

Quantum Computing

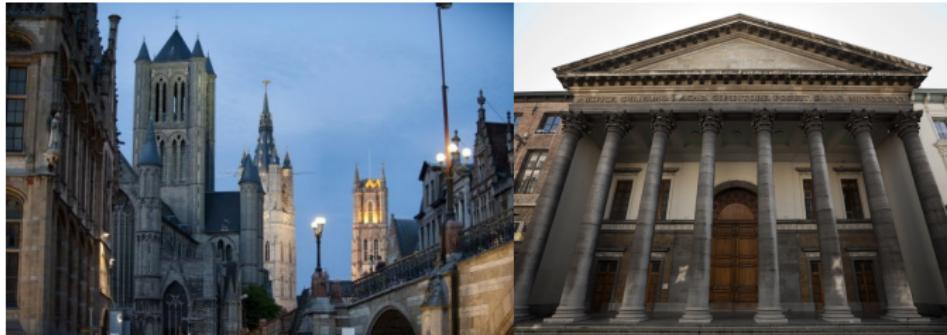
A gentle parachute from the 30 000ft overview



Matthias Degroote

Aspuru-Guzik Group

A bit of history



Popular science is rarely the full story



<https://www.smbc-comics.com/comic/the-talk-3>



Ask your friendly neighborhood theorist



<https://www.smbc-comics.com/comic/the-talk-3>



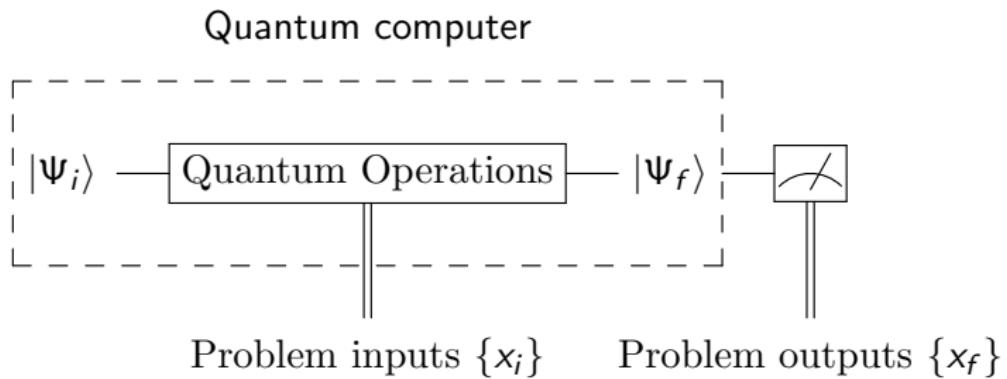
Funny coincidence



- 1 What is a quantum computer?
- 2 What are quantum algorithms?
- 3 Why do they matter for chemistry?



