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Knowledge Grounding in Language Models: An Empirical Study

Martin Fixman

Supervised By: Tillman Weyde Collaborators: Chenxi Whitehouse and Pranava Madhyastha

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Declaration

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In submitting this work I acknowledge that I have read and understood the regulations and code regarding academic misconduct, including that relating to plagiarism, as specified in the Programme Handbook. I also acknowledge that this work will be subject to a variety of checks for academic misconduct.

Signed: Martin Fixman

Acknowledgements

Abstract

In recent years large language models have exploded in quality and prevalence, and they have become crucial for work in a wide range of areas. However, their tendency to produce hallucinations presents a critical challenge in context where accuracy is crucial.

Retrieval-Augmented Generation (RAG), which leverages external information to provide more accurate and contextually appropriate responses, has been proposed as a solution to this issue. However, this solution is far from perfect as it's unclear when a large language model will choose the information provided by the RAG model over its learned, parametric knowledge.

This thesis explores the *Knowledge Grounding* of various large language models. In particular, it attempts to answer a simple research question: when would a model choose an answer using its parametric or contextual knowledge, and why?

To investigate this, we developed a diverse dataset comprising questions from various topics and globally representative data, which we used to construct queries with counterparametric context across four models of different types and sizes. We later analyse the perplexity of these answers to understand the level of surprise that a model has when presented with the parametric or contextual answer.

Our findings suggest that, when using RAG-enhanced systems, smaller and simpler models might produce fewer hallucinations. In particular, the smaller models Meta-Llama-3.1-8B and Flan-T5-XL tend to have better knowledge grounding and fewer hallucinations than their larger versions. Additionally, we propose novel methods for determining whether a given response originates from the RAG context or the model's internal memory using its resulting perplexity, which may indicate a potential hallucination.

This thesis forms the foundational part of a broader project aimed at publishing a comprehensive study on knowledge grounding in retrieval-augmented language models, as outlined in the preprint "Knowledge Grounding in Retrieval-Augmented LMs: An Empirical Study" (Whitehouse et al. 2023). We build on existing literature, incorporating the use of counterparametric context in queries, to advance our understanding of this phenomenon."

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1 Introduction and Objectives

1.1 Problem Background

In recent years, Large Language Models (LLMs) have become ubiquitous in solving general problems across a wide range of tasks, from text generation to question answering and logic problems. However, recent research suggests that using these models alone might not be the most effective way to solve problems that are not directly related to text generation (Yao et al. 2023).

One approach to improving the performance on knowledge problems for LLMs is Retrieval-Augmented Generation (RAG) (Lewis et al. 2020). RAG involves retrieving relevant context related to a query and incorporating it into the model's input, enhancing the model's ability to generate accurate and contextually appropriate responses.

As RAG-enhanced systems become more widespread, studies on the performance of different retrieval systems and their interaction with LLMs have become crucial. Many explore the performance of these downstream tasks depending on both the retriever and the generator (Ghader et al. 2023, ?), examining whether the knowledge is *grounded* in the context. Retrieval-Augmented models, such as ATLAS (Izacard et al. 2022) and RETRO (Borgeaud et al. 2022), use this approach to fine-tune a model on both a large body of knowledge and an existing index for context retrieval.

This project aims to understand the performance of various LLMs by measuring their knowledge grounding on a dataset consisting of a large variety of questions across a wide range of topics. We follow the approach by Yu et al. of running queries with counterparametric context to understand whether a particular answer originates from the model's inherent knowledge (i.e., its training data) or from the provided context (i.e., the context retrieved by RAG).

This thesis builds on this knowledge and improve our understanding of how different LLMs interact with the given context in the problem of question answering. Specifically, we investigate whether these interactions vary depending on the type of question being answered, contributing to a more nuanced understanding of LLM performance in diverse knowledge domains.

1.2 Research Question

How do we know what large language models really know?

This thesis attempts to answer this question by asking a different but related question: What happens when the context in a query contradicts the parametric knowledge of this model?

The rest of this section gives an overview of the steps we take to answer this question.

1.3 Research Objectives

This thesis is structured around three different sub-objectives to deepen our understanding knowledge grounding in large language models.

1.3.1 Creating a representative dataset of questions

We require a dataset of questions that's useful for answering our research question. This dataset should allow us to understand the responses of the models to know whether they came from the model's parametric memory or from the RAG context, and should be reasonably representative of the world to prevent biases.

1.3.2 When does a model choose the provided context knowledge over its inherent knowledge?

Currently, little is understood about the factors and mechanisms that control whether an LLM will generate text respecting either the context or the memorised information.

Previous research found out that, when the context of a query contradicts the ground knowledge of a model, the final answer depends on the size and type of the model used (Yu et al. 2023).

This thesis extends this research by testing the representative set of questions and counterfactuals described in the previous section with both Seq2Seq and Decoder-only models of various sizes. We also research the cases when the answer doesn't correspond to either the parametric or contextual knowledge, and why the model chooses a third type of answer when adding counterfactual context.

1.3.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

Yu et al. showed that there is a correlation between the probability of a large language model choosing a parametric answer over a counterfactual contextual answer and the amount of times this answer appears in the ground truth data of the model. This gives us clues on whether the result of a query came from parametric or contextual knowledge if we have access to this ground truth, as is the case in models like Pythia (Biderman et al. 2023).

Unfortunately, most so-called open-source large language models do not give us access to the source data being used to train it and therefore do not allow this kind of analysis.

The **perplexity** score of answer gives a measure of how "certain" a large language model is of its answer (Jiang et al. 2021). We hypothesise that we can use this metric to serve as a reliable indicator of whether a particular answer was memorised by the LLM or was derived from the provided context.

2 Context

This research is the latest on a long line of academic articles on the topics of retrievalaugmented generation, counterparametric and contextual data, and how to enhance knowledge on large language models.

This section summarizes key articles that informed this research.

2.1 Foundational Papers on Large Language Models

Large language models have exploded in popularity since the development of the transformer architecture (Vaswani et al. 2017). This architecture relies entirely on self-attention mechanisms rather than recurrent or convolutional layers, which allow the model to weigh the importance of different words in a sequence relative to each other, irrespective of their position. This mechanism enables the model to capture complex dependencies and relationships across long sequences more effectively than traditional models.

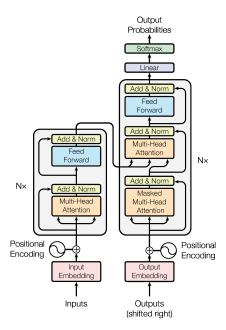


Figure 1: Transformer Architecture, from "Attention is all you need" (Vaswani et al. 2017).

GPT models (Radford & Narasimhan 2018) improve upon this architecture by running a supervised task-specific fine-tuning round after the unsupervised pre-training on large amount of test data. Later models, starting from GPT-2, use zero-shot transfer learning to improve their performance (Radford et al. 2019). Zero-shot learning (Norouzi et al. 2014) trains a model to perform a task without having been explicitly trained on examples of that task; instead, it leverages knowledge gained from pre-training to infer and generalise to new tasks with the context on the prompt.

By adding only a few examples of the task at hand, a model can use few-shot learning to

improve generalisation to new tasks with a limited amount of labelled data. GPT-3 uses this to understand the structure and nature of a task with a few examples (Brown et al. 2020)

TODO: Talk about T5, Flan-T5, and Llama here.

Despite these improvements, the models themselves are still uncalibrated and not very good at question answering (Jiang et al. 2021). Hallucinations are common, even for short Q&A tasks

2.2 Retrieval-Augmented Generation

Large pre-trained language models store factual knowledge in their parameters. Their ability to access this knowledge is limited, which affects their performance on knowledge-intensive tasks.

Retrieval-Augmented Generation (RAG) attempts to solve this problem by adding extra non-parametric context gathered from an index with a retriever that's trained independently (Lewis et al. 2020). This retrieved context is fed back to the original query by adding context, which generates a combined representation which contains both the query and the original context. An overview of this method is presented in Figure 2.

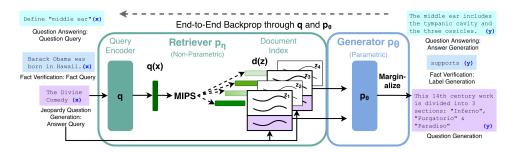


Figure 2: An overview of the RAG approach, combining a pre-trained retriever with a pre-trained model. From "Retrieval-Augmented Generation for Knowledge-Intensive NLP tasks" (Lewis et al. 2020)

RAG can be effective in preventing hallucinations by incorporating relevant external information into the generation process, ensuring that responses are more grounded in factual data from a knowledge base. However, this is not perfect and an even after adding a correct context the model could answer data from its internal memory.

2.3 Knowledge Grounding on Queries with Added Context

Knowledge grounding is the process of ensuring that information generated by a language model is consistent with a reliable external source of knowledge. In the context of RAG-enhanced queries, this can include ensuring that answers are consistent with the knowledge in the index rather than in the model's inherent knowledge.

Various attempts have been made at understanding how good the knowledge grounding of a RAG system is, and on what is the optimal configuration of RAG.

In "RAGGED: Towards Informed Design of Retrieval Augmented Systems" (Hsia et al. 2024), the authors create a framework to evaluate these systems and find that different models suit substantially varied RAG setups. In particular, the performance of the models decreases strongly in Decoder-only models such as Llama when the context passages provides more context, while this does not happen on Seq2Seq models such as Flan.

"Characterizing Mechanisms for Factual Recall in Language Models" (Yu et al. 2023), which is one of the main sources for this thesis, finds that when there is disagreement between the model's knowledge and the provided context then the type and size of the large language model will greatly affect the probability of the model choosing to use the context (which is much less prone to hallucinating) as an answer.

