

City, University of London MSc in Artificial Intelligence Project Report Year 2023/2024

Knowledge Grounding in Language Models: An Empirical Study

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Declaration

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In submitting this work I acknowledge that I have read and understood the regulations and code regarding academic misconduct, including that relating to plagiarism, as specified in the Programme Handbook. I also acknowledge that this work will be subject to a variety of checks for academic misconduct.

Signed: Martin Fixman

Acknowledgements

${f Abstract}$

This is an abstract

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1 Introduction and Objectives

1.1 Problem Background

In recent years, Large Language Models (LLMs) have become ubiquitous in solving general problems across a wide range of tasks, from text generation to question answering and logic problems. However, recent research suggests that using these models alone might not be the most effective way to solve problems that are not directly related to text generation (Yao et al. 2023).

One approach to improving the performance on knowledge problems for LLMs is Retrieval-Augmented Generation (RAG) (Lewis et al. 2020). RAG involves retrieving relevant context related to a query and incorporating it into the model's input, enhancing the model's ability to generate accurate and contextually appropriate responses.

As RAG-enhanced systems become more widespread, studies on the performance of different retrieval systems and their interaction with LLMs have become crucial. Many explore the performance of these downstream tasks depending on both the retriever and the generator (Ghader et al. 2023, Brown et al. 2020), examining whether the knowledge is *grounded* in the context. Retrieval-Augmented models, such as ATLAS (Izacard et al. 2022) and RETRO (Borgeaud et al. 2022), use this approach to fine-tune a model on both a large body of knowledge and an existing index for context retrieval.

This project aims to understand the performance of various LLMs by measuring their knowledge grounding on a dataset consisting of a large variety of questions across a wide range of topics. We follow the approach by Yu et al. of running queries with counterparametric context to understand whether a particular answer originates from the model's inherent knowledge (i.e., its training data) or from the provided context (i.e., the context retrieved by RAG).

This thesis builds on this knowledge and improve our understanding of how different LLMs interact with the given context in the problem of question answering. Specifically, we investigate whether these interactions vary depending on the type of question being answered, contributing to a more nuanced understanding of LLM performance in diverse knowledge domains.

1.2 Thesis Questions & Objectives

This thesis is structured around three different objectives to deepen our understanding knowledge grounding in large language models.

1.2.1 Creating a representative dataset of questions

The research of this thesis requires a large dataset of questions from a variety of categories to test large language models. In order to understand knowledge grounding in these models, we require a dataset with the following properties.

- 1. The dataset must contain questions that have short, unambiguous answers.
- 2. The questions must cover a large set of topics.
- 3. It must allow for the creation of counterparametric answers in the same format as correct ones to test contextual versus inherent knowledge.

The existing literature uses various existing question-and-answer datasets, none of which are useful for this research.*

Natural Questions Dataset Created by Google Research (Kwiatkowski et al. 2019), and commonly used in research related to understanding the answers of LLMs in question-and-answer problems (Hsia et al. 2024, Mallen et al. 2023, Ghader et al. 2023). While the dataset provides an excellent range of questions and existing literature to compare these results to, the lack of categorisation is an obstacle in our objective to generate counterparametric answers.

Human-Augmented Dataset Sometimes used in research related to quality control of large language models (Kaushik et al. 2020). However, the high cost associated with this dataset would limit the size of our questions.

Countries' Capitals Question Dataset Used in "Characterizing Mechanisms for Factual Recall in Language Models" (Yu et al. 2023), this dataset contains a single question about the capital city of certain countries which can be easily transformed to a counterparametric question. This format is ideal for the research done in this thesis, but having a single question pattern will not allow a deep dive into the source of each answer in a general question.

Instead of using an existing dataset, this research takes inspiration from the paper by Yu et al. to create a similar but larger dataset of questions and answers from a wide range of topics, where questions can be grouped by question pattern to ensure that their formats are similar. This way, we can emulate the approach of that paper of using the answer from a certain question as the counterfactual question of another.

This dataset will be used to test the remaining questions of this thesis. Since it might be useful for future research, it will also be presented as its own result.

^{*}TODO: Maybe this entire subsubsection should go on Section 2 or Section 3.

1.2.2 When does a model choose the provided context knowledge over its inherent knowledge?

Currently, little is understood about the factors and mechanisms that control whether an LLM will generate text respecting either the context or the memorised information.

Previous research found out that, when the context of a query contradicts the ground knowledge of a model, the answer picked depends on the type and size of the model used (Yu et al. 2023).

This thesis extends this research by testing the representative set of questions and counterfactuals described in the previous section with both Seq2Seq and Decoder-only models of various sizes. We also research the cases when the answer doesn't correspond to either the parametric or contextual knowledge, and why the model chooses a third type of answer when adding counterfactual context.

This thesis also gathers insights from answering this question on different categories and patterns of questions to find out if this depends on what is being asked.

1.2.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

Yu et al. showed that there is a correlation between the probability of a large language model choosing a parametric answer over a counterfactual contextual answer and the amount of times this answer appears in the ground truth data of the model. This gives us clues on whether the result of a query came from parametric or contextual knowledge if we have access to this ground truth, as is the case in models like Pythia (Biderman et al. 2023).

Unfortunately, most so-called open-source large language models do not give us access to the source data being used to train it and therefore do not allow this kind of analysis.

The **perplexity** score of answer gives a measure of how "certain" a large language model is of its answer (Jiang et al. 2021). We hypothesise that we can use this metric to serve as a reliable indicator of whether a particular answer was memorised by the LLM or was derived from the provided context.

2 Context

This research is the latest on a long line of academic articles on the topics of retrievalaugmented generation, counterparametric and contextual data, and how to enhance knowledge on large language models.

This section presents a short summary of some of the articles that were useful in researching this topic.

- 2.1 Foundational Papers on Large Language Models
- 2.2 Papers working with RAG and contextual data
- 2.3 On disentangling parametric and context-augmented counterparametric knowledge

^{*}This entire section is in progress.

