Fiscal Multipliers and Financial Crises

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Federal Reserve Bank of St. Louis

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The views expressed on this presentation do not necessarily reflect the positions of the Federal Reserve Bank of St. Louis or the Federal Reserve System.

- "Conventional" fiscal stimulus
 - 1. Govt purchases (Cogan et al. '10; Conley & Dupor '13)
 - Transfers to households (Oh & Reis '12; Parker et al. '13; Drautzburg & Uhlig '15)
- Financial sector interventions
 - 3. Equity injections (Blinder & Zandi '10; Philippon & Schnabl '13)
 - 4. Credit guarantees (Philippon & Skreta '12; Lucas '16)

Large debate on the effectiveness and composition of the response

This paper

- 1. How important was the fiscal policy response?
- 2. Which tools were the most important?

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Approach and Results

- 1. Structural model of fiscal policy
 - Potential stabilization roles for each of the tools
 - State dependent effects of shocks and policies
- 2. Quantitative Exercise
 - Calibrated nonlinear model + data on fiscal policy response
 - Use particle filter to estimate structural shocks given policy response
 - Study counterfactuals
 - Crisis and Great Recession without fiscal response

Results:

- Aggregate consumption falls by twice as much w/o policy
- Transfers and equity injections most important
- Fiscal multipliers extremely state dependent
- New transmission channels for fiscal policy during crises

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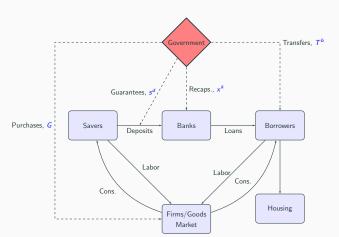
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Model

Nominal Rigidities \Longrightarrow Government purchases
Incomplete Markets \Longrightarrow Transfers
(Frictional) Financial Sector \Longrightarrow Bank Recaps.

Credit Risk & Default \Longrightarrow Credit Guarantees



Borrowers Detail

- 1. Borrow in long-term debt B_t^b , purchase houses h_t
- 2. Family construct w/ housing quality and moving shocks,

$$\text{household default}_t = f_t \left(\frac{B_{t-1}^b}{\Pi_t p_t^h h_{t-1}} \right)$$

3. New borrowing subject to LTV constraint

$$B_t^{b,\text{new}} \leq \theta^{LTV} p_t^h h_t^{\text{new}}$$

Banks P Detail

- 1. Invest in mortgages, financed w/ deposits and retained earnings
- 2. Subject to iid shock on portfolio return, default if $V_t \leq 0$
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- Aggregate shocks:
 - 1. TFP A_t
 - 2. Financial shock σ_t

Household Default
$$Rate_t = f(LT^+V_t, \overset{+}{\sigma_t})$$

- Financial shock: defaults ↑
 - Bank equity ↓
 - 2. If bank constraint binds \Rightarrow spreads rise, lending falls
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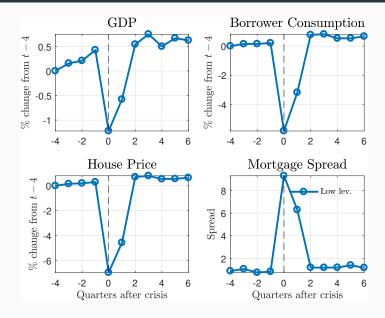
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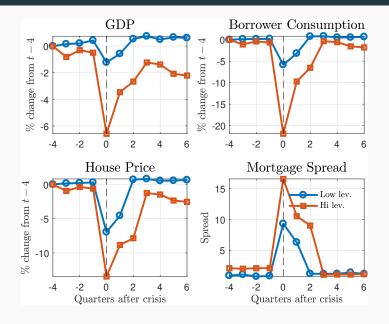
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State Dependence: Financial Shock with Low Leverage