This paper also introduces a novel way to test this hypothesis by creating a dataset with questions and counterfactual context, an example of which is shown in Listing 1.

```
The capital of {country} is {in-context city} Q: What is the capital of {country}?
A:
```

Listing 1: Example of queries used in (Yu et al. 2023). These queries form the basis and inspiration for the dataset creation done in this thesis

By adding counterparametric information to the context, this method allows us to understand whether an answer came is parametric (that is, came from the memory of the model) or contextual (that is, came from the provided context).

3 Methods

3.1 Creating a representative dataset of questions

As argued in Section 1.3.1, the research of this thesis requires a large dataset of questions from a variety of categories to test large language models.

3.1.1 Dataset Description

The dataset we aim to create for this research is designed to be a comprehensive and versatile tool for evaluating large language models. By choosing this criteria when selecting questions, we ensure that the dataset will provide meaningful insights into knowledge grounding of large language models across a wide spectrum of knowledge domains.

In order to understand knowledge grounding in these LLMs, we require a dataset with the following properties:

1. Questions should have short, unambiguous answers.

Our goal is to compare these results for both equality and perplexity. Longer answers make this objective more complicated since two long, correct answers might be equivalent. Shorter answers reduce the space of possible answers that are equivalent, but not equal.

2. Questions must cover a large and diverse set of topics in a comprehensive global and historical range.

The parametric knowledge of a model comes from a pre-existing dataset of training data, which might be biased towards certain topics or groups of people. For example, it is known that Wikipedia contains a significant geographical bias on biographies (Beytía 2020), and that this affects the probability of giving a correct answer without context (Yu et al. 2023). We require a large and diverse and set of topics to counteract potential biases.

3. Questions must allow for the creation of counterparametric answers in the same format as correct ones.

Part of the requirements of this thesis is to allow some tests of contextual versus inherent knowledge. A simple way to do this is to repeat and enhance the approach used by Yu et al. of adding counterparametric answers to a query context. This allows us to to easily disambiguate whether an answer came from the model's memory or from the context. This approach is only possible if the set of answers allows us to create a set of alternative answers that are plausibly correct and have the same format as the parametric answer, but are still counterparametric.

The existing literature uses various existing question-and-answer datasets. We believe that none of these datasets are a good fit for this research for not following some of the three desired properties. However, understanding them can be useful when designing the final dataset.

Natural Questions Dataset Created by Google Research (Kwiatkowski et al. 2019), and commonly used in research related to understanding the answers of LLMs in question-and-answer problems (Hsia et al. 2024, Mallen et al. 2023, Ghader et al. 2023). While the dataset provides an excellent range of questions and existing literature to compare these results to, the lack of categorisation is an obstacle in our objective to generate counterparametric answers.

Human-Augmented Dataset Sometimes used in research related to quality control of large language models (Kaushik et al. 2020). However, the high cost associated with this dataset would limit the size of our questions.

Countries' Capitals Question Dataset Used in "Characterizing Mechanisms for Factual Recall in Language Models" (Yu et al. 2023), this dataset contains a single question about the capital city of certain countries which can be easily transformed to a counterparametric question. This format is ideal for the research done in this thesis, but having a single question pattern will not allow a deep dive into the source of each answer in a general question.

3.1.2 Dataset Creation

Instead of using an existing dataset, this research takes inspiration from the paper by Yu et al. to create a similar but larger dataset of questions and answers from a wide range of topics, where questions can be grouped by question pattern to ensure that their formats are similar. This way, we can emulate the approach of that paper of using the answer from a certain question as the counterfactual question of another.

This dataset will be used to test the remaining questions of this thesis. Since it might be useful for future research, it will also be presented as its own result.

To address these items, we follow the approach done by Yu et al. in creating base questions that refer to a specific object, so all the answers for the same base question have a similar format and creating counterparametric answers is easy.

Since this thesis requires a set of questions that covers a large set of topics, eras, and places, we enhance this method by creating a set of categories, each of which has a large set of base questions and another set of objects that can be matched. An example of this approach is shown in Table 1.

This list of questions will enable the research on whether the answers given by large language models depend on the category and the format of the questions.

Category	Base Questions	Object	Queries	
Person	Q: What is the date of birth of {person}? A: The date of birth of {person} is Q: In what city was {person} born? A: {person} was born in	Che Guevara Confucius	Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is Q: What is the date of birth of Confucius? A: The date of birth of Confucius is Q: In what city was Che Guevara born? A: Che Guevara was born in Q: In what city was Confucius born? A: Confucius was born in	
City	Q: What country is $\{city\}$ in? A: $\{city\}$ is in	Cairo Mumbai Buenos Aires London	Q: What country is Cairo in? A: Cairo is in Q: What country is Mumbai in? A: Mumbai is in Q: What country is Buenos Aires in? A: Buenos Aires is in Q: What country is London in? A: London is in	

Table 1: Some examples of the base-question and object generation that are fed to the models for finding parametric answers.

3.2 Understanding when a model chooses contextual knowledge versus parametric knowledge

3.2.1 Model Selection

In order to get a general understanding of large language models with added context, we test the queries generated in Section 3.1 into four models of different types and sizes, which are listed in Table 2.

	Seq2Seq Model	Decoder-Only Model
Smaller	Flan-T5-XL	Meta-Llama-3.1-8B-Instruct
Larger	Flan-T5-XXL	Meta-Llama-3.1-70B-Instruct

Table 2: The four large language models chosen for this research.

Both Sequence-to-Sequence models are based on T5 models (Raffel et al. 2020), which employ an encoder-decoder architecture: while an encoder processed the input sequence into a context vector, and an decoder generates an input sequence from this vector. The Flan-T5 models are fine-tuned to follow instructions, and have improved zero-shot performance compared to the original T5 models (Chung et al. 2022).

Flan-T5-XL contains approximately 3 billion parameters, and is considerably bigger than the base Flan-T5 model, which should improve the accuracy of its parametric answers.

Flan-T5-XXL contains 11 billion parameters, so it should have higher accuracy on the parametric answers as the XL model. However, how the higher amount of parameters

will affect the experiments that we are running is still unknown.

Unlike Seq2Seq models, Decoder-only models focus on the generation of text based on the previous tokens. In a sense, given a sequence of tokens they solve the problem of predicting the following token, repeating sequentially until some final token is found.

These architectures leverages autoregressive attention (Vaswani et al. 2017), where each token attends to its preceding tokens, maintaining the temporal order of the sequence. This approach allows them to generate coherent and contextually relevant text by sampling from this learned distribution, while also capturing long-range dependencies and complex patterns in language.

The Llama models (Dubey et al. 2024) use this architecture and fine-tune it to tasks of instruction-following, and are specially adept at complex prompts.

The Decoder-only model Meta-Llama-3.1-8B-Instruct has 8 billion parameters, while Meta-Llama-3.1-70B-Instruct has 70 billion. Meta provides an even larger model, Meta-Llama-3.1-405B-Instruct, that is too large to easily experiment with. However, we expect the difference between this model and the 70B model to be roughly the same as the difference between the 70B and 8B models.

The properties of the models are summarised in Table 3.

Model	Type	Developer	Parameters	Context
Flan-T5-XL	Seq2Seq	Google Brain	3 Billion	512 Tokens
Flan-T5-XXL	Seq2Seq	Google Brain	11 Billion	512 Tokens
Meta-Llama-3.1-8B-Instruct	Decoder-Only	Meta AI	8 Billion	128k Tokens
Meta-Llama-3.1-70B-Instruct	Decoder-Only	Meta AI	70 Billion	128k Tokens

Table 3: Model cards of the large language models used in this research.

3.2.2 What type of answer does each model select for each question?

The first step to understanding the knowledge grounding of large language models is to create queries that contain counterparametric data as part of the context. By comparing the result to the existing answers it becomes trivial to understand whether an answer came from the model's memory, the queries' context, or neither of these.

Following the approach of Yu et al., for every query we randomly sample from the set of answers of the same base question for answers that are different to the parametric answer which is given by the original query. An example of this shuffling is in Table 5.

Later, we add this *counterparametric answer* to the context, to form a new query and query the same model again; this is exemplified in Table 4.

To ensure that the results are simple to interpret and minimise the effect of randomness, once we select the queries we follow the example of Hsia et al. and use Greedy Decoding to find the answer. While beam search with a short beam width tends to produce more

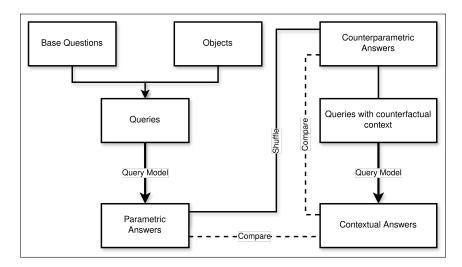


Figure 3: Example diagram of steps used to calculate the two sets of answers, *parametric* and *contextual*, and to compare them to answer the question in this objective. Many of the terms in this diagram are explained in the Glossary.

accurate results for long answers (Sutskever et al. 2014, Wu et al. 2016) and there are many other sampling methods that produce better results (Holtzman et al. 2020), this is likely to not have an effect on experiments that result in shorter answers (Raffel et al. 2020).

We compare the parametric answer to the previous values to come to one of three cases:

Parametric answers are equal to the answer given by the model when queried without context. This answer would come from the parametric memory of the model, and could potentially include hallucinations not fixed by RAG.

Contextual answers are equal to the context given in the query.

Other answers are neither of these, and this answer comes from a mis-interpretation of the input by the model or from some other source.

To minimise the amount of problems caused by large language models generating extra information, we define two strings to be equal by removing all text after a period or an <EOS> token, removing punctuation and stop words, and finding whether one is a subsequence of another.