Any device that uses quantum information to perform calculations



Any device that uses quantum information to perform calculations

com·put·er
/kəm'pyoodər/ 

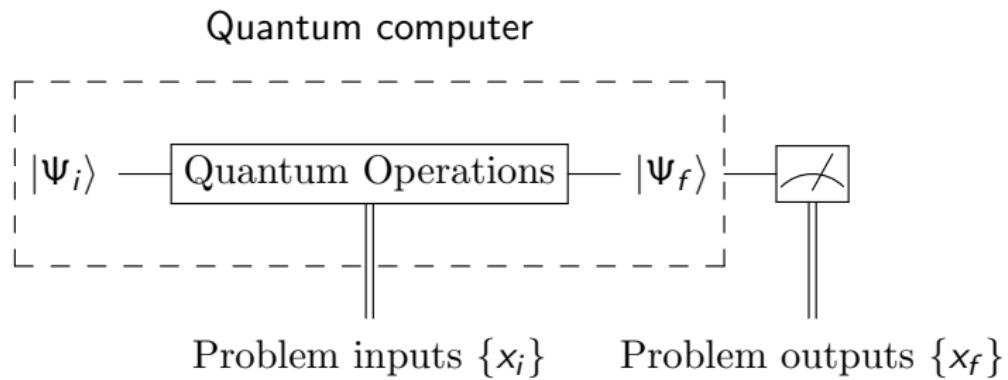
noun

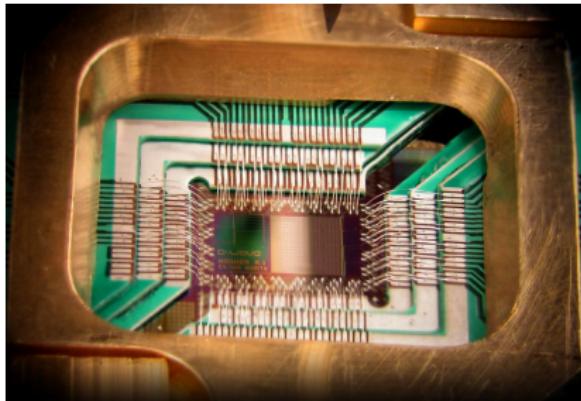
an electronic device for storing and processing data, typically in binary form, according to instructions given to it in a variable program.

- a person who makes calculations, especially with a calculating machine.



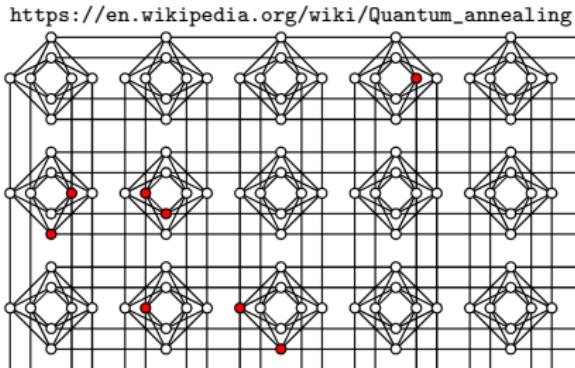
Any device that uses quantum information to perform calculations





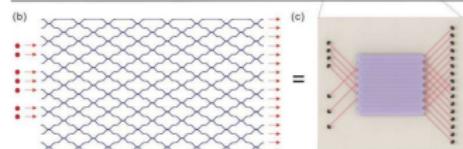
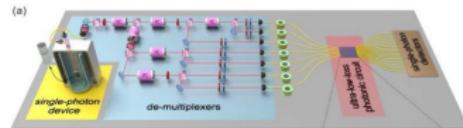
D'Wave

- $H = (1 - s)H_0 + sH_1(x_i)$
- start in **easy** $|\Psi_0\rangle$
- naturally go to **hard** $|\Psi_1\rangle$
- set parameters in H_1 once
- specific for optimization
- controversy about speedup

