# Abstract

1. Dynamic occupancy models, which estimate local colonization and extinction rates from detection / non-detection data collected across multiple sampling periods (e.g., years), are powerful but data hungry statistical tools. However, many ecological studies lack sufficient sample sizes to estimate these dynamic parameters. Autologistic occupancy models, which estimate occupancy patterns through time and account for temporal autocorrelation in a species occupancy status, offer a parsimonious alternative that is well suited for datasets with fewer sites or seasons of data.
2. Here, I introduce the autoOcc R package, which can be used to fit autologistic occupancy models in a frequentist framework. This package also supports model comparison via AIC and making predictions from fitted models, making it a flexible and accessible option for those with detection / non-detection data collected over time.
3. Through simulations I show that autologistic occupancy models estimate parameters with less bias and more precision than dynamic occupancy models across a wide range of scenarios and sample sizes. These results suggest that autologistic occupancy models are a useful alternative when data are limited —a common constraint in ecological studies.
4. To illustrate practical use of autoOcc I provide two worked examples: estimating habitat associations of Virginia opossum (*Didelphis virginiana*) throughout Chicago, Illinois, USA and quantifying spatiotemporal patterns in black-backed woodpecker (*Picoides arcticus*) distributions as a function of fire severity throughout California’s montane forests. These examples demonstrate not only how to implement fitting autologistic occupancy models, but also how meaningful ecological inference can be drawn from them.
5. By formally introducing this modeling framework and lowering the barrier for others to use, autoOcc increases the range of tools available for researchers that study species occupancy dynamics, especially when data are limited.

# Keywords

autoOcc, detection probability, detection / non-detection data, occupancy models, species distribution models

# Introduction

Dynamic occupancy models—which estimate a species distribution through time as a function of local colonization and extinction rates—are powerful statistical tools. These models have been used to quantify wolf (*Canis lupus*) recolonization throughout France (Louvrier et al. 2018), predict avian range dynamics (Kalle et al. 2017, Briscoe et al. 2021), and estimate pulses in colonization rates based on a species reproductive phenology (Fidino and Magle 2017). Dynamic occupancy models are unfortunately also data hungry (Briscoe et al. 2021, Mckann et al. 2012), which can limit how useful they are to study rare species or apply them in regions where data are limited. Consequently, there is a need for an accessible tool that effectively quantifies species distributions through time, especially with reduced sample sizes.

One approach to quantify species distributions through time is to fit a single-season occupancy model with a “stacked” design (Schrimpf et al. 2020). This model treats each site and primary sampling period (i.e., discrete units of time where the occupancy status of a species is assumed to be constant at each site) combination as a separate detection history and accounts for pseudoreplication via a site-level random intercept. A study with 50 sites and 4 primary sampling periods would have 200 detection histories if no data was missing and 50 random effect terms to estimate. Stacked design occupancy models are now relatively simple to fit because random intercepts can be incorporated into occupancy models via the unmarked R package (Fiske and Chandler 2011). This model does not account for temporal dependence in occupancy between seasons and instead assumes that site-level occurrence per season is random and uncorrelated. Any temporal dependence in the data—which is likely present—would therefore be absorbed by some combination of the random effect term, the residual variance of the model, or regression coefficients associated with covariates that vary through time, if included. As there is no way to know where the temporal dependence is absorbed, using a “stacked” design could bias covariate effect estimates and hinder model interpretation. Furthermore, if there is insufficient data to fit a dynamic occupancy model, stacked design occupancy models may have the same problem, if not worse. As a “stacked” design occupancy model ignores temporal dependence and requires many parameters to be estimated from detection/non-detection data, they are not likely the ideal solution to address sample size issues with data collected over time.

Autologistic occupancy models are another approach that can account for spatial or temporal dependence in species distributions. Spatial autologistic occupancy models account for spatial autocorrelation such that the occupancy probability at a site can vary if nearby sites are also occupied. Temporal autologistic occupancy models account for temporal autocorrelation as a first-order Markov process so that the occupancy probability at a site can vary if it was also occupied in the previous timestep. While I specifically focus on temporal autologistic occupancy models here, those interested in spatial autologistic models can refer to Royle and Dorazio (2008). Temporal autologistic occupancy models (hereafter autologistic occupancy models) have been applied to numerous taxa. This model, for example, has been used to quantify the relationship between urban mammals and gentrification (Fidino et al. 2024), between bird diversity and variation in fire severity (Tingley et al. 2016), and between amphibian occupancy and climate change (Zipkin et al. 2012). Autologistic occupancy models are a useful option because they only require one additional parameter to quantify temporal dependence in occupancy. This makes autologistic occupancy models a statistically parsimonious method for those more interested in quantifying occupancy patterns rather than the processes that inform them (Yackulic et al. 2015). Yet, despite their utility, autologistic occupancy models are seldom used because they require researchers to write custom code to fit them, which severely limits the pool of researchers able to use this statistical method.

