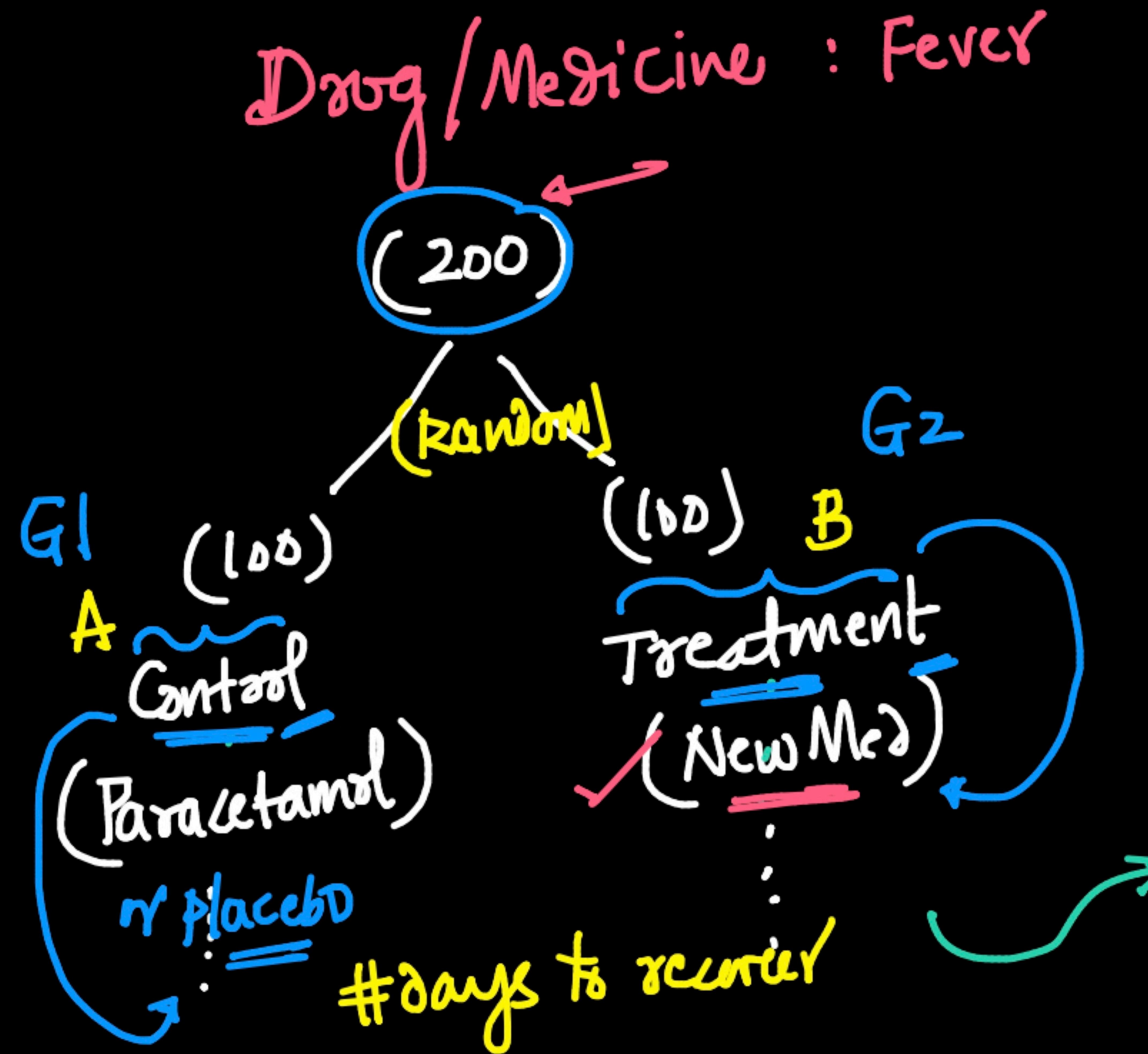


# A/B Testing

Case: Facebook status  
background color change

class status @ 9:03 PM



[Phased trials]

A/B Test

randomized Control-Treat  
-ment Test

T-test ✓

A/B Test



randomized Control-Treat  
-ment Test

case:

Facebook - "status"



colored background  
status msgs

Test on a reasonable sample size

① what do we hope to achieve with this  
feature. → more engagement

② has this been tried earlier?

③ external proof that this work?

④ Subset or all users?

Metric  
NSM: %age of "engaged" users  
Metric  
Measure  
liked, comment, save  
logged-in + Spent 2 min  
in a week

Alt: Total mins  
spent on FB

⌚ Supporting metric(s):

↳ DAV

→ % increase in status messages

:

:

:

# Grass rail metric:

→ that should change in a  
negative manner coz of  
new feature

↓  
→ avg time spent per user per week

→ % age of users consuming rich media  
→ % of users



# Experimentation:

①  $H_0: \tilde{P}_A = \tilde{P}_B$

$H_a: \tilde{P}_A \neq \tilde{P}_B$  (or)

Two-sided

METRIC = percentage of "engaged" users ( $P$ )

$\tilde{P}_A < \underline{\tilde{P}_B}$  ✓  
one-sided

②

Test:

t-test (?) → X

$\chi^2$ -test → X

Proportions test → Z

→ t } ✓

- $p = (41 + 351) / (195 + 605) = 0.49.$

Set this number aside for a moment.

$$\hat{P} = \frac{n_1 + n_2}{d_1 + d_2}$$

Step 3: Insert the numbers from Step 1 and Step 2 into the test statistic formula:

$$z = \frac{(\hat{p}_1 - \hat{p}_2)}{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}} \sim Z(0,1)$$

# users in G<sub>1</sub>

G<sub>1</sub>

G<sub>2</sub>

$\hat{p}_1$

$\hat{p}_2$

$$\frac{n_1}{d_1} = \hat{p}_1$$

$$\hat{p}_1 = \frac{n_1}{d_1} = \frac{\# \text{engaged users}}{\text{Total # users}}$$

Solving the formula, we get:

$$z = 8.99$$

We need to find out if the z-score falls into the “rejection region.”

