

City, University of London MSc in Artificial Intelligence Project Report Year 2023/2024

# Knowledge Grounding in Language Models: An Empirical Study

#### **Martin Fixman**

Supervised By: Tillman Weyde Collaborators: Chenxi Whitehouse and Pranava Madhyastha

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#### Declaration

By submitting this work, I declare that this work is entirely my own except those parts duly identified and referenced in my submission. It complies with any specified word limits and the requirements and regulations detailed in the assessment instructions and any other relevant programme and module documentation.

In submitting this work I acknowledge that I have read and understood the regulations and code regarding academic misconduct, including that relating to plagiarism, as specified in the Programme Handbook. I also acknowledge that this work will be subject to a variety of checks for academic misconduct.

Signed: Martin Fixman

#### Acknowledgements

#### ${f Abstract}$

This is an abstract

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#### 1 Introduction and Objectives

#### 1.1 Problem Background

In recent years, Large Language Models (LLMs) have become ubiquitous in solving general problems across a wide range of tasks, from text generation to question answering and logic problems. However, recent research suggests that using these models alone might not be the most effective way to solve problems that are not directly related to text generation (Yao et al. 2023).

One approach to improving the performance on knowledge problems for LLMs is Retrieval-Augmented Generation (RAG) (Lewis et al. 2020). RAG involves retrieving relevant context related to a query and incorporating it into the model's input, enhancing the model's ability to generate accurate and contextually appropriate responses.

As RAG-enhanced systems become more widespread, studies on the performance of different retrieval systems and their interaction with LLMs have become crucial. Many explore the performance of these downstream tasks depending on both the retriever and the generator (Ghader et al. 2023, Brown et al. 2020), examining whether the knowledge is *grounded* in the context. Retrieval-Augmented models, such as ATLAS (Izacard et al. 2022) and RETRO (Borgeaud et al. 2022), use this approach to fine-tune a model on both a large body of knowledge and an existing index for context retrieval.

This project aims to understand the performance of various LLMs by measuring their knowledge grounding on a dataset consisting of a large variety of questions across a wide range of topics. We follow the approach by Yu et al. of running queries with counterfactual context to understand whether a particular answer originates from the model's inherent knowledge (i.e., its training data) or from the provided context (i.e., the context retrieved by RAG).

This thesis builds on this knowledge and improve our understanding of how different LLMs interact with the given context in the problem of question answering. Specifically, we investigate whether these interactions vary depending on the type of question being answered, contributing to a more nuanced understanding of LLM performance in diverse knowledge domains.

#### 1.2 Thesis Questions & Objectives

This thesis is structured around three different objectives to deepen our understanding knowledge grounding in large language models.

#### 1.2.1 Creating a representative dataset of questions

The research of this thesis requires a large dataset of questions from a variety of categories to test large language models. In order to understand knowledge grounding in these models, we require a dataset with the following properties.

- 1. The dataset must contain questions that have short, unambiguous answers.
- 2. The questions must cover a large set of topics.
- 3. It must allow for the creation of counterfactual answers in the same format as correct ones to test contextual versus inherent knowledge.

The existing literature uses various existing question-and-answer datasets, none of which are useful for this research.\*

Natural Questions Dataset Created by Google Research (Kwiatkowski et al. 2019), and commonly used in research related to understanding the answers of LLMs in question-and-answer problems (Hsia et al. 2024, Mallen et al. 2023, Ghader et al. 2023). While the dataset provides an excellent range of questions and existing literature to compare these results to, the lack of categorisation is an obstacle in our objective to generate counterfactual answers.

**Human-Augmented Dataset** Sometimes used in research related to quality control of large language models (Kaushik et al. 2020). However, the high cost associated with this dataset would limit the size of our questions.

Countries' Capitals Question Dataset Used in "Characterizing Mechanisms for Factual Recall in Language Models" (Yu et al. 2023), this dataset contains a single question about the capital city of certain countries which can be easily transformed to a counterfactual question. This format is ideal for the research done in this thesis, but having a single question pattern will not allow a deep dive into the source of each answer in a general question.

Instead of using an existing dataset, this research takes inspiration from the paper by Yu et al. to create a similar but larger dataset of questions and answers from a wide range of topics, where questions can be grouped by question pattern to ensure that their formats are similar. This way, we can emulate the approach of that paper of using the answer from a certain question as the counterfactual of another.

This dataset will be used to test the remaining questions of this thesis. Since it might be useful for future research, it will also be presented as its own result.

<sup>\*</sup>TODO: Maybe this entire subsubsection should go on Section 2 or Section 3.

## 1.2.2 When does a model choose the provided context knowledge over its inherent knowledge?

Currently, little is understood about the factors and mechanisms that control whether an LLM will generate text respecting either the context or the memorised information.

Previous research found out that, when the context of a query contradicts the ground knowledge of a model, the answer picked depends on the type and size of the model used (Yu et al. 2023).

This thesis extends this research by testing the representative set of questions and counterfactuals described in the previous section with both Seq2Seq and Decoder-only models of various sizes. We also research the cases when the answer doesn't correspond to either the parametric or contextual knowledge, and why the model chooses a third type of answer when adding counterfactual context.

This thesis also gathers insights from answering this question on different categories and patterns of questions to find out if this depends on what is being asked.

# 1.2.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

Yu et al. showed that there is a correlation between the probability of a large language model choosing a parametric answer over a counterfactual contextual answer and the amount of times this answer appears in the ground truth data of the model. This gives us clues on whether the result of a query came from parametric or contextual knowledge if we have access to this ground truth, as is the case in models like Pythia (Biderman et al. 2023).

