6631	Foreign offices: noninterest-bearing deposits
BHFN 6636	Foreign offices: interest-bearing deposits
BHCK JJ33	Provision for loan and lease losses
BHCA P793	Common Tier 1 Capital Ratio

**Notes:** The table lists variables that are collected from the Consolidated Financial Statements or FR Y-9C filings for Bank-Holding Companies from the Board of Governors' National Information Center database. The one-year income gap is defined as  $(BHCK\ 3197 - (BHCK\ 3296 + BHCK\ 3298 + BHCK\ 3408 + BHCK\ 3409)) / BHCK\ 2170$ . Total deposits are given by  $(BHDM\ 6631 + BHDM\ 6636 + BHFN\ 6631 + BHFN\ 6636)$ . Nominal series are converted into real series using the consumer price index for all items taken from St. Louis Fed's FRED database. The FR Y-9C form for March 2020 can be found at: [https://www.federalreserve.gov/reportforms/forms/FR\\_Y-9C20200401\\_f.pdf](https://www.federalreserve.gov/reportforms/forms/FR_Y-9C20200401_f.pdf).

## A.1 Sample Restrictions and Filtering Steps

1. We restrict the sample to begin in 2012:Q3. The Y14 collection began in 2011:Q3, but there was a significant expansion in the number of BHCs required to submit Y14 commercial loan data until 2012:Q3. Moreover, the starting date in 2012:Q3 also affords a short phase-in period for the structure of the collection and variables to stabilize.
2. We constrain the sample to loan facilities with line reported on the HC-C schedule in the FR Y9-C filings as commercial and industrial loans, “other” loans, “other” leases, and owner-occupied commercial real estate (corresponding to Field No. 26 in the H.1 schedule of the Y14 to be equal to 4, 8, 9, or 10; see Table A.2). In addition, we drop all observations with NAICS codes 52 and 53 (loans to financial firms and real estate firms).
3. Observations with negative or zero values for committed exposure, negative values for utilized exposure, and with committed exposure less than utilized exposure are excluded.
4. When aggregating loans at the firm-level, we exclude observations for which the firm identifier “TIN” is missing. To preserve some of these missing values, we fill in missing TINs from a history where the non-missing TIN observations are all the same over a unique facility ID.
5. When using information on firms’ financials in the analysis, we apply a set of filters to ensure that the reported information is sensible. We exclude observations (i) if total assets, total liabilities, short-term debt, long-term debt, cash assets, tangible assets, or interest expenses are negative, (ii) if tangible assets, cash assets, or total liabilities are greater than total assets, and (iii) if total debt (short term + long term) is greater than total liabilities.
6. A loan facility may include both credit lines and term loans. We assume that all unused credit (i.e., committed exposure - utilized exposure) takes the form of unused capacity on the firm’s credit lines. That is, we include unused borrowing capacity on a firm’s term loans in the total unused credit line measure.
7. When using the interest rate on loans in our calculations, we exclude observations with interest rates below 0.5 or above 50 percent to minimize the influence of data entry errors.

## B Risk-Reporting and Bank Capital

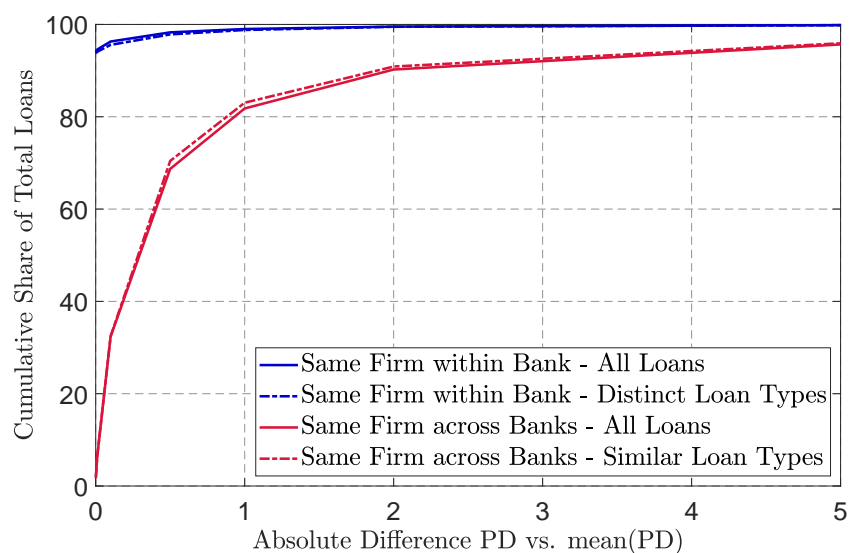


Figure B.1: Probability of Default Dispersion.