3 Methods

3.1 Creating a representative dataset of questions

As argued in Section 1.2.1, our codebase requires the creation of a new dataset of questions with three main properties.

- 1. The questions should have short an unambiguous answers.
- 2. They must cover a large set of topics, eras, and places.
- 3. They must allow for the creation of sensible counterparametric answers (different than what the model would normally answer) by having sets of questions with the same answer format.

To address these items, we follow the approach done by Yu et al. in creating base questions that refer to a specific object, so all the answers for the same base question have a similar format and creating counterparametric answers is easy.

Since this thesis requires a set of questions that covers a large set of topics, eras, and places, we enhance this method by creating a set of categories, each of which has a large set of base questions and another set of objects that can be matched. An example of this approach is shown in Table 1.

Category	Base Questions	Object	Queries
Person	Q: What is the date of birth of {person}? A: The date of birth of {person} is Q: In what city was {person} born? A: {person} was born in	Che Guevara Confucius	Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is Q: What is the date of birth of Confucius? A: The date of birth of Confucius is Q: In what city was Che Guevara born? A: Che Guevara was born in Q: In what city was Confucius born? A: Confucius was born in
City	Q: What country is $\{city\}$ in? A: $\{city\}$ is in	Cairo Mumbai Buenos Aires London	Q: What country is Cairo in? A: Cairo is in Q: What country is Mumbai in? A: Mumbai is in Q: What country is Buenos Aires in? A: Buenos Aires is in Q: What country is London in? A: London is in

Table 1: Some examples of the base-question and object generation that are fed to the models for finding parametric answers.

This list of questions will enable the research on whether the answers given by large language models depend on the category and the format of the questions.

3.2 When does a model choose the provided context knowledge over its inherent knowledge?

3.2.1 Model Selection

In order to get a general understanding of large language models with added context, we test the queries generated in Section 4.1 into four models of different types and sizes.

	Seq2Seq Model	Decoder-Only Model
Small	Flan-T5-XL	Meta-Llama-3.1-8B-Instruct
Large	Flan-T5-XXL	Meta-Llama-3.1-70B-Instruct

Table 2: The four large language models chosen for this research.

The Flan-T5 models (Chung et al. 2022) are an extension to the original Seq2Seq T5 models (Raffel et al. 2020) which are fine-tuned to particular NLP tasks framed as text-to-text problems. Compared to T5, it's generally better at following instructions and has improved zero-shot performance.

The Llama models (Dubey et al. 2024) are Decoder-only models with a dense transformer architecture that are fine-tuned for instruction-following tasks, and are specially adept at complex prompts.

3.2.2 What type of answer does each model select for each question?

The first step to understanding the knowledge grounding of large language models is to create queries that contain counterparametric data as part of the context. By comparing the result to the existing answers it becomes trivial to understand whether an answer came from the model's memory, the queries' context, or neither of these.

Following the approach of Yu et al., for every query we randomly sample from the set of answers of the same base question for answers that are different to the parametric answer (given by the original query). Later, we add this *counterparametric answer* to the context, to form a new query and query the same model again.

To ensure that the results are simple to interpret and minimise the effect of randomness, once we select the queries we follow the example of Hsia et al. and use Greedy Decoding to find the answer.

We compare the parametric answer to the previous values to come to one of three cases: either this answer is identical to the **Parametric** answer and the model inferred it from its memor, to the **Contextual** answer and the model inferred it from the context, or the answer is different to these two and the model inferred it from some **Other** place.

This approach is detailed in Figure 1; Table 3 contains an example of the shuffling done for this experiment while Table 4 contains an example of each of the three categories.

Base Question	Object	Parametric Answer	Counterparametric Answer	Question with Counterparametric Context
	Che Guevara	June 14, 1928	965 AD	Context: [the date of birth of Che Guevara is 965 AD]. Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is
Q: What is the date of birth of {person}? A: The date of birth of {person} is	Ibn al-Haytham	965 AD	June 14, 1928	Context: [the date of birth of Ibn al-Haytham is June 14, 1928]. Q: What is the date of birth of Ibn al-Haytham? A: The date of birth of Ibn al-Haytham is
	W.E.B Du Bois F	ebruary 23, 1868	3 June 14, 1928	Context: [the date of birth of W.E.B Du Bois is June 14, 1928]. Q: What is the date of birth of W.E.B Du Bois? A: The date of birth of W.E.B Du Bois is
Q: What country	Cairo	Egypt	India	Context: [Cairo is in India] Q: What country is Cairo in? A: Cairo is in
is $\{city\}$ in? A: $\{city\}$ is in	Mumbai	India	Egypt	Context: [Mumbai is in Egypt]. Q: What country is Mumbai in? A: Mumbai is in

Table 3: Using the same question format allows us to repurpose previous parametric answers as counterparametric ones.

Question with counterparametric context	Model Answer	Category
Context: [the nearest major body of water to Windhoek is the Rio de la Plata] Q: What is the nearest major body of water to Windhoek? A: The nearest major body of water to Windhoek is	the Atlantic Ocean	Parametric
Context: [the date of birth of Che Guevara is 965 AD]. Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is	965 AD	Contextual
Context: [Rome is in Georgia] Q: What country is Rome in? A: Rome is in	the United States	Other

Table 4: Example for results with **Parametric**, **Contextual**, and **Other** values. Note that, in the third query, the model is interpreting the question as asking about Rome in the US State of Georgia, rather than the country of Georgia.

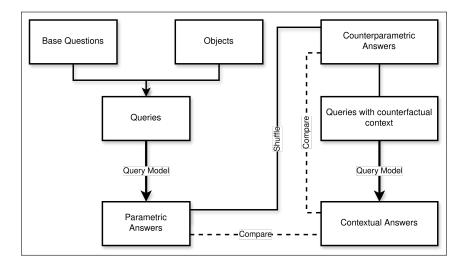


Figure 1: Example diagram of steps used to calculate the two sets of answers, *parametric* and *contextual*, and to compare them to answer the question in this objective. Many of the terms in this diagram are explained in the Glossary.