Unfortunately, most so-called open-source large language models do not give us access to the source data being used to train it and therefore do not allow this kind of analysis.

The **perplexity** score of answer gives a measure of how "certain" a large language model is of its answer (Jiang et al. 2021). We hypothesise that we can use this metric to serve as a reliable indicator of whether a particular answer was memorised by the LLM or was derived from the provided context.

#### 2 Context

This research is the latest on a long line of academic articles on the topics of retrievalaugmented generation, counterparametric and contextual data, and how to enhance knowledge on large language models.

This section presents a short summary of some of the articles that were useful in researching this topic.

#### 2.1 Foundational Papers on Large Language Models

- "Language models are unsupervised multitask learners" (Radford et al. 2019).
  - The foundational paper for GPT2.
- "Exploring the Limits of Transfer Learning with a Unified Text-to-Text Transformer" (Raffel et al. 2020).
  - The foundational paper for T5.
- "Language Models are Few-shot Learners" (Brown et al. 2020).
  - Introduces "in-context learning".
- "Prompt programming for large language models: Beyond the few-shot paradigm" (Reynolds & McDonell 2021).
  - Improves the previous paper.

#### 2.2 Papers working with RAG and contextual data

- "Retrieval-Augmented Generation for Knowledge-Intensive NLP Tasks" (Lewis et al. 2020).
  - Foundational paper for RAG.
- "Self-RAG: Learning to Retrieve, Generate, and Critique through Self-Reflection" (Asai et al. 2023).
  - Interesting RAG system.
- "Can Retriever-Augmented Language Models Reason? The Blame Game Between the Retriever and the Language Model" (Ghader et al. 2023).
  - Nice evaluation of RAG models.

#### 2.3 Retrieval-Augmented Language Models

• "Shall We Pretrain Autoregressive Language Models with Retrieval? A Comprehensive Study" (Wang et al. 2023).

<sup>\*</sup>This entire section is in progress — short summaries of the named papers will come soon.

- Reproduces and pretraines RETRO.
- "Atlas: Few-shot Learning with Retrieval Augmented Language Models" (Izacard et al. 2022).
  - Introduces ATLAS.
- "Improving language models by retrieving from trillions of tokens" (Borgeaud et al. 2022).
- "RAGGED: Towards Informed Design of Retrieval Augmented Generation Systems" (Hsia et al. 2024).
  - Analyses results of these systems; compares Llama to Flan-T5.

# 2.4 On disentangling parametric and context-augmented counterparametric knowledge

- "DISCO: Distilling Counterfactuals with Large Language Models" (Chen et al. 2023).
  - Does similar analysis with counterfactuals to this thesis
- "DisentQA: Disentangling Parametric and Contextual Knowledge with Counterfactual Question Answering" (Neeman et al. 2022).
  - Also does a similar analysis to this thesis.
- "Characterizing Mechanisms for Factual Recall in Language Models" (Yu et al. 2023).
  - Very simple analysis, but tries to understand WHERE in the model the contextual answers come from.
- "Can We Edit Factual Knowledge by In-Context Learning?" (Zheng et al. 2023).
- "Learning the Difference that Makes a Difference with Counterfactually-Augmented Data" (Kaushik et al. 2020).

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#### 3 Methods

#### 3.1 Creating a representative dataset of questions

As shown in Section 1.2.1, our codebase requires the creation of a new dataset of questions with three main properties.

- 1. Questions should have short an unambiguous answers.
- 2. They must cover a large set of topics, eras, and places.
- 3. They must allow for the creation of sensible counterfactuals by having sets of questions with the same answer format.

To address Items 1 and 3, we follow the approach done by Yu et al. in creating questions which have a question with a particular "object" as its nucleus. This way, it's possible to create counterfactuals that have the same format of the original answer by randomly sampling from the set of answers, as shown in Table 1.

Base Question	Object	Parametric Answer	Counterparametric Answer	Question with counter- parametric context
	Che Guevara	June 14, 1928	965 AD	Context: [the date of birth of Che Guevara is 965 AD]. Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is
Q: What is the date of birth of {person}? A: The date of	Ibn al-Haytham	965 AD	June 14, 1928	Context: [the date of birth of Ibn al-Haytham is June 14, 1928]. Q: What is the date of birth of Ibn al-Haytham? A: The date of birth of Ibn al-Haytham is
a: The date of birth of {person} is	Boyan Slat	27 January 1994	February 23, 1868	Context: [the date of birth of Boyan Slat is February 23, 1868]. Q: What is the date of birth of Boyan Slat? A: The date of birth of Boyan Slat is
	W.E.B Du Bois	February 23, 1868	June 14, 1928	Context: [the date of birth of W.E.B Du Bois is June 14, 1928]. Q: What is the date of birth of W.E.B Du Bois? A: The date of birth of W.E.B Du Bois is

**Table 1:** Using the same question format allows us to repurpose previous parametric answers as counterparametric ones.

To address Item 2, we manually create a large of different topics, questions, and objects referred to that question in various categories. To create the questions that are being queries, every question is matched to an object of its corresponding category as shown in Table 5.

Category	Base Questions	Object	Final Questions
Person	Q: What is the date of birth of {person}? A: The date of birth of {person} is Q: In what city was {person} born? A: {person} was born in	Che Guevara Confucius	Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is Q: What is the date of birth of Confucius? A: The date of birth of Confucius is Q: In what city was Che Guevara born? A: Che Guevara was born in Q: In what city was Confucius born? A: Confucius was born in
City	Q: What country is {city} in? A: {city} is in	Cairo Mumbai	Q: What country is Cairo in? A: Cairo is in Q: What country is Mumbai in? A: Mumbai is in

**Table 2:** Some examples of the base-question and object generation that are fed to the models for finding parametric answers.