Close X

DO YOU

DUP

Step 4: Find the z-score associat

Z Test: Definition & Two Propor X S.6 Test of Proportion | STAT O X +

← → C Home https://statisticshowto.com/probability-and-statistics/hypothesis-testing/z-test/ G Q Update :

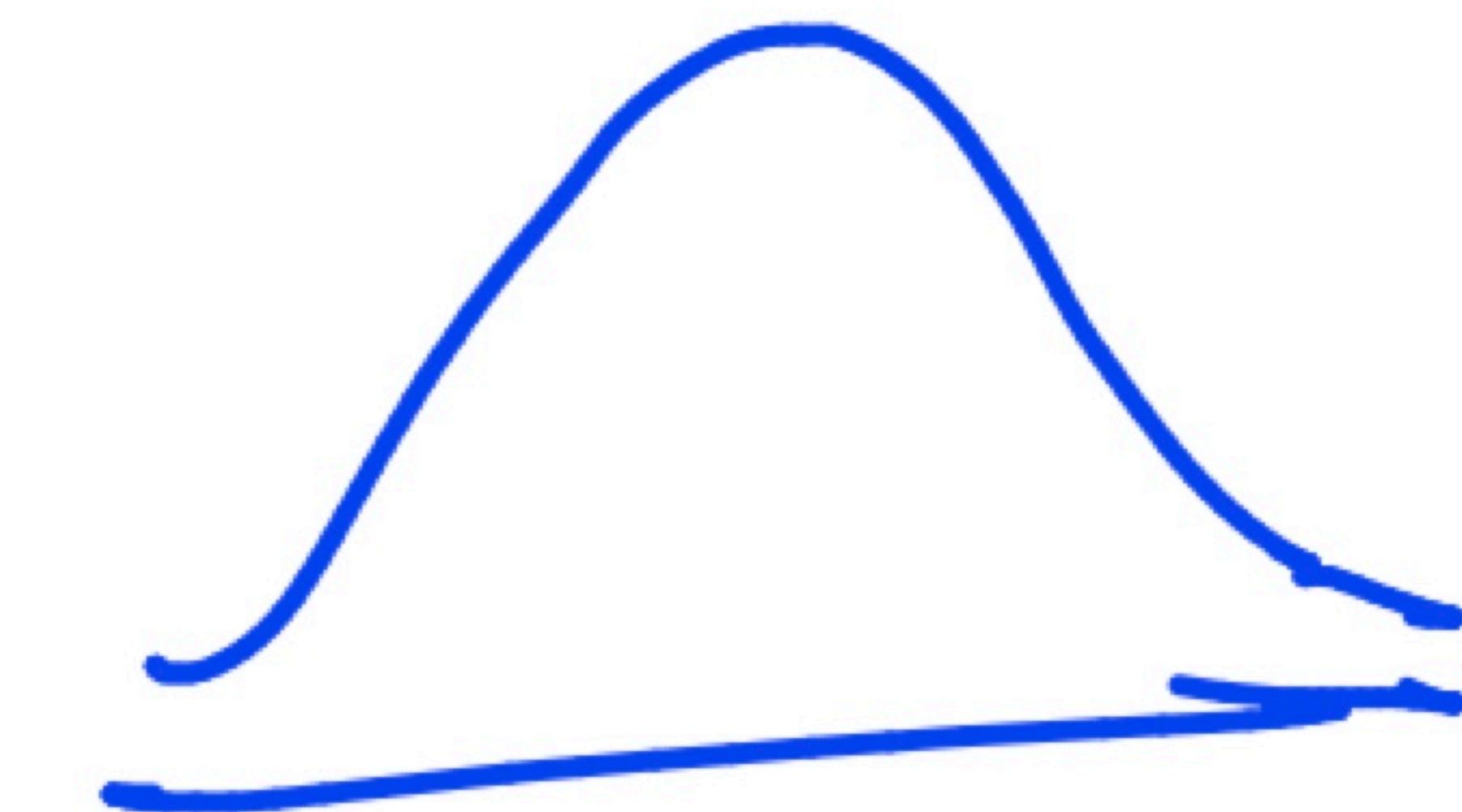
- $p = (41 + 351) / (195 + 605) = 0.49.$

Set this number aside for a moment.

Step 3: Insert the numbers from Step 1 and Step 2 into the test statistic formula:

$$Z = \frac{(\hat{p}_1 - \hat{p}_2) - 0}{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

$\sim z(0,1)$



p-value

Solving the formula, we get:

$$Z = 8.99$$

We need to find out if the z-score falls into the “rejection region.”

Close X



Step 4: Find the z-score associat

- $$\bullet p = (41 + 351) / (195 + 605) = 0.49.$$

Set this number aside for a moment.

**Step 3:** Insert the numbers from Step 1 and Step 2 into the test statistic formula:

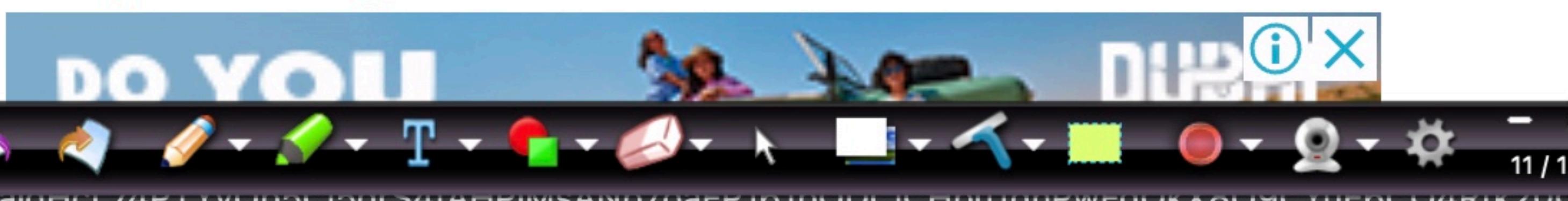
$$Z = \frac{(\hat{p}_1 - \hat{p}_2) - 0}{\sqrt{\hat{p}(1-\hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

Solving the formula, we get:

**Z = 8.99**

We need to find out if the z-score falls into the “rejection region.”

**Close**



Z Test: Definition & Two Propor X S.6 Test of Proportion | STAT O X +  
← → C Home https://statisticshowto.com/probability-and-statistics/hypothesis-testing/z-test/ G Q Update

- $p = (41 + 351) / (195 + 605) = 0.49.$

Set this number aside for a moment.

**Step 3:** Insert the numbers from Step 1 and Step 2 into the test statistic formula:

$$Z = \frac{(\hat{p}_1 - \hat{p}_2) \cancel{-} 0}{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

$H_0: P_1 = P_2$

$\hookrightarrow P_1 - P_2 = 0$

$\underline{P_1} - \underline{P_2} = \underline{\sigma}$

Solving the formula, we get:

$$Z = 8.99$$

We need to find out if the z-score falls into the “rejection region.”