State Dependence: Financial Shock with High Leverage



- 1. Calibrate model to U.S. pre-crisis
 - Match moments on household and bank balance sheets Calibration
- 2. Use data + particle filter to estimate sequences of structural shocks

$$\{A_t, \sigma_t\}_{t=2000Q1}^{T=2015Q4}$$

- $Y^T \equiv \text{Observed Macro Variables}^T = \{C_t, \text{spread}_t\}_t^T$
- $\Omega^T \equiv \text{Observed Fiscal Policy Response}^T = \left\{G_t, T_t^b, x_t^k, s_t^d\right\}_t^T$
- 3. What $\{\hat{A}_t, \hat{\sigma}_t\}_t^T$ make the model match Y^T given Ω^T ?
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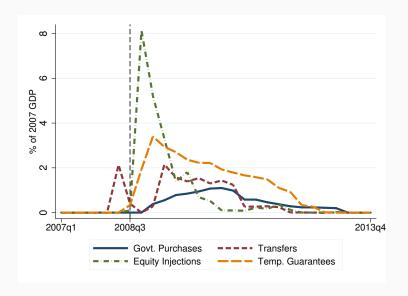
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- x_t^k: TARP '08 equity injection programs (CPP, CDCI, PPIP, AIG, BofA/Citi), auto bailout (AIFP, ASSP), GSE bailout (PSI)
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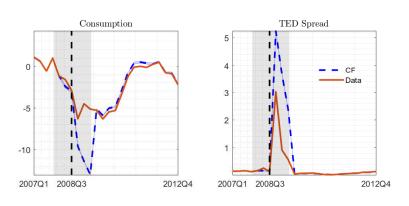
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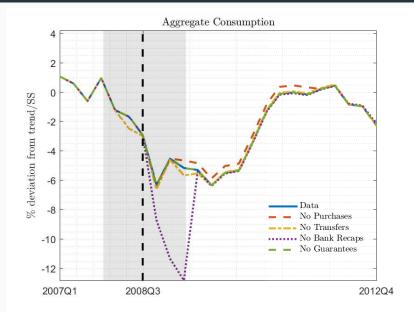
Fiscal Policy Response Data



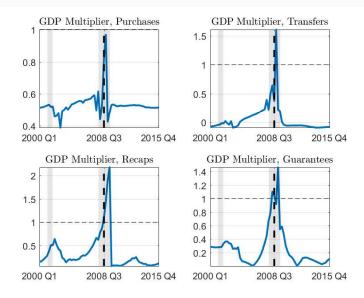
Main Counterfactual: No Fiscal Policy



Policy Decomposition



Time Series for Fiscal Multipliers



Two channels:

- 1. Borrower Constraint ⇒ standard MPC channe
- 2. Borrower Const. + Bank Const. ⇒ new channel
 - Transfers \Rightarrow house prices \uparrow (only when borrowers are constrained)
 - Default rates fall, banks post fewer losses
 - Lending ↑, spreads ↓ (only when banks are constrained)
 - Disposable income 1

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- Analysis of fiscal policy response to the Great Recession
- Structural Model + Data

Contribution

- Conventional stimulus and financial sector interventions
 - Quantitative evaluation
 - Important for normative analysis
- New transmission channels for fiscal policy
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Appendix

Borrowers: Debt and Default

- Face value B_{t-1}^b ,
- ullet Fraction γ matures every period
- Family construct (Landvoigt, 2015)
- 1. Borrower family enters period with states

$$h_{t-1}, B_{t-1}^b$$

2. Continuum of members $i \in [0, 1]$, each with

$$h_{t-1}, B_{t-1}^b, \nu_t(i), \zeta_t(i)$$

where

- $\nu_t(i) \sim F_t^b \in [0, \infty)$ is a house quality shock
- $\zeta_t(i) = 1$ w.p. m is a moving shock