In addition to having the previous properties, it's easy to make a long list of questions using this method.

## 3.2 When does a model choose the provided context knowledge over its inherent knowledge?

#### 3.2.1 Model Selection

In order to get a general understanding of large language models with added context, we test the queries generated in Section 3.1 into models of different types and sizes.

	Seq2Seq Model	Decoder-Only Model
Small	Flan-T5-XL	Meta-Llama-3.1-8B-Instruct
Large	Flan-T5-XXL	Meta-Llama-3.1-70B-Instruct

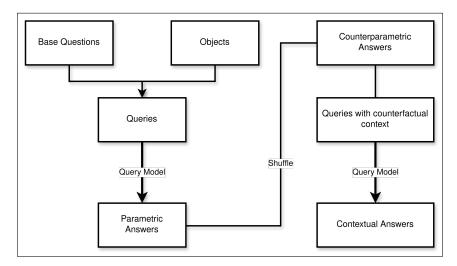
Table 3: The four large language models chosen for this research.

The Flan-T5 models (Chung et al. 2022) are an extension to the original Seq2Seq T5 models (Raffel et al. 2020) which are fine-tuned to particular NLP tasks framed as text-to-text problems. Compared to T5, it's generally better at following instructions and has improved zero-shot performance.

The Llama models (Dubey et al. 2024) are Decoder-only models with a dense transformer architecture that are fine-tuned for instruction-following tasks, and are specially adept at complex prompts.

#### 3.2.2 What type of answer does each model select for each question?

TODO: Maybe I should explain the whole drama with the counterparamteric answers here.



**Figure 1:** Example diagram of steps used to calculate the two sets of answers, *parametric* and *contextual*, and to compare them to answer the question in this objective. Many of the terms in this diagram are explained in the Glossary.

To ensure that the results are simple to interpret and minimise the chance that the result is affected by randomness, once we select the queries we follow the example of Hsia et al. and use Greedy Decoding to find the answer.

While beam search with a short beam width tends to produce more accurate results for long answers (Sutskever et al. 2014, Wu et al. 2016) and there are many other sampling methods that produce better results (Holtzman et al. 2020), this is likely to not have an effect on experiments that result in shorter answers (Raffel et al. 2020).

# 3.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

#### 3.3.1 Perplexity Score

The Perplexity score of an answer is normally used to measure the inverse of the certainty that the model has of a particular answer (Brown et al. 2020, Borgeaud et al. 2022). In a sense, it's the "surprise" of a model that a certain answer is correct.

We can define the probability of model Q choosing a token  $x_n$  with context  $x_1, \ldots, x_{n-1}$  by calculating the softmax value of all the logits for the possible words for this token.

This probability of the tokens corresponding to a particular answer  $x_1, \ldots, x_n$  can be accumulated to calculate the negative log-likelihood NLL, which is used to calculate the perplexity PPL using the formulas from Equations (1) and (2).

$$NLL(x_1,...,x_n \mid Q) = -\frac{1}{n} \sum_{i=1}^{n} \log_2 P(x_i \mid Q, x_1,...,x_{i-1})$$
 (1)

$$PPL(x_1, ..., x_n \mid Q) = 2^{NLL(x_1, ..., x_n \mid Q)}$$
(2)

## **3.3.2** Perplexity of the parametric answer with counterfactual context and vice-versa

Note that the token  $x_n$  does not necessarily have to be the result of applying the query  $x_1, \ldots, x_{n-1}$  to a model. We can instead use teacher-forcing (Lamb et al. 2016) to calculate the perplexity values of finding the parametric answer in the query with counterfactual context, and the

### 4 Methods (Old)

#### 4.1 Models and Resources Used

#### • Reader Models

- Llama-8B.
- Llama-70B.
- Flan-T5-XL.
- Flan-T5-XXL.
- Atlas?

#### • Questions

- Our own dataset, shown in Appendix A.
- Maybe add Natural Questions, HotpotQA, and/or BioASQ as in RAGGED (Hsia et al. 2024).

#### 4.2 Preprocessing and Inference Methodology

#### 4.2.1 Source Data Preparation

Our source data is prepared by extending the ideas presented by Yu et al.. Instead of using one simple question, our approach consists of separating this data into 7 categories, where each category has a set of base questions and another set of objects that are paired together and presented to our models.

This work contains 7 categories in the configuration shown by Table 4, for a total of 3840 questions. The full list of questions can be found in Appendix A.

Category	Questions	Objects	Total
Person	14	47	658
City	14	60	840
Principle	10	30	300
Element	10	35	350
Book	10	45	450
Painting	14	39	546
Historical Event	6	56	336
Total	68	312	3840

**Table 4:** The amount of questions for each category. The full list of questions can be found in Appendix A. This is still a work in progress and I expect to add more questions.

We enhance the zero-shot learning prompt used by Brown et al. by using the prompt format example format presented Jiang et al. for calibrating the T5 language model by adding both the question and the first part of the answer.

#### 4.2.2 Prompting

There is plenty of research that suggests that for zero-shot problems (Brown et al. 2020, Reynolds & McDonell 2021), it's convenient to create a minimal prompt (Jiang et al. 2021, Yu et al. 2023). This is helpful when later calculating the perplexity of the answers, as it tends to bias for short answers without any extra information that might change the individual probabilities of each token.

Examples of the prompting format explained in Sections 4.2.1 and 4.2.2 can be found in Table 5. For later queries, this is enhanced with context as in ??.