This approach to compare strings is not enough, and understanding whether two answers are identical is an ongoing problem. This is explained in the Future Work section in Section 6.1.1.

The approach to finding out the source of knowledge of each query is specified in Figure 3.

Question with counterparametric context	Model Answer	Category
Context: [the nearest major body of water to Windhoek is the Rio de la Plata] Q: What is the nearest major body of water to Windhoek? A: The nearest major body of water to Windhoek is	the Atlantic Ocean	Parametric
Context: [the date of birth of Che Guevara is 965 AD]. Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is	965 AD	Contextual
Context: [Rome is in Georgia] Q: What country is Rome in? A: Rome is in	the United States	Other

Table 4: Example for results with **Parametric**, **Contextual**, and **Other** values. Note that, in the third query, the model is interpreting the question as asking about Rome in the US State of Georgia, rather than the country of Georgia.

Base Question	Object	Parametric Answer	Counterparametric Answer	Question with Counterparametric Context
	Che Guevara	June 14, 1928	965 AD	Context: [the date of birth of Che Guevara is 965 AD]. Q: What is the date of birth of Che Guevara? A: The date of birth of Che Guevara is
Q: What is the date of birth of {person}? A: The date of birth of {person} is	Ibn al-Haytham	965 AD	June 14, 1928	Context: [the date of birth of Ibn al-Haytham is June 14, 1928]. Q: What is the date of birth of Ibn al-Haytham? A: The date of birth of Ibn al-Haytham is
	W.E.B Du Bois F	ebruary 23, 1868	3 June 14, 1928	Context: [the date of birth of W.E.B Du Bois is June 14, 1928]. Q: What is the date of birth of W.E.B Du Bois? A: The date of birth of W.E.B Du Bois is
Q: What country	Cairo	Egypt	India	Context: [Cairo is in India]. Q: What country is Cairo in? A: Cairo is in
is {city} in? A: {city} is in	Mumbai	India	Egypt	<pre>Context: [Mumbai is in Egypt]. Q: What country is Mumbai in? A: Mumbai is in</pre>

Table 5: Using the same question format allows us to repurpose previous parametric answers as counterparametric ones.

3.3 Studying the Role of Perplexity Scores of the Provided Answers

3.3.1 Perplexity Score

The Perplexity score of an answer is normally used to measure the inverse of the certainty that the model has of a particular answer (Brown et al. 2020, Borgeaud et al. 2022). In a sense, it's the "surprise" of a model that a certain answer is correct.

We can define the probability of a model choosing a token x_n with context x_1, \ldots, x_{n-1} from a query Q by calculating the softmax value of all the logits for the possible words for this token.

The probabilities of the tokens if an answer can be accumulated to calculate the negative log-likelihood NLL, which is used to calculate the perplexity PPL using the formulas from Equations (1) and (2).

$$NLL(x_1, ..., x_n \mid Q) = -\frac{1}{n} \sum_{i=1}^n \log_2 P(x_i \mid Q, x_1, ..., x_{i-1})$$
 (1)

$$PPL(x_1, ..., x_n \mid Q) = 2^{NLL(x_1, ..., x_n \mid Q)}$$
(2)

3.3.2 Perplexity of the parametric answer with counterparametric context and vice-versa

Note that the token x_n does not necessarily have to be the result of applying the query x_1, \ldots, x_{n-1} to a model.

Therefore, it becomes necessary to use teacher-forcing (Lamb et al. 2016) to feed some answer to the model regardless of what's the answer to this particular query. This allows us to calculate the perplexity scores of the parametric answers for both the regular query and the one with counterparametric context, and the perplexity scores of the contextual answers for these two queries.

For a given parametric answer p_1, \ldots, p_n and randomly sampled counterparametric answer q_1, \ldots, q_m , a query without context Q, and a query with this counterparametric context Q' we can calculate four different perplexity scores as shown in Table 6.

Since the parametric answer is by definition the response of the model to the regular query, $P_0 \leq P_1$. In fact, the perplexity of the parametric value is lower than the perplexity of any other answer on query Q.

Figure 4 contains an example of the calculation of the perplexity values for a particular query.

		Tokens					
		Parametric p	Counterparametric q				
ext	Base Query	$P_0 = \mathrm{PPL}\left(p_1, \dots, p_n \mid Q\right)$	$P_1 = \operatorname{PPL}(q_1, \dots, q_m \mid Q)$				
Context	Counterparametric Context	$P_2 = \operatorname{PPL}(p_1, \dots, p_n \mid Q')$	$P_3 = \operatorname{PPL}(q_1, \dots, q_m \mid Q')$				

Table 6: Four different perplexity values: one for each set of tokens, and one for each query context.

3.3.3 Predicting whether an answer came from memory or from context

One question remains: if the response of the query with counterparametric context Q' is a certain answer x_1, \ldots, x_n , how can we predict whether this answer is came from the model's memory p or from the given context q without requiring an extra query?

We propose investigating the value of the perplexity $PPL(x_1, ..., x_n \mid Q')$ and comparing it to the distribution of perplexities on the answers with added parametric context P_2 and P_3 . For simplicity reasons, we are obviating the case when the preferred answer is neither of these; instead, we focus on whether the parametric or counterparametric answer are more likely.*

^{*}TODO: Maybe include a KDE or a K-S test here.

$P\left(p_i \mid Q', p_1, \dots, p_{i-1}\right)$							
0.94	4e-05	0.87	0.93	0.06	3		
0.92	0.26	0.04	0.61	0.98	0.72		
0.49	0.59	0.90					

$$-\frac{1}{n}\sum_{i=1}^{n}\log_2 P\left(p_i \mid Q', p_1, \dots, p_{i-1}\right) = 2.0566$$

 $\mathrm{NLL}\left(p_1,\ldots,p_n\mid Q'\right)$

$$P_2 = PPL(p_1, \dots, p_n \mid Q')$$

$$P_2 = 2^{NLL(q_1, \dots, q_m \mid Q')} = 4.1599$$

Query with Counterparametric Context Q'

[Context: The Son of Man is housed in in the refectory of the Convent of Santa Maria delle Grazie in Milan, Italy]

Q: Where is The Son of Man primarily housed?

A: The Son of Man is currently in

Counterparametric Answer Tokens q_1, \dots, q_m										
the	ref	ect	ory	of	t	he	Co	n	vent	
of	Santa	М	laria	del:	le	G	raz	i€		

$P\left(q_i \mid Q', q_1, \dots, q_{i-1}\right)$									
	0.94	0.96	0.99	1.00	0.98	0.99	0.99	1.00	
	0.99	0.99	0.99	0.99	0.99	0.99			
	0.96	0.99	0.98	0.99					

NLL
$$(q_1, ..., q_m \mid Q')$$

$$-\frac{1}{n} \sum_{i=1}^m \log_2 P(q_i \mid Q', q_1, ..., q_{i-1}) = 0.0154$$

$$P_3 = \text{PPL}(q_1, \dots, q_m \mid Q')$$

$$P_3 = 2^{\text{NLL}}(q_1, \dots, q_m \mid Q') = 1.0107$$

 $P_2 > P_3$ \Longrightarrow Contextual

Figure 4: Example of perplexity calculation for the parametric and counterparametric answers in a query with the counterparametric context. Note that, due to teacher forcing, the calculation finds the probability of the next token p_i given the previous tokens of the searched answer p_1, \ldots, p_{i-1} rather than given the most likely tokens. For example, once we feed the string "National Gallery of Canada in", the probability of the next token being "Ottawa" is very high.

4 Results

4.1 Creating a representative dataset of questions

We manually create a set of 4760 questions using the method explained in Section 3.1.

In order to be able to reuse objects for different questions, we separated the questions and objects in 9 different categories.

- 1. **Person** Historical people living from early antiquity to the present day from all around the globe. The questions have short, unambiguous answers, such as date of birth or most famous invention.
- 2. **City** Cities from all over the globe. Questions may include population, founding date, notable landmarks, or geographical features.
- 3. **Principle** Scientific principles, discovered from the 16th century forward. Questions about their discovery, use, and others.
- 4. **Element** Elements from the periodic table. Questions may cover discovery, atomic number, chemical properties, or common uses.
- 5. **Book** Literary works from various genres, time periods, and cultures. Questions may involve authors, publication dates, plot summaries, or literary significance.
- 6. **Painting** Famous artworks from different art movements and periods. Questions may cover artists, creation dates, styles, or current locations.
- 7. **Historical Event** Significant occurrences that shaped world history, from ancient times to the modern era. Questions may involve dates, key figures, causes, or consequences.
- 8. **Building** Notable structures from around the world, including ancient monuments, modern skyscrapers, and architectural wonders. Questions may cover location, architect, construction date, or architectural style.
- 9. **Composition** Musical works from various genres and time periods. Questions may involve composers, premiere dates, musical style, or cultural significance.

Each one of these categories has a number of questions that are assigned one of the objects, enhancing the done by Yu et al..

The full list of base questions and objects for all categories can be found in Appendix A. The total amount of these and composition of the 4760 questions can be found in Table 7.

Category	Base Questions	Objects	Total Questions
Person	17	57	969
City	17	70	1190
Principle	5	37	185
Element	15	43	645
Book	11	49	539
Painting	12	44	528
Historical Event	4	64	256
Building	9	22	198
Composition	10	25	250
Total	100	411	4760

Table 7: The amount of base questions, objects, and the total amount of questions in each category on the final dataset.

4.2 When does a model choose the provided context knowledge over its inherent knowledge?

The results of running the queries created in Section 3.1 with added counterparametric context on each of the four models the four models can be found in Table 8 and Figure 5.

