First session: computer lab exercises

Software installation

The main packages we will need are mgcv, mgcViz, qgam and mgcFam which should have been installed by doing

```
install.packages("devtools")
library(devtools)
install_github("mfasiolo/mgcFam")
install_github("mfasiolo/testGam")
```

If this worked, stop reading this section and go to the exercises. Otherwise, if install_github fails saying "Rate limit remaining: 0/60", then Plan B consists in running the code:

and then

```
# I will pass you these packages via a USB stick
install.packages("mgcFam_0.0.2.tar.gz", repos = NULL, type = "source")
install.packages("testGam_0.0.1.tar.gz", repos = NULL, type = "source")
```

If plan B fails (e.g. no internet connection), we follow Plan C (!!). I will give you a USB containing all the dependencies, then you need to run:

Assuming that this worked, we continue as in Plan B:

```
# I will pass you these files via a USB stick
install.packages("mgcFam_0.0.2.tar.gz", repos = NULL, type = "source")
install.packages("testGam_0.0.1.tar.gz", repos = NULL, type = "source")
```

GAM exercises

All the data sets we will use in the workshop should now be available in your R system. The rest of the material for the workshop can be downloaded from https://github.com/mfasiolo/workshop_EDF19. If you download it as a zip file and extract it, the solutions can be found in the exercises/solutions folder.

In this session you could try one or more of the following exercises on electricity demand forecasting:

- 1. Forecasting electricity demand on GEFCom2014 data (solution in: "gefcom_small.html"). Simple exercise, featuring only 1D smooth effects on a relatively small data set.
- 2. Big GAM modelling of GEFCom14 electricity demand data (sol: "gefcom_big.html"). Featuring Big Data GAM methods and 2D tensor interactions.
- 3. Individual electricity demand modelling (solution in: "Ind_elect.html"). Featuring Big Data GAM methods and by-costumer smooth effects.

Otherwise you could try one of these other exercises, not focused on the electricity industry:

- 4. Mackerel egg data (sol: "Mackerel.html"). Featuring 2D spatial interactions.
- 5. Bone mineral density modelling (sol: "bone_density.html"). Featuring simple random effects.

but feel free to try mgcv and mgcViz on your own data.

1 Forecasting electricity demand on GEFCom2014 data

Here we consider the electricity demand dataset taken from the GEFCom2014 challenge. The dataset covers the period January 2005 to December 2011 and it contains the following variables:

- NetDemand net electricity demand between 11am and 12am.
- wM instantaneous temperature.
- wM_s95 exponential smooth of wM, that is wM_s95[i] = a*wM[i] + (1-a)*wM_s95[i] with a=0.95.
- Posan periodic index in [0, 1] indicating the position along the year.
- Dow factor variable indicating the day of the week (I think that 0=Sunday and 6=Saturday, but I am not sure).
- Trend progressive counter, useful for defining the long term trend.
- NetDemand. 24 lagged version of NetDemand, that is demand at the same time of the previous day.
- Year should be obvious.

Questions:

1. Load testGam, mgcViz and the data (data("gefcom_small")). Use gamV to fit a Gaussian GAM where the model formula (e.g. y~s(x)) contains: smooth effects for wM, wM_s95, Posan (optionally use a cyclic basis for the latter by doing s(Posan, bs="cc")); parametric effects for Trend, Dow and NetDemand.24. In the call to gamV set the argument aViz=list(nsim = 50) to have some simulated responses for residuals checking. Plot all the fitted effects using plot.

- 2. Use check1D with the 1_gridCheck1D layer to check that the mean of the residuals does not depart too much from 0, depending on the value of Trend. Do you see any systematic pattern? Use the function check to see whether you should increase k for any of the smooth effects.
- 3. Refit the model but now include a smooth effect for Trend (with k=6) and increase the basis dimension of the effects of wM, wM_s95, Posan to k = 20, 15 and 15 respectively. Compare this model to the old one in terms of AIC, re-check the residuals using check1D and recheck the bases dimension using check. Does everything look good? Increasing too much the basis dimension for Trend is not a good idea, why?
- 4. Use qq to produce a QQ-plot of the residuals, do you see any problem? Refit the same model, but now use a scaled Student-t distributions by setting family = scat. Any improvement in AIC? How do the residuals look now?
- 5. Check whether a scaled Student-t with log-link function scat(link=log) achieves lower AIC. Then plot all the fitted effects of final model using plot (you can set allTerms=TRUE to plot also the parametric effects). Do the effects make sense?