In this paper, I introduce the autoOcc R package (<https://github.com/mfidino/autoOcc>), which can be used to fit autologistic occupancy models under a frequentist framework, compare the relative fit of models via AIC, and make model predictions. After explaining the basic sampling scheme and statistical formulation, I use simulations to show that autologistic occupancy models are accurate and precise under most scenarios. Furthermore, I show how autoOcc can be used with two worked examples: estimating habitat associations of Virginia opossum (*Didelphis virginiana*, hereafter opossum) throughout Chicago, Illinois, USA and quantifying spatiotemporal patterns in black-backed woodpecker (*Picoides arcticus*) distributions as a function of fire severity throughout California’s montane forests (Stillman et al. 2023). I hope that by formally introducing autologistic occupancy models, their assumptions, and making them easier to fit in R, that this class of model will become a viable option for more researchers collecting species detection/non-detection data through time.

# Explanation of the method

## Basic sampling scheme and model assumptions

The sampling protocol for autologistic occupancy models is identical to the multi-season protocol developed by MacKenzie et al. (2003) for dynamic occupancy models. Briefly, sites are surveyed over multiple primary sampling periods to collect species detection/non-detection data. We assume that while the occupancy status of a species may change at sites between our primary sampling periods, the occupancy status does not change within a primary sampling period (i.e., the closure assumption). During each primary sampling period, a researcher conducts multiple independent surveys at each site to generate a detection history, which are a collection of 1’s and 0’s that respectively indicate whether a species was or was not detected.

Autologistic occupancy models have four key assumptions in addition to the closure assumption described above. First, sampling can result in false negatives (i.e., a species is present but not detected) but not false positives (i.e., the species is not present but was mistakenly detected). Second, all sampled sites are spatially independent. Third, autologistic occupancy models assume a first-order Markov process such that the occupancy status of a site at time *t* conditionally depends on the preceding state at *t-1*. Temporal dependence over longer time spans (e.g., *t-3* to *t*) is therefore indirectly estimated through the first-order Markov process, which lessens with increasing time span. Fourth, the probability of occupancy and detection is either constant across sites and surveys or explained by covariates. In other words, there is no unmodeled site-specific heterogeneity. If such assumptions are violated then the resulting model may be over precise or estimators could be biased and, as a result, the inference made from the associated model could be wrong (Bailey et al. 2013).

## The model

The simplest way to describe autologistic occupancy models is with a latent binary variable that denotes whether the species of interest is present or not at a site. While autoOcc does not use this parameterization, this is the best way to understand how the autologistic term, *θ*, is used in the model. Thus, for *i* in 1,…,*I* sites and *t* in 1,…,*T* primary sampling periods (hereafter seasons), let *zi,t* be the latent binary occupancy status of a species at site *i* and time *t* and let *ψi,t* be the occupancy probability. During the first season there is no information about the occupancy status of the species before sampling began. Thus, when *t* = 1 the latent state model is

|  |  |  |
| --- | --- | --- |
|  | *,* | Eq. 1 |

where is the product of a vector of regression coefficients (, which includes the model intercept) and their associated covariates (), which is indexed by *i* and *t* because the covariates could vary across space, time, or both. The first element of is a 1 to account for the model intercept. For *t* > 1 we modify the logit-linear predictor by adding our autologistic term, *θ*, that is multiplied by a species’ occupancy status at the site of interest in the previous season.

|  |  |  |
| --- | --- | --- |
|  | *,* for  *t > 1* | Eq. 2 |

When the species is present during the previous season then and *θ* is added to the logit-linear predictor (i.e., ), otherwise it is excluded (i.e., ). Positive *θ* values indicate that species presence in the previous timestep increases *ψi,t* in the current timestep, whereas negative *θ* values indicate the opposite. However, if the species was absent at t-1, then , which means that *θ* has no bearing on the occupancy status at time *t* when this occurs. As such, when the autologistic *θ* term is added to the linear predictor it just increases or decreases the latent state model intercept, depending on its direction, given that the species is present at t-1.

For the detection model, let *pi,t,j* be the conditional probability of detecting the species during *j* in 1,…,*J* secondary sampling periods (hereafter surveys) given the species is present. Further, let *y*i,t,j represent the detection / non-detection data for site *i*, season *t*, and survey *j* which equals 1 if the species was detected, 0 if not, and NA if data was not collected. This level of the model is described as,

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| --- | --- | --- |
|  |  | Eq. 3 |

where is the product of a vector of regression coefficients (**)** and their associated covariates () that can vary across sites, seasons, or surveys. Given Eq. 1 through Eq. 3, autologistic occupancy models only add one new parameter to the model, *θ*, to account for temporal dependence in species occupancy from one timestep to the next and add nothing to the detection-level of the model.