Model	Parametric	Contextual	Other
llama-3.1-8B	745	3662	353
llama-3.1-70B	1070	3303	387
flan-t5-xl	248	4284	228
flan-t5-xxl	242	4304	214

Table 8: Results when running all entries on a decoder-only model.

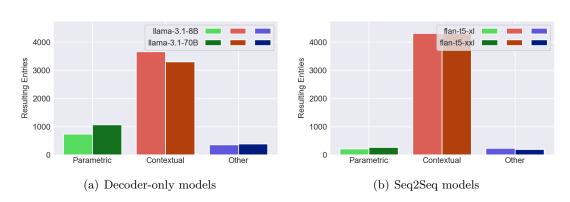


Figure 5: Results by type depending on which model; these are the same results as Table 8.

As hypothesised in Section 1.3.2, there are vast differences on how the models of different types and sizes act when presented with a context that contradicts their knowledge. This is investigated further in Section 5.

A similar pattern emerges in most (but not all) of the categories, which can be seen in Tables 9 and 10 and Figures 6 and 7.

	llama-3.1-8B			llama-3.1-70B		
	Parametric	Contextual	Other	Parametric	Contextual	Other
Person	40	833	96	209	614	146
City	117	1007	66	166	966	58
Principle	44	118	23	44	117	24
Element	218	385	42	275	347	23
Book	135	344	60	154	318	67
Painting	47	458	23	49	445	34
Historical Event	81	154	21	117	118	21
Building	27	163	8	31	159	8
Composition	36	200	14	25	219	6

Table 9: Results for running each one of the 10 categories separately on the Decoder-only models.

	flan-t5-xl			flan-t5-xxl		
	Parametric	Contextual	Other	Parametric	Contextual	Other
Person	32	900	37	23	890	56
City	120	1030	40	78	1093	19
Principle	13	164	8	9	168	8
Element	6	637	2	102	515	28
Book	26	488	25	18	457	64
Painting	26	446	56	4	498	26
Historical Event	11	217	28	1	254	1
Building	14	174	10	0	189	9
Composition	0	228	22	7	240	3

Table 10: Results for running each one of the 10 categories separately on the Seq2Seq models.

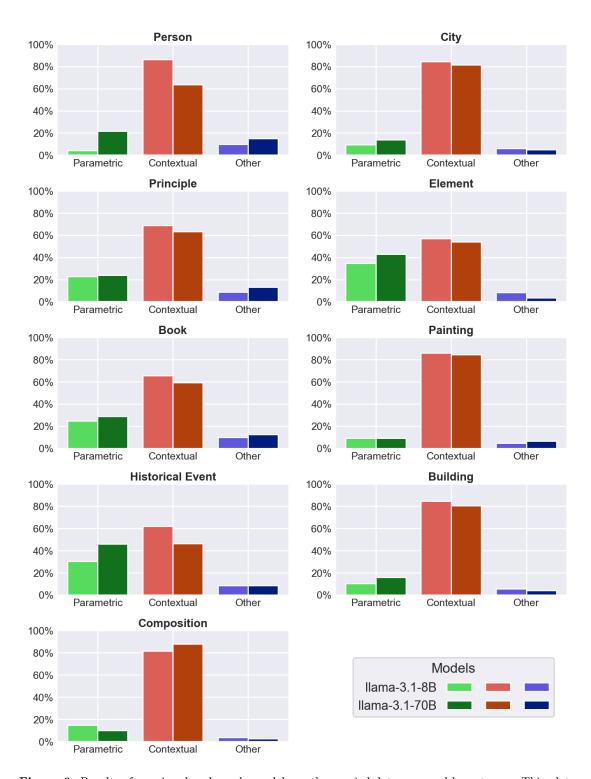


Figure 6: Results of running decoder-only models on the queried data, grouped by category. This plots the information shown in Table 9.

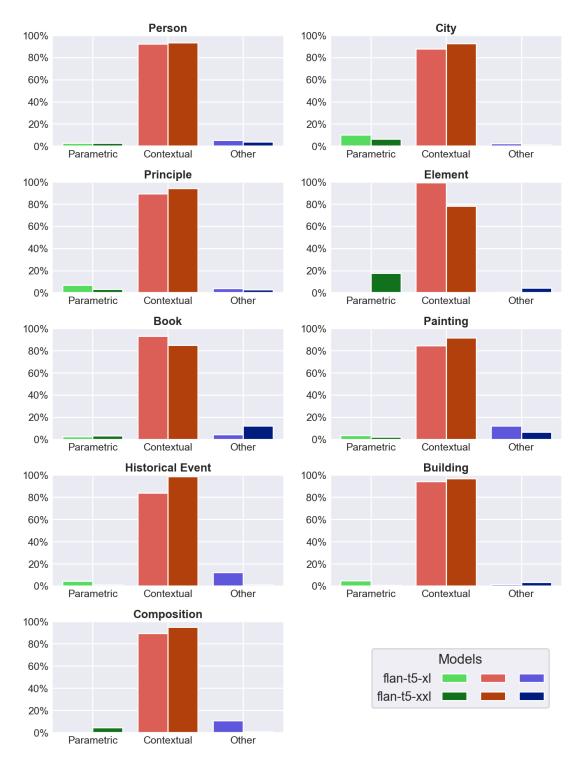


Figure 7: Results of running Seq2Seq models on the queried data, grouped by category. This plots the information shown in Table 10.

4.3 Can we use the perplexity score of an answer to predict whether it came from inherent or contextual knowledge?

We calculate the resulting perplexity of each query as explained in Section 3.3. These are accumulated in three distributions, depending on answer type, which are summarised in Tables 11 and 12 and Figure 8.

	llama-	3.1-8B	llama-3.1-70B		
	Parametric	Parametric Contextual		Contextual	
count	313	4447	383	4377	
mean	1.67	1.20	1.56	1.22	
$\operatorname{\mathbf{std}}$	0.79	0.32	0.46	0.31	
25 %	1.28	1.05	1.28	1.06	
50 %	1.43	1.10	1.43	1.12	
75%	1.78	1.23	1.68	1.25	

Table 11: Distribution of perplexity values for Decoder-only models

	flan-	T5-XL	flan-T5-XXL		
	Parametric Contextual		Parametric	Contextual	
count	651	4109	507	4253	
mean	6.38	1.56	11.75	1.27	
$\operatorname{\mathbf{std}}$	9.07	0.56	18.47	0.75	
25 %	3.21	1.19	2.41	1.02	
50 %	4.71	1.39	3.89	1.09	
75%	7.14	1.71	7.70	1.24	

Table 12: Distribution of perplexity values for Seq2Seq models

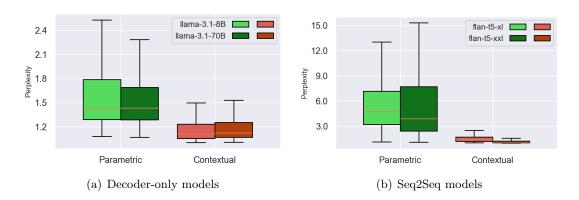


Figure 8: Perplexity distribution according to model type and size. These represent the same distributions as Tables 11 and 12.

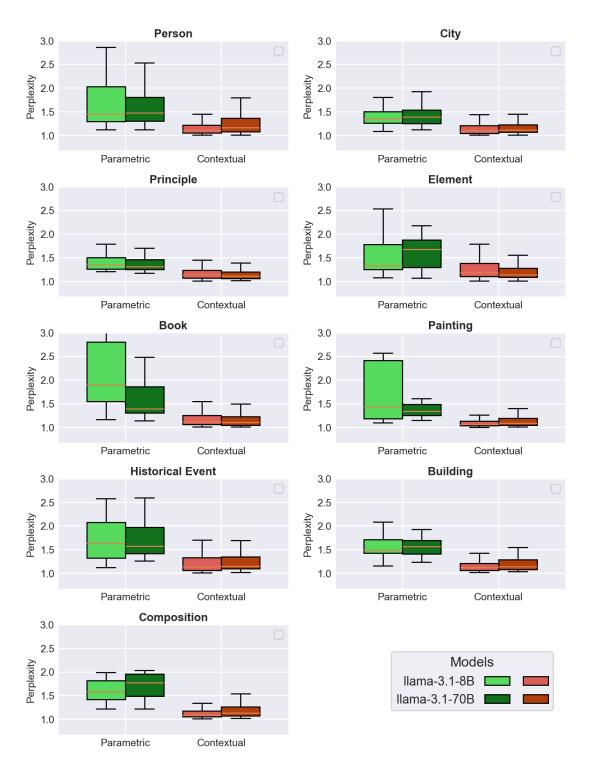


Figure 9: Box plots representing the distribution of the perplexities when running both Llama models, grouped by category.

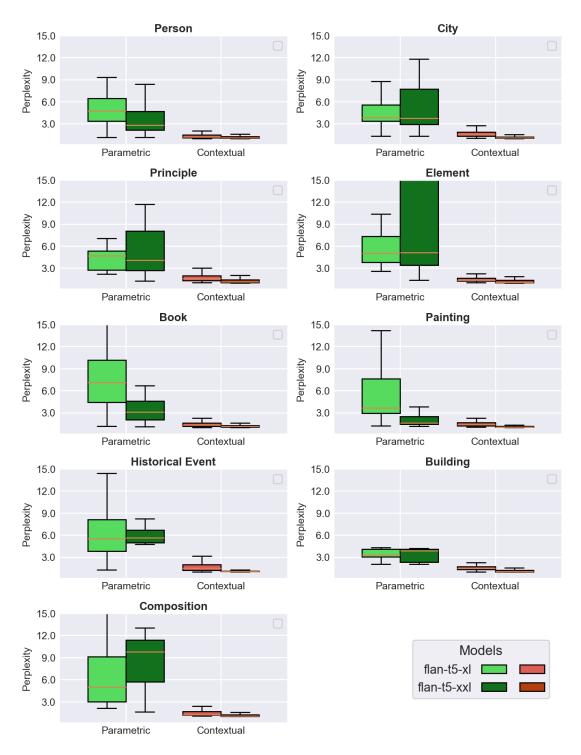


Figure 10: Box plots representing the distribution of the perplexities when running both Flan-T5 models, grouped by category.

