



FAC RMatrix for Impact Width and Shift

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SLSP7

Sep 30– Oct 4, 2024
Gran Canaria, Spain

Baranger's Formula

The starting point of electron impact width and shift is the Baranger's formula, in the case of FWHM w :

$$w = n_e v \left[\sum_{k \neq i} \sigma_{ik} + \sum_{k \neq f} \sigma_{fk} + \int d\Omega |f_i(\Omega) - f_f(\Omega)|^2 \right] \quad (1)$$

Complications from angular momentum coupling treated according to Baranger (1958, PR 112, p856).

Unitarity of the S matrix allows simplifications under spherical symmetry (Peach 1996, Atomic, Molecular, Optical Physics Handbook):

$$\begin{aligned} w + i2s &= n_e v \frac{\pi a_0^2}{2E} \Omega(E) \\ \Omega &= \sum_{if} (-1)^{2J_i + 2J_f^T + j + j'} \left(2J_i^T + 1 \right) \times \left(2J_f^T + 1 \right) \\ &\times \left\{ \begin{matrix} J_f^T & J_i^T & 1 \\ J_i & J_f & j \end{matrix} \right\} \left\{ \begin{matrix} J_f^T & J_i^T & 1 \\ J_i & J_f & j' \end{matrix} \right\} \times \left[\delta_{\kappa\kappa'} - S_{ii} S_{ff}^* \right] \end{aligned} \quad (2)$$

RMatrix Inner Region

We construct a basis set for the $N + 1$ electron system using the anti-symmetrized product of target and one electron continuum basis functions with a fixed boundary condition at $r = a$ (Norrington, DARC manual), which diagonalizes the $N + 1$ Hamiltonian in the inner region

$$\Psi_k = \sum_{ij} c_{ijk} \mathcal{A} [\Phi_i, \phi_{ij}]^{J^T \pi} + \sum_m d_{mk} \theta_m(J^T, \pi) \quad (3)$$

Such that Ψ_k is the k -th eigenvector with eigenvalue E_k .

The boundary condition of continuum basis ϕ_{ij} is defined in terms of radial large and small components of the Dirac radial wavefunctions

$$\frac{Q_{ij}(a)}{P_{ij}(a)} = \frac{b + \kappa}{2ac} \quad (4)$$

R Matrix at Boundary Surface

The total scattering wavefunction at given energy E is expanded in terms of Ψ_k

$$\Psi(E) = \sum_k A_k(E) \Psi_k \quad (5)$$

Define

$$\begin{aligned} w_{ik}(r) &= \sum_j c_{ijk} \mathcal{P}_{ij}(r) & P_i(r) &= \sum_k A_k(E) w_{ik}(r) \\ v_{ik}(r) &= \sum_j c_{ijk} \mathcal{Q}_{ij}(r) & Q_i(r) &= \sum_k A_k(E) v_{ik}(r) \end{aligned}$$

and the R matrix

$$R_{ij} = \frac{1}{2a} \sum_k \frac{w_{ik}(a) w_{jk}(a)}{E_k - E} \quad (6)$$

It can be shown

$$P_i(a) = \sum_j R_{ij} [2acQ_j(a) - (b + \kappa_j)P_j(a)] \quad (7)$$

K Matrix from Boundary Matching

The reactance K matrix is defined through the asymptotic behavior of the continuum wavefunction as $r \rightarrow \infty$. For n_o open channels and n_c closed channels, there are $n_o + n_c$ independent solutions in the asymptotic region,

$$P_{ij} \sim \sin \theta_i \delta_{ij} + \cos \theta_i K_{ij} \quad (8)$$

for open channels, and

$$P_{ij} \sim \exp -|k_i|r \quad (9)$$

for closed channels. Solutions with these asymptotic behavior can be integrated inward until the RMatrix boundary at $r = a$, where using the R matrix boundary condition yields a system of linear equations for the reactance matrix K . The S matrix is obtained via

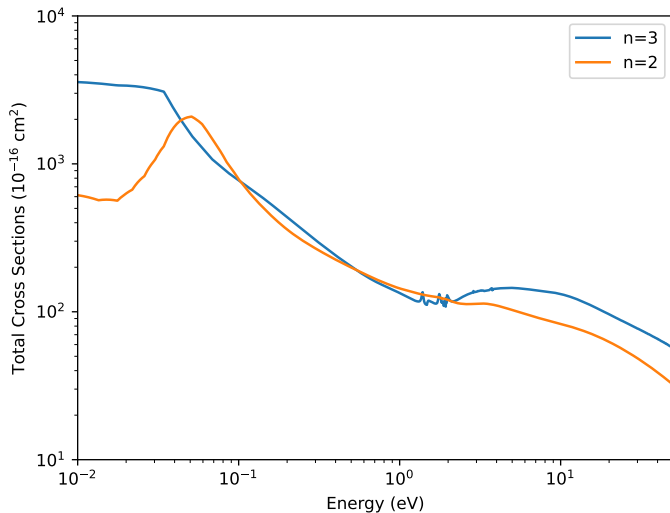
$$S = \frac{1 + iK}{1 - iK} \quad (10)$$