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Borrower Family Problem

$$V_t^b(B_{t-1}^b, h_{t-1}) = \max_{c_t^b, h_t^b, h_t^{\text{new}}, B_t^b, \text{new}, \iota(\nu)} \left\{ u(c_t, n_t) + \xi^b \log(h_t) + \beta \mathbb{E}_t V_{t+1}^b(B_t^b, h_t) \right\}$$

subject to budget constrain

$$c_t^b + \underbrace{\gamma \frac{B_{t-1}^b}{\Pi_t} \left\{ (1-\mathrm{m})\gamma + \mathrm{m} \int [1-\iota(\nu)] \mathrm{d}F_t^b(\nu) \right\}}_{\text{debt repayment}} + \underbrace{p_t h_t^{\mathrm{new}}}_{\text{house purchase}} \leq \underbrace{(1-\tau)w_t n_t^b + \underbrace{Q_t^b B_t^{b,\mathrm{new}}}_{\text{new debt}} + \underbrace{\mathrm{m}p_t h_{t-1}}_{\text{sale of non-forecl. houses}} + \underbrace{T_{t-1}^b}_{\text{Transfers}} = \underbrace{T_{t-1}^b}_{\text{Transfers}}$$

and borrowing constraint

$$B_t^{b,\text{new}} \leq \theta^{LTV} p_t h_t^{\text{new}}$$

Borrower Family Problem

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Borrower Default

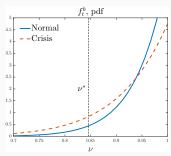
Default iff $\nu \leq \nu_t^*$,

$$u_t^* = \frac{B_{t-1}^b}{\Pi_t p_t h_{t-1}} \simeq \text{Loan-to-Value}$$

- $F_t^b = \text{Beta}(1, \sigma_t^b)$
- $\sigma_t^b \sim$ two-state Markov
- Mean preserving spread

Lenders earn (per unit of debt)

$$Z_t^{\mathsf{loans}} = \underbrace{(1-\mathrm{m})[(1-\gamma)Q_t^b+\gamma]}_{\mathsf{non-movers}} + \mathrm{m}$$



$$\left\{\underbrace{\frac{1-F_t^b(\nu_t^*)}{\text{repaid}} + \underbrace{\frac{\text{Resource Cost}}{(1-\lambda^b)}\int_0^{\nu_t^*} \nu \frac{p_t h_{t-1}}{B_{t-1}^b/\Pi_t} \mathrm{d}F_t^b}_{\text{foreclosed}}\right\}$$

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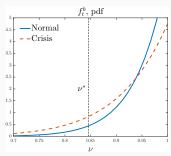
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$$\left\{\underbrace{1 - F_t^b(\nu_t^*)}_{\text{repaid}} + \underbrace{\underbrace{\left(1 - \lambda^b\right)}_{0} \int_{0}^{\nu_t^*} \nu \frac{p_t h_{t-1}}{B_{t-1}^b / \Pi_t} \mathrm{d}F_t^b}_{\text{foreclosed}}\right\}$$

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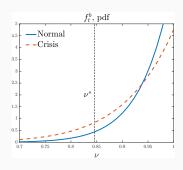
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- Fixed income portfolios, maturity transformation, risky deposits
- Fraction $1-\theta$ of earnings paid out as dividends every period
- Invest in loan securities b_t , raise deposits d_t

Problem for intermediary $j \in [0, 1]$ with current earnings $e_{j,t}$

$$\underbrace{V_t^k(e_{j,t})}_{\text{current mkt value}} = \max_{b_{j,t},d_{j,t}} \left\{ \underbrace{(1-\theta)e_{j,t}}_{\text{dividend}} + \underbrace{\mathbb{E}_t \left[\frac{\Lambda_{t,t+1}^s}{\Pi_{t+1}} \max\left\{0,V_{t+1}^k(e_{j,t+1})\right\} \right]}_{\text{ex-dividend value}} \right\}$$

subject to

flow of funds :
$$Q_t^b b_{j,t} = \left[\theta e_{j,t}(1+x_t^k) - \text{Payments to Govt}_t\right] + Q_t^d d_{j,t}$$
 capital req. : $\kappa Q_t^b b_{j,t} \le \mathbb{E}_t \left[\frac{\Lambda_{t,t+1}^s}{\Pi_{t+1}} \max\left\{0, V_{t+1}^k(e_{j,t+1})\right\}\right]$