3.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

3.3.1 Perplexity Score

The Perplexity score of an answer is normally used to measure the inverse of the certainty that the model has of a particular answer (Brown et al. 2020, Borgeaud et al. 2022). In a sense, it's the "surprise" of a model that a certain answer is correct.

We can define the probability of a model choosing a token x_n with context x_1, \ldots, x_{n-1} from a query Q by calculating the softmax value of all the logits for the possible words for this token.

The probabilities of the tokens if an answer can be accumulated to calculate the negative log-likelihood NLL, which is used to calculate the perplexity PPL using the formulas from Equations (1) and (2).

$$NLL(x_1,...,x_n \mid Q) = -\frac{1}{n} \sum_{i=1}^{n} \log_2 P(x_i \mid Q, x_1,...,x_{i-1})$$
 (1)

$$PPL(x_1, \dots, x_n \mid Q) = 2^{NLL(x_1, \dots, x_n \mid Q)}$$
(2)

3.3.2 Perplexity of the parametric answer with counterparametric context and vice-versa

Note that the token x_n does not necessarily have to be the result of applying the query x_1, \ldots, x_{n-1} to a model.

Therefore, it becomes necessary to use teacher-forcing (Lamb et al. 2016) to feed some answer to the model regardless of what's the answer to this particular query. This allows us to calculate the perplexity scores of the parametric answers for both the regular query and the one with counterparametric context, and the perplexity scores of the contextual answers for these two queries.

For a given parametric answer p_1, \ldots, p_n and randomly sampled counterparametric answer q_1, \ldots, q_m , a query without context Q, and a query with this counterparametric context Q' we can calculate four different perplexity scores as shown in Table 5.

		Tokens					
		Parametric p	Counterparametric q				
ext	Base Query	$P_0 = \mathrm{PPL}\left(p_1, \dots, p_n \mid Q\right)$	$P_1 = \operatorname{PPL}(q_1, \dots, q_m \mid Q)$				
Context	Counterparametric Context	$P_2 = \operatorname{PPL}\left(p_1, \dots, p_n \mid Q'\right)$	$P_3 = \operatorname{PPL}(q_1, \dots, q_m \mid Q')$				

Table 5: Four different perplexity values: one for each set of tokens, and one for each query context.

Since the parametric answer is by definition the response of the model to the regular query, $P_0 \leq P_1$. In fact, the perplexity of the parametric value is lower than the perplexity of any other answer on query Q.

Figure 2 contains an example of the calculation of the perplexity values for a particular query.

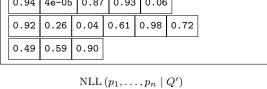
3.3.3 Predicting whether an answer came from memory or from context

One question remains: if the response of the query with counterparametric context Q' is a certain answer x_1, \ldots, x_n , how can we predict whether this answer is came from the model's memory p or from the given context q without requiring an extra query?

We propose investigating the value of the perplexity PPL $(x_1, ..., x_n \mid Q')$ and comparing it to the distribution of perplexities on the answers with added parametric context P_2 and P_3 . For simplicity reasons, we are obviating the case when the preferred answer is neither of these; instead, we focus on whether the parametric or counterparametric answer are more likely.[†]

[†]TODO: Maybe include a KDE or a K-S test here.

Base Query QQ: Where is The Son of Man primarily housed? A: The Son of Man is currently in Parametric Answer Tokens p_1, \ldots, p_n collection National the of t.he Gallery Canada Ottawa of in Ontario Canada $P\left(p_i \mid Q', p_1, \dots, p_{i-1}\right)$ 0.94 4e-05 0.87 0.93 0.06 0.61 0.98 0.72 0.92 0.26 0.04 0.49 0.59 0.90



$$-\frac{1}{n}\sum_{i=1}^{n}\log_2 P\left(p_i \mid Q', p_1, \dots, p_{i-1}\right) = 2.0566$$

$$P_2 = \text{PPL}(p_1, \dots, p_n \mid Q')$$

$$P_2 = 2^{\text{NLL}}(q_1, \dots, q_m \mid Q') = 4.1599$$

Query with Counterparametric Context Q'

[Context: The Son of Man is housed in in the refectory of the Convent of Santa Maria delle Grazie in Milan, Italy]

Q: Where is The Son of Man primarily housed?

A: The Son of Man is currently in

Counterparametric Answer Tokens q_1, \dots, q_m

the	ref	ect	ory	of	t	he	Co	on	vent
of	Santa	ı M	aria	del	le	Gı	raz	i	9
in	Milan	ι,	Ita:	ly					

NLL
$$(q_1, ..., q_m \mid Q')$$

$$-\frac{1}{n} \sum_{i=1}^{m} \log_2 P(q_i \mid Q', q_1, ..., q_{i-1}) = 0.0154$$

$$P_3 = \text{PPL}(q_1, \dots, q_m \mid Q')$$

$$P_3 = 2^{\text{NLL}(q_1, \dots, q_m \mid Q')} = 1.0107$$

 $P_2 > P_3$ Contextual

Figure 2: Example of perplexity calculation for the parametric and counterparametric answers in a query with the counterparametric context. Note that, due to teacher forcing, the calculation finds the probability of the next token p_i given the previous tokens of the searched answer p_1, \ldots, p_{i-1} rather than given the most likely tokens. For example, once we feed the string "National Gallery of Canada in", the probability of the next token being "Ottawa" is very high.

4 Results

4.1 Creating a representative dataset of questions

We manually create a set of 4760 questions using the method explained in Section 4.1.

In order to be able to reuse objects for different questions, we separated the questions and objects in 9 different categories.