Li I and B III 2s-2p Width and Shift

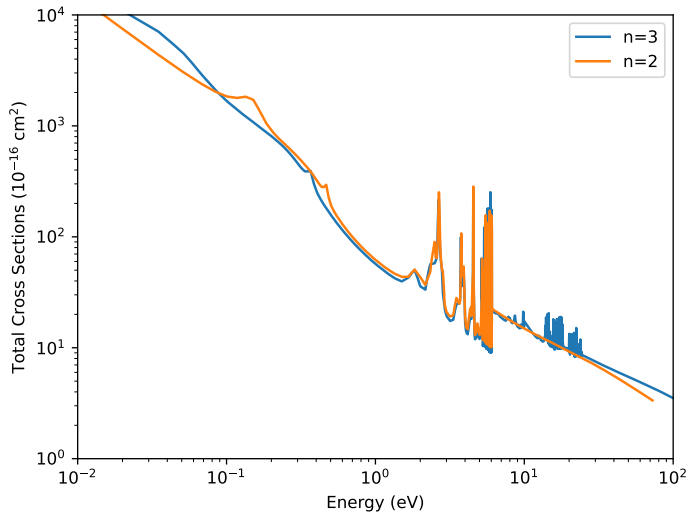
- Default target states, $1s^22l$.
- Expanded target states, $1s^22l$ and $1s^23l$.
- Widths, shifts and partial wave cross sections at requested energy grid for SLSP7.
- Widths and shifts with sufficient energy resolution to resolve electron capture resonances.
- Partial wave expansion up to $l = 100$.

For SLSP7 tabulated results, the default target states are used, and we average over $2p_{1/2}$ and $2p_{3/2}$ fine structure components. The $2p_{1/2} - 2p_{3/2}$ excitation cross sections are also ignored in the submitted results.

Total Cross Section of Li I 2s-2p Width

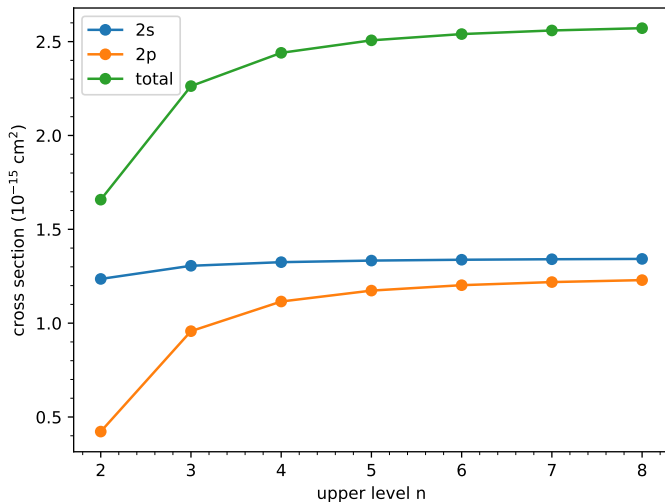


Total Cross Sections of B III 2s-2p Width



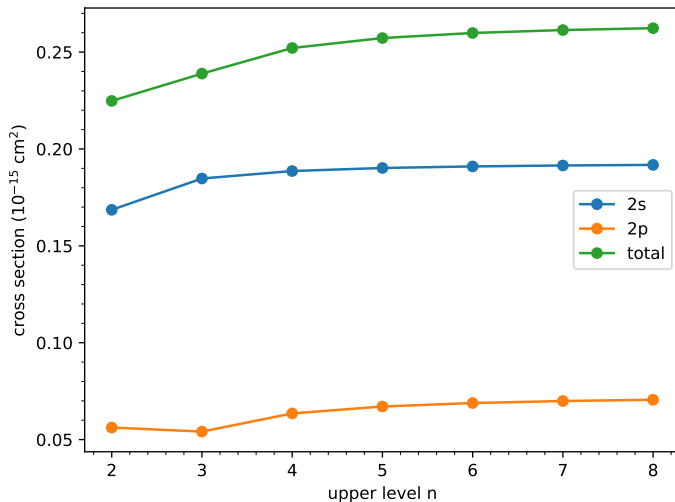
Effects of Excitation to $n > 3$: Li I

Distorted-wave estimation at $E = 100$ eV



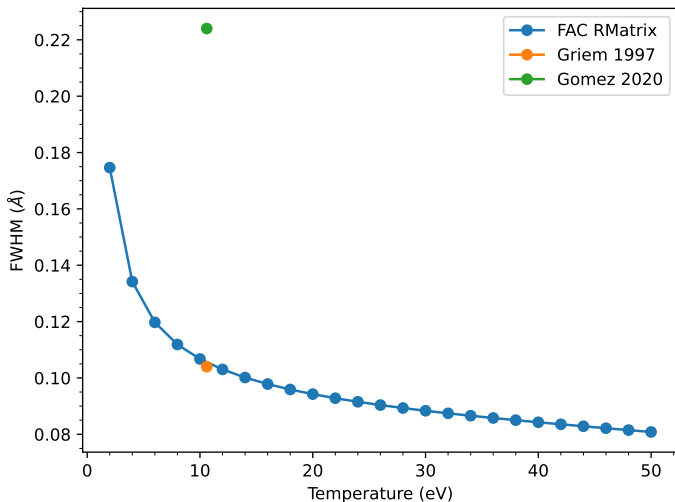
Effects of Excitation to $n > 3$: B III

Distorted-wave estimation at $E = 100$ eV



FWHM of B III 2s-2p in Thermal Plasma

$$n_e = 1.8 \times 10^{18} \text{ cm}^{-3}$$



Comparison of Total Cross sections of B III 2s-2p