The latent variable approach described above could be written as a Bayesian hierarchical model in either NIMBLE (de Valpine et al. 2017) or JAGS (Plummer 2003). However, if we drop the latent variable and write the model with matrix notation it is possible to estimate the associated parameters via maximum likelihood, which is what I did for autoOcc. To follow along with this model formulation, assume one site has been sampled across four seasons (indicated in square brackets) with three surveys per season to generate the detection history [110], [000], [101], [100]. Thus, the species was detected at least once in the first, third, and fourth seasons and was not detected at all during the second season. For this formulation let the parameter *ηt* represent the occupancy probability at survey *t* during either the first season or when the species was not present at time t-1, while the parameter *ωt* is the occupancy probability if the species was present at *t - 1*. These two probabilities are nearly identical and can share parameters. For example, an intercept only model for these probabilities could be written as logit(*ηt*) = *β*0 and logit(*ωt*) = *β*0  + θ. Following MacKenzie et al. (2003), and dropping the site subscript for simplicity, the probability of observing the first season detection history is

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| --- | --- | --- |
|  | . | Eq. 4 |

A verbal description of Eq. 4 is “the species was present and detected on the first two surveys but not the last survey.” In the second season the species was not detected, which means either the species was not present at *t* = 2 or the species was present but not detected. Because the species was present in the previous season we use *ω*2 instead of *η2*. Thus, the probability of observing the second season detection history is

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| --- | --- | --- |
|  | . | Eq. 5 |

For *t* = 3, we are uncertain if the species was present in the previous season and so we use *η3* and *ω3* to generate the probability of this survey, multiplying both by the necessary detection probabilities:

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| --- | --- | --- |
|  |  | Eq. 6 |

A verbal description of Eq. 6 is “the species either was or was not present in season 2 and was detected on the first and third survey of season 3, but not the second survey.” Looking at Eq. 6, it could be further simplified by factoring out the detection probabilities. Finally, for t = 4 we know that the species was present in the previous timestep, so we use *ω4*:

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| --- | --- | --- |
|  | . | Eq. 7 |

The probability of observing the entire detection history across time is the product of Eq. 4 – 7.

While it would be possible to write out the likelihood of each detection history as I did throughout Eq. 4 – 7, doing so would be difficult to generalize to any dataset. Fortunately, MacKenzie et al. (2003) describe a more general approach that uses matrix notation for their dynamic occupancy model, which I modified for autoOcc. Let *ϕ0* be a row vector for the first sampling period:

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| --- | --- | --- |
|  | . | Eq. 8 |

For the remaining seasons we use a 2 x 2 matrix of transition probabilities, ***ϕ****t*, that describes how a site may move from one state to the next from season *t* to *t + 1*.

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| --- | --- | --- |
|  | . | Eq. 9 |

Note that rows of ***ϕ****t* denote the occupancy state at *t*, columns are the occupancy state at *t + 1*, and all rows sum to 1. For example, *ω*t is the probability the species was present at *t* and *t + 1*, while 1 –*ηt* is the probability the species was not present at *t* and *t + 1*. The elements that make up ***ϕ****t* in Eq. 9 is the primary difference between autologistic and dynamic occupancy models. Finally, let *δ****y,t*** be a column vector that contains the probability you would observe detection history **y**t,1:J on season *t*, conditional on the occupancy state. While this is not how autoOcc handles this component of the model, it may help to imagine *δ****y,t*** as a matrix of column vectors with a number of columns equal to the total number of possible detection histories. When considered in this way, **y**t,1:J indexes the appropriate column vector that matches its detection history to index the correct detection probabilities. Two examples of these column vectors are

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| --- | --- | --- |
|  | and  . | Eq. 10 |

The second element of each column vector takes either the value 0 if the species was detected at least once across surveys during a season or 1 if the species was not detected. With those three components the probability of observing a given detection history is

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| --- | --- | --- |
|  | . | Eq. 11 |

In Eq. 11, the D(***δ****y,t*) function indicates that the elements in the column vector of ***δ****y,t* are placed along the main diagonal of a diagonal matrix. This transformation is done to ensure that all the elements of Eq. 11 are conformable and that the appropriate likelihood is calculated. Because Eq. 11 is the probability of one detection history, the model likelihood is

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| --- | --- | --- |
|  |  | Eq. 12 |

As with the dynamic occupancy model outlined in MacKenzie et al. (2003), the autologistic occupancy model can accommodate covariates via the logit link and handle missing surveys by including NA values in the detection history where data were not collected. These extensions are implemented in autoOcc.

## Deriving expected occupancy estimates from autologistic occupancy models

Expected occupancy estimates from autologistic occupancy models can be generated in a similar fashion to expected occupancy estimates from dynamic occupancy models. As dynamic occupancy models estimate local colonization (γ) and extinction rates (ε), the expected occupancy of these probabilities is γ / (γ + ε). By replacing those probabilities with those estimated from the autologistic occupancy model, we arrive at the following formula:

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| --- | --- | --- |
|  | . | Eq. 12 |

To demonstrate how this may look with parameters estimated via autoOcc and their associated covariates we could rewrite Eq. 12 as

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| --- | --- | --- |
|  | , | Eq. 13 |

where ilogit() represents the inverse logit link function, .