**Close X**



Step 4: Find the z-score associat

$$\bullet p = (41 + 351) / (195 + 605) = 0.49.$$

Set this number aside for a moment.

$N(\mu, \sigma)$

**Step 3:** Insert the numbers from Step 1 and Step 2 into the test statistic formula:

$$z = \frac{(\hat{p}_1 - \hat{p}_2) - 0}{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}} \quad \text{or } z = \frac{\underline{\hat{p}_1 - \hat{p}_2}}{\underline{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}}$$

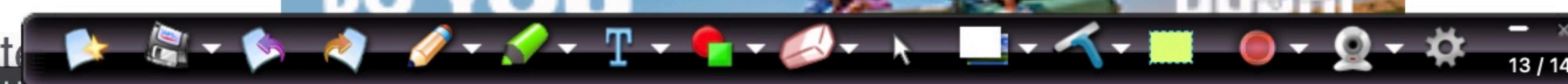
Solving the formula, we get:

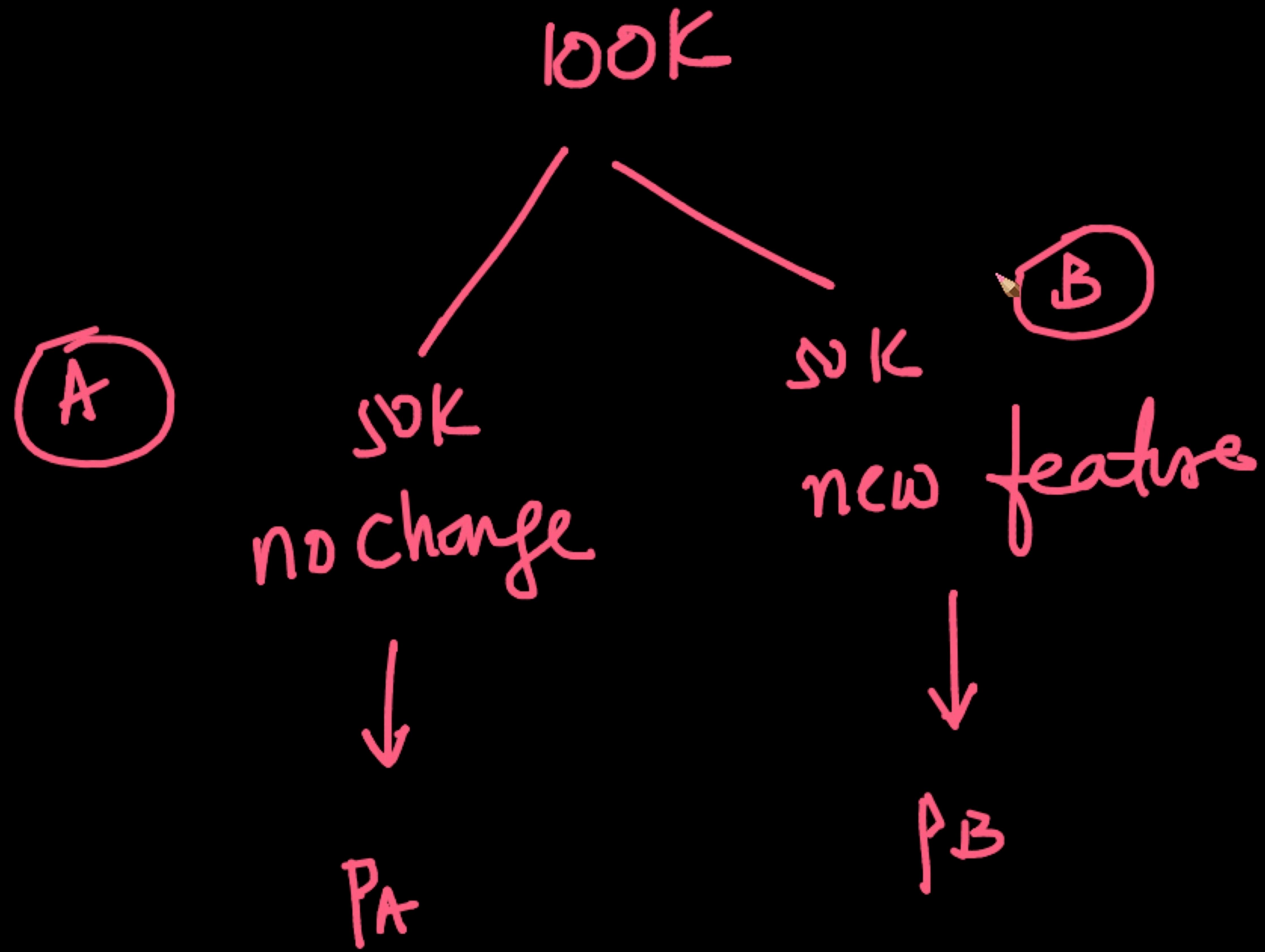
$$z = 8.99$$

We need to find out if the z-score falls into the “rejection region.”

**Close X**

**Step 4:** Find the z-score associat





P-value =  $P(\underline{\text{observing}} \mid H_0)$  ~~5%~~ 100k (?)  
 (all - uses NS)  
 or Ged - specific

$$\begin{array}{c} A \\ \downarrow \\ \beta_A \approx 0.45 \end{array}$$

$$\begin{array}{c} B \\ \downarrow \\ P_B \approx \end{array}$$

$\rightarrow$  Minimum detectable effect (MDE)  $P_B = 0.46$  :  $1\%$  (?)  
Biz impact  $= 0.451$  :  $0.1\%$  (?)