5 Discussion

- 5.1 Model type and memorised knowledge
- 5.2 Model size and memorised knowledge
- 5.3 Differences in perplexity scores for larger and smaller models
- 5.3.1 Can we use this to predict from where an answer came from?
- 5.4 Differences in distributions for different categories and questions.

6 Evaluations, Reflections, and Conclusions

6.1 Future Work

6.1.1 Better Categorisation of the Answers

To test whether two answers are equal and to know whether an answer came from parametric or contextual knowledge, the code in this thesis checks for string equality among after removing a few stop simple words such as 'the'.

This solution might not be enough, and some answers classified as **Other** should have been classifier as something else. Table 13 provides some examples of answers where this is the case.

Query	Parametric Answer	Query Answer	Comparison	Expected
[Context: The primary leader associated with The Construction of Hadrian's Wall was Napoleon Bonaparte] Q: Who was the primary leader associated with The Construction of Hadrian's Wall? A: The primary leader associated with The Construction of Hadrian's Wall was	Emperor Hadrian	Hadrian, the Roman Emperor	Other	Parametric
[Context: Che Guevara was born in Kensington, London, England] Q: In what city was Che Guevara born? A: Che Guevara was born in	Rosario, Argentina	London	Other	Contextual

Table 13: Example of incorrectly-categorised answers. These were categorised as "Other", since their answer strings are different from both parametric and contextual answers. However, a closer look reveals that this is just either answer with a slight formatting difference.

A more complete solution might include using another LLM to compare whether two answers are truly equal.

6.1.2 Knowledge Grounding in Retrieval-Augmented LMs

This thesis was originally based on a preprint, "Knowledge Grounding in Retrieval-Augmented LMs: An Empirical Study" (Whitehouse et al. 2023), and contains work towards understanding how large language models retrieve data which can ultimately help prevent hallucinations.

We plan to continue this work and complete the paper created by the preprint by running the methods outlined on this thesis on retrieval-augmented LMs such as ATLAS (Izacard

et al. 2022) and Retro (Borgeaud et al. 2022) and creating a full evaluation framework that specifically focuses on their grounding. A well-grounded model should demonstrate the capability to adapt its generation based on the provided context, specially in cases like the ones experimented in this thesis when the context contradicts the model's parametric memorisation.

6.1.3 Further Memory Locator Prediction

The results of Section 4.3 show a clear difference in perplexity value between answers that come from the parametric memory of a model and those that come from a context.

This could be used to create a predictor where, given a certain answered query, it could give you a probability of the source the model used for this answer by using the perplexity of the answer and comparing against the distribution of perplexities for this model on similar questions.

In RAG-enhanced models, where the RAG context might contradict the parametric knowledge of a model, this might prevent hallucinations.

6.1.4 Fine-tuning a LLM for a RAG Context

Existing retrieval-augmented LMs, such as ATLAS and RETRO, are trained on existing models along with an index. In the fast-moving world of large language models, this might not be ideal: the generator part of models is based on T5, a model created in 2019. Meanwhile, between the time I started writing this thesis and this moment Meta launched a new Llama model.

The current dataset and experiments might be useful for being able to fine-tune a modern model to prefer the context generated by RAG when it contradicts its parametric knowledge. This might improve retrieval-augmented models, and make it easier to use them with newer models.

Glossary

Base Questions

Objects

Queries

Parametric Answers

Counterparamteric answers

 ${\bf Queries\ with\ counterfactual/counterparametric\ context}$

Contextual Answer

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Appendices

A Questions and objects used to form the queries

```
What is the date of birth of {person}? The date of birth of {person} is In what city was {person} born? {person} was born in What is the date of death of {person}? The date of death of {person} is
What is the date of death of {person}? The date of death of {person} is
What is the primary profession of {person}? The primary profession of {person} is
What is {person} primarily known for? {person} is primarily known for
What's the main nationality of {person}? {person} is
What educational institution did {person} attend? {person} attended
What was the native language of {person}? The native language of {person} was
Who was {person}'s most influential mentor? The most influential mentor of {person} was
What was {person}'s religious affiliation? The religious affiliation of {person} was
What was {person}'s primary field of study? The primary field of study of {person} was
What was {person}'s most famous work or invention? The most famous work or invention of {person} was
What historical period did {person} live in? {person} lived during the
What was {person}'s family's social class? {person}'s family belonged to the
What was {person}'s political ideology? The political ideology of {person} was
What was {person}'s preferred artistic or scientific medium? The preferred medium of {person} was
What was {person}'s cultural background? The cultural background of {person} was
 What country is {city} in? {city} is in What's the highest administrative subdivision {city} is part of? {city} is part of
What's the highest administrative subdivision {city} is part of? {city} is part of
In what year was {city} founded? {city} was founded in
What major river is nearest to {city}? The nearest major river to {city} is
What is the time zone of {city}? The time zone of {city} is
What is the current population of {city}? The current population of {city} is
What is the altitude of {city} above sea level? {city} is at an altitude of
What is the primary language spoken in {city}? The primary language spoken in {city} is
What is the predominant architectural style in {city}? The predominant architectural style in {city} is
What is the main economic industry of {city}? The main economic industry of {city} is
What is the average annual temperature in {city}? The average annual temperature in {city} is
What is the nearest major body of water to {city}? The nearest major body of water to {city} is
What is the most famous landmark in {city}? The most famous landmark in {city} is
What is the primary mode of public transportation in {city}? The primary mode of public transportation in {city} is
                          {city} is
 What is the name of the airport serving {city}? The airport serving {city} is
What is the sister city of {city}? The sister city of {city} is
What is the traditional cuisine {city} is known for? The traditional cuisine {city} is known for is
  Who is credited with the discovery of {principle}? {principle} was discovered by
 Which scientific discipline encompasses {principle}? {principle} is encompassed by What is the primary application of {principle}? The primary application of {principle} is In which year was {principle} first formulated? {principle} was first formulated in What is the SI unit most commonly associated with {principle}? The SI unit most commonly associated with
  What's the chemical formula for {element}? The chemical formula for {element} is
What's the chemical formula for {element}? The chemical formula for {element} is

When was {element} first isolated? {element} was first isolated in

What's the atomic number of {element}? The atomic number of {element} is

What is the melting point of {element}? The melting point of {element} is

In which group of the periodic table is {element} found? {element} is found in group

What's the standard atomic weight of {element}? The standard atomic weight of {element} is

What's the electron configuration of {element}? The electron configuration of {element} is

What's the most common oxidation state of {element}? The most common oxidation state of {element} is

What's the crystal structure of {element} at room temperature? The crystal structure of {element} at room
What's the crystal structure of {element} at room temperature: Int Clystal School temperature is
What's the primary isotope of {element}? The primary isotope of {element} is
What's the electronegativity value of {element}? The electronegativity value of {element} is
What's the ionization energy of {element}? The ionization energy of {element} is
What's the atomic radius of {element}? The atomic radius of {element} is
What's the boiling point of {element}? The boiling point of {element} is
In which period of the periodic table is {element} located? {element} is located in period
 What genre does {book} belong to? The genre of {book} is
Who's the author of {book}? {book} was written by
In what year was {book} first published? {book} was first published in
How many pages are in the original publication of {book}? The original publication of {book} has
What is the name of the main protagonist in {book}? The main protagonist in {book} is
 What is the original language of {book}? The original language of {book} is Who is the original publisher of {book}? The publisher of {book} is What is the highest award {book} won? The highest award won by {book} is What is the opening line of {book}? The opening line of {book} is How many chapters are in {book}? {book} has How many pages are in {book}? {book} has
 Who painted {painting}? {painting} was painted by
```

```
What artistic movement does {painting} belong to? {painting} belong to What artistic movement does {painting} belong to? {painting} was created with Where is {painting} primarily housed? {painting}? {painting} was created with Where is {painting} primarily housed? {painting}? The dimensions of {painting}? The dimensions of {painting} are In which museum was {painting} first exhibited? {painting} was first exhibited in What is the dominant color in {painting}? The dominant color in {painting} is Who commissioned {painting}? Tpainting} was commissioned by What is the estimated value of {painting}? The subject matter of {painting} is In which country was {painting} created? {painting} was created in What year did {historical_event} happen? {historical_event} happened in the year Who was the primary leader associated with {historical_event} was What was the duration of {historical_event}? {historical_event} lasted for In which country did {historical_event} primarily take place? {historical_event} primarily took place in What is the height of {building}? The height of {building} was In which year was {building} completed? {building} was completed in In which city is {building} completed? {building} was completed in In which city is {building} hozered? {building} is located in What architectural style is {building}? The architectural style of {building} is How may floors does {building} hozered? {building}? The primary construction material of {building}? The primary construction material of {building}? The primary construction material of {building}? The unsured in the total floor area of {building}? The miscal genre of {composition} was first performed in What is the total floor area of {building}? The opus number of {composition} is What is the opus number of {composition}? The musical genre of {composition} is What is the opus number of {composition}? The duration of {composition} was first performed in What is the opus number of {composition}? The duration of {composition} was premiered in What is the duration
```