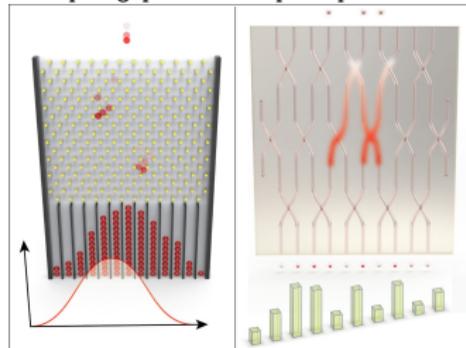


<https://doi.org/10.1371/journal.pone.0172505>





<https://phys.org/news/2018-06-boson-sampling-photons-output-spit.html>

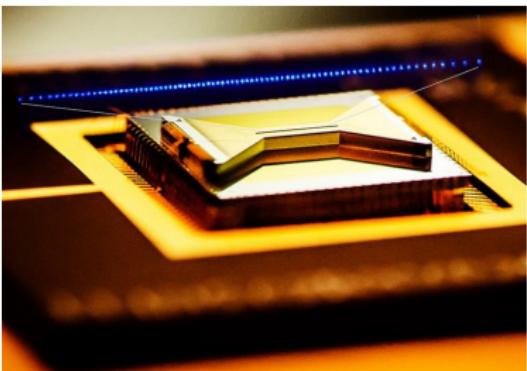


<http://www.2physics.com/2013/03/experimental-boson-sampling.html>

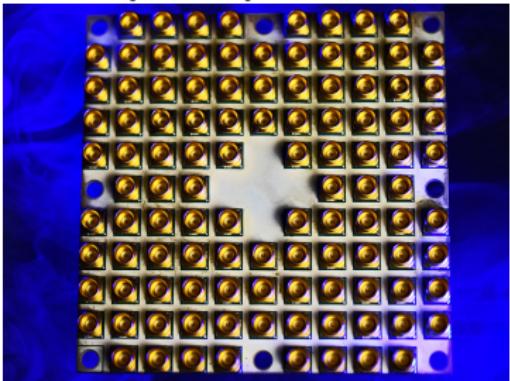
Boson sampling

- quantum computer as sampler
- Proposed in 2011 by Aaronson
- Set parameters of circuit unitary U through optical elements
- sample from $\text{perm}(U)$
- provably hard ($\#P$ -hard)
- similar to Galton board





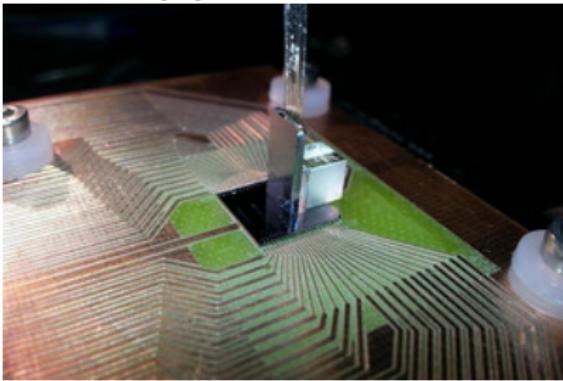
<https://physicsworld.com/a/ion-based-commercial-quantum-computer-is-a-first/>



<https://newsroom.intel.com/news/intel-advances-quantum-neuromorphic-computing-research/>



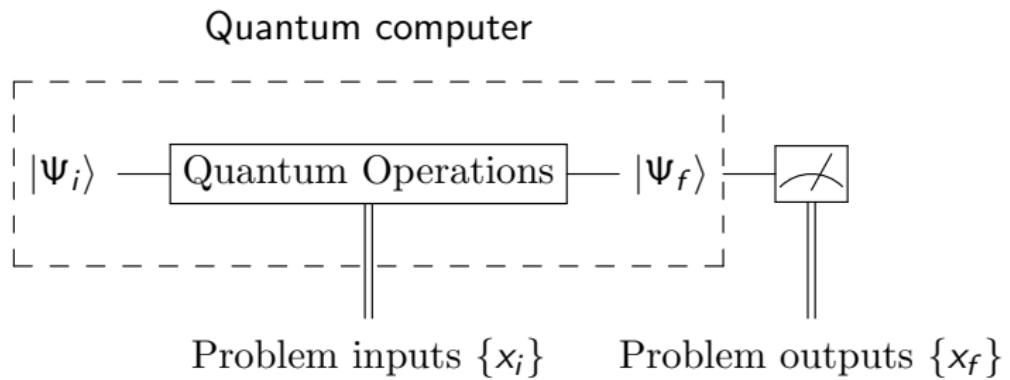
<https://ai.googleblog.com/2018/03/a-preview-of-bristlecone-googles-new.html>



https://www.tuwien.ac.at/en/news/news_detail/article/8946/



Any device that uses quantum information to perform calculations



Digital (quantum) computing

Classical bits

- Express numbers base 2
 $47 = 101111$
- first non-trivial base
- with enough bits, represent any number
- easy to realize \Rightarrow transistor

Quantum bit

- Expand wave function in basis vectors of 2-level systems
 $|\Psi\rangle = a|000\rangle + b|001\rangle + c|010\rangle + \dots$
- with enough qubits, represent any quantum system
- easiest to realize
 \Rightarrow quantum control



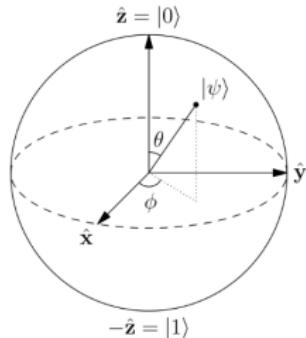
Digital (quantum) computing

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DiVincenzo requirements

- ① scalable well characterizable
- ② the ability to initialize the state of the qubits
- ③ long relevant decoherence times
- ④ a universal set of quantum gates
- ⑤ a qubit-specific measurement capability