- 1. **Person** Historical people living from early antiquity to the present day from all around the globe. The questions have short, unambiguous answers, such as date of birth or most famous invention.
- 2. City Cities from all over the globe. Questions may include population, founding date, notable landmarks, or geographical features.
- 3. **Principle** Scientific principles, discovered from the 16th century forward. Questions about their discovery, use, and others.
- 4. **Element** Elements from the periodic table. Questions may cover discovery, atomic number, chemical properties, or common uses.
- 5. **Book** Literary works from various genres, time periods, and cultures. Questions may involve authors, publication dates, plot summaries, or literary significance.
- 6. **Painting** Famous artworks from different art movements and periods. Questions may cover artists, creation dates, styles, or current locations.
- 7. **Historical Event** Significant occurrences that shaped world history, from ancient times to the modern era. Questions may involve dates, key figures, causes, or consequences.
- 8. **Building** Notable structures from around the world, including ancient monuments, modern skyscrapers, and architectural wonders. Questions may cover location, architect, construction date, or architectural style.
- 9. **Composition** Musical works from various genres and time periods. Questions may involve composers, premiere dates, musical style, or cultural significance.

Each one of these categories has a number of questions that are assigned one of the objects, enhancing the done by Yu et al..

The full list of base questions and objects for all categories can be found in Appendix A. The total amount of these and composition of the 4760 questions can be found in Table 6.

Category	Base Questions	Objects	Total Questions
Person	17	57	969
City	17	70	1190
Principle	5	37	185
Element	15	43	645
Book	11	49	539
Painting	12	44	528
Historical Event	4	64	256
Building	9	22	198
Composition	10	25	250
Total	100	411	4760

Table 6: The amount of base questions, objects, and the total amount of questions in each category on the final dataset.

4.2 When does a model choose the provided context knowledge over its inherent knowledge?

The results of running the queries created in Section 4.1 with added counterparametric context on each of the four models the four models can be found in Table 7 and Figure 3.

Model	Parametric	Contextual	Other
llama-3.1-8B	745	3662	353
llama-3.1-70B	1070	3303	387
flan-t5-xl	248	4284	228
flan-t5-xxl	242	4304	214

Table 7: Results when running all entries on a decoder-only model.

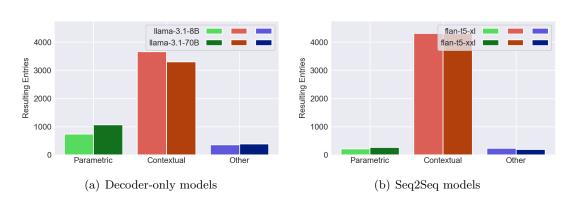


Figure 3: Results by type depending on which model; these are the same results as Table 7.

As hypothesised in Section 1.2.2, there are vast differences on how the models of different types and sizes act when presented with a context that contradicts their knowledge. This is investigated further in Section 5.

A similar pattern emerges in most (but not all) of the categories, which can be seen in Tables 8 and 9 and Figures 4 and 5.

	llama-3.1-8B			llama-3.1-70B		
	Parametric	Contextual	Other	Parametric	Contextual	Other
Person	40	833	96	209	614	146
City	117	1007	66	166	966	58
Principle	44	118	23	44	117	24
Element	218	385	42	275	347	23
Book	135	344	60	154	318	67
Painting	47	458	23	49	445	34
Historical Event	81	154	21	117	118	21
Building	27	163	8	31	159	8
Composition	36	200	14	25	219	6

Table 8: Results for running each one of the 10 categories separately on the Decoder-only models.

	flan-t5-x1			flan-t5-xxl		
	Parametric	Contextual	Other	Parametric	Contextual	Other
Person	32	900	37	23	890	56
City	120	1030	40	78	1093	19
Principle	13	164	8	9	168	8
Element	6	637	2	102	515	28
Book	26	488	25	18	457	64
Painting	26	446	56	4	498	26
Historical Event	11	217	28	1	254	1
Building	14	174	10	0	189	9
Composition	0	228	22	7	240	3

Table 9: Results for running each one of the 10 categories separately on the Seq2Seq models.

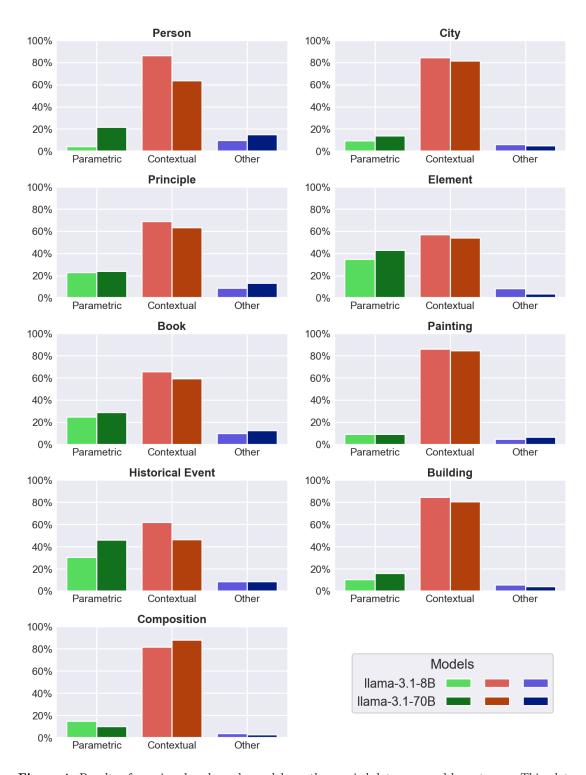


Figure 4: Results of running decoder-only models on the queried data, grouped by category. This plots the information shown in Table 8.