Base Question	Object	Final Question
What is the date of birth of {person}? The date of birth of {person} is In what city was {person} born? {person} was born in What country is {city} in?	Che Guevara Confucius Cairo Mumbai	Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is Q: What is the date of birth of Confucius? A: The date of birth of Confucius is Q: In what city was Che Guevara born? A: Che Guevara was born in Q: In what city was Confucius born? A: Confucius was born in
{city} is in		Q: What country is Cairo in? A: Cairo is in Q: What country is Mumbai in?
		A: Mumbai is in

**Table 5:** Some examples of the base-question and object generation that are fed to the models for finding parametric answers.

#### 4.2.3 Generating and scoring parametric answers

We query each of the models listed in Section 4.1 with the data from the previous subsubsections.

To ensure results are simple to interpret and not affected by randomness, we follow the example of Hsia et. al (Hsia et al. 2024) and use greedy decoding to find the answer. While beam search with a short beam width tends to produce more accurate results for long answers (Sutskever et al. 2014, Wu et al. 2016) and there are many other sampling methods that produce better results (Holtzman et al. 2020), this is likely to not have an effect on experiments that result in shorter answers (Raffel et al. 2020).

The negative log-likelihood of an answer x is calculated in base of the conditional probability of generating each token given the prior tokens. We can use this value to calculate the perplexity, which measures the level of "surprise" of a particular answer.

$$NLL(x_{1},...,x_{N}|Q) = -\frac{1}{N} \sum_{i=1}^{N} \log P(x_{i} | Q, x_{i-1},...,x_{1})$$

$$PPL(x_{1},...,x_{N}|Q) = e^{NLL(x_{1},...,x_{N}|Q)}$$
(3)

		Tokens		
		Parametric $p$	Counterparametric $\overline{p}$	
Context	$\mathop{\rm Empty}_{Q}$	$\mathrm{PPL}\left(p_1,\ldots,p_N\mid Q\right)$	$\mathrm{PPL}\left(\overline{p}_{1},\ldots,\overline{p}_{ar{N}}\mid Q ight)$	
	$\begin{array}{c} \text{Counterparametric} \\ W \end{array}$	$\mathrm{PPL}\left(p_{1},\ldots,p_{N}\mid W ight)$	$\mathrm{PPL}\left(\overline{p}_{1},\ldots,\overline{p}_{ar{N}}\mid W ight)$	

Figure 2: Four different perplexity values: one for each set of tokens, and one for each query context...

We can ensure that the probabilities are calculated based on the intended tokens rather than the "most probable" generated ones by using teacher forcing (Lamb et al. 2016).

#### 4.2.4 Shuffling to generate counterparametric answers

Previous work related to finding per token probabilities of answers in large language models focus on either a pre-existing list of questions or on a single question format (Yu et al. 2023). This approach does not work for our use case for three reasons.

- 1. Having 68 different types of questions, rather than just 1, makes finding counterfactual answers technically challenging.
- 2. Our focus is not on finding *counterfactual* answers, but *counterparametric* ones. We do not care about correctness; we care about answers not being parametric.
- 3. Since we are measuring perplexity of these answers, we focus on answers that are generated by the same base question and the same model. This way we ensure that the format of the answer is the same.

We propose a novel way of generating counterparametric answers while focusing on these three points: rather than generating new answers for each question, counterfactual answers are randomly sampled from the parametric answers corresponding to the same base question. An example of this approach can be seen in ??.

#### 4.2.5 Counterparametric and contextual perplexity scores

This works extends the approach of analysing answers found in [citation needed] and explained in Section 4.2.3 by also calculating the perplexity of *alternative* answers to each question.

That is, we take the result of applying each model to both the answer with and without counterparametric context, and we calculate the perplexity scores of getting both the parametric and counterparametric answer to each one of these. This produces four different scores which are detailed in Figure 2: one for each answer using either empty and counterparametric context.

<sup>\*</sup>I am finding it hard to explain this subsubsection. Maybe I should add pseudocode here.

By definition, the tokens of the parametric answer  $p_1, \ldots, p_N$  are the ones corresponding to the lowest perplexity answer for the query without any context. This is not the case for the tokens of the counterparametric answer  $\bar{p}_1, \ldots, \bar{p}_{\bar{N}}$ , which produces the inequality in Equation (4).

$$PPL(p_1, \dots, p_N \mid Q) \le PPL(\bar{p}_1, \dots, \bar{p}_{\bar{N}} \mid Q)$$
(4)

Finding the result of the inequality for the queries with the counterparametric context W is one of the main goals of this research. In fact, we know that if the perplexity of the parametric tokens  $p_1, \ldots, p_N$  is greater than the tokens for the counterparametric answer  $\bar{p}_1, \ldots, \bar{p}_{\bar{N}}$  then the answer was memorised. Otherwise, the answer was generated in-context.

Answer Source = 
$$\begin{cases} \text{Memory} & \text{if } P(p_1, \dots, p_N \mid W) < P(\overline{p}_1, \dots, \overline{p}_{\bar{N}} \mid W) \\ \text{Context} & \text{otherwise} \end{cases}$$
(5)

#### 4.2.6 Comparing the Final Answers

There is a third case that's not present in Equations (4) and (5): the case where the answer comes from neither the model's memory nor the query's context, but that instead the model generates a third answer combining both.

There are several cases where this can happen. The most interesting are explained in ??, while the full results can be found in Appendix B.

In particular, we categorise the final answers in one of three groups depending on whether the answer with minimal perplexity on the query with the counterfactual context W is equal to the parametric answer, to the counterparametric answer, or to something else.