Listing 2: All base questions used in this work. Each one of these will get combined with data from Listing 2 as detailed in Section 3.1.

```
Ada Lovelace, person
Alan Turing, person
Albert Einstein, person
Alexander Fleming, person
Aristotle, per
Billie Jean King, person
Boyan Slat, person
Catherine the Great, person
Che Guevara, person
Cleopatra, person
Confucius, person
Ernest Rutherford, person
Florence Nightingale, person
Freddie Mercury, person
Frida Kahlo, person
Greta Thunberg, person
Harriet Tubman, person
Ibn al-Haytham, person
Isaac Newton, person
Isaac Newton, person
Karl Marx, person
Leonardo da Vinci, person
Mahatma Gandhi, person
Malala Yousafzai, person
Mansa Musa, person
Marie Curie, person
Martin Luther King Jr., person
Michelangelo, person
Mohandas Gandhi, person
Mozart, per
Muhammad Ali, person
Neil Armstrong, person
Nelson Mandela, person
Nikola Tesla, person
Pablo Picasso, person
Rosalind Franklin, person
Shirin Ebadi, person
Simon Bolivar, person
Srinivasa Ramanujan, person
Stephen Hawking, person
```

```
Sun Yat-sen, person
Virginia Woolf, person
Vladimir Lenin, person
Wangari Maathai, person
W.E.B. Du Bois, person
William Shakespeare, person
William Shakespeare, per Wu Zetian, person Yuri Gagarin, person Amelia Earhart, person Galileo Galilei, person Joan of Arc, person Lise Meitner, person Marcus Aurelius, person Maya Angelou, person Queen Nzinga, person Socrates, person Voltaire, person Alexandria, city Amsterdam, city
Amsterdam, city
Amsterdam, city
Antananarivo, city
Athens, city
Baghdad, city
 Berlin, city
Buenos Aires, city
Buenos Aires, c:
Bukhara, city
Cairo, city
Cape Town, city
Cartagena, city
Chicago, city
Cusco, city
Cuzco, city
Delhi, city
Dubrownik, city
 Dubrovnik, city
 Fez, city
Havana, city
 Istanbul, city
Jerusalem, city
 Kyoto, city
La Paz, city
La Paz,city
Lhasa,city
Lisbon,city
London,city
Luang Prabang,city
Mexico City,city
Montevideo,city
Moscow,city
Mumbai,city
Numbai,city
New York,city
 New York, city
Nur-Sultan, city
Nur-Sultan, city
Paris, city
Petra, city
Prague, city
Quebec City, city
Reykjavik, city
Rome, city
Sao Paulo, city
Sao Paulo, city
Sarajevo, city
Shanghai, city
Singapore, city
St. Petersburg, city
St. Petersburg, cit
Sydney, city
Tbilisi, city
Tenochtitlan, city
Timbuktu, city
Tokyo, city
Ulaanbaatar, city
Varanasi, city
 Venice, city
Vienna, city
Wellington, city
Windhoek, city
Windhoek, city
Xi'an, city
Yogyakarta, city
Zanzibar City, city
Addis Ababa, city
Bangkok, city
Dubai, city
Helsinki, city
Machu Picchu, city
```

```
Nairobi, city
Rio de Janeiro, city
Samarkand, city
 Yangon, city
Yanchimedes' Principle, principle
Bernoulli's Principle, principle
 Boyle's Law,principle
Cell Theory,principle
Conservation of Energy,principle
 DNA Replication, principle
 Electromagnetism, principle
Entropy, principle
Entropy, principle
Evolution by Natural Selection, principle
Evolution, principle
General Relativity, principle
Germ Theory of Disease, principle
Gravity, principle
Hardy-Weinberg Principle, principle
Heliocentrism, principle
Hubble's Law, principle
Kepler's Laws of Planetary Motion, principle
Le Chatelier's Principle, principle
Mendel's Laws of Inheritance, principle
Newton's Laws of Motion, principle
Pauli Exclusion Principle, principle
Periodic Law, principle
 Periodic Law, principle
Photosynthesis, principle
 Plate Tectonics, principle
Principle of Least Action, principle
 Principle of Least Action, principle
Quantum Mechanics, principle
Relativity, principle
Superconductivity, principle
Thermodynamics, principle
Uncertainty Principle, principle
Avogadro's Law, principle
 Coulomb's Law, principle
Faraday's Laws of Electrolysis, principle
 Heisenberg Uncertainty Principle, principle Ohm's Law, principle
 Schrä¶dinger Equation, principle
Special Relativity, principle
 Aluminum, element
Barium, element
 Bismuth, element Bromine, element
 Calcium, element
Carbon, element
Chlorine, element
Chromium, element
 Copper, element Gold, element
 Helium . element
 Hydrogen, element
 Iodine, element
 Iron, element
 Lead, element
 Lithium, element
 Magnesium, element
Manganese, element
Mercury, element
Neon, element
Nitrogen, element
 Oxygen, element
Phosphorus, element
Plutonium, element
 Potassium, element
Radon, element
Silicon, element
Silver, element
Sodium, element
 Sulfur, element
Thorium, element
 Tin, element
Titanium, element
 Uranium .element
 Zinc, element
 Argon, element
Boron, element
 Cobalt, element Fluorine, element
 Gallium, element Krypton, element
```

```
Nickel, element
 Xenon, element
 1984, bo
 Anna Karenina, book
Beloved, book
Brave New World, book
Catch-22, book
 Crime and Punishment, book
Don Quixote, book
Fahrenheit 451, book
 Frankenstein, b
Jane Eyre, book
Midnight's Children, book
Moby-Dick, book
One Flew Over the Cuckoo's Nest, book
 One Hundred Years of Solitude, book
 Pride and Prejudice, book
 Slaughterhouse-Five, book
The Alchemist, bo
The Art of War, b
The Book Thief, b
The Brothers Karamazov, book
The Catcher in the Rye, book
The Chronicles of Narnia, book
The Color Purple, book
The Count of Monte Cristo, book
The Count of Monte Cristo, book
The Grapes of Wrath, book
The Handmaid's Tale, book
The Hitchhiker's Guide to the Galaxy, book
The Hobbit, book
The Hunger Games, book
 The Kite Runner,
The Little Prince, book
The Lord of the Rings, book
The Metamorphosis, book
The Name of the Rose, book
The Odyssey, book
The Picture of Dorian Gray, book
The Pillars of the Earth, book
The Stranger, book
The Sun Also Rises, bo
The Wind-Up Bird Chronicle, book
To Kill a Mockingbird, book
Ulysses, book
War and Peace, bo
War and Peace, book
Wuthering Heights, book
The Iliad, book
The Tale of Genji, book
Things Fall Apart, book
To the Lighthouse, book
American Gothic, painting
Christina's World, painting
Girl with a Pearl Earring, painting
Guernica, painting
Les Demoiselles d'Avignon, painting
Les Demoiselles d'Avignon, painting
Liberty Leading the People, painting
Mona Lisa, painting
School of Athens, painting
Starry Night, painting
The Absinthe Drinker, painting
The Anatomy Lesson of Dr. Nicolaes Tulp, painting
The Arnolfini Portrait, painting
The Astronomer, painting
The Birth of Venus, painting
 The Calling of Saint Matthew, painting
The Carling of Saint matthew, painting
The Card Players, painting
The Death of Marat, painting
The Fighting Temeraire, painting
The Garden of Earthly Delights, painting
The Gross Clinic, painting
The Hay Wain, painting The Kiss, painting
The Kiss, painting
The Last Supper, painting
The Nighthawks, painting
The Night Watch, painting
The Ninth Wave, painting
The Persistence of Memory, painting
The Potato Eaters, painting
The Raft of the Medusa, painting
The Scream, painting
The Sleeping Gypsy, painting
The Son of Man, painting
```

```
The Swing, painting
The Third of May 1808, painting
The Tower of Babel, painting
The Treachery of Images, painting
The Triumph of Galatea, painting
The Wanderer above the Sea of Fog, painting
Water Lilies, painting
The Creation of Adam, painting
The Girl with a Pearl Earling, painting
The Great Wave off Kanagawa, painting
The Thinker, painting
Venus de Milo, painting
Decimalisation in the UK, historical_event
Queen Elizabeth II's Platinum Jubilee, historical_event Queen Victoria's Coronation, historical_event
The Act of Union between England and Scotland, historical_event
The Battle of Adrianople, historical_event
The Battle of Adwa, historical_event
The Battle of Agincourt, historical_eve
The Battle of Hastings, historical_event
The Battle of Sekigahara, historical_event
The Battle of Teutoburg Forest, historical_event
The Battle of the Milvian Bridge, historical_event
The Battle of the milvian bridge, mistorical_event
The Battle of Waterloo, historical_event
The Brexit Referendum, historical_event
The Codification of Roman Law by Justinian, historical_event
The Construction of Hadrian's Wall, historical_event
The Construction of the Great Pyramid of Giza, historical_event
The Conversion of Constantine, historical_event
The Council of Chalcedon, historical_event
The Council of Chalcedon, historical_event
The Crisis of the Third Century, historical_event
The Defeat of the Spanish Armada, historical_event
The Discovery of the Americas by Columbus, historical_event
The Dissolution of the Soviet Union, historical_event
The Division of the Roman Empire, historical_event
The Dunkirk Evacuation, historical_event
The Edit of Caracalla, historical_event
The Edict of Caracalla, historical_event
The Fall of Constantinople, historical_event
The Fall of the Aztec Empire, historical_event
The Fall of the Western Roman Empire, historical_event
The First Circumnavigation of the Earth, historical_event
The First Council of Nicaea, historical_event
The First Crusade, historical event
The Founding of Constantinople, historical_event
The Founding of Rome, historical_event
The Founding of the British Broadcasting Corporation, historical_event
The Founding of the League of Nations, historical_event
The French Revolution, historical_event
The Glorious Revolution, historical_event
The Gothic War in Italy, historical_event
The Great Fire of London, historical_event
The Indian Independence Act, historical_event
The Industrial Revolution, historical_event
The London 7/7 Bombings, historical_event
The Meiji Restoration, historical_event
The Plague of Justinian, historical_event
The Reforms of Diocletian, historical_even
        Reunification of the Empire by Aurelian, historical_event
The Sack of Rome by Alaric, historical_event
The Sack of Rome by the Vandals, historical_event
The Signing of the Good Friday Agreement, historical_event
The Signing of the Magna Carta, historical_event
The Signing of the Magna Carta, historical_event
The Treaty of Westphalia, historical_event
The UK Abolition of the Slave Trade Act, historical_event
The Unification of Italy, historical
The Wedding of Prince Charles and Lady Diana, historical_event
The Year of the Four Emperors, historical_event
The American Revolution, historical_event
The Black Death, historical_event
The Cuban Missile Crisis, historical_event
The Fall of the Berlin Wall, historical_event
The Moon Landing, historical_event
The Renaissance, historical_event
The Russian Revolution, historical_event
The Signing of the Declaration of Independence, historical_event
Angkor Wat, building
Buckingham Palace, building
Burj Khalifa, building
Chichen Itza, building
Chrysler Building, building
Colosseum, building
Eiffel Tower, building
```

```
Empire State Building, building
Forbidden City, building
Guggenheim Museum, building
Hagia Sophia, building
Hagia Sophia, building
Machu Picchu, building
Museuchwantein Castle, building
Petra, building
Petra, building
Petronas Towers, building
Petronas Towers, building
Potale Palace, building
Stans Towers, building
Stans Tower, building
Taj Mahal, building
Adagio for Strings, composition
Billie Jean, composition
Bohemian Hapsody, composition
Cannin Burana, composition
Cannin Burana, composition
Clair de Lune, composition
Clair de Lune, composition
Glair de Lune, composition
Glair de June, composition
Imagine, composition
Imagine, composition
Intel Mood, composition
Intel Mood, composition
Intel Mood, composition
Nbube (The Lion Sleeps Tonight), composition
Messun Dorma, composition
Nessun Dorma, composition
Raga Malkaune, composition
Rhapsody on a Theme of Paganini, composition
Symphony No. 5, composition
The Blue Danube, composition
The Blue Danube, composition
The Four Seasons, composition
The Blue Danube, composition
The Rate of Spring, composition
```