# Things to consider

To provide some guidance on how much data should be collected before using autoOcc — and illustrate how it performs compared to other statistical techniques a researcher may use — I conducted a simulation study to compare the accuracy and precision of autologistic occupancy models to dynamic occupancy models across a range of sample sizes. For each class of model (autologistic and dynamic), simulations varied in how common or rare the species was, the number of sites sampled, and the number of seasons sampled. Specifically, I used four scenarios where the expected occupancy of a species was either 0.2, 0.3, 0.4, or 0.5. For the autologistic occupancy model this was done by setting *ϑ* = 1 and using Eq.13 to determine what the model intercept should be to achieve the desired expected occupancy. For the dynamic occupancy model there are multiple colonization and extinction rates that could generate these expected occupancy probabilities. After determining possible solutions for each expected occupancy scenario I chose one at random. The number of sites sampled ranged from 30 to 100 locations in intervals of 10 while seasons sampled ranged from 4 to 12 in intervals of 2. Thus, for the four expected occupancy, seven site, and six season scenarios there was a total of 160 different combinations to simulate for both the autologistic and dynamic occupancy models. Every combination was simulated and fitted 550 times and resulted in a total of 176,000 simulations and model fits.

For each simulation scenario I considered one continuous covariate on each fundamental parameter (i.e., occupancy and detection for autologistic models and initial occupancy, colonization, extinction, and detection for dynamic models). Across both model classes I set slope terms to 1 on the logit scale for all latent states except for the initial occupancy slope term of the dynamic model, which was set to 0 (i.e., the covariate was not associated to initial occupancy, though I still tried to estimate the association with the model). The initial occupancy intercept in the dynamic model was set to 1 (i.e., an initial occupancy probability of ~0.73). To model detection, the same covariate was used, but the slope term associated with this covariate was set to 0.50 across both models. Finally, I set the intercept to -0.90 on the logit scale, which resulted in a 0.29 average detection probability per survey. As I assumed 4 surveys per sampling period the overall probability of detecting the species at least once if they were present was about 0.75 (i.e., 1 – (1 – 0.29)4). In total, the autologistic and dynamic occupancy model respectively had five and eight parameters to estimate from their simulated datasets. After I fitted the simulated datasets across all scenario combinations using functions within autoOcc, I calculated the relative bias of each model parameter as the root mean square error (RMSE), and precision (i.e., width of 95% confidence intervals) of latent state parameters. Across the *n* simulations for each scenario, the RMSE of each model parameter can be derived as , where is the true parameter value and is the estimated parameter value.

Autologistic occupancy models had less parametric bias than dynamic occupancy models. For example, all latent state parameters had an RMSE ≤ 0.5 for 53.13% of scenarios for autologistic occupancy models and 0.00% for dynamic occupancy models, with the smallest sample size to achieve this RMSE cutoff being either 70 sites with 4 seasons of data or 30 sites with 10 seasons. Averaged across scenarios, the relative bias of the autologistic latent state intercept was about 6.5 times less than the dynamic colonization intercept but was about 1.45 times greater than the dynamic extinction intercept (Figure 1). The autologistic term, θ, term had consistently less bias which was respectively 51.0 and 5.4 times smaller than the dynamic colonization and extinction intercepts. Across all parameters, the dynamic model colonization intercept had the greatest bias when the number of sites ≤ 50 and the number of seasons ≤ 8 (Figure 1K, Fig 10). Averaged across scenarios, the relative bias in the autologistic model slope term was 4.2 times smaller than the dynamic model colonization slope term and 1.6 times smaller than the extinction slope term (Figure 2). Furthermore, the relative bias in the colonization slope term increased with the expected occupancy of the species and, like the colonization intercept, was highest when the number of sites and seasons were at their lowest across scenarios (Figure 2.K).



**Figure 1**. The relative bias of the latent state intercept (Ψ0) and autologistic term (θ0) of autologistic occupancy models as well as the colonization (γ0) and extinction (ε­0) intercepts of dynamic occupancy models across 160 different simulation scenarios. Rows represent different scenarios where the expected occupancy of the simulated species ranges from 0.2 to 0.5, whereas the number of sites and seasons simulated varying within each subplot.



**Figure 2**. The relative bias of the latent state slope (Ψ1) of autologistic occupancy models as well as the colonization (γ1) and extinction (ε­1) slope terms of dynamic occupancy models across 160 different simulation scenarios. Rows represent different scenarios where the expected occupancy of the simulated species ranges from 0.2 to 0.5, whereas the number of sites and seasons simulated varying within each subplot.