Group = 
$$\begin{cases} \text{Parametric} & \text{if } (\nexists x_1, \dots, x_N) \text{ PPL } (x_1, \dots, x_N \mid W) < A \\ \text{Counterparametric} & \text{if } (\nexists x_1, \dots, x_N) \text{ PPL } (x_1, \dots, x_N \mid W) < B \end{cases}$$
(6)

where

$$A = \operatorname{PPL}(p_1, \dots, p_N \mid W)$$
  
$$B = \operatorname{PPL}(\overline{p}_1, \dots, \overline{p}_{\bar{N}} \mid W)$$

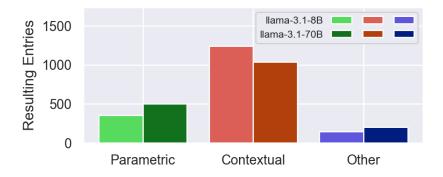
There is a correlation between Equation (6) and Equation (5): an answer in the Parametric group will come from the model's memory, and an answer in the Counterparametric group will come from the query's (counterparametric) context.

#### 5 Results

Some results I want to show.

- Larger models tend to prefer parametric knowledge over contextual knowledge.
  - This is the case in "Characterizing Mechanisms for Factual Recall in Language Models" (Yu et al. 2023), but I'm proving this on a larger set of question.
  - This is using exact match. Maybe attempting Unigram F<sub>1</sub> would produce interesting results (Petroni et al. 2021).
- How this compares between Decoder-only models, Seq2Seq models, and Retrieval-Augmented Language Models.
- How does the perplexity between parametric answers and contextual answers compare within the same model.
  - From the perplexity alone, can we predict whether an answer came from the model's memory or from the context?
  - It might be worth experimenting this with factual answers in the context, to simulate a RAG-difference detector.
- Is there any correlation between the perplexity of the parametric and contextual answer without any context and which one will be chosen when adding context?
  - This one is interesting, but I'm not sure we'll get significative results.
- Interesting "Other" results.
- Anything else?

#### 5.1 Comparing the amounts of each type of answer



**Figure 3:** Amount of entries for each result after applying counterfactual context to Llama models. Generally, larger models tend to prefer parametric to contextual knowledge; this is further discussed in Section 6.2.

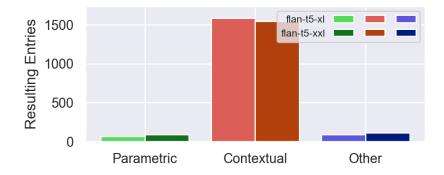


Figure 4: Same results for the Seq2Seq models Flan-T5. While these models tend to be more biased towards contextual knowledge, as discussed in Section 6.1, larger models still are biased towards parametric knowledge.

#### 5.2 Comparing the perplexity distribution for each type of answer

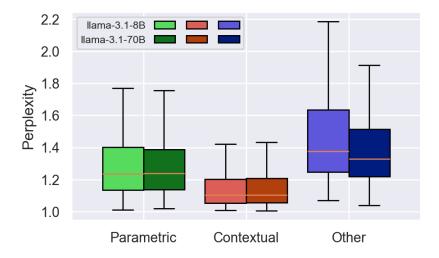


Figure 5: Perplexity box plots for Decoder-only Llama models.

Despite the amount for small and large Llama models being considerably different, the average values and distributions remain roughly the same. This is discussed in Section 6.

Additionally, the perplexity of contextual answers is considerably lower than the one for parametric answers.

Interestingly, the larger models tend to have a much lower perplexity for both paramteric and contextual answers.

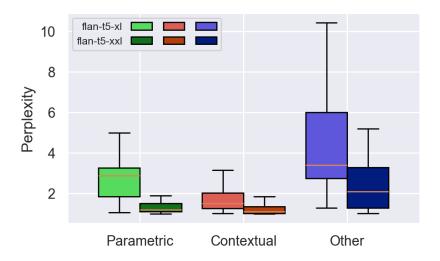


Figure 6: Perplexity box plots for Seq2Seq Flan models.

### 6 Discussion

- 6.1 Model type and memorised knowledge
- 6.2 Model size and memorised knowledge
- 6.3 Differences in perplexity scores for larger and smaller models
- 6.3.1 Can we use this to predict from where an answer came from?
- 6.4 Differences in distributions for different categories and questions.