**Notes:** For different subsets of loans, the figure shows the cumulative share of total loans up to a specific absolute difference between the PD and the average PD for each respective subset of loans. For these calculations, firms with a single loan from a bank are excluded. The solid blue line considers all loans for a particular bank-firm pair. The dashed blue line additionally distinguishes loans by whether they are syndicated, adjustable-rate, and a credit line or a term loan. Similarly, the dashed red line compares loans to the same firm across banks that are similar across those three characteristics, whereas the solid red line considers all loans. Sample: 2014:Q4-2020:Q4.

Table B.1: Reported PDs and Bank Capital – Local Projections.

	(i) PD	(ii) PD	(iii) PD-Gap	(iv) PD-Gap
Capital	0.09* (0.04)	0.07* (0.04)	0.10** (0.04)	0.09** (0.04)
Fixed Effects				
Firm $\times$ Time	✓	✓		
Time			✓	✓
Bank		✓		✓
Bank Controls	✓	✓	✓	✓
Portfolio Risk Controls		✓		✓
R-squared	0.66	0.66	0.00	0.00
Observations	278,319	278,319	284,686	284,684
Number of Firms	9,206	9,206	9,427	9,427
Number of Banks	32	32	32	32

**Notes:** Estimation results for  $y_{i,j,t+2} - y_{i,j,t-1} = \beta \Delta Capital_{j,t-1} + \gamma X_{j,t-1} + \alpha_{i,t-1} + \kappa_j + u_{i,j,t+2}$ , where  $y_{i,j,t}$  is either given by  $PD_{i,j,t}$  in columns (i) and (ii) or by  $PD\text{-}Gap_{i,j,t}$  in columns (iii) and (iv). Bank controls: bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), and banks' income gap (see Table A.3 in Appendix A for details on the data). Portfolio risk controls: RWA/total assets, weighted portfolio PD. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2014:Q4-2020:Q4. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

Table B.2: Reported PDs and Bank Capital – Interactions.

	PD	PD	PD	PD	PD	PD
Capital $\times$ log(Loan)	-0.00 (0.01)					-0.00 (0.01)
Capital $\times$ log(Assets)		-0.03*** (0.01)				-0.01 (0.01)
Capital $\times$ mean(PD)			0.08*** (0.02)			0.06** (0.03)
Capital $\times$ Syndicated				0.12*** (0.02)		0.06** (0.03)
Capital $\times$ Public					-0.06*** (0.02)	-0.05* (0.03)
Fixed Effects						
Bank $\times$ Time	✓	✓	✓	✓	✓	✓
Firm $\times$ Time	✓	✓	✓	✓	✓	✓
R-squared	0.8	0.74	0.8	0.8	0.8	0.74
Observations	412,537	253,417	412,537	373,996	412,537	224,954
Number of Firms	12,189	8,599	12,189	11,889	12,189	8,318
Number of Banks	32	32	32	32	32	32

**Notes:** Estimation results for  $PD_{i,j,t} = \beta Capital_{j,t-1} \times X_{i,j,t} + \alpha_{i,t} + \kappa_{j,t} + u_{i,j,t}$ , where  $X_{i,j,t}$  is either given by loan size (natural log of used credit), firm size (natural log of total assets), the average PD for firm  $i$  (weighted average across all loans), or binary variables indicating whether the loan is syndicated or the firm is publicly traded. All specifications include firm-time  $\alpha_{i,t}$  and bank-time  $\kappa_{j,t}$  fixed effects and are estimated using OLS. Standard errors in parentheses are clustered at the bank-firm level. Sample: 2014:Q4-2020:Q4. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .



## C PDs, Bank Capital, and Credit Supply

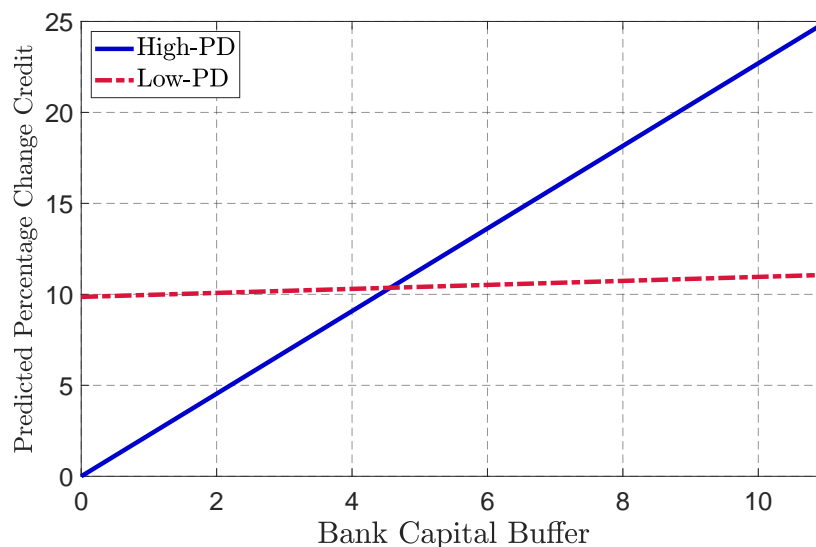


Figure C.1: Graphical Illustration of Regression Coefficients.

**Notes:** The figure plots the regression estimates from column (iv) of Table 3.2,  $\beta_1 = 2.27$ ,  $\beta_2 = 9.86$ ,  $\beta_3 = -2.16$ , constant=0. Bank capital buffers in 2019:Q4 range from 1.66 to 10.19 among the Y14-banks in our sample.

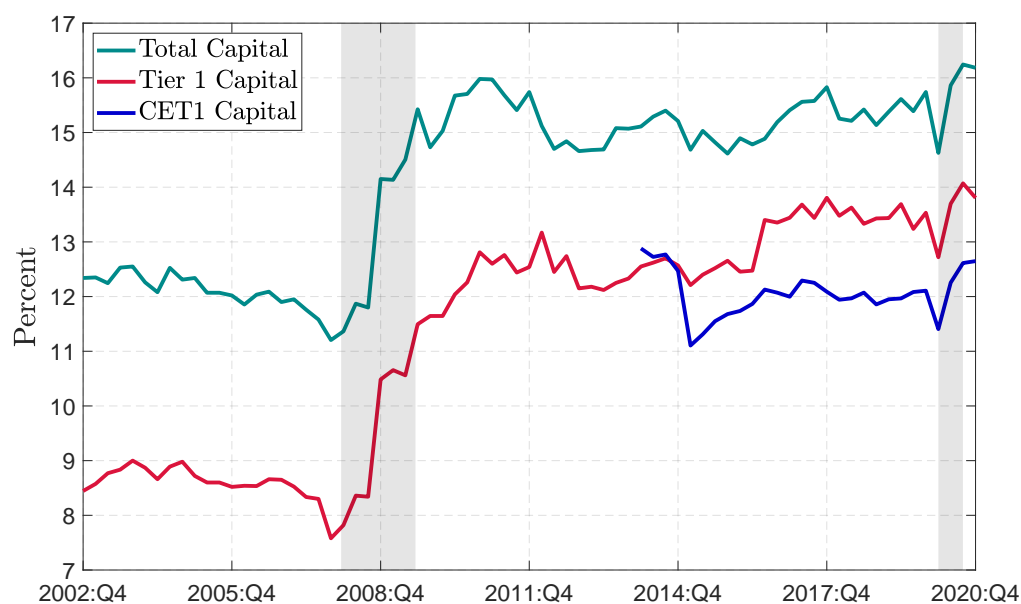


Figure C.2: Bank Capital Ratios.

**Notes:** For each date, the figure shows the median of the CET1, Tier 1, and total capital ratios across the Y14-banks. Gray bars denote NBER recessions.