0.1% or 1%

Guess

\$10B  
profit

2B users

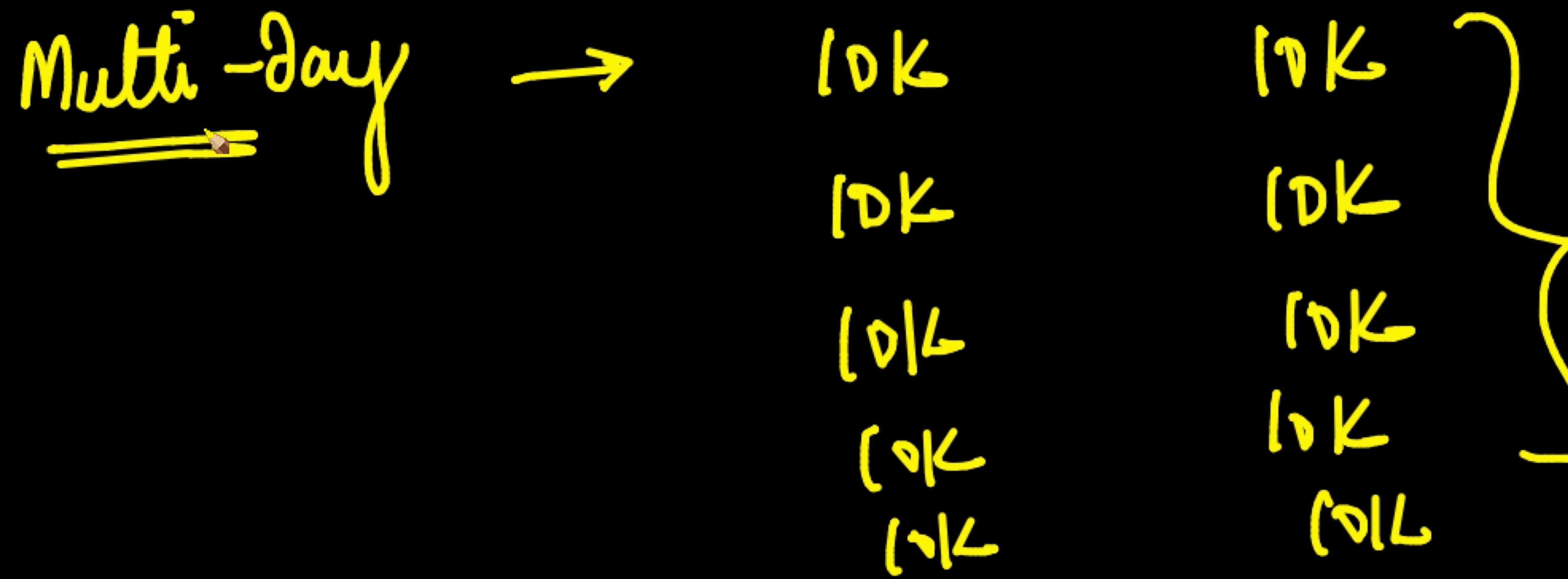
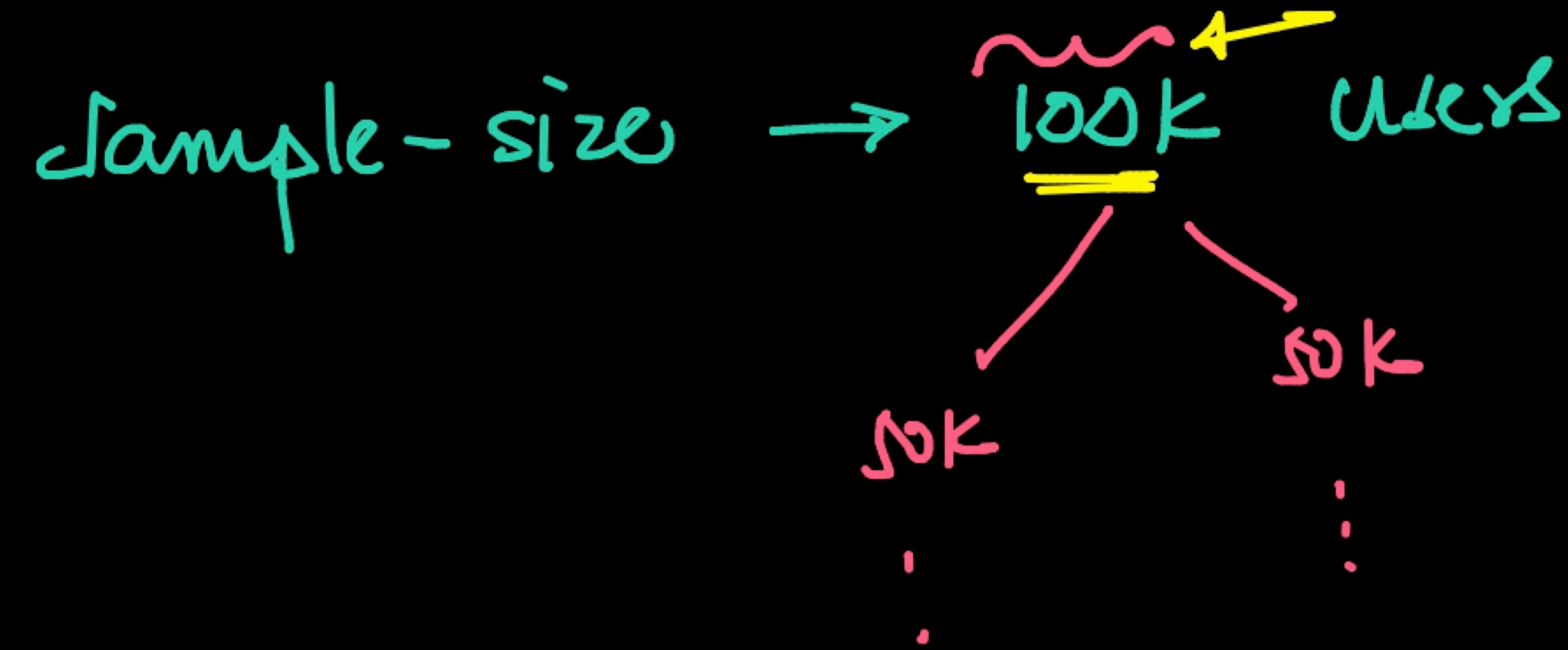
45% or 0.45