7 Evaluations, Reflections, and Conclusions

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### **Appendices**

#### A Questions and objects used to form the queries

```
What is the date of birth of {person}? The date of birth of {person} is In what city was {person} born? {person} was born in What is the date of death of {person}? The date of death of {person} is
What is the date of death of {person}? The date of death of {person} is
What is the primary profession of {person}? The primary profession of {person} is
What is {person} primarily known for? {person} is primarily known for
What's the main nationality of {person}? {person} is
What educational institution did {person} attend? {person} attended
What was the native language of {person}? The native language of {person} was
Who was {person}'s most influential mentor? The most influential mentor of {person} was
What was {person}'s religious affiliation? The religious affiliation of {person} was
What was {person}'s primary field of study? The primary field of study of {person} was
What was {person}'s most famous work or invention? The most famous work or invention of {person} was
What historical period did {person} live in? {person} lived during the
What was {person}'s family's social class? {person}'s family belonged to the
What was {person}'s political ideology? The political ideology of {person} was
What was {person}'s preferred artistic or scientific medium? The preferred medium of {person} was
What was {person}'s cultural background? The cultural background of {person} was
  What country is {city} in? {city} is in What's the highest administrative subdivision {city} is part of? {city} is part of
What's the highest administrative subdivision {city} is part of? {city} is part of
In what year was {city} founded? {city} was founded in
What major river is nearest to {city}? The nearest major river to {city} is
What is the time zone of {city}? The time zone of {city} is
What is the current population of {city}? The current population of {city} is
What is the altitude of {city} above sea level? {city} is at an altitude of
What is the primary language spoken in {city}? The primary language spoken in {city} is
What is the predominant architectural style in {city}? The predominant architectural style in {city} is
What is the main economic industry of {city}? The main economic industry of {city} is
What is the average annual temperature in {city}? The average annual temperature in {city} is
What is the nearest major body of water to {city}? The nearest major body of water to {city} is
What is the most famous landmark in {city}? The most famous landmark in {city} is
What is the primary mode of public transportation in {city}? The primary mode of public transportation in {city} is
                           {city} is
  What is the name of the airport serving {city}? The airport serving {city} is
What is the sister city of {city}? The sister city of {city} is
What is the traditional cuisine {city} is known for? The traditional cuisine {city} is known for is
   Who is credited with the discovery of {principle}? {principle} was discovered by
  Which scientific discipline encompasses {principle}? {principle} is encompassed by What is the primary application of {principle}? The primary application of {principle} is In which year was {principle} first formulated? {principle} was first formulated in What is the SI unit most commonly associated with {principle}? The SI unit most commonly associated with
   What's the chemical formula for {element}? The chemical formula for {element} is
 What's the chemical formula for {element}? The chemical formula for {element} is

When was {element} first isolated? {element} was first isolated in

What's the atomic number of {element}? The atomic number of {element} is

What is the melting point of {element}? The melting point of {element} is

In which group of the periodic table is {element} found? {element} is found in group

What's the standard atomic weight of {element}? The standard atomic weight of {element} is

What's the electron configuration of {element}? The electron configuration of {element} is

What's the most common oxidation state of {element}? The most common oxidation state of {element} is

What's the crystal structure of {element} at room temperature? The crystal structure of {element} at room
 What's the crystal structure of {element} at room temperature? The crystal structure of {element} temperature is
What's the primary isotope of {element}? The primary isotope of {element} is
What's the electronegativity value of {element}? The electronegativity value of {element} is
What's the ionization energy of {element}? The ionization energy of {element} is
What's the atomic radius of {element}? The atomic radius of {element} is
What's the boiling point of {element}? The boiling point of {element} is
In which period of the periodic table is {element} located? {element} is located in period
  What genre does {book} belong to? The genre of {book} is
Who's the author of {book}? {book} was written by
In what year was {book} first published? {book} was first published in
How many pages are in the original publication of {book}? The original publication of {book} has
What is the name of the main protagonist in {book}? The main protagonist in {book} is
  What is the original language of {book}? The original language of {book} is Who is the original publisher of {book}? The publisher of {book} is What is the highest award {book} won? The highest award won by {book} is What is the opening line of {book}? The opening line of {book} is How many chapters are in {book}? {book} has How many pages are in {book}? {book} has
Who painted {painting}? {painting} was painted by
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What artistic movement does {painting} belong to? {painting} belong to What artistic movement does {painting} belong to? {painting} was created with Where is {painting} primarily housed? {painting}? {painting} was created with Where is {painting} primarily housed? {painting}? The dimensions of {painting}? The dominant color in {painting}? Is who commissioned {painting}? The subject matter of {painting} is What is the subject matter of {painting}? The subject matter of {painting} is In which country was {painting} created? {painting} was created in What year did {historical_event} happen? {historical_event} happened in the year Who was the primary leader associated with {historical_event}? The primary leader associated with {historical_event} was What was the duration of {historical_event}? {historical_event} lasted for In which country did {historical_event} primarily take place? {historical_event} primarily took place in What is the height of {building}? The height of {building} was In which year was {building} completed? {building} is located in What architectural style is {building}? The architectural style of {building} is How may floors does {building} have? {building} has What is the primary construction material of {building}? The primary construction material of {building}? The primary construction material of {building}? The order of {building} took

Who composed {composition}? {composition} was composed by In what year was {composition} first performed? {composition} was first performed in What is the open marking of {composition}? The emsical genre of {composition} is What is the was {composition} first performed? {composition} was primary of {composition} is What is the durat
```