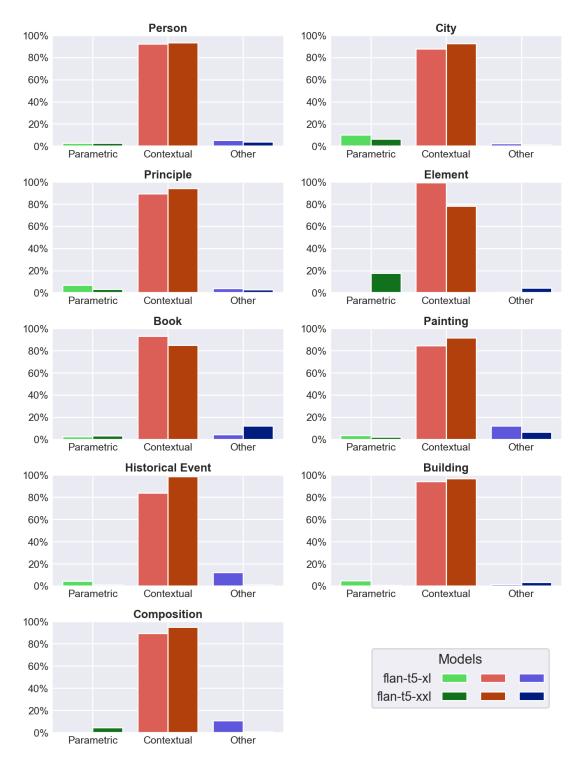


Figure 5: Results of running Seq2Seq models on the queried data, grouped by category. This plots the information shown in Table 9.

4.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

We calculate the resulting perplexity of each query as explained in Section 3.3. These are accumulated in three distributions, depending on answer type, which are summarised in Tables 10 and 11 and Figure 6.

	llama-3.1-8B		llama-3.1-70B	
	Parametric	Contextual	Parametric	Contextual
count	313	4447	383	4377
mean	1.67	1.20	1.56	1.22
$\operatorname{\mathbf{std}}$	0.79	0.32	0.46	0.31
25 %	1.28	1.05	1.28	1.06
50 %	1.43	1.10	1.43	1.12
75%	1.78	1.23	1.68	1.25

Table 10: Distribution of perplexity values for Decoder-only models

	flan-T5-XL		flan-T5-XXL	
	Parametric	Contextual	Parametric	Contextual
count	651	4109	507	4253
mean	6.38	1.56	11.75	1.27
$\operatorname{\mathbf{std}}$	9.07	0.56	18.47	0.75
25%	3.21	1.19	2.41	1.02
50 %	4.71	1.39	3.89	1.09
75%	7.14	1.71	7.70	1.24

Table 11: Distribution of perplexity values for Seq2Seq models

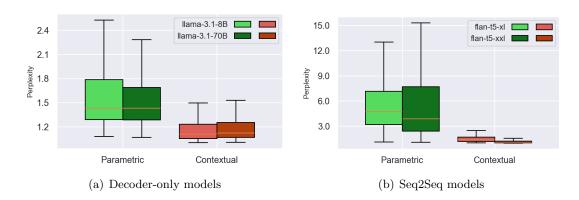


Figure 6: Perplexity distribution according to model type and size. These represent the same distributions as Tables 10 and 11.

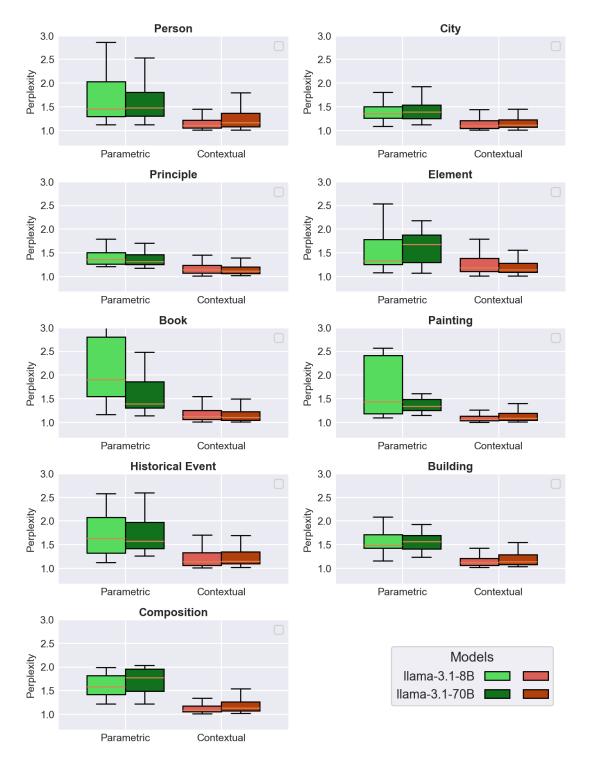


Figure 7: Box plots representing the distribution of the perplexities when running both Llama models, grouped by category.

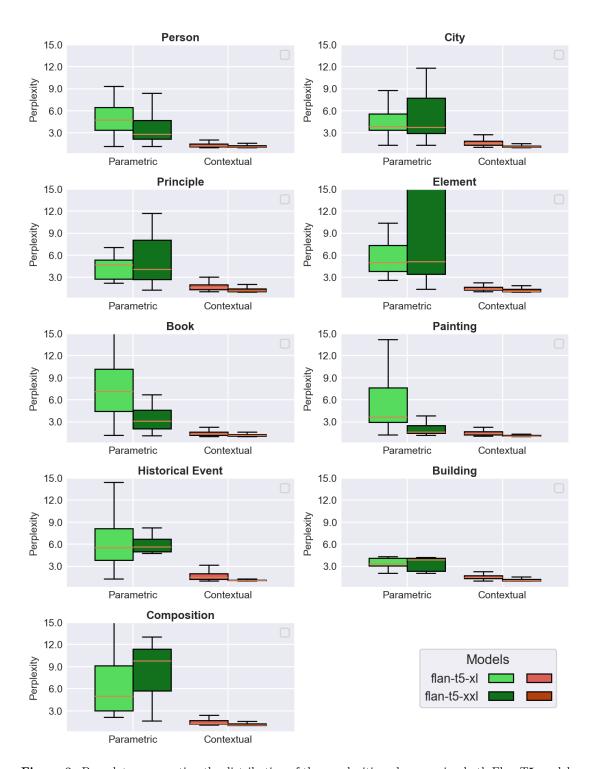


Figure 8: Box plots representing the distribution of the perplexities when running both Flan-T5 models, grouped by category.