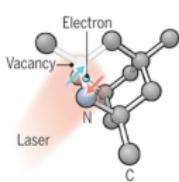
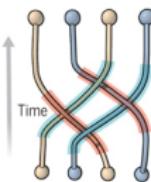
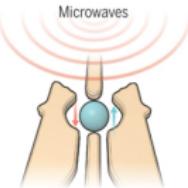
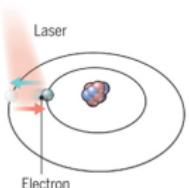
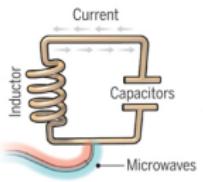
Quantum specific

- entanglement $|\Psi\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$
- superposition $|\Psi\rangle = \frac{1}{\sqrt{2}} (|0\rangle - |1\rangle)$



A bit of the action

In the race to build a quantum computer, companies are pursuing many types of quantum bits, or qubits, each with its own strengths and weaknesses.



Superconducting loops

A resistance-free current oscillates back and forth around a circuit loop. An injected microwave signal excites the current into superposition states.

Longevity (seconds)

0.00005

Trapped ions

Electrically charged atoms, or ions, have quantum energies that depend on the location of electrons. Tuned lasers cool and trap the ions, and put them in superposition states.

>1000

Silicon quantum dots

These "artificial atoms" are made by adding an electron to a small piece of pure silicon. Microwaves control the electron's quantum state.

0.03

Topological qubits

Quasiparticles can be seen in the behavior of electrons channeled through semiconductor structures. Their braided paths can encode quantum information.

N/A

Diamond vacancies

A nitrogen atom and a vacancy add an electron to a diamond lattice. Its quantum spin state, along with those of nearby carbon nuclei, can be controlled with light.

10

Logic success rate

99.4%

99.9%

-99%

N/A

99.2%

Number entangled

9

14

2

N/A

6

Company support

Google, IBM, Quantum Circuits

ionQ

Intel

Microsoft, Bell Labs

Quantum Diamond Technologies

Pros

Fast working. Build on existing semiconductor industry.

Very stable. Highest achieved gate fidelities.

Stable. Build on existing semiconductor industry.

Greatly reduce errors.

Can operate at room temperature.

Cons

Collapse easily and must be kept cold.

Slow operation. Many lasers are needed.

Only a few entangled. Must be kept cold.

Existence not yet confirmed.

Difficult to entangle.

Note: Longevity is the record coherence time for a single qubit superposition state, logic success rate is the highest reported gate fidelity for logic operations on two qubits, and number entangled is the maximum number of qubits entangled and capable of performing two-qubit operations.

<http://science.sciencemag.org/content/354/6316/1090.summary>

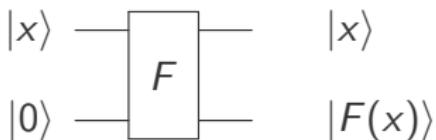


Reversible computation

- all computations are unitary
- $U^{-1} = U^\dagger$
- problems with function evaluation

$$\begin{cases} U|x\rangle = |z\rangle \\ U|y\rangle = |z\rangle \end{cases}$$

$$\Rightarrow U(|x\rangle - |y\rangle) = 0$$



Quantum parallelism

- flip bits
- 00, 01, 10, 11
- $\frac{1}{2} (|00\rangle + |01\rangle + |10\rangle + |11\rangle)$

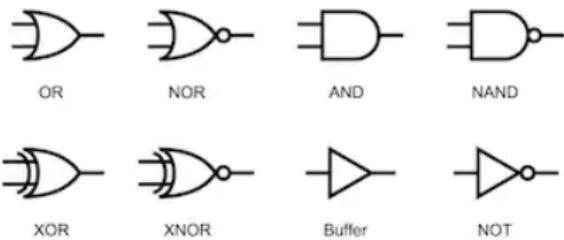
Measurement

- from quantum to classical
- projective \Rightarrow collapse
- probability distribution