2 Big GAM modelling of GEFCom14 electricity demand data

Here we use again data from the GEFCom14 challenge, but this data set is 24 times larger than the one used in the previous exercise. This is because it contains data corresponding to all the 24 hourly slots. The variable Instant indicates the hourly window corresponding to each row of the data set. All remaining covariates have the same interpretation as before. Questions:

- 1. Load testGam, mgcViz and the data (data("gefcom_big")). Create a model formula with smooth effects wM, wM_s95, Instant, Trend and Posan. Use regression splines bases (bs='cr') for all smooths apart from Posan, for which you should use a cyclic basis (bs='cc'). Use k = 6 for Trend and k = 20 for Posan. Leave k to its default for the other smooths. Use parametric fixed effects for Dow and NetDemand.24. Use this formula within a bamV call to fit a Gaussian GAM. When calling bamV set aGam=list(discrete=TRUE) to speed up computations (do this in all subsequent bamV calls) and aViz = list(nsim = 50) to perform the response simulations needed for residuals checking. Having fitted the model, look at the effects using plot (recall that you can use argument allTerms=TRUE to plot also the parametric effects).
- 2. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Also, use the check1D function with the l_gridCheck1D layer to look for residual patterns across the variables.
- 3. Double k for any of the effects where the number of basis functions seems to small, and re-fit. After re-fitting, check whether AIC has improved and repeat the residual checks.
- 4. We expect that several of the effects might depend on the time of day. Use the check2D function with the l_gridCheck2D layer to look for interactions between Instant and NetDemand.24, wM, wM_s95 and Posan. Notice that the binned mean residuals should ideally fall in the range (-2, 2) if the model was correct. Do you see any residual pattern? If so, fit a model which includes the necessary tensor product interactions (e.g. ti(wM, Instant, k = c(10, 10))) and repeat the checks. Are the patterns still there?

- 5. Assuming that we are now satisfied with our model, we'll now have a detailed look at the fitted smooth effects. First, look at the marginal effects using the plot function. Use the expression print(plot(fit2, select = ???), pages = 1) to plot all the marginal effects on one page (substitute ??? with the indexes of the univariate effects in your model). Do the same to plot the 2D interactions. Think about whether each effect makes physical sense to you. As an alternative to plot, recall that you can extract any effect using the sm function and produce a plot with customized layers. You can use the listLayers function to get a list of the available layers. Then, use the plotRGL function to manipulate each bivariate effect interactively.
- 6. Extra question: the model could be improved further. For instance, use the check2D function with the l_gridCheck2D layer to look at how the standard deviation and skewness of the residuals vary across pairs of covariates (the e1071 package provides a skewness function, then you simply need to set gridFun = skewness in the call to l_gridCheck2D). Do you see any pattern? At this point we could consider a GAMLSS model with linear predictors for location, variance and skewness (e.g. the gaulss or shash family). However, bam methods does not yet support such models, so you'll need to use gam which can be much slower for large models.

3 Individual electricity demand modelling

Here we consider electricity demand from 28 commercial customers. The dataset covers roughly three months and it contains the following variables:

- load power usage from an individual customer (in KW, I guess);
- DateTime the date and the time of day;
- instant the time of day, where 1 corresponds to 00:00-00:30, 2 to 00:30-01:00 and so on;
- dow factor variable indicating the day of the week;
- temp instantaneous temperature;
- tempL exponential smooth of temp, that is tempL[i] = a*temp[i] + (1-a)*tempL[i-1] with a=0.95;
- ID the unique ID of each individual customer;
- load48SM lagged version of smoothed load, where the smoothing was performed as for tempL.
- day a counter depending on the day.

Questions:

- 1. Load testGam, mgcViz and the data (data("Ind_elect")). Then use bamV to fit a Gaussian GAM model with smooth effects for instant, temp and day, and parametric effects for dow and ID. In the call to bamV set aViz = list(nsim = 50) to perform the response simulations needed for residuals checking. Look at the model output using plot and summary.
- 2. Now we start looking for interactions. Use the check2D function with the 1_gridCheck2D layer to look for interactions between ID and instant, temp and day. Notice that the binned mean residuals should ideally fall in the range (-2, 2), if the model is correct. Do you see large deviation? If so, for which customer(s) in particular?