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- Default iff

$$u_{j,t} < u_t^* \equiv rac{d_{j,t-1}}{Z_t^{\mathsf{loans}} b_{j,t-1}} \simeq \mathsf{Leverage}$$

- Aggregation ⇒ representative bank
- Payoff per unit of deposits,

$$Z_t^{\text{deposits}} = \underbrace{s_t^d}_{\text{guaranteed}} + (1 - s_t^d) \left\{ \underbrace{1 - F^d(u_t^*)}_{\text{repaid}} + \underbrace{(1 - \lambda^d) \int_0^{u_t^*} u \frac{Z_t^{\text{loans}} B_{t-1}^b}{D_{t-1}} \mathrm{d} F^d}_{\text{liquidated}} \right\}$$

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Closing the Model

Standard DSGE model w/ nominal rigidities

- Producers → Phillips Curve
- Savers → Euler Equation (IS)
- · Housing in fixed supply,

$$h_t = 1$$

ullet Central Bank o Taylor Rule

$$rac{1}{Q_t} = rac{1}{ar{Q}} \left[rac{\Pi_t}{\Pi}
ight]^{\phi_\pi} \left[rac{Y_t}{Y}
ight]^{\phi_y}$$

Aggregate resource constraint,

$$C_t + G_t + \text{DWL Default}_t = \underbrace{A_t N_t}_{=Y_t} \underbrace{[1 - d(\Pi_t)]}_{\text{Menu Costs}}$$

Fiscal Authority

Budget constraint,

$$\underbrace{\tau_t Y_t + Q_t B_t^g - \bar{G} - \frac{B_{t-1}^g}{\Pi_t}}_{\text{Standard Surplus}} = \text{Net Cost from Discretionary Measures}_t$$

Fiscal rule for taxes,

$$\tau_t = \bar{\tau} \left(\frac{B_{t-1}^g}{\bar{B}^g} \right)^{\phi_\tau}$$

Net Cost from Discretionary Measures:

$$(G_t - \bar{G}) + \chi T_t^b + (x_t^k \theta E_t - \text{Income from Recaps}) + s_t^d \frac{D_{t-1}}{\Pi_t} \times (1 - \text{Recovery Rate}_t)$$



Calibration

1. Crises

$$\sigma_t^b = [\sigma_t^{b, \text{normal}}, \sigma_t^{b, \text{crisis}}]^T$$
 and $\mathbf{P}^{\sigma} = \begin{bmatrix} .995 & .005 \\ .2 & .8 \end{bmatrix}$

2. Households

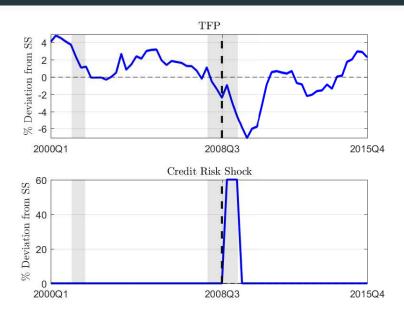
larget	larget	Parameter
Fraction Borrowers	Parker et al. (2013)	$\chi = 0.475$
Avg. Maturity	5 years	$\gamma=1/20$
Max LTV Ratio	85%	$\underline{m} = 0.1160$
Debt/GDP	80%	$\xi = 0.0899$
Avg. Delinquency Rate	2%	$\sigma^{b, {\sf normal}} = 4.351$

3. Banks

$$F^d(u) = \frac{u^{\sigma} - \underline{u}^{\sigma}}{\bar{u}^{\sigma} - u^{\sigma}}$$

Target	Target	Parameter
Book Leverage	10	$\kappa = 0.10$
Payout Rate	20%	$\theta = 0.80$
Avg. Lending Spread	2%	$\varpi = 0.068$
Avg. TED Spread	0.2%	$\lambda^d = 0.15$
CDS-Implied Def. Prob.	2% in recessions	$\underline{u} = 0.90, \sigma^d = 1$

Smoothed Shocks



Other Smoothed Vars.