5 Discussion

- 5.1 Model type and memorised knowledge
- 5.2 Model size and memorised knowledge
- 5.3 Differences in perplexity scores for larger and smaller models
- 5.3.1 Can we use this to predict from where an answer came from?
- 5.4 Differences in distributions for different categories and questions.

6 Evaluations, Reflections, and Conclusions

Glossary

Base Questions

Objects

Queries

Parametric Answers

Counterparamteric answers

 ${\bf Queries\ with\ counterfactual/counterparametric\ context}$

Contextual Answer

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Appendices

A Questions and objects used to form the queries

```
What is the date of birth of {person}? The date of birth of {person} is In what city was {person} born? {person} was born in What is the date of death of {person}? The date of death of {person} is
What is the date of death of {person}? The date of death of {person} is
What is the primary profession of {person}? The primary profession of {person} is
What is {person} primarily known for? {person} is primarily known for
What's the main nationality of {person}? {person} is
What educational institution did {person} attend? {person} attended
What was the native language of {person}? The native language of {person} was
Who was {person}'s most influential mentor? The most influential mentor of {person} was
What was {person}'s religious affiliation? The religious affiliation of {person} was
What was {person}'s primary field of study? The primary field of study of {person} was
What was {person}'s most famous work or invention? The most famous work or invention of {person} was
What historical period did {person} live in? {person} lived during the
What was {person}'s family's social class? {person}'s family belonged to the
What was {person}'s political ideology? The political ideology of {person} was
What was {person}'s preferred artistic or scientific medium? The preferred medium of {person} was
What was {person}'s cultural background? The cultural background of {person} was
  What country is {city} in? {city} is in What's the highest administrative subdivision {city} is part of? {city} is part of
What's the highest administrative subdivision {city} is part of? {city} is part of
In what year was {city} founded? {city} was founded in
What major river is nearest to {city}? The nearest major river to {city} is
What is the time zone of {city}? The time zone of {city} is
What is the current population of {city}? The current population of {city} is
What is the altitude of {city} above sea level? {city} is at an altitude of
What is the primary language spoken in {city}? The primary language spoken in {city} is
What is the predominant architectural style in {city}? The predominant architectural style in {city} is
What is the main economic industry of {city}? The main economic industry of {city} is
What is the average annual temperature in {city}? The average annual temperature in {city} is
What is the nearest major body of water to {city}? The nearest major body of water to {city} is
What is the most famous landmark in {city}? The most famous landmark in {city} is
What is the primary mode of public transportation in {city}? The primary mode of public transportation in {city} is
                           {city} is
  What is the name of the airport serving {city}? The airport serving {city} is
What is the sister city of {city}? The sister city of {city} is
What is the traditional cuisine {city} is known for? The traditional cuisine {city} is known for is
   Who is credited with the discovery of {principle}? {principle} was discovered by
  Which scientific discipline encompasses {principle}? {principle} is encompassed by What is the primary application of {principle}? The primary application of {principle} is In which year was {principle} first formulated? {principle} was first formulated in What is the SI unit most commonly associated with {principle}? The SI unit most commonly associated with
   What's the chemical formula for {element}? The chemical formula for {element} is
 What's the chemical formula for {element}? The chemical formula for {element} is

When was {element} first isolated? {element} was first isolated in

What's the atomic number of {element}? The atomic number of {element} is

What is the melting point of {element}? The melting point of {element} is

In which group of the periodic table is {element} found? {element} is found in group

What's the standard atomic weight of {element}? The standard atomic weight of {element} is

What's the electron configuration of {element}? The electron configuration of {element} is

What's the most common oxidation state of {element}? The most common oxidation state of {element} is

What's the crystal structure of {element} at room temperature? The crystal structure of {element} at room
 What's the crystal structure of {element} at room temperature? The crystal structure of {element} temperature is
What's the primary isotope of {element}? The primary isotope of {element} is
What's the electronegativity value of {element}? The electronegativity value of {element} is
What's the ionization energy of {element}? The ionization energy of {element} is
What's the atomic radius of {element}? The atomic radius of {element} is
What's the boiling point of {element}? The boiling point of {element} is
In which period of the periodic table is {element} located? {element} is located in period
  What genre does {book} belong to? The genre of {book} is
Who's the author of {book}? {book} was written by
In what year was {book} first published? {book} was first published in
How many pages are in the original publication of {book}? The original publication of {book} has
What is the name of the main protagonist in {book}? The main protagonist in {book} is
  What is the original language of {book}? The original language of {book} is Who is the original publisher of {book}? The publisher of {book} is What is the highest award {book} won? The highest award won by {book} is What is the opening line of {book}? The opening line of {book} is How many chapters are in {book}? {book} has How many pages are in {book}? {book} has