Autologistic occupancy models were also more precise than dynamic occupancy models. Averaged across scenarios the average 95% CI width of the autologistic intercept was 1.86 times narrower than the dynamic model colonization intercept and 1.3 times narrower than the extinction intercept (Figure 3). However the autologistic term, θ, had greater uncertainty under some scenarios. The average 95% CI width for θ was roughly 1.09 times larger than the dynamic colonization intercept and 1.6 times larger than the dynamic extinction intercept. This difference was largely driven by the 0.4 and 0.5 expected occupancy scenarios, which had relatively wide 95% CI widths for both θ (Figure 3N) and the colonization intercept (Figure 3O). Averaged across scenarios, the autologistic model slope term confidence interval was 2.67 and 1.56 times narrower than the dynamic model colonization and extinction slope term confidence intervals, respectively (Figure 4). The largest difference between models was when the expected occupancy of the species was 0.5, especially at small sample sizes. This last result should not be surprising given that binomially distributed variables have the greatest variance when the probability of success is 0.5.



**Figure 3**. The precision (95% confidence interval width) of the latent state intercept (Ψ0) and autologistic term (θ0) of autologistic occupancy models as well as the colonization (γ0) and extinction (ε­0) intercepts of dynamic occupancy models across 160 different simulation scenarios. Rows represent different scenarios where the expected occupancy of the simulated species ranges from 0.2 to 0.5, whereas the number of sites and seasons simulated varying within each subplot.



**Figure 4**. The precision (95% confidence interval width) of the latent state slope (Ψ1) of autologistic occupancy models as well as the colonization (γ1) and extinction (ε­1) slope terms of dynamic occupancy models across 160 different simulation scenarios. Rows represent different scenarios where the expected occupancy of the simulated species ranges from 0.2 to 0.5, whereas the number of sites and seasons simulated varying within each subplot.

When considered together, autologistic occupancy models had less bias and more precision than dynamic occupancy models across a wider range of sample sizes. Notably, across all scenarios autologistic occupancy models had relatively low bias for all latent state parameters. This was not true for dynamic models, which especially struggled when the species was more common and when a smaller number of sites were sampled. As other researchers have suggested that dynamic occupancy models require at least 120 sites to be used reliably (McKann et al. 2012), autologistic occupancy models are clearly a valid option when dealing with small sample sizes, especially when the number of sites ≥ 70 and number of seasons ≥ 4. Increasing sample size did deliver a notable increase in precision for both class of models, especially with respect to θ in the autologistic model. Most importantly, autologistic model slope terms were far more precise than dynamic model slope terms, which showcases that autoOcc can be especially useful if the goal of a study is to evaluate the habitat associations of a species and a researcher is limited with the amount of data they may be able to collect.

I want to caution that the results of this simulation study cannot provide rigorous suggestions for how much data are needed before using autologistic occupancy models. The natural world is far more complex than the simulations I ran. The appropriate sample size will vary depending on your research questions, logistical constraints, and the ecology of the species you plan to study. To provide some recommendations to start with, I suggest to focus on increasing precision because the relative bias was low across all scenarios of the autologistic model simulations. As such, people interested in using this class of model may be able to achieve high precision with a minimum of 70 sites sampled for 8 seasons and a moderate precision with 40 sites sampled for 6 seasons.

# Worked examples

To demonstrate how models can be fitted within autoOcc I have two worked examples coming from different taxa and data collection methods. For the first, I analyzed camera trap data collected throughout Chicago, Illinois USA to quantify if different social-ecological gradients are associated to the distribution of Virginia opossum (*Didelphis virginiana*). For the second, I recreated an analysis by Stillman et al. (2023) who used a Bayesian autologistic occupancy model with survey data to assess how pyrodiversity, or the spatial and temporal variation of fire characteristics, affects black-backed woodpecker occupancy throughout the montane forests of California, USA. Across both worked examples I compare the relative fit of different models using AIC (Anderson and Burnham, 2004), and use a ΔAIC of 2 as a cutoff value to determine which models within a model set were competitive.

## Virginia opossum occupancy throughout Chicago, IL

The data for this example comes from 96 spatial locations across the greater Chicago metropolitan area (Chicago, IL, USA). In 2019, camera traps were deployed throughout urban greenspace for 28-day sampling seasons in January, April, July, and October for a total of four primary sampling periods (see Magle et al. 2019 for further sampling details). Weekly detection histories were generated from these data where one occasion represented a week of sampling.

For this example, we are interested in understanding how patterns of urban intensity and neighborhood wealth are associated with opossum occupancy, both of which may be associated with opossum occupancy in non-linear ways. Furthermore, as opossum activity changes throughout the year due to Chicago’s cold winters (Gallo et al. 2022), we also want to quantify the relationship between opossum detection probability and average weekly temperature.

For our analysis, we need to assemble three components in R: 1) the opossum detection history, 2) occupancy covariates, and 3) detection covariates. The detection data for this example are already included within autoOcc so those can be loaded and set up for further analysis.