**Listing 1:** All base questions used in this work. Each one of these will get combined with data from Listing 2 as detailed in Section 4.2.1.

```
Ada Lovelace, person
Alan Turing, person
Albert Einstein, person
Alexander Fleming, person
Aristotle,p
Billie Jean King, person
Boyan Slat, person
Catherine the Great, person
Che Guevara, p
Cleopatra, person
Confucius, person
Ernest Rutherford, person
Florence Nightingale, person
Freddie Mercury, person
Frida Kahlo, person
Greta Thunberg, person
Harriet Tubman, person
Ibn al-Haytham, person
Isaac Newton, person
Isaac Newton, person
Karl Marx, person
Leonardo da Vinci, person
Mahatma Gandhi, person
Malala Yousafzai, person
Mansa Musa, person
Marie Curie, per
Martin Luther King Jr., person
Michelangelo, person
Mohandas Gandhi, person
Mozart, p
Muhammad Ali, persor
Neil Armstrong, person
Nelson Mandela, person
Nikola Tesla, person
Pablo Picasso
Rosalind Franklin, person
Shirin Ebadi, person
Simon Bolivar, person
Srinivasa Ramanujan, person
Stephen Hawking, person
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Sun Yat-sen, person
Virginia Woolf, person
Vladimir Lenin, person
 Wangari Maathai, person
W.E.B. Du Bois, person
William Shakespeare, person
William Shakespeare, per Wu Zetian, person Yuri Gagarin, person Amelia Earhart, person Galileo Galilei, person Genghis Khan, person Joan of Arc, person Lise Meitner, person Marcus Aurelius, person Maya Angelou, person Queen Nzinga, person Socrates, person Voltaire, person
 Voltaire, person
Alexandria, city
Amsterdam, city
Amsterdam, city
Antananarivo, city
Athens, city
Baghdad, city
 Berlin, city
Buenos Aires, city
Buenos Aires, c:
Bukhara, city
Cairo, city
Cape Town, city
Cartagena, city
Chicago, city
Cusco, city
Cuzco, city
Delhi, city
Dubrownik, city
 Dubrovnik, city
 Fez, city
Havana, city
 Istanbul, city
Jerusalem, city
 Kyoto, city
La Paz, city
La Paz,city
Lhasa,city
Lisbon,city
London,city
Luang Prabang,city
Mexico City,city
Montevideo,city
Moscow,city
Mumbai,city
Numbai,city
New York,city
 New York, city
Nur-Sultan, city
Paris, city
Petra, city
Prague, city
Quebec City, city
Reykjavik, city
Rome, city
Sao Paulo, city
Sao Paulo, city
Sarajevo, city
Shanghai, city
Singapore, city
St. Petersburg, city
St. Petersburg, cit

Sydney, city

Tbilisi, city

Tenochtitlan, city

Timbuktu, city

Tokyo, city

Ulaanbaatar, city

Varanasi, city

Venice, city

Venice, city

Wellington, city
 Wellington, city
Windhoek, city
Windhoek, city
Xi'an, city
Yogyakarta, city
Zanzibar City, city
Addis Ababa, city
Bangkok, city
Dubai, city
Helsinki, city
Machu Picchu, city
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Nairobi, city
Rio de Janeiro, city
Samarkand, city
 Yangon, city
Yarchimedes' Principle, principle
Bernoulli's Principle, principle
 Boyle's Law, principle
Cell Theory, principle
Conservation of Energy, principle
 DNA Replication, principle
Electromagnetism, principle
Entropy, principle
Entropy, principle
Evolution by Natural Selection, principle
Evolution, principle
General Relativity, principle
Germ Theory of Disease, principle
Gravity, principle
Hardy-Weinberg Principle, principle
Heliocentrism, principle
Hubble's Law, principle
Hubble's Law, principle
Kepler's Laws of Planetary Motion, principle
Le Chatelier's Principle, principle
Mendel's Laws of Inheritance, principle
Newton's Laws of Motion, principle
Pauli Exclusion Principle, principle
Priodic Law, principle
Photosynthesis, principle
Plate Tectonics, principle
 Plate Tectonics, principle
Principle of Least Action, principle
 Quantum Mechanics, principle
 Relativity, principle
Superconductivity, principle
 Thermodynamics, principle
Uncertainty Principle, principle
Avogadro's Law, principle
 Coulomb's Law, principle
Faraday's Laws of Electrolysis, principle
 Heisenberg Uncertainty Principle, principle Ohm's Law, principle
 Schrä¶dinger Equation, principle
Special Relativity, principle
 Aluminum, element
Barium, element
Bismuth, element
Bromine, element
 Calcium, element
Carbon, element
Chlorine, element
Chromium, element
 Copper, element Gold, element
 Helium, element
 Hydrogen, element
 Iodine, element
Iron, element
 Lead, element
 Magnesium, element
Manganese, element
Mercury, element
Neon, element
Nitrogen, element
 Oxygen, element
Phosphorus, element
Plutonium, element
 Potassium, element
 Radon, element
Silicon, element
Silver, element
 Sodium, element
 Sulfur, element
Thorium, element
 Tin, element
Titanium, element
 Uranium, element
 Zinc, element
 Argon, element
Boron, element
 Cobalt, element Fluorine, element
 Gallium, element Krypton, element
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Nickel, element
 Xenon, element
 1984,b
 Anna Karenina, book
 Beloved, book
Brave New World, book
Catch-22, book
 Crime and Punishment, book
Don Quixote, book
Fahrenheit 451, book
 Frankenstein,
 Jane Eyre, book
Midnight's Children, book
 Moby-Dick, book
One Flew Over the Cuckoo's Nest, book
 One Hundred Years of Solitude, book
 Slaughterhouse - Five, boo
 The Alchemist, bo
The Art of War,
The Book Thief,
 The Brothers Karamazov, book
The Catcher in the Rye, book
The Chronicles of Narnia, book
 The Color Purple, b
 The Color Purple, book
The Count of Monte Cristo, book
The Grapes of Wrath, book
The Great Gatsby, book
The Handmaid's Tale, book
The Hitchhiker's Guide to the Galaxy, book
 The Hobbit, book
The Hunger Games,
 The Kite Runner,
 The Little Prince, book
The Lord of the Rings, book
The Metamorphosis, book
 The Name of the Rose, book
The Odyssey, book
The Picture of Dorian Gray, book
The Pillars of the Earth, book
 The Stranger, book
The Sun Also Rises, b
 The Wind-Up Bird Chronicle, book
To Kill a Mockingbird, book
 Ulysses, book
War and Peace,
War and Peace, book
Wuthering Heights, book
The Iliad, book
The Tale of Genji, book
Things Fall Apart, book
To the Lighthouse, book
American Gothic, painting
Christina's World, painting
Girl with a Pearl Earring, painting
 Guernica, painting
Les Demoiselles d'Avignon, painting
Les Demoiselles d'Avignon, painting