- 3. Modify the model formula to include by-factor smooths, that is s(instant, by = ID, id = 1) s(temp, by = ID, id = 2) and s(day, by = ID, id = 3). The id argument make so that each of the 3 by-factor smooths has its own smoothing parameter, but the same smoothing parameter is used across all customers. Refit the model using bamV, and set the argument aGam=list(discrete=TRUE) to speed up computation by discretisation. Compare this model to the previous one using AIC, and repeat the residuals checks. Any improvement?
- 4. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Double k for any of the effects where the number of basis functions seems to small, and re-fit. After re-fitting, check whether AIC has improved.
- 5. Use the check2D function with the 1_gridCheck2D layer to look for interactions between ID and load48SM. If the effect of load48SM seems important, include the corresponding by-factor smooth by adding s(load48SM, by = ID, id = 4) to the model and re-fit.
- 6. Look at the model output using plot, using the select argument to plot any specific effect (you can't plot them all together, because the model includes tens of them). Compare the consumption of some of the individual customers with the model predictions (which you can find in fittedModel\$fitted.values). Do some customers look much harder to predict than others?

4 Mackerel egg data

The following code loads and plots some data from a fish egg survey, for the purposes of spatial modelling.

```
library(testGam); library(mgcViz); data("mack"); data("coast")
## plot data....
with(mack,plot(lon,lat,cex=0.2+egg.dens/150,col="red"))
lines(coast)
ind <- c(1,3,4,5,10,11,16)
pairs(mack[,ind])</pre>
```

The main variables of interest in the mack data set are:

- egg.count number of eggs found in the net;
- c.dist distance from 200m seabed contour;
- b.depth depth of the ocean;
- temp.surf surface temperature of the ocean;
- temp. 20m water temperature at a depth of 20 meters;
- lat latitude;
- lon longitude;
- salinity;
- net.area the area of the net used in m².

Questions:

- 1. Use the code above to load and plot the data;
- 2. Create a new variable mack\$log.net.area <- log(mack\$net.area), and use gamV to fit a Poisson GAM with egg.count as response variable and 1D smooth effects for all the other variables, with the exceptions of net.area and log.net.area. Instead, include in the model formula the term offset(log.net.area), meant to take into account the fact that the number of eggs captured is proportional to the net area.
- 3. Look at the model residuals using qq. What kind of problem do you see? Re-fit the models using a negative binomial (family=nb) or Tweedie (family=tw) response distribution, and check which model is better in terms of residuals QQ-plots and AIC.
- 4. Let fit be the best of the three GAM models you just fitted. Use fit<-getViz(fit,nsim=50) to get some simulated residuals, and then use the check2D function with the l_gridCheck2D layer to look for residual patters across lon and lat. Then refit the model using a bivariate isotropic effect s(lon, lat, k=100), re-check the residuals and see whether AIC has improved.
- 5. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Then use the check1D function with the l_gridCheck1D layer look for residual patterns across some of the variables. If necessary, modify the model.
- 6. Plot the fitted effects using plot. Which effects look more important (look at the scales)? Use the plotRGL function to manipulate spatial effect interactively.

5 Bone mineral density modelling

This dataset is taken from the package lava. It consists of 112 girls randomized to receive calcium or placebo. The response variable of interests consists of longitudinal measurements of bone mineral density (g/cm^2) measured approximately every 6th month for 3 years. All girls are approximately 11yo at the start of the trial. The main variables are:

- bmd bone mass density;
- group placebo or supplement;
- person factor indicating the id of each girl;
- age the age of each girl at the time of each measurement;

Questions:

- 1. Load testGam, mgcViz and the data data("calcium"). Then use gamV to fit a Gaussian GAM model with bmd as response and linear effects for age and group. In the call to gamV set the argument aViz=list(nsim = 50) to have some simulated responses for residuals checks. Use summary to print the model output. Is the placebo effect significant? (which is the same as asking whether the treatment effect is significant)
- 2. Use check1D with the l_gridCheck1D layer to check that the mean of the negative residuals does not depart too much from 0, for any of the subjects. If you see significant departures add a random effect for person to the models formula (s(person, bs="re")), then re-fit and re-check the residuals. Print the model output again using summary.

- 3. Now modify the model formula to use a smooth effect for age, and plot the fitted effects using plot. Use the function AIC to compare the model with a smooth effects for age with the model which uses a linear age effect.
- 4. Verify whether the smooth age effect is different between the placebo and the treatment group, by using a by-factor smooth. To do this substitute s(age) with s(age, by=group) in the model formula, refit and then plot the fitted effects. To see the difference between the two smooths more clearly, use the plotDiff function with the l_fitLine and l_ciLine layers.