Classical bits

Logic Gate Symbols



Quantum bit

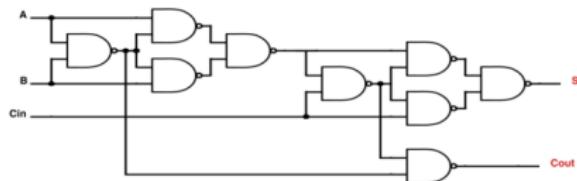
$$\begin{aligned}
 \text{X Gate} &\quad \boxed{X} \equiv \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \beta|0\rangle + \alpha|1\rangle \\
 \text{Bit-flip, Not} & \\
 \text{Z Gate} &\quad \boxed{Z} \equiv \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \alpha|0\rangle - \beta|1\rangle \\
 \text{Phase-flip} & \\
 \text{H Gate} &\quad \boxed{H} \equiv \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \frac{\alpha + \beta|0\rangle + \alpha - \beta|1\rangle}{\sqrt{2}} \\
 \text{Hadamard} & \\
 \text{T Gate} &\quad \boxed{T} \equiv \begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \alpha|0\rangle + e^{i\pi/4}\beta|1\rangle \\
 \text{Controlled Not} & \\
 \text{Controlled X} & \\
 \text{CNot} &\quad \begin{array}{c} \bullet \\ \text{Control} \\ \bullet \\ \text{Control} \\ \text{---} \\ \text{Target} \end{array} \equiv \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = a|00\rangle + b|01\rangle + c|10\rangle + d|11\rangle \\
 \text{Swap} &\quad \begin{array}{c} * \\ \text{Control} \\ * \\ \text{Control} \\ \text{---} \\ \text{Target} \end{array} \equiv \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = a|00\rangle + c|01\rangle + b|10\rangle + d|11\rangle
 \end{aligned}$$

<https://ieeexplore.ieee.org/document/1263787?arnumber=1263787>

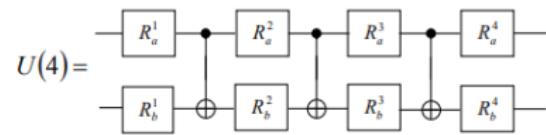


How many gates do you need?

Classical bits



Quantum bit



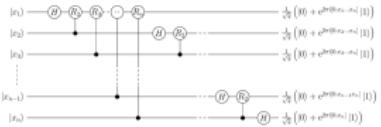
<https://arxiv.org/abs/quant-ph/0602174>

- NAND and XOR are universal

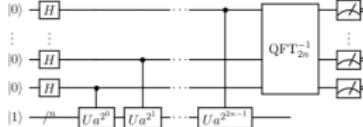
- single qubit rotation and CNOT ($\sqrt{\text{SWAP}}$) are universal
- different sets possible
- strongly depends on architecture



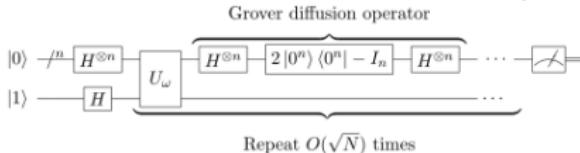
Using building blocks



https://en.wikipedia.org/wiki/Quantum_Fourier_transform



https://en.wikipedia.org/wiki/Shor%27s_algorithm



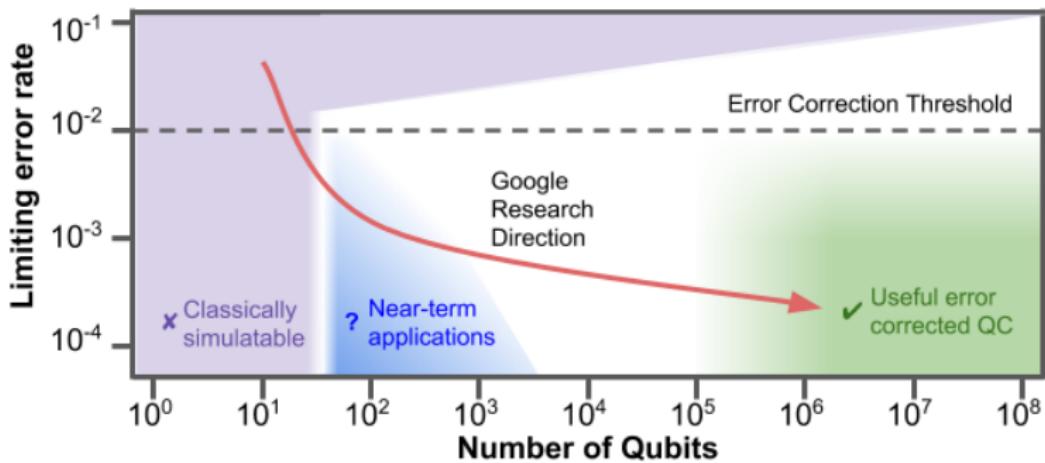
https://en.wikipedia.org/wiki/Grover%27s_algorithm