# load opossum detection / non-detection data

library(autoOcc)

data("opossum\_det\_hist")

# convert long format data to an array

opossum\_y <- format\_y(

x = opossum\_det\_hist,

site\_column = "Site",

time\_column = "Season",

history\_columns = "Week"

)

This dataset has 6 columns that provide information on the name of the sampled location (Site), the season sampled (Season), and the detection data (Week\_1 through Week\_4). Furthermore, this dataset is in long format and is sorted along two columns, season and site, such that sites are sorted alphabetically within each of the four seasons of data. To use this dataset in autoOcc, our detection history needs to be set up as a site by season by survey three-dimensional array, which is similar to other occupancy modeling packages like spOccupancy (Doser et al. 2022). The format\_y() function carries this out so long as you specify which columns denote sites, seasons, and detection data. For the history columns, format\_y() uses regular expressions to locate all columns that include whatever is included as an argument.

After setting up the detection data we need to prepare our occupancy covariates for analysis. To represent a gradient of urban intensity I used the proportion of impervious cover within 1 km of each sampling location which was queried from the National Land Cover Database (Dewitz, 2019). To represent neighborhood wealth I used the median per capita income within 1 km of each site from the 2014-2018 American Community Survey (U.S. Census Bureau 2012). These two covariates can be queried from the opossum\_covariates dataset located within autoOcc. After subsetting the data I scaled the covariates for our analysis by subtracting their mean and dividing by their standard deviation, which can help improve model convergence and interpretation.

# load covariates

data("opossum\_covariates")

# subset only impervious and income

opossum\_covariates <- opossum\_covariates[,

grep("Impervious|Income", colnames(opossum\_covariates))

]

# make new data.frame, scale covariates, and convert back to numeric

occ\_cov\_list <- opossum\_covariates

occ\_cov\_list$Impervious <- as.numeric(scale(occ\_cov\_list$Impervious))

occ\_cov\_list$Income <- as.numeric(scale(occ\_cov\_list$Income))

As a reminder, we wanted to quantify the relationship between opossum detection probability and average weekly temperature, which was summarized from daily temperatures provided by NCDC (NCDC 2023). As temperature varies across each week of sampling, these data need to be stored in a matrix with a number of rows equal to the number of sites and a number of columns equal to the number of surveys conducted over the entire study. From there, this matrix can be stored within a named list. In our example we have 96 sites, 4 seasons of data, and 4 weeks of sampling within each season so the matrix for our weekly temperature covariate will have 96 rows and 16 columns such that the first four columns are associated to the four weeks of sampling in the first season and the last four columns are associated to the four weeks of sampling in the last season. As the temperature data I queried did not vary across space I replicated the same value along each column vector. Thus, assuming we have summarized our weather data down to 16 values, one for each week of sampling, the matrix for this detection covariate is

Temperature <- matrix(

rep(

as.numeric(

scale(

weather\_data\_vector

)

),

each = dim(opossum\_y)[1]

),

nrow = dim(opossum\_y)[1],

ncol = prod(

dim(opossum\_y)[2:3]

)

)

Where weather\_data\_vector is a numeric vector that contains the 16 temperature values that were queried. If we had a temporal covariate or spatiotemporal covariate that only varied by primary sampling period and not surveys we could instead store those data in a site by season matrix. Our temperature matrix, as well as any other covariates we may want to include on opossum detection probability, are stored within a named list. For example, if I wanted to control for our two social-ecological gradients on detection probability they can be included like so

det\_cov\_list <- list(

Temperature = Temperature,

Impervious = occ\_cov\_list$Impervious,

Income = occ\_cov\_list$Income

)

With these three pieces of data you can use autoOcc to fit a suite of models with the auto\_occ() function and then compare their relative fit with compare\_models(). For this analysis I fitted 10 models. Models understandably varied in which covariates were included but also whether those covariates had a quadratic term. For example, there are 8 possible models that could be fitted with two occupancy covariates, both with and without quadratic terms. The last two models included a temperature only model (i.e., intercept only for occupancy, but temperature and temperature2 on detection probability) and a null model. Every model except for the null model included temperature and temperature2 in the detection logit-linear predictor. As an example, the global model could be specified as

global\_quadratic <- auto\_occ(

~Temperature + I(Temperature^2) +

Impervious + I(Impervious^2) + Income + I(Income^2)

~Impervious + I(Impervious^2) + Income + I(Income^2),

y = opossum\_y,

det\_covs = det\_cov\_list,

occ\_covs = occ\_cov\_list

)

Note that the model formulas are the first argument of this function, and just as with the unmarked package, are written as a double right-hand side formula for detection and occupancy, in that order. After fitting the remaining models and storing them in a list you can compare their relative fit with the compare\_models() function via AIC. There was only one competitive model which included a linear effect of income on opossum occupancy but a quadratic effect of impervious cover, and we can use the summary() function to look at the estimated parameters of this model.