Who painted {painting}? {painting} was painted by
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Listing 1: All base questions used in this work. Each one of these will get combined with data from Listing 2 as detailed in ??.

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Ada Lovelace, person
Alan Turing, person
Albert Einstein, person
Alexander Fleming, person
Aristotle, pe
Billie Jean King, person
Boyan Slat, person
Catherine the Great, person
Che Guevara, p
Cleopatra, person
Confucius, person
Ernest Rutherford, person
Florence Nightingale, person
Freddie Mercury, person
Frida Kahlo, person
Greta Thunberg, person
Harriet Tubman, person
Ibn al-Haytham, person
Isaac Newton, person
Isaac Newton, person
Karl Marx, person
Leonardo da Vinci, person
Mahatma Gandhi, person
Malala Yousafzai, person
Mansa Musa, person
Marie Curie, person
Martin Luther King Jr., person
Michelangelo, person
Mohandas Gandhi, person
Mozart, person
Muhammad Ali, person
Neil Armstrong, person
Nelson Mandela, person
Nikola Tesla, person
Pablo Picasso, person
Rosalind Franklin, person
Shirin Ebadi, person
Simon Bolivar, person
Srinivasa Ramanujan, person
Stephen Hawking, person
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Sun Yat-sen, person
Virginia Woolf, person
Vladimir Lenin, person
Wangari Maathai, person
W.E.B. Du Bois, person
William Shakespeare, person
William Shakespeare, per Wu Zetian, person Yuri Gagarin, person Amelia Earhart, person Galileo Galilei, person Joan of Arc, person Lise Meitner, person Marcus Aurelius, person Maya Angelou, person Queen Nzinga, person Socrates, person Voltaire, person Alexandria, city Amsterdam, city
Amsterdam, city
Amsterdam, city
Antananarivo, city
Athens, city
Baghdad, city
 Berlin, city
Buenos Aires, city
Buenos Aires, c:
Bukhara, city
Cairo, city
Cape Town, city
Cartagena, city
Chicago, city
Cusco, city
Cuzco, city
Delhi, city
Dubrownik, city
 Dubrovnik, city
 Fez, city
Havana, city
 Istanbul, city
Jerusalem, city
 Kyoto, city
La Paz, city
La Paz,city
Lhasa,city
Lisbon,city
London,city
Luang Prabang,city
Mexico City,city
Montevideo,city
Moscow,city
Mumbai,city
Numbai,city
New York,city
 New York, city
Nur-Sultan, city
Paris, city
Petra, city
Petra, city
Prague, city
Quebec City, city
 Reykjavik, city
Rome, city
Sao Paulo, city
Sao Paulo, city
Sarajevo, city
Shanghai, city
Singapore, city
St. Petersburg, city
St. Petersburg, cit

Sydney, city

Tbilisi, city

Tenochtitlan, city

Timbuktu, city

Tokyo, city

Ulaanbaatar, city

Varanasi, city

Venice, city

Venice, city

Wellington, city
 Wellington, city
Windhoek, city
Windhoek, city
Xi'an, city
Yogyakarta, city
Zanzibar City, city
Addis Ababa, city
Bangkok, city
Dubai, city
Helsinki, city
Machu Picchu, city
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Nairobi, city
Rio de Janeiro, city
Samarkand, city
 Yangon, city
Yarchimedes' Principle, principle
Bernoulli's Principle, principle
 Boyle's Law, principle
Cell Theory, principle
Conservation of Energy, principle
 DNA Replication, principle
 Electromagnetism, principle
Entropy, principle
Entropy, principle
Entropy, principle
Evolution by Natural Selection, principle
Evolution, principle
General Relativity, principle
Germ Theory of Disease, principle
Gravity, principle
Hardy-Weinberg Principle, principle
Heliocentrism, principle
Hubble's Law, principle
Hubble's Law, of Planetary Motion, principle
Le Chatelier's Principle, principle
Mendel's Laws of Inheritance, principle
Newton's Laws of Motion, principle
Pauli Exclusion Principle, principle
Principle Description of Principle
Principle of Least Action, principle
Quantum Mechanics, principle
 Quantum Mechanics, principle
Quantum nechanics, principle
Superconductivity, principle
Thermodynamics, principle
Uncertainty Principle, principle
Avogadro's Law, principle
 Coulomb's Law, principle
Faraday's Laws of Electrolysis, principle
 Heisenberg Uncertainty Principle, principle Ohm's Law, principle
 Schrä¶dinger Equation, principle
Special Relativity, principle
 Aluminum, element
Barium, element
Bismuth, element
Bromine, element
 Calcium, element
Carbon, element
Chlorine, element
Chromium, element
 Copper, element Gold, element
 Helium, element
 Hydrogen, element
 Iodine, element
Iron, element
 Lead, element
 Magnesium, element
Manganese, element
Mercury, element
Neon, element
Nitrogen, element
 Oxygen, element
Phosphorus, element
Plutonium, element
 Potassium, element
Radon, element
Silicon, element
Silver, element
Sodium, element
 Sulfur, element
Thorium, element
 Tin, element
Titanium, element
 Uranium, element
Zinc, element
 Argon, element
Boron, element
 Cobalt, element Fluorine, element
 Gallium, element Krypton, element
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Nickel, element
 Xenon, element
 1984,b
 Anna Karenina, book
 Beloved, book
Brave New World, book
Catch-22, book
 Crime and Punishment, book
Don Quixote, book
Fahrenheit 451, book
 Frankenstein,
 Jane Eyre, book
Midnight's Children, book
 Moby-Dick, book
One Flew Over the Cuckoo's Nest, book
 One Hundred Years of Solitude, book
 Slaughterhouse - Five, boo
 The Alchemist, bo
The Art of War,
The Book Thief,
 The Brothers Karamazov, book
The Catcher in the Rye, book
The Chronicles of Narnia, book
 The Color Purple,b
 The Color Purple, book
The Count of Monte Cristo, book
The Grapes of Wrath, book
The Great Gatsby, book
The Handmaid's Tale, book
The Hitchhiker's Guide to the Galaxy, book
 The Hobbit, book
The Hunger Games,
 The Kite Runner,
 The Little Prince,
 The Lord of the Rings, book
The Metamorphosis, book
 The Name of the Rose, book
The Odyssey, book
The Picture of Dorian Gray, book
The Pillars of the Earth, book
 The Stranger, book
The Sun Also Rises,
 The Wind-Up Bird Chronicle, book
To Kill a Mockingbird, book
 Ulysses, book
War and Peace,
 war and reace, book
Wuthering Heights, book
The Iliad, book
The Tale of Genji, book
Things Fall Apart, book
 To the Lighthouse, book
American Gothic, painting
Christina's World, painting
Girl with a Pearl Earring, painting
 Guernica, painting
Les Demoiselles d'Avignon, painting
Les Demoiselles d'Avignon, painting