Speedups

- polynomial
- exponential
- heuristics
- oracles

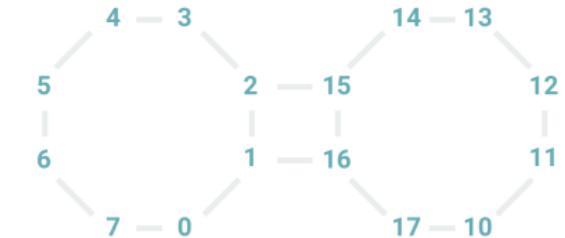


NISQ = Noisy Intermediate Scale Quantum

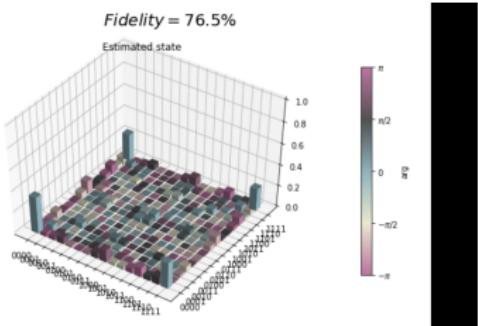


<https://ai.googleblog.com/2018/03/a-preview-of-bristlecone-googles-new.html>





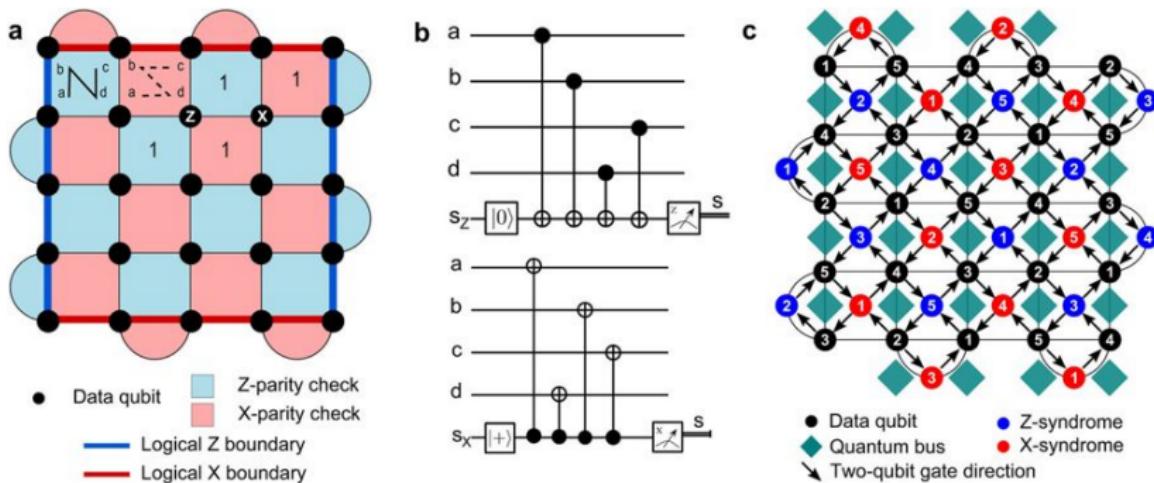
www.rigetti.com



Challenges

- connectivity
- decoherence
- qubit errors
- gate errors
- readout errors



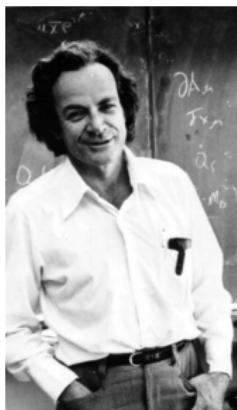


<https://www.nature.com/articles/s41534-016-0004-0>

- redundancy **but** no-cloning theorem
- add ancilla qubits
- measure syndrome and adjust upon error
- huge overhead ± 1000 physical qubits per logical