Listing 3: All objects which will be combined with the questions in Listing 1.

- B Full Results for Each Question
- C Grounder Usage and Documentation

D Source Code of the Experiments

The latest version of the source code, including the input data generated in Section 3.1, is available in https://github.com/mfixman/rag-thesis[†].

```
1 import warnings
  warnings.simplefilter(action = 'ignore', category = FutureWarning)
4 from argparse import ArgumentParser
  import csv
6 import logging
7 import random
8 import ipdb
9 import os
10 import sys
11 import wandb
12
13 from Models import Model_dict
14 from QuestionAnswerer import QuestionAnswerer
15
  from Utils import print_parametric_csv, LogTimeFilter, combine_questions
16
17 def parse_args():
       parser = ArgumentParser(
18
          description = 'Combines questions and data and optionally provides
19
       parametric data'
20
21
22
       parser.add_argument('--debug', action = 'store_true', help = 'Go to IPDB
       console on exception.')
       parser.add_argument('--lim-questions', type = int, help = 'Question limit')
23
       parser.add_argument('--device', choices = ['cpu', 'cuda'], default = 'cuda',
24
       help = 'Inference device')
       parser.add_argument('--models', type = str.lower, default = [], choices =
25
       Model_dict.keys(), nargs = '+', metavar = 'model', help = 'Which model or
       models to use for getting parametric data')
26
       parser.add_argument('--offline', action = 'store_true', help = 'Tell HF to
       run everything offline.')
       parser.add_argument('--rand', action = 'store_true', help = 'Seed randomly')
parser.add_argument('--max-batch-size', type = int, default = 120, help =
27
28
       Maximimum size of batches. All batches contain exactly the same question.')
29
30
       parser.add_argument('--per-model', action = 'store_true', help = 'Write one
       CSV per model in stdout.')
31
       parser.add_argument('--output-dir', help = 'Return one CSV per model, and
       save them to this directory.')
32
       parser.add_argument('--runs-per-question', type = int, default = 1, help =
33
       How many runs (with random counterfactuals) to do for each question.')
34
       parser.add_argument('base_questions_file', type = open, help = 'File with
       questions')
36
       parser.add_argument('things_file', type = open, help = 'File with things to
       combine')
37
38
       args = parser.parse_args()
39
40
       args.base_questions = [x.strip() for x in args.base_questions_file if any(not
       y.isspace() for y in x)]
```

[†]TODO: Move all of this to a new repo.

```
args.things = [{k: v for k, v in p.items()} for p in
41
       csv.DictReader(args.things_file)]
42
43
       del args.base_questions_file
44
       del args.things_file
45
46
       if args.per_model and args.output_dir:
47
           raise ValueError('Only one of --per-model and --output-dir can be
       specified.')
48
49
       return args
50
  def main(args):
51
52
       logging.getLogger('transformers').setLevel(logging.ERROR)
53
       logging.basicConfig(
           format='[%(asctime)s] %(message)s',
54
55
           level=logging.INFO,
56
           datefmt = ', ', Y - ', m - ', d ', H : ', M : ', S '
57
58
       logging.getLogger().addFilter(LogTimeFilter())
59
       if args.offline:
60
          os.environ['TRANSFORMERS_OFFLINE'] = '1'
61
       else:
62
63
           wandb.init(project = 'knowledge-grounder', config = args)
64
65
       logging.info('Getting questions')
66
       questions = combine_questions(args.base_questions, args.things,
       args.lim_questions)
67
68
       if args.output_dir:
69
           try:
70
               os.mkdir(args.output_dir)
           except FileExistsError:
71
72
               pass
73
       logging.info(f'About to answer {len(questions) * len(args.models) *
74
       args.runs_per_question * 2} questions in total.')
75
       answers = {}
76
       for model in args.models:
77
           if not args.rand:
               random.seed(0)
78
79
80
           qa = QuestionAnswerer(
81
               model,
82
               device = args.device,
83
               max_length = 20,
84
               max_batch_size = args.max_batch_size,
85
               runs_per_question = args.runs_per_question,
86
           )
87
           model_answers = qa.answerQueries(questions)
88
           del qa
89
90
           if args.output_dir:
               empty = lambda s: sum([x == '' for x in model_answers[s]])
91
92
               count = lambda s: sum([x == s for x in model_answers['comparison']])
93
               logging.info(f"{model}:\t{empty('parametric')} empty parametrics,
       {empty('counterfactual')} empty counterfactuals, {empty('contextual')} empty
       contextuals")
94
               logging.info(f"\t{count('Parametric')} parametrics,
       {count('Contextual')} contextual, {count('Other')} others")
95
```

```
model_filename = os.path.join(args.output_dir, model + '.csv')
97
                with open(model_filename, 'w') as out:
98
                    print_parametric_csv(out, model_answers)
99
100
            elif args.per_model:
101
                print_parametric_csv(sys.stdout, model_answers)
102
            else:
103
                answers |= model_answers
104
105
       if answers:
106
            logging.info('Writing CSV')
107
            print_parametric_csv(sys.stdout, answers)
108
109 if __name__ == '__main__':
110
       args = parse_args()
111
       if not args.debug:
112
           main(args)
113
        else:
114
            with ipdb.launch_ipdb_on_exception():
                main(args)
```