Liberty Leading the People, painting
Mona Lisa, painting
School of Athens, painting
Starry Night, painting
The Absinthe Drinker, painting
The Anatomy Lesson of Dr. Nicolaes Tulp, painting
The Arnolfini Portrait, painting
 The Astronomer, painting
The Birth of Venus, painting
The Calling of Saint Matthew, painting
The Calling of Saint Matthew, Painting
The Card Players, painting
The Death of Marat, painting
The Fighting Temeraire, painting
The Garden of Earthly Delights, painting
The Gross Clinic, painting
The Hay Wain, painting
The Kiss, painting
The Last Supper Deainting
 The Kiss, painting
The Last Supper, painting
The Nighthawks, painting
The Night Watch, painting
The Ninth Wave, painting
The Persistence of Memory, painting
The Potato Eaters, painting
 The Raft of the Medusa, painting The Scream, painting
 The Sleeping Gypsy, painting
The Son of Man, painting
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The Swing, painting
The Third of May 1808, painting
The Tower of Babel, painting
The Treachery of Images, painting
The Triumph of Galatea, painting
The Wanderer above the Sea of Fog, painting
Water Lilies, painting
The Creation of Adam, painting
The Girl with a Pearl Earling, painting
The Great Wave off Kanagawa, painting The Thinker, painting
Venus de Milo, painting
Decimalisation in the UK, historical_event
Queen Elizabeth II's Platinum Jubilee, historical_event Queen Victoria's Coronation, historical_event
 The Act of Union between England and Scotland, historical_event
The Battle of Advanple, historical_event
The Battle of Adva, historical_event
The Battle of Agincourt, historical_event
The Battle of Hastings, historical_event
The Battle of Sekigahara, historical_event
The Battle of Teutoburg Forest, historical_event
The Battle of the Milvian Bridge, historical_event
The Battle of Waterloo, historical_event
The Brexit Referendum, historical_event
The Codification of Roman Law by Justinian, historical_event
The Construction of Hadrian's Wall, historical_event
The Construction of the Great Pyramid of Giza, historical_event
The Conversion of Constantine, historical_event
The Council of Chalcedon, historical_event
 The Crisis of the Third Century, historical_event
The Crisis of the Third Century, historical_event
The Defeat of the Spanish Armada, historical_event
The Discovery of the Americas by Columbus, historical_event
The Dissolution of the Soviet Union, historical_event
The Division of the Roman Empire, historical_event
The Dunkirk Evacuation, historical_event
The Edict of Caracalla, historical_event
The Fall of Constantinople, historical_event
The Fall of the Aztec Empire, historical_event
The Fall of the Western Roman Empire, historical_event
The First Circumpayigation of the Earth, historical_event
The First Circumnavigation of the Earth, historical_event The First Council of Nicaea, historical_event
 The First Crusade, historical event
 The Founding of Constantinople, historical_event
The Founding of Rome, historical_event
The Founding of the British Broadcasting Corporation, historical_event
The Founding of the League of Nations, historical_event
The French Revolution, historical_event
The Glorious Revolution, historical_event
The Gothic War in Italy, historical_event
The Great Fire of London, historical_event
The Indian Independence Act, historical_event
The Indian Independence Act, historical_event
The Industrial Revolution, historical_event
The London 7/7 Bombings, historical_event
The Meiji Restoration, historical_event
The Plague of Justinian, historical_event
The Reforms of Diocletian, historical_event
The Reunification of the Empire by Aurelian, historical_event
The Sack of Rome by Alaric, historical_event
The Sack of Rome by the Vandals, historical_event
The Signing of the Good Friday Agreement, historical_event
The Signing of the Magna Carta, historical_event
The Suze Crisis, historical_event
The Treaty of Westphalia, historical_event
The UK Abolition of the Slave Trade Act, historical_event
The Unification of Italy, historical_event
The Wedding of Prince Charles and Lady Diana, historical_event
The Year of the Four Emperors, historical_event
The American Revolution, historical_event
The Black Death, historical_event
The Cuban Missile Crisis, historical_event
The Fall of the Berlin Wall, historical_event
The Moon Landing, historical_event
The Renaissance, historical_event
The Russian Revolution, historical_event
 The Signing of the Declaration of Independence, historical_event
Angkor Wat, building
Buckingham Palace, building
Burj Khalifa, building
 Chichen Itza, building
 Chrysler Building, building
Colosseum, building
Eiffel Tower, building
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Empire State Building, building
Corpidden City, building
Guggenheim Museum, building
Hagia Sophia, building
Hacker Pyramid, building
Machu Picchu, building
Ruschwanstein Castle, building
Parthenon, building
Petronas Towers, building
Petronas Towers, building
Petronas Towers, building
Potala Palace, building
Stass Tower, building
St. Basil's Cathedral, building
Sydney Opera House, building
Sydney Opera House, building
Taj Mahal, building
Adagio for Strings, composition
Billie Jean, composition
Canon in D. composition
Canon in D. composition
Carsina Burana, composition
Clair de Lune, composition
Clair de Lune, composition
Clair de Lune, composition
Inagine, composition
Inagine, composition
Inagine, composition
In the Mood, composition
Like a Rolling Stone, composition
Novesong, composition
Novesong, composition
Mbube (The Lion Sleeps Tonight), composition
Nessum Dorna, composition
Raga Malkauns, composition
Rhapsody in Blue, composition
Rhapsody in Blue, composition
Rhapsody on a Theme of Paganini, composition
The Blue Danube, composition
The Flanets, composition
The Flanets, composition
The Rite of Spring, composition
Toccata and Fugue in D minor, composition
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Listing 2: All objects which will be combined with the questions in Listing 1.

- B Full Results for Each Question
- C Grounder Usage and Documentation
- D Source Code of the Experiments