Liberty Leading the People, painting
Mona Lisa, painting
School of Athens, painting
Starry Night, painting
The Absinthe Drinker, painting
The Anatomy Lesson of Dr. Nicolaes Tulp, painting
The Arnolfini Portrait, painting
 The Astronomer, painting
The Birth of Venus, painting
The Calling of Saint Matthew, painting
The Calling of Saint Matthew, Painting
The Card Players, painting
The Death of Marat, painting
The Fighting Temeraire, painting
The Garden of Earthly Delights, painting
The Gross Clinic, painting
The Hay Wain, painting
The Kiss, painting
The Last Sunner Dainting
 The Kiss, painting
The Last Supper, painting
The Nighthawks, painting
The Night Watch, painting
The Ninth Wave, painting
The Persistence of Memory, painting
The Potato Eaters, painting
 The Raft of the Medusa, painting The Scream, painting
 The Sleeping Gypsy, painting
The Son of Man, painting
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The Swing, painting
The Third of May 1808, painting
The Tower of Babel, painting
The Treachery of Images, painting
The Triumph of Galatea, painting
The Wanderer above the Sea of Fog, painting
Water Lilies, painting
The Creation of Adam, painting
The Girl with a Pearl Earling, painting
The Great Wave off Kanagawa, painting
The Thinker, painting
Venus de Milo, painting
Decimalisation in the UK, historical_event
Queen Elizabeth II's Platinum Jubilee, historical_event Queen Victoria's Coronation, historical_event
 The Act of Union between England and Scotland, historical_event
The Battle of Advanple, historical_event
The Battle of Adva, historical_event
The Battle of Agincourt, historical_event
The Battle of Hastings, historical_event
The Battle of Sekigahara, historical_event
The Battle of Teutoburg Forest, historical_event
The Battle of the Milvian Bridge, historical_event
The Battle of Waterloo, historical_event
The Brexit Referendum, historical_event
The Codification of Roman Law by Justinian, historical_event
The Construction of Hadrian's Wall, historical_event
The Construction of the Great Pyramid of Giza, historical_event
The Council of Constantine, historical_event
The Council of Chalcedon, historical_event
 The Crisis of the Third Century, historical_event
The Crisis of the Third Century, historical_event
The Defeat of the Spanish Armada, historical_event
The Discovery of the Americas by Columbus, historical_event
The Dissolution of the Soviet Union, historical_event
The Division of the Roman Empire, historical_event
The Dunkirk Evacuation, historical_event
The Edict of Caracalla, historical_event
The Fall of Constantinople, historical_event
The Fall of the Aztec Empire, historical_event
The Fall of the Western Roman Empire, historical_event
The First Circumpayigation of the Earth, historical_event
The First Circumnavigation of the Earth, historical_event
The First Council of Nicaea, historical_event
 The First Crusade, historical event
 The Founding of Constantinople, historical_event
The Founding of Rome, historical_event
The Founding of the British Broadcasting Corporation, historical_event
The Founding of the League of Nations, historical_event
The French Revolution, historical_event
The Glorious Revolution, historical_event
The Gothic War in Italy, historical_event
The Great Fire of London, historical_event
The Indian Independence Act, historical_event
The Indian Independence Act, historical_event
The Industrial Revolution, historical_event
The London 7/7 Bombings, historical_event
The Meiji Restoration, historical_event
The Plague of Justinian, historical_event
The Reforms of Diocletian, historical_event
The Reunification of the Empire by Aurelian, historical_event
The Sack of Rome by Alaric, historical_event
The Sack of Rome by the Vandals, historical_event
The Signing of the Good Friday Agreement, historical_event
The Signing of the Magna Carta, historical_event
The Suze Crisis, historical_event
The Suez Crisis, historical_event
The Treaty of Westphalia, historical_event
The UK Abolition of the Slave Trade Act, historical_event
The Unification of Italy, historical_event
The Wedding of Prince Charles and Lady Diana, historical_event
The Year of the Four Emperors, historical_event
The American Revolution, historical_event
The Black Death, historical_event
The Cuban Missile Crisis, historical_event
The Fall of the Berlin Wall, historical_event
The Moon Landing, historical_event
The Renaissance, historical_event
The Russian Revolution, historical_event
 The Signing of the Declaration of Independence, historical_event
Angkor Wat, building
Buckingham Palace, building
Burj Khalifa, building
Chichen Itza, building
Chrysler Building, building
 Colosseum , building
 Eiffel Tower, building
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Empire State Building, building
Forbidden City, building
Guggenheim Museum, building
Hagia Sophia, building
Hagia Sophia, building
Hacker Pyramid, building
Machu Picchu, building
Ruschurstein Castle, building
Parthenon, building
Petronas Towers, building
Petronas Towers, building
Petronas Towers, building
Potale Palace, building
State Tower, building
State Tower, building
State Tower, building
St. Basil's Cathedral, building
Sydney Opera House, building
Taj Mahal, building
Adagio for Strings, composition
Billie Jean, composition
Canon in D, composition
Canon in D, composition
Carnina Burnan, composition
Clair de Lume, composition
Clair de Lume, composition
Clair de Lume, composition
GymonjAGies, composition
Imagine, composition
In the Mood, composition
Like a Rolling Stome, composition
Like a Rolling Stome, composition
Numbube (The Lion Sleeps Tonight), composition
Massan Dorma, composition
Raga Malkauns, composition
Rhapsody on a Theme of Paganini, composition
Symphony No. 5, composition
The Blue Danube, composition
The Planets, composition
The Rite of Spring, composition
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**Listing 2:** All objects which will be combined with the questions in Listing 1.

- B Full Results for Each Question
- C Grounder Usage and Documentation
- D appendixD