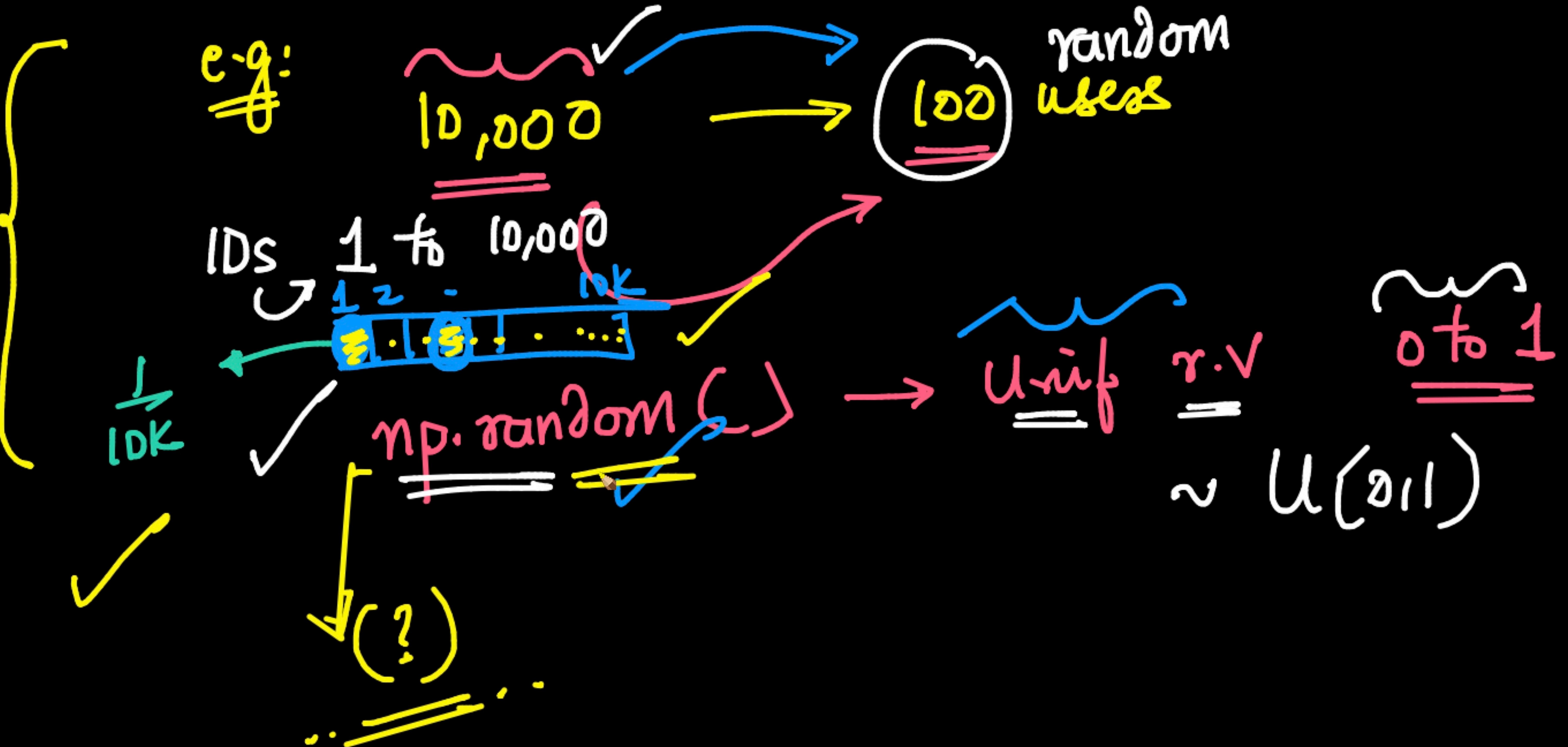
0.451

(0.1%)

0.1% ↑

⇒ 10% → 1B  
0.1% → 10M \$ additional money





Cnt = 0

while (Cnt < 100)

{  
    0 to 1  
    .  
    .

    tmp = np. random ()

    if tmp  $\leq$  1/10,000

        ;

    Cnt++

PARTIAL  
CODE

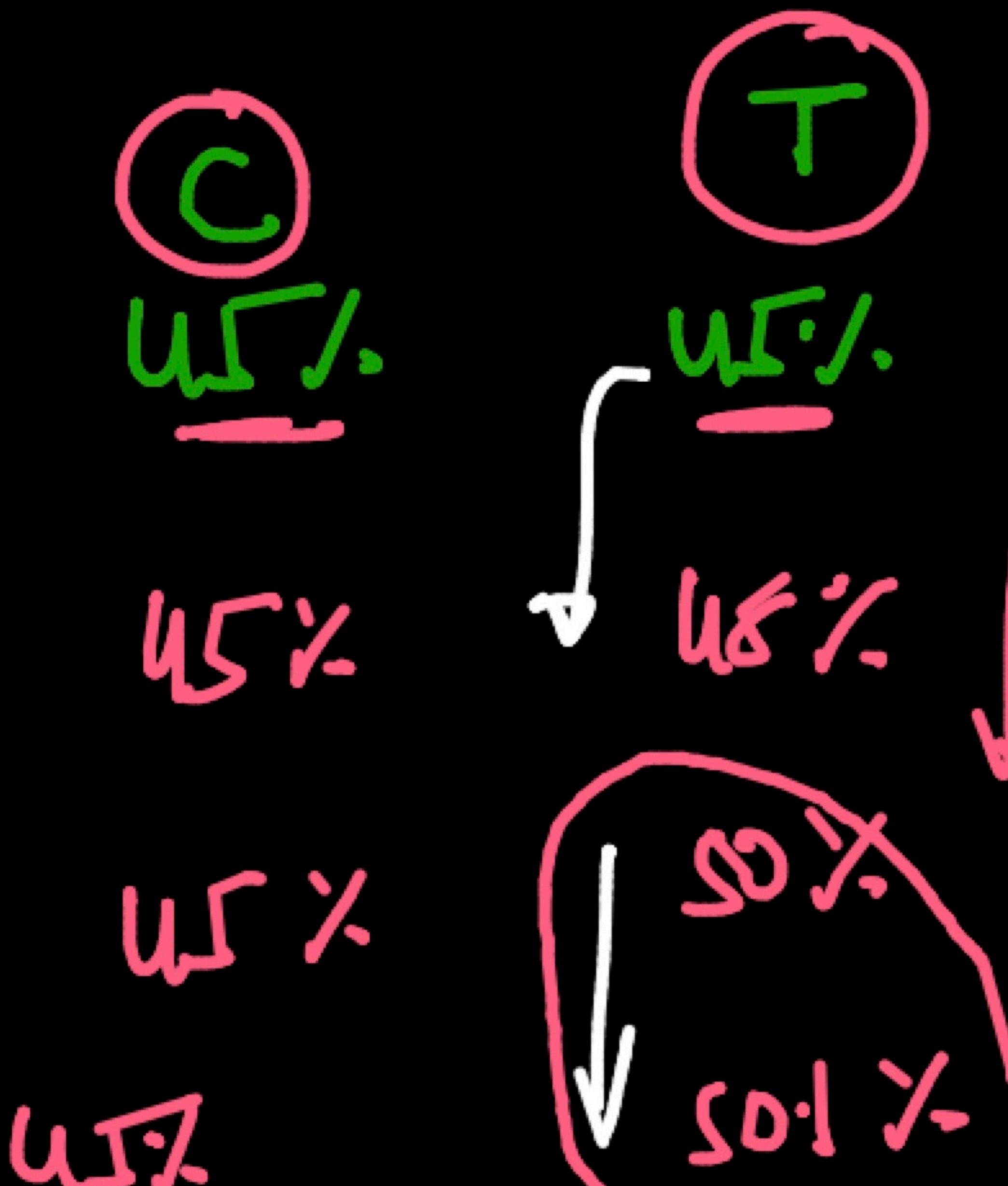
Recap:

- ① Clarify objective & questions
- ② Metrics: NSM, Supporting: Gant charts
- ③ Expt:  $H_0, H_a$ , test;  $\alpha: 5\%$ ; MDE  $\rightarrow$  sample size  
multi-day test

# Pitfalls / Problems

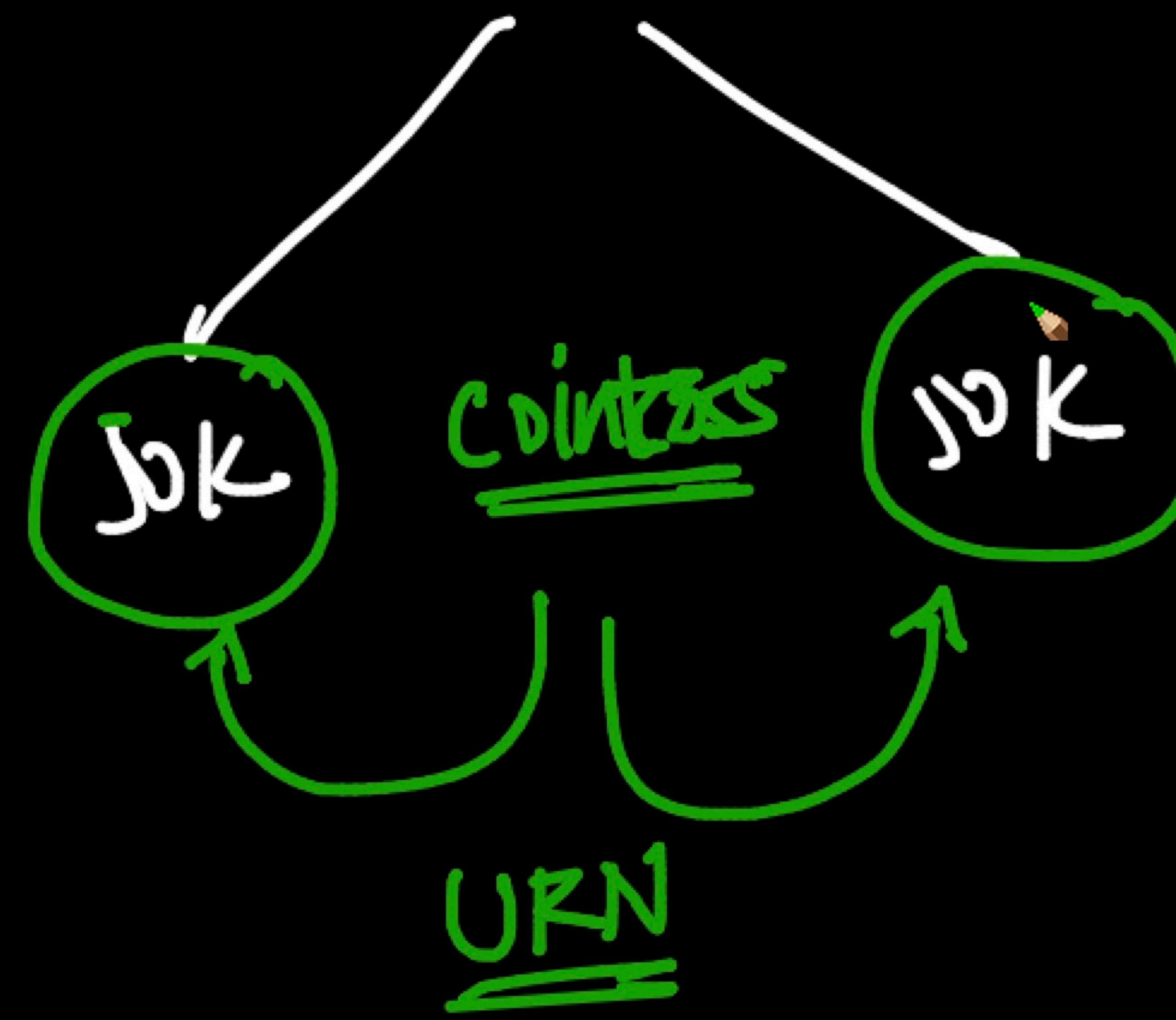
① Primacy →

✓ { WK1 →  
: WK2 →  
: WK3 →  
WK4 →



C T  
↓  
don't want  
to use the new  
feature

look wens



2

## Novelty:

WF1

C

T

45%

65%

WK2

45%

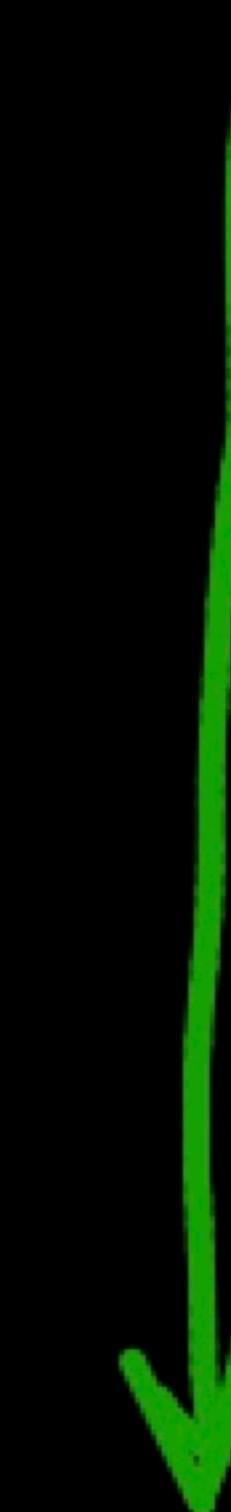
68%

WK3

45%

52%

:



51.2%  
51%  
SMU



24 / 24

# Statistics How To

**Step 3:** Insert the numbers from Step 1 and Step 2 into the test statistic formula:

$$Z = \frac{(\hat{p}_1 - \hat{p}_2) - 0}{\sqrt{\hat{p}(1-\hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

wk1

wk2

wks

Solving the formula, we get:

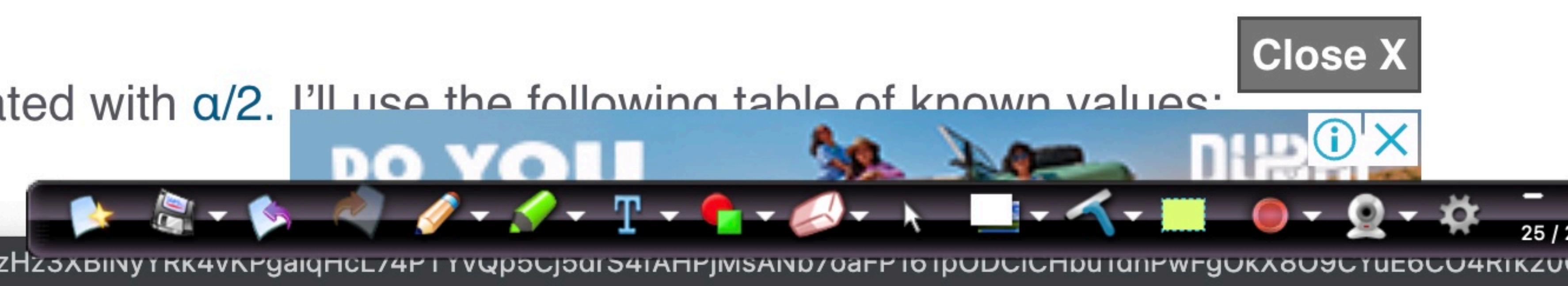
Z = 8.99

We need to find out if the z-score falls into the “rejection region.”

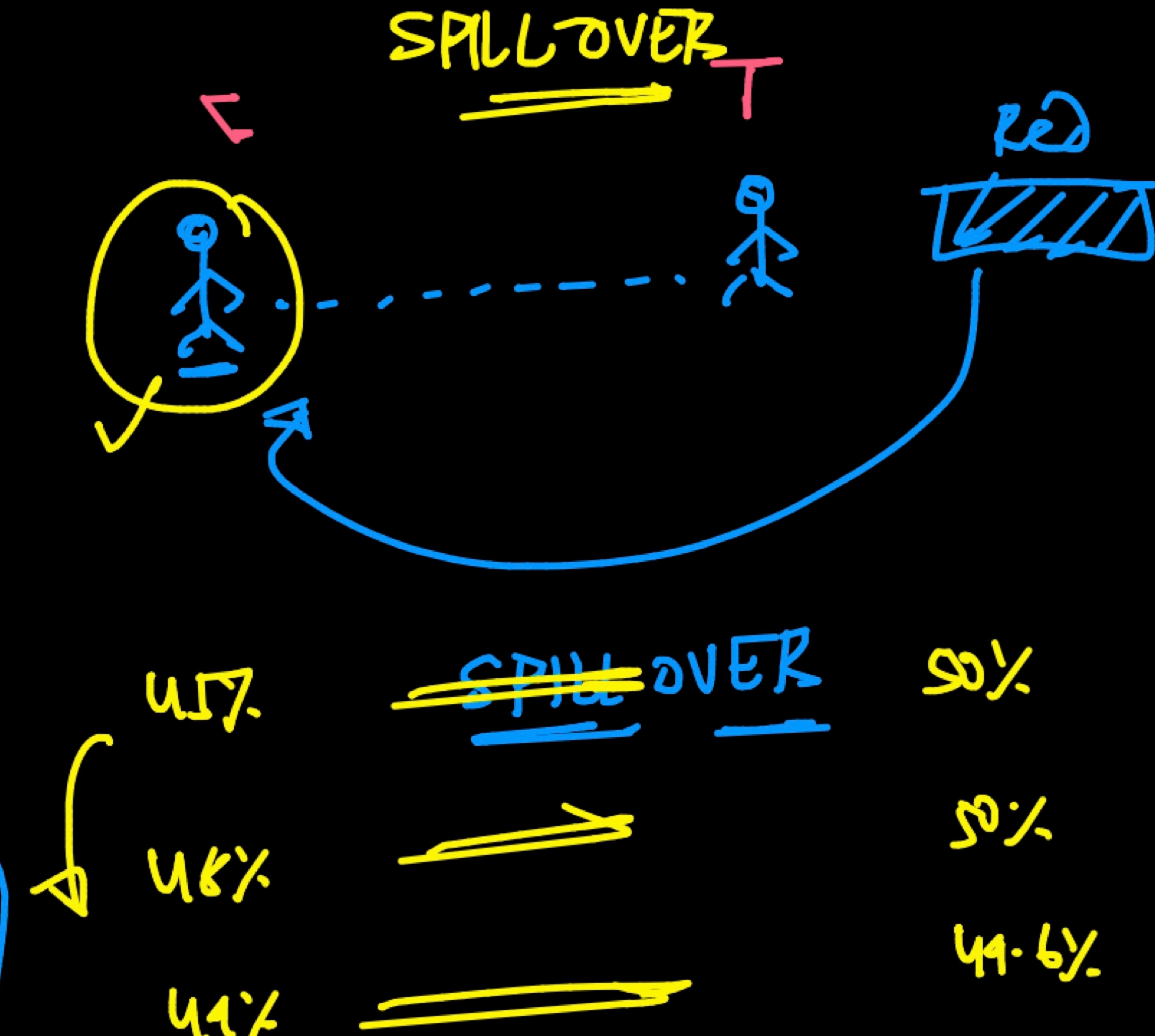
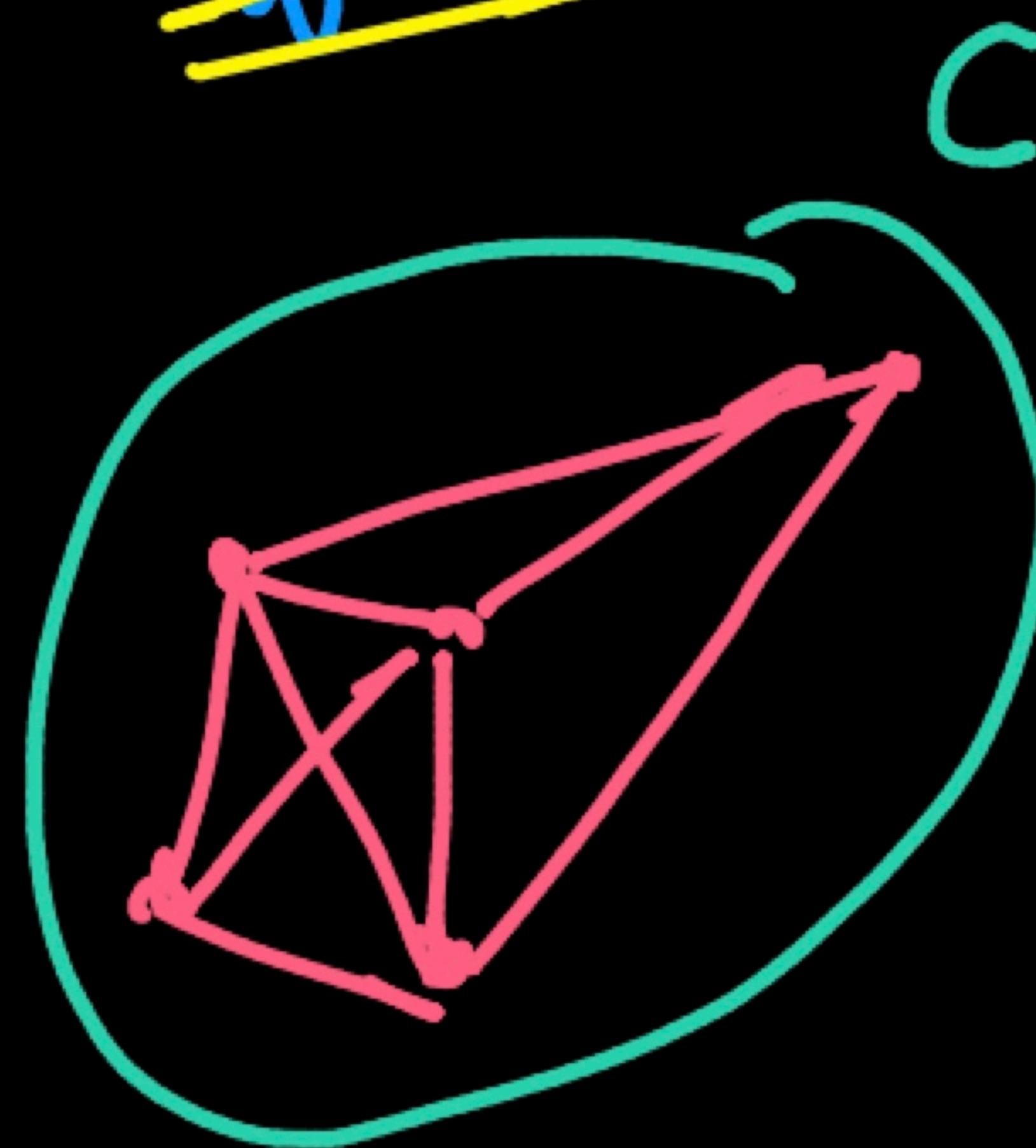
**Step 4:** Find the z-score associated with  $\alpha/2$ . I'll use the following table of known values.