Hamiltonian Simulation $|\Psi(t)\rangle = \exp(-iHt) |\Psi(0)\rangle$



Combination of algorithms

- State preparation
- Unitary evolution
- Phase estimation
- Amplitude amplification

Resource estimates $\text{Fe}_7\text{MoS}_9\text{C}$

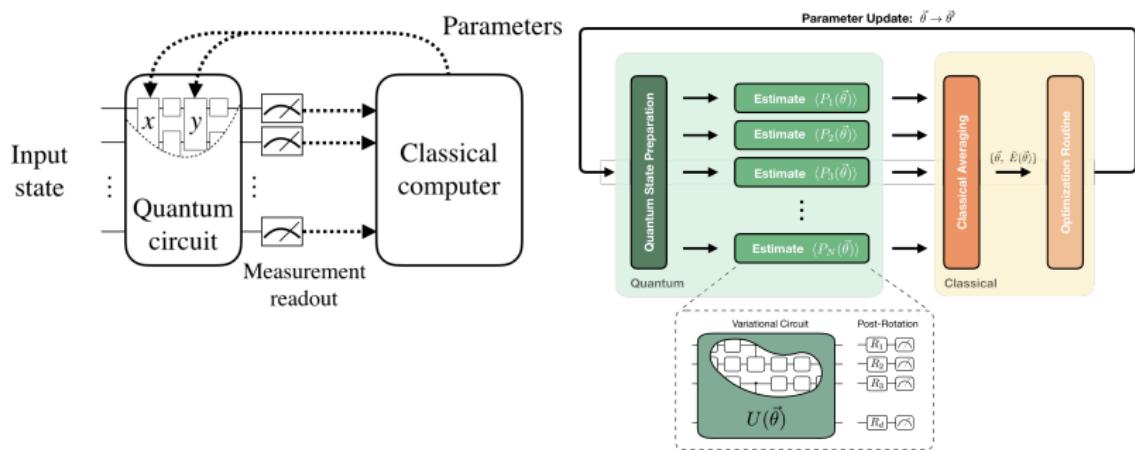
Structure	T gates	Ci. gates	Δt (10 ns)	Δt (100 ns)	Qubits
Quantitatively accurate simulation (0.1 mHa)					
Structure 1					
Serial	1.1×10^{15}	1.7×10^{15}	130 d	3.6 y	111
Nesting	3.5×10^{15}	5.7×10^{15}	15 d	4.9 mo	135
PAR	3.1×10^{16}	3.1×10^{16}	110 h	1.5 mo	1,982
Structure 2					
Serial	2.0×10^{15}	3.1×10^{15}	240 d	6.6 y	117
Nesting	6.5×10^{15}	1.0×10^{16}	27 d	8.9 mo	142
PAR	6.0×10^{16}	6.0×10^{16}	210 h	2.9 mo	2,024
Qualitatively accurate simulation (1 mHa)					
Structure 1					
Serial	1.0×10^{14}	1.6×10^{14}	12 d	3.9 mo	111
Nesting	3.3×10^{14}	5.6×10^{14}	1.4 d	14 d	135
PAR	3.0×10^{15}	3.0×10^{15}	11 h	4.6 d	1,982
Structure 2					
Serial	1.9×10^{14}	3.0×10^{14}	22 d	7.2 mo	117
Nesting	6.0×10^{14}	9.9×10^{14}	2.5 d	25 d	142
PAR	5.5×10^{15}	5.5×10^{15}	20 h	8.3 d	2,024