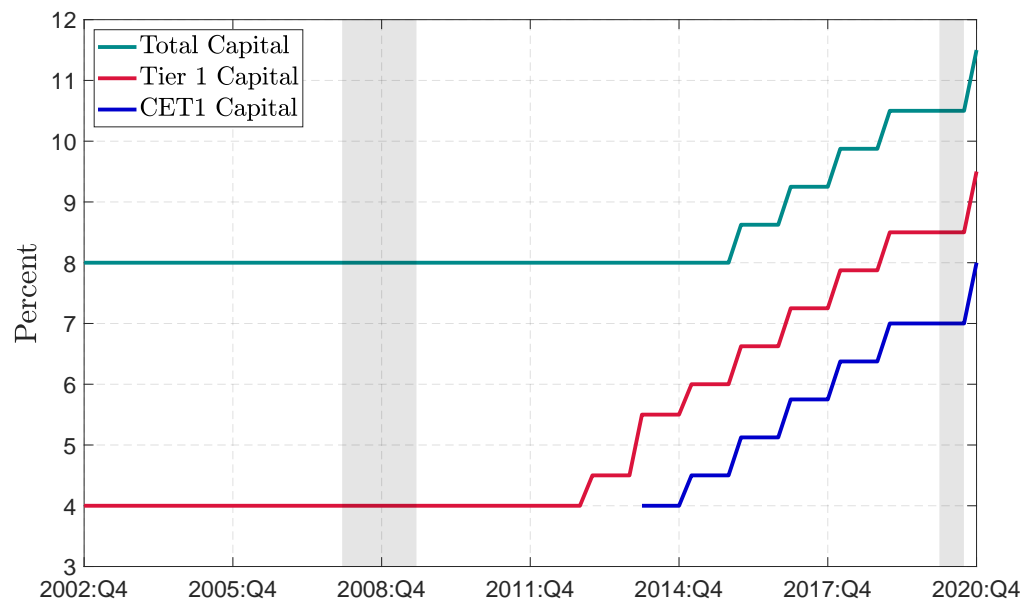


Figure C.3: Bank Capital Requirements.

**Notes:** For each date, the figure shows the median of the CET1, Tier 1, and total capital requirements across the Y14-banks. Gray bars denote NBER recessions.

Table C.1: Low Capital Buffers Excluding COVID – Credit Supply.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	-0.20 (0.34)	-0.18 (0.42)	0.58 (0.48)	0.85* (0.47)	1.09 (0.76)	
Low-PD		0.04 (1.38)	4.98** (2.39)	4.95* (2.53)	5.96* (3.23)	3.71 (2.89)
Capital $\times$ Low-PD			-1.27*** (0.43)	-1.54*** (0.46)	-1.55** (0.69)	-0.93 (0.54)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.5	0.53	0.53	0.53	0.52	0.56
Observations	5,292	3,477	3,477	3,097	2,663	3,456
Number of Firms	606	422	422	386	335	420
Number of Banks	28	25	25	25	24	23

**Notes:** Estimation results for regression (3.2). All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2019:Q4. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

Table C.2: Low Capital Buffers – Interest Rates.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	-0.00 (0.00)	-0.00 (0.00)	-0.01* (0.00)	-0.01** (0.00)	-0.01** (0.00)	
Low-PD		0.01** (0.00)	-0.02** (0.01)	-0.02** (0.01)	-0.03** (0.01)	-0.03*** (0.01)
Capital $\times$ Low-PD			0.01*** (0.00)	0.01*** (0.00)	0.01*** (0.00)	0.01*** (0.00)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.88	0.89	0.89	0.88	0.87	0.91
Observations	6,538	4,399	4,399	3,944	3,416	4,368
Number of Firms	652	474	474	433	379	470
Number of Banks	29	27	27	26	27	24

**Notes:** Estimation results for regression (3.2), where the dependent variable is given by changes in interest rates  $i_{i,j,t+2}^k - i_{i,j,t}^k$ . Interest rates are weighted by used credit and observations within the 1% tails of the dependent variable are excluded. All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2020:Q2. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

Table C.3: Low Capital Buffers – Omitting Firm Fixed Effects.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	0.13 (0.17)	0.54** (0.24)	0.92*** (0.29)	1.05*** (0.31)	1.14*** (0.29)	
Low-PD		-0.07 (0.97)	2.37* (1.22)	2.97** (1.22)	2.85** (1.29)	2.93** (1.07)
Capital $\times$ Low-PD			-0.66** (0.24)	-0.81*** (0.18)	-0.73*** (0.26)	-0.65** (0.25)
Fixed Effects						
Rate $\times$ Time	✓	✓	✓			✓
Rate $\times$ Syn. $\times$ Time				✓		
Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.01	0.02	0.02	0.02	0.03	0.05
Observations	84,274	8,033	8,033	7,529	7,996	8,022
Number of Firms	15,258	1,135	1,135	1,093	1,133	1,135
Number of Banks	31	27	27	27	27	27

**Notes:** Estimation results for regression (3.2). All specifications include time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are two-way clustered by bank and firm. Sample: 2018:Q1 - 2020:Q2. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

Table C.4: Low Capital Buffers – Alternative Fixed Effects.