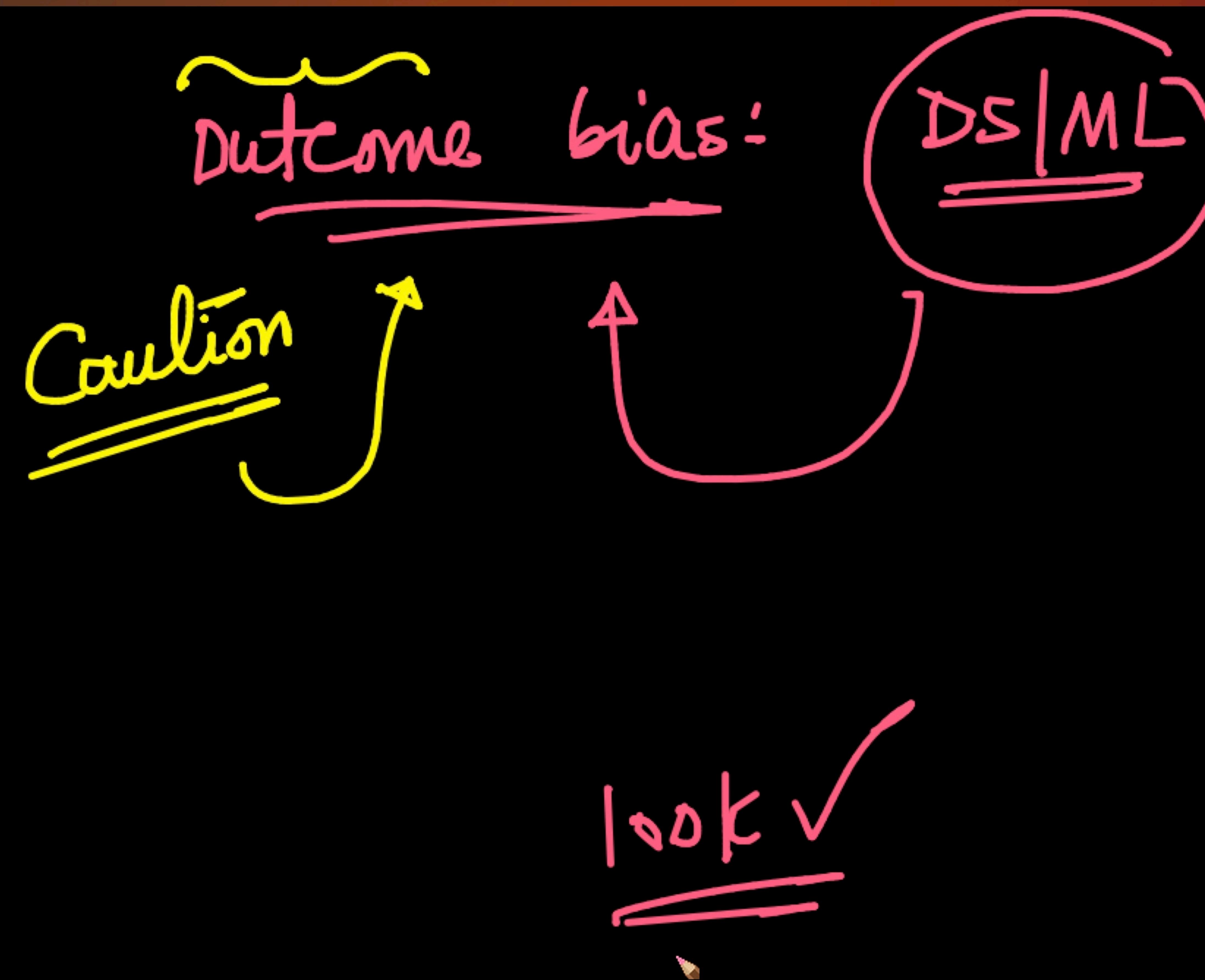
Close

8



network  
effect





Launches to 1B+ users