<https://www.pnas.org/content/114/29/7555.abstract>

⇒ Out of reach



Hybrid quantum classical algorithms



<https://arxiv.org/abs/1812.09976>



Year	Calculation	Citation	Number of qubits
1933	H_2	[74]	1
1950	Be	[76]	3, 4
1952	He	[77]	2
1955	He	[78]	2, 3
1956	BH	[41]	5
1956	H_2O	[41]	7
1957	LiH	[79]	3, 4, 5
1957	BeH^+	[79]	3, 4, 5
1960	Be	[82]	6
1960	CH_2	[83]	19
1963	H_2	[84]	3, 4, 5, 6
1966	HeH	[85]	3
1966	Li_2	[85]	3
1967	H_2O	[86]	10
1967	H_2O	[87]	24
1967	H_2O	[88, 89]	38, 39
1968	H_2O	[90]	39, 46
1968	Be	[91]	11
1969	Li , Be^+ , B^{++}	[92]	9, 10
1969	BH , FH	[93]	12, 14
1970	H_2O	[94]	23

<https://arxiv.org/abs/1208.5524>

Architecture/ Platform	System- of-interest	Number of physical qubits	Year
Photonic chip	HeH^+	2	2014
Single trapped ion	HeH^+		2017
Superconducting processor (transmon qubits)	H_2	2	2016
Superconducting processor (transmon qubits)	H_2	2	2017
	LiH	4	2017
	BeH_2	6	2017
Ion trap processor (Ca^{+} ions)	H_2	2	2018
	LiH	3	2018
Superconducting processor (transmon qubits)	H_2	2	2018
Silicon photonic chip	Two chlorophyll units in 18-mer ring of LHII complex	2	2018
Superconducting processor (transmon qubits) via Cloud	Deuteron	2-3	2018
Ion trap processor ($^{171}Yb^{+}$ ions)	H_2O	2-3	2019

<https://arxiv.org/abs/1812.09976>





<https://www.bbc.com/news/technology-12181153>



<https://www.research.ibm.com/ibm-q/>



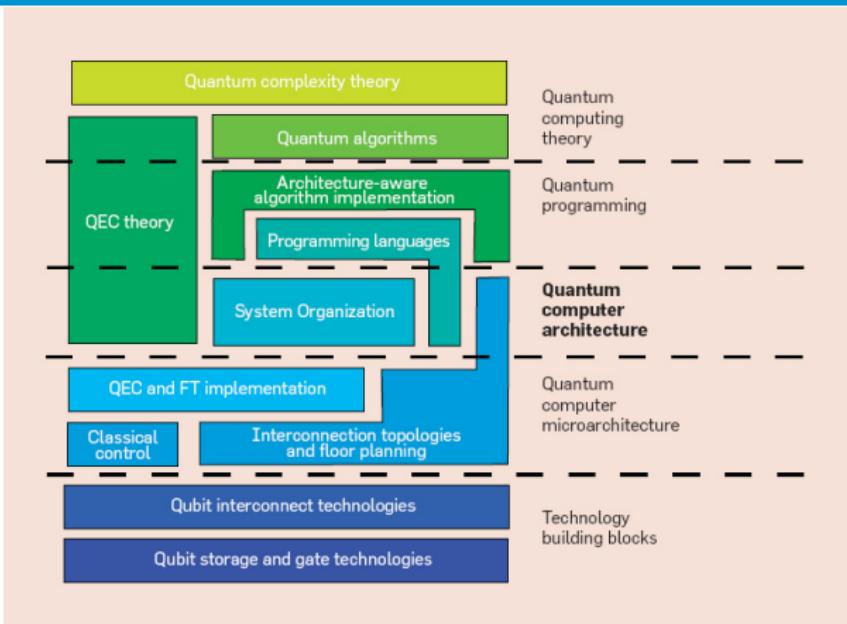
[https://en.wikipedia.org/wiki/Summit_\(supercomputer\)](https://en.wikipedia.org/wiki/Summit_(supercomputer))



<https://www.dwavesys.com>



Many things need to work together



<https://cacm.acm.org/magazines/2013/10/168172-a-blueprint-for-building-a-quantum-computer/fulltext>



Thank you for your attention!



Further reading and self-promotion:

Quantum Chemistry in the Age of Quantum Computing

<https://arxiv.org/abs/1812.09976>

slides @ <https://mfdgroot.github.io/>



Quantum Computing for Chemistry

A seminar with

Dr. Alán Aspuru-Guzik



Thursday
February 28th
2019

LM159
5:30PM-6:30PM