# What the model list could look like after fitting the 10 models

model\_list <- list(

global\_quadratic = global\_quadratic,

global = global,

income\_quadratic = income\_quadratic,

income\_quad\_imperv = income\_quad\_imperv,

income = income,

imperv\_quadratic = imperv\_quadratic,

imperv\_quad\_income = imperv\_quad\_income,

imperv = imperv,

temperature = temp,

null = null

)

# compare models via AIC

aic\_results <- compare\_models(

model\_list,

digits = 2

)

# Look at first few models

head(aic\_results, 3)

model npar AIC delta AICwt cumltvWt

imperv\_quad\_income 11 1213.11 0.00 0.55 0.55

global\_quadratic 13 1215.27 2.16 0.19 0.74

imperv\_quadratic 9 1216.16 3.05 0.12 0.86

# Summarise best-fit model

summary(imperv\_quad\_income)

Call:

autoOcc::auto\_occ(formula = ~Temperature + I(Temperature^2) +

Impervious + I(Impervious^2) + Income ~ Impervious + I(Impervious^2) +

Income, y = opossum\_y, det\_covs = det\_cov\_list, occ\_covs = occ\_cov\_list)

optim convergence code: 0

optim iterations: 51

Occupancy estimates:

parameter Est SE lower upper p

psi – (Intercept) -0.324 0.200 -0.716 0.0674 1.05e-01

psi – Impervious -0.341 0.165 -0.664 -0.0177 3.87e-02

psi – I(Impervious^2) -0.274 0.131 -0.531 -0.0180 3.60e-02

psi – Income -0.279 0.164 -0.601 0.0436 9.02e-02

psi – theta 1.637 0.365 0.922 2.3517 7.16e-06

Note: psi – theta is the autologistic term

Detection estimates:

parameter Est SE lower upper p

rho – (Intercept) 0.3826 0.145 0.0984 0.6667 0.008315

rho – Temperature 0.3374 0.133 0.0761 0.5986 0.011373

rho – I(Temperature^2) -0.4384 0.116 -0.6661 -0.2106 0.000162

rho – Impervious -0.0536 0.145 -0.3386 0.2315 0.712669

rho – I(Impervious^2) -0.1291 0.110 -0.3446 0.0863 0.240025

rho – Income -0.2054 0.130 -0.4601 0.0493 0.113935

AIC: 1213.113

Making predictions for this model is relatively straightforward via the predict() function in autoOcc. Assume we want to predict opossum occupancy across a gradient of impervious cover, which ranged from about 20% to 80% across this study. These predictions can be made in three steps. First, we generate a dataset with covariate values we’d like to make predictions with, holding other covariates at their mean. As we mean-centered our continuous covariates we can keep all other columns at their mean value of 0.

# A vector of impervious cover

imperv\_vec <- seq(20, 80, length.out = 300)

# The prediction data.frame

imperv\_dm <- data.frame(

matrix(

0,

ncol = ncol(imperv\_quad\_income@occcovs),

nrow = length(imperv\_vec)

)

)

# add column names

colnames(imperv\_dm) <- names(imperv\_quad\_income@occcovs)

Second, our impervious cover data needs to be scaled exactly as we for our analysis. Thus, we center and scale the prediction impervious cover vector by the mean and standard deviation of the impervious cover data at our sampled sites.

# add in imperv and scale it in the same way as we did in the model

imperv\_dm$Impervious <- (

imperv\_vec – mean(opossum\_covariates$Impervious)

) / sd(opossum\_covariates$Impervious)

Finally, we can make predictions. At a minimum the predict()function in autoOcc requires you to provide the model you’d like to make predictions with and the type of prediction you’d like to make (“psi” for the latent state, “rho” for detection). You can also add a new dataset to make predictions with and input the confidence level you would like for confidence intervals. Finally, because this function uses Monte Carlo simulations to approximate confidence intervals you can also specify a sufficiently large number of Monte Carlo simulations (defaults to 3000) and a seed.

Imperv\_pred <- predict(

object = imperv\_quad\_income,

type = "psi",

newdata = imperv\_dm,

nsim = 3000,

seed = 453

)

These predictions can then be plotted out (Figure 5). In this example, opossum occupancy was greatest when impervious cover was roughly 43% and decreased with increasing levels of neighborhood wealth. I also detected a non-linear relationship between opossum detection probability and weekly temperature such that opossum detection probability was highest when the weekly average temperature was around 15 °C (Figure 5).



**Figure 5.** Opossum occupancy throughout Chicago, Illinois varied non-linearly with impervious cover and linearly with per capita income whereas opossum detection probability had a non-linear relationship with mean weekly temperature. The detection/non-detection data used to generate this figure are supplied with autoOcc and came from a long-term camera trapping study throughout Chicago.

## Black-backed woodpecker occupancy throughout the montane forests of California

For this worked example I recreated the analysis conducted by Stillman et al. (2023), who used a Bayesian autologistic occupancy model to quantify how pyrodiversity affects black-backed woodpecker occupancy. For this study these authors had an impressive 10 years of woodpecker survey data at nearly 2,400 sites, though sites were not surveyed each year. For their sampling protocol, they used single-visit surveys that were divided into multiple independent surveys. Specifically, each survey consisted of playing black-backed woodpecker vocalizations for 30 seconds and then listening for responses for 1.5 minutes. A maximum of three playback surveys were conducted at each site, and playback surveys were stopped after the first detection (i.e., a removal design). Finally, point counts were also conducted at roughly half of these sites after the playback surveys. For further information on sampling see Tingley et al. (2018, 2020).