	(i)	(ii)	(iii)	(iv)
Capital	1.02*** (0.25)	0.86*** (0.29)	0.73** (0.34)	0.77** (0.36)
Low-PD	2.78* (1.35)	2.60* (1.44)	2.38 (1.45)	1.27 (1.33)
Capital $\times$ Low-PD	-0.77*** (0.25)	-0.78** (0.29)	-0.75** (0.31)	-0.75** (0.30)
Fixed Effects				
Time	✓			
Location $\times$ Time		✓		
Location $\times$ Industry $\times$ Time			✓	
Location $\times$ Industry $\times$ Size $\times$ Time				✓
Bank Controls	✓	✓	✓	✓
R-squared	0.01	0.09	0.29	0.42
Observations	8,033	5,822	5,388	3,536
Number of Firms	1,135	833	736	570
Number of Banks	27	27	27	26

**Notes:** Estimation results for regression (3.2). All specifications include time fixed effects that additionally vary by location (state-level) in columns (ii)-(iv), industry (two-digit NAICS code) in columns (iii) and (iv), and firm size (deciles of the unconditional firm size distribution) in column (iv). All regressions include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). All specifications are estimated using OLS. Standard errors in parentheses are two-way clustered by bank and firm. Sample: 2018:Q1 - 2020:Q2. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

Table C.5: Low Capital Buffers – Probability of Default.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	0.07 (0.37)	0.11 (0.35)	0.07 (0.35)	0.13 (0.30)	0.36 (0.40)	
PD		-0.11 (0.10)	-0.27* (0.14)	-0.27** (0.12)	-0.21 (0.13)	-0.28 (0.17)
Capital $\times$ PD			0.05 (0.04)	0.04 (0.04)	-0.01 (0.03)	0.05 (0.05)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.5	0.51	0.51	0.52	0.51	0.54
Observations	9,930	7,263	7,263	6,348	5,701	7,251
Number of Firms	969	754	754	674	606	752
Number of Banks	29	27	27	27	27	26

**Notes:** Estimation results for regression (3.2), where  $\text{Low-PD}_{i,j,t}^k$  is replaced by  $\text{PD}_{i,j,t}^k$ . All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2020:Q2. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

Table C.6: Low Capital Buffers – Low-PD Interactions.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	0.28 (0.33)	0.30 (0.30)	1.18* (0.65)	1.29** (0.60)	2.04** (0.80)	
Low-PD		-23.52 (58.28)	29.03 (71.36)	20.58 (87.25)	68.99 (72.53)	44.40 (63.60)
Capital $\times$ Low-PD			-1.62* (0.83)	-1.93** (0.86)	-2.23** (0.98)	-1.69* (0.89)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
Bank Controls $\times$ Low-PD	✓	✓	✓	✓	✓	✓
R-squared	0.54	0.54	0.54	0.54	0.54	0.57
Observations	4,674	4,674	4,674	4,188	3,617	4,649
Number of Firms	495	495	495	455	396	491
Number of Banks	27	27	27	26	27	24

**Notes:** Estimation results for regression (3.2). All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). All specifications include interaction terms of each of the bank controls with Low-PD. Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2020:Q2. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .



Table C.7: Low Capital Buffers – Credit Lines and Loan Commitments.

	(i)	(ii)	(iii)	(iv)	(v)	(vi)
Capital	0.15 (0.13)	0.13 (0.14)	0.36** (0.17)	0.45** (0.19)	0.61** (0.26)	
Low-PD		0.34 (0.50)	2.20** (0.82)	2.61*** (0.81)	3.07*** (1.08)	1.81* (0.96)
Capital $\times$ Low-PD			-0.50*** (0.18)	-0.68*** (0.21)	-0.66** (0.27)	-0.44** (0.19)
Fixed Effects						
Firm $\times$ Rate $\times$ Time	✓	✓	✓			✓
Firm $\times$ Rate $\times$ Syn. $\times$ Time				✓		
Firm $\times$ Rate $\times$ Pur. $\times$ Time					✓	
Bank $\times$ Time						✓
Bank Controls	✓	✓	✓	✓	✓	
R-squared	0.6	0.63	0.64	0.63	0.63	0.64
Observations	21,712	15,152	15,152	11,193	10,233	15,146
Number of Firms	1,881	1,315	1,315	1,075	918	1,314
Number of Banks	30	28	28	27	28	27

**Notes:** Estimation results for regression (3.2), where the dependent variable covers term loan and credit line commitments. All specifications include firm-time fixed effects that additionally vary by rate type (adjustable- or fixed-rate) and whether the loan is syndicated (column iv) or the loan purpose (column v). Columns (i)-(v) include various bank controls at time  $t$ : bank size (natural log of total assets), return on assets (net income/total assets), deposit share (total deposits/total assets), banks' income gap, and the ratio of unused credit lines to assets (see Table A.3 in Appendix A for details on the data). Column (vi) includes bank-time fixed effects. All specifications are estimated using OLS. Standard errors in parentheses are clustered by bank. Sample: 2018:Q1 - 2020:Q2. \*\*\* $p < 0.01$ , \*\* $p < 0.05$ , \* $p < 0.1$ .

Table C.8: Effects at the Firm Level – Credit Supply.

	<u>Δ Total Debt</u>		<u>Investment</u>	
	(i)	(ii)	(iii)	(iv)
Capital	0.14*** (0.04)	2.62** (1.03)	-0.17*** (0.01)	2.08*** (0.75)
Low-PD		6.11 (4.37)		9.25*** (3.33)
Capital × Low-PD		-3.55*** (0.86)		-1.50** (0.62)
Fixed Effects				
Firm	✓	✓	✓	✓
Time × Industry	✓	✓	✓	✓
Firm Controls	✓	✓	✓	✓
R-squared	0.4	0.4	0.39	0.39
Observations	82,204	82,204	74,926	74,926
Number of Firms	13,861	13,861	12,081	12,081
Number of Banks	37	37	37	37

**Notes:** Estimation results for regression (3.3), where  $y_{i,t}$  is either given by total firm debt in columns (i) and (ii) or fixed assets in columns (iii) and (iv). All specifications include firm fixed effects, industry-time fixed effects, and various firm controls dated at time  $t$ : cash, net income, tangible assets, liabilities (all relative to assets), firm size (natural log of total assets), public-firm-indicator, total term loans/debt, total observed unused credit/debt. Standard errors in parentheses are two-way clustered by main-bank and firm. All specifications are estimated using OLS. Sample: 2016:Q3-2020:Q4. \*\*\*  $p < 0.01$ , \*\*  $p < 0.05$ , \*  $p < 0.1$ .

## D Marginal Revenue Product of Capital

This section outlines how we approximate firms' marginal revenue product of capital. Using standard notation, assume that firm  $i$  faces production function and isoelastic demand

$$Y_{i,t} = A_{i,t} K_{i,t}^{\alpha_i} L_{i,t}^{\beta_i} \quad , \quad Y_{i,t} = \left( \frac{P_{i,t}}{P_t} \right)^{-\sigma} Y_t \quad .$$

Maximizing profits

$$\Pi_{i,t} = P_{i,t} Y_{i,t} - (1 + \tau_{i,t}^K)(r_t + \delta_{i,t}) K_{i,t} - (1 + \tau_{i,t}^L) w_{i,t} L_{i,t}$$

with respect to capital yields

$$MRPK_{i,t} = \alpha_i \left( \frac{\sigma - 1}{\sigma} \right) \left( \frac{P_{i,t} Y_{i,t}}{K_{i,t}} \right) = (1 + \tau_{i,t}^K)(r_t + \delta_{i,t}) \quad ,$$

where  $\tau_{i,t}^K$  and  $\tau_{i,t}^L$  denote capital and labor distortions for firm  $i$  at time  $t$  (see, e.g., [Hsieh and Klenow, 2009](#)). To compare  $MRPK_{i,t}$  across firms, we approximate

$$\frac{P_{i,t}Y_{i,t}}{K_{i,t}} \approx \frac{\text{Sales}_{i,t}}{\text{Fixed Assets}_{i,t}} \quad , \quad \alpha_i \approx \text{Median}_i\left(\frac{\text{Operating Surplus}_{i,t}}{\text{Sales}_{i,t}}\right) ,$$

which are based on firm balance sheet and income statements. The results are robust to using Compustat data to approximate  $\alpha$  by industry  $s$

$$\alpha_{i,s} \approx \alpha_s \approx \text{Mean}_s\left(\frac{\text{Operating Surplus}_{i,s,t}}{\text{Sales}_{i,s,t}}\right) .$$

## E Model Appendix

### E.1 Static Model Parametrization

The static model has three parameters only:  $\alpha, \beta^f, \beta^k$ . All plots are based on the following parametrization:

Table E.1: Static Model Parametrization

Parameter	Description	Value
$\alpha$	Returns to scale	0.35
$\beta^f$	Discount factor Firm	0.9
$\beta^k$	Discount factor Lender	0.98