Stillman et al. (2023) compared three models: a static occupancy model, a temporal autologistic occupancy model, and a landscape-temporal autologistic occupancy. These last two models varied in which covariates were present within the model. While Stillman et al. (2023) also incorporated random effects into their models, autoOcc cannot. As such, random effects were not used for this worked example.

I fitted three models to these data. All models had the same detection logit-linear predictor, which included whether a survey was 2 or 3 minutes in length (2 min = 0, 3 min = 1), the ordinal day of a survey, and the survey type (point count = 0, playback = 1). As a departure from Stillman et al. (2023), I did not fit a static occupancy model as the first model and instead used an intercept-only autologistic model. The second model, which Stillman et al. (2023) described as their “temporal occupancy model,” accounted for the effects of years since fire on occupancy. This model included 5 occupancy covariates: the number of years since a fire had started at a site, the average burn severity of the last fire within 100m, the proportion pre-fire canopy cover within 100m, elevation, and latitude. This model also included quadratic terms for elevation and fire age as well as a statistical interaction between elevation and latitude. The third, “landscape-temporal occupancy model,” had the covariates from the temporal occupancy model but also included other covariates to account for post-fire habitat dynamics. As such, in addition to the aforementioned covariates this model included a metric for diversity in burn severity, distance to a low burn severity forest patch, and the summed basal area of pre-fire live red fir and white fir within 100m. This landscape-temporal occupancy model included quadratic terms for elevation and fire age as well as statistical interactions between burn severity and fire age, elevation and fire age, and fir basal area and fire age.

Just like Stillman et al. (2023), I found that the landscape-temporal occupancy model had the best relative fit with the temporal occupancy model having a ΔAIC of 122.48 from the landscape-temporal model. Parameter estimates from the best-fit model were similar to the Bayesian analysis of Stillman et al. (2023) such that inference made across models is comparable (Figure 6). However, because I did not include random effects in the autologistic occupancy model there was also less parametric uncertainty (i.e., smaller confidence intervals) with the autoOcc analysis across every model parameter. Regardless, had this analysis originally been conducted with autoOcc, Stillman et al. (2023) would have found similar results and concluded that woodpecker occupancy was highest directly after a fire, especially if the site had a high burn severity (Figure 6). For the complete analysis in R, see supporting information.



**Figure 6.** A comparison of autologistic occupancy model parameter estimates of the same dataset analyzed under a frequentist framework in autoOcc or a Bayesian framework in JAGS (Stillman et al. 2013). Though the models fitted were not identical (i.e., the Bayesian analysis included random effects), similar inference can be made from the resulting model parameters. Median parameter estimates and 95% credible intervals of the Stillman et al. (2013) analysis was collected from the supporting information of their manuscript. The right two plots represent occupancy predictions generated from autoOcc as a function of years since a fair occurred as well as the relationship between years since fire and burn severity.

# Caveats

One of the main strengths of autologistic occupancy models is that temporal dependence in site-level occupancy is accounted for with a single parameter. This makes the model simple and easier to apply to datasets that are smaller. However, this simple formulation may also be a weakness as it inherently assumes that *θ* does not vary across seasons or sites. Certainly, spatiotemporal covariates can be included within the model, but that does not explicitly quantify whether site-level persistence (i.e., the probability a site remains occupied if a species is present there in the previous timestep) varies across space or time. Autologistic occupancy models could be extended to address this specific issue, but at that point such a model is nearly equivalent to a dynamic occupancy model. Therefore, as with any analysis, it is important to consider what your research questions or management goals are to ensure that the model used is appropriate.

# Additional resources

In addition to this manuscript, autoOcc has an associated vignette that can be accessed so long as it is built when installing autoOcc. This can be viewed by running vignette("Overview") in R after loading the package. This vignette provides a description of autologistic occupancy models, how to add spatial, temporal, or spatiotemporal covariates to your autologistic occupancy models, and shows how all the functions within autoOcc can be used to run a complete analysis on the opossum dataset.

# Conclusion

Biodiversity monitoring surveys that collect data through time are increasingly common, yet the statistical tools to quantify habitat associations with such data have been somewhat limited when said data are subject to imperfect detection. The autoOcc package offers up perhaps the simplest approach that accounts for temporal dependence, and through simulations I demonstrated how autologistic occupancy models can have relatively little bias even with small sample sizes. Through worked examples I provided a general outline for how an analysis can be conducted within the autoOcc ecosystem and then recreated the results of an already published study assessing black-backed woodpecker responses to fire severity (Stillman et al. 2023). Ultimately, I hope that all the information and results presented here, in combination with the autoOcc R package, will be help to researchers who are interested in understanding species occupancy patterns over time.

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