Listing 4: knowledge_grounder.py is the main entry point and contains mostly argument parsing and output printing.

```
1 import warnings
  warnings.simplefilter(action = 'ignore', category = FutureWarning)
4 import logging
5 import math
6 import torch
7 import typing
9 from Models import Model
10 from typing import Optional, Union, Any
11 from Utils import Question, sample_counterfactual_flips, chunk_questions
12
13 from collections import defaultdict
14 from transformers import BatchEncoding
15
16 FloatTensor = torch.Tensor
17 LongTensor = torch.Tensor
18 BoolTensor = torch.Tensor
19
20 # A QuestionAnswerer is the main class to answer queries with a given model.
21
  # Example Usage:
     qa = QuestionAnswerer('llama', device = 'cuda', max_length = 20,
      max_batch_size = 75)
      output = qa.answerQueries(Utils.combine_questions(base_questions, objects))
24 # The list of models can be found in 'Model_dict' in 'Models.py'.
25 class QuestionAnswerer:
26
      device: str
27
      max_length: int
28
      max_batch_size: int
29
      runs_per_question: int
30
      llm: Model
31
32
      def __init__(
33
           self,
34
           model: Union[str, Model],
35
           device: str = 'cpu',
36
           max_length: Optional[int] = None,
```

```
max_batch_size: Optional[int] = None,
38
           runs_per_question: Optional[int] = None,
39
      ):
40
           self.device = device
41
           self.max_length = max_length or 100
42
           self.max_batch_size = max_batch_size or 120
           self.runs_per_question = runs_per_question or 1
43
44
45
           if type(model) == str:
46
               model = Model.fromName(model, device = device)
47
48
           model = typing.cast(Model, model)
49
           self.llm = model
50
51
           # Generated list of stop tokens: period, newline, and various different
      end tokens.
           stop_tokens = {'.', '\n'}
           self.stop_token_ids = torch.tensor([
53
54
               for k, v in self.llm.tokenizer.get_vocab().items()
55
56
57
                   k in ['<start_of_turn>', '<end_of_turn>',
      self.llm.tokenizer.special_tokens_map['eos_token']] or
58
                   not stop_tokens.isdisjoint(self.llm.tokenizer.decode(v))
59
           ]).to(self.device)
60
61
      \mbox{\tt\#} Query data related to a list of questions, and return a dict with
       information about these runs.
62
      # Output elements:
63
      # parametric: Parametric answer, as a string.
64
         base_proba: Perplexity of parametric answer in base query.
65
         counterfactual: Randomly selected counterfactual answer.
66
       # base_cf_proba: Perplexity of counterfacutal answer in base query.
67
         contextual: Contextual answer, as a string.
68
         ctx_proba: Perplexity of contextual answer.
       # ctx_param_proba: Perplexity of parametric answer when running contextual
69
      query.
70
       # ctx_cf_proba: Perplexity of counterfactual answer when running contextual
      query.
      # comparison: Comparison between parametric and contextual answer. Where
71
      does this answer come from?
      # preference: Comparison between perplexity of paramertic and counterfactual
72
      answer on contextual query. Which one is the least surprising?
      def answerChunk(self, questions: list[Question]) -> dict[str, Any]:
73
           output: defaultdict[str, list[Any]] = defaultdict(lambda: [])
74
75
76
           base_tokens = self.tokenise([q.format(prompt = self.llm.prompt) for q in
      questions])
77
           parametric = self.generate(base_tokens)
78
79
           parametric_output = self.decode(parametric)
80
           base_proba_output = self.perplexity(base_tokens, parametric)
81
           for run in range(self.runs_per_question):
82
               run_output: dict[str, list[Any]] = dict(
83
                   parametric = parametric_output,
84
                   base_proba = base_proba_output,
85
86
87
               run_output['question'] = questions
88
               flips = sample_counterfactual_flips(questions,
      run_output['parametric'])
89
               counterfactual = parametric[flips]
```

```
run_output['counterfactual'] = self.decode(counterfactual)
91
92
                run_output['base_cf_proba'] = self.perplexity(base_tokens,
       counterfactual)
93
94
                run_output |= self.answerCounterfactuals(questions,
       run_output['counterfactual'], parametric, counterfactual)
95
96
                run_output['comparison'] = [
                    'Parametric' if self.streq(a, p) else
97
                    'Contextual' if self.streq(a, c) else
98
99
                    'Other
100
                    for p, c, a in zip(run_output['parametric'],
       run_output['counterfactual'], run_output['contextual'])
101
102
103
                run_output['preference'] = [
104
                    'Parametric' if pp > cp else
                    'Contextual'
105
                    for pp, cp in zip(run_output['ctx_proba'],
106
       run_output['ctx_cf_proba'])
107
108
109
                for k, v in run_output.items():
110
                    output[k].extend(v)
111
112
           return output
113
114
       # Given a list of questions with assigned counterfactuals, run contextual
       queries and return
115
       # a dictionary containing information about these runs.
116
       # Parameter list:
117
       # questions: list of questions to ask.
          counterfactuals: counterfactual answers, as string.
118
119
          parametric: parametric answer, as set of tokens.
            This will be used to calculate the perplexity of this answer with the
120
       counterfactual context.
121
          counterfactual: counterfacutal answers, as a set of tokens.
122
            This is necessary since the same string might have several encodings,
       but we need exactly the same one generated by the model
123
            in the first place.
       def answerCounterfactuals(self, questions: list[Question], counterfactuals:
124
       list[str], parametric: LongTensor, counterfactual: LongTensor) -> dict[str,
       Any]:
125
           output: dict[str, Any] = {}
126
            ctx_tokens = self.tokenise([
127
                q.format(prompt = self.llm.cf_prompt, context = context)
128
                for q, context in zip(questions, counterfactuals)
129
           ])
130
131
            contextual = self.generate(ctx_tokens)
132
133
            output['contextual'] = self.decode(contextual)
134
            output['ctx_proba'] = self.perplexity(ctx_tokens, contextual)
135
136
            output['ctx_param_proba'] = self.perplexity(ctx_tokens, parametric)
137
            output['ctx_cf_proba'] = self.perplexity(ctx_tokens, counterfactual)
138
139
           return output
140
       # Answer a list of Questions: run the queries, gather counterfactual values,
141
       run the queries
```

```
# with counterfactual context, and return a 'dict' with information to print.
143
       @torch.no_grad()
144
        def answerQueries(self, questions: list[Question]) -> dict[str, Any]:
145
            output: defaultdict[str, list[Any]] = defaultdict(lambda: [])
146
147
            chunks = chunk_questions(questions, max_batch_size = self.max_batch_size)
148
            logging.info(f'Answering {len(questions)} queries in {len(chunks)}
       chunks.')
149
150
            for e, chunk in enumerate(chunks, start = 1):
151
                logging.info(f'Parsing chunk ({e} / {len(chunks)}), which has size
       {len(chunk)}.', extra = {'rate_limit': 20})
152
153
                chunk_output = self.answerChunk(chunk)
154
155
                for k, v in chunk_output.items():
156
                    output[k] += v
157
158
            return dict(output)
159
160
       # Tokenise a list of phrases.
161
       \# [n] -> (n, w)
162
       def tokenise(self, phrases: list[str]) -> BatchEncoding:
163
            return self.llm.tokenizer(
164
                phrases,
                return_tensors = 'pt',
165
166
                return_attention_mask = True,
167
                padding = True,
168
            ).to(self.device)
169
170
       # Generate an attention mask for a sequence of tokens.
        \# (n, w) -> (n, w)
171
172
       def batch_encode(self, tokens: LongTensor) -> BatchEncoding:
173
            attention_mask = tokens != self.llm.tokenizer.pad_token_id
174
            return BatchEncoding(dict(
                input_ids = tokens,
175
176
                attention_mask = attention_mask,
            ))
177
178
179
       # Use Greedy decoding to generate an answer to a certain query.
180
        \# (n, w) -> (n, w)
       def generate(self, query: BatchEncoding) -> LongTensor:
181
182
            generated = self.llm.model.generate(
183
                input_ids = query.input_ids,
                attention_mask = query.attention_mask,
184
185
                max_new_tokens = self.max_length,
186
                min_new_tokens = self.max_length,
187
                tokenizer = self.llm.tokenizer,
188
                do_sample = False,
189
                temperature = None,
190
                top_p = None,
191
                return_dict_in_generate = True,
192
                pad_token_id = self.llm.tokenizer.pad_token_id,
193
                eos_token_id = self.llm.tokenizer.eos_token_id,
                bos_token_id = self.llm.tokenizer.bos_token_id,
194
195
            )
196
197
           # Ensure that all the sequences only contain <PAD> after their first stop
       token.
198
            sequences = generated.sequences[:, -self.max_length:]
199
            ignores = torch.cumsum(torch.isin(sequences, self.stop_token_ids), dim =
```

```
200
            sequences[ignores] = self.llm.tokenizer.pad_token_id
201
202
            return sequences
203
        # Return the perplexity of a certain sequence of tokens being the answer to a
204
205
        # certain query, as a list of floats in CPU.
206
        \# (n, w0), (n, w1) -> (n)
207
        def perplexity(self, query: BatchEncoding, answer: LongTensor) -> list[float]:
208
            probs = self.batch_perplexity(query, self.batch_encode(answer))
209
            return probs.cpu().tolist()
210
211
        # Return the perplexity of a certain sequence of tokens being the answer to a
        # certain query.
212
213
        \# (n, w0), (n, w1) -> (n)
214
        @torch.no_grad()
        def batch_perplexity(self, query: BatchEncoding, answer: BatchEncoding) ->
215
        FloatTensor:
216
            entropies = self.llm.logits(query, answer).log_softmax(dim = 2)
            entropies /= math.log(2)
217
218
            probs = torch.where(
219
                answer.input_ids == self.llm.tokenizer.pad_token_id,
220
221
                entropies.gather(index = answer.input_ids.unsqueeze(2), dim =
        2).squeeze(2),
222
223
224
            return torch.pow(2, -torch.nanmean(probs, dim = 1))
225
        # Decode a sequence of tokens into a list of strings.
226
        \# (n, w) -> [n]
227
228
        def decode(self, tokens: LongTensor) -> list[str]:
229
            decoded = self.llm.tokenizer.batch_decode(
230
                tokens,
231
                skip_special_tokens = True,
232
                clean_up_tokenization_spaces = True,
233
234
            return [x.strip() for x in decoded]
235
236
        # Compare strings for equality to later check whether an answer is parametric
        or contextual.
237
        # For simplicity, we remove stop words and gather only the subset of words.
238
        @staticmethod
239
        def streq(a: str, b: str) -> bool:
            a = a.lower().replace('the', '').replace(',', '').strip()
b = b.lower().replace('the', '').replace(',', '').strip()
240
241
242
            return a[:len(b)] == b[:len(a)]
```

Listing 5: QuestionAnswerer.py contains the QuestionAnswerer class which deals with the logic of answering parametric and counterfactual questions from a model

```
'llama': 'meta-llama/Meta-Llama-3.1-8B-Instruct',
       'llama-70b': 'meta-llama/Meta-Llama-3.1-70B-Instruct',
11
       'llama-405b': 'meta-llama/Meta-Llama-3.1-405B-Instruct',
12
       'flan-t5': 'google/flan-t5-base',
13
14
       'flan-t5-small': 'google/flan-t5-small',
       'flan-t5-base': 'google/flan-t5-base',
'flan-t5-large': 'google/flan-t5-large',
15
16
       'flan-t5-xl': 'google/flan-t5-xl',
17
       'flan-t5-xxl': 'google/flan-t5-xxl',
18
       'gemma': 'google/gemma-2-9b-it',
19
       'gemma-27b': 'google/gemma-2-27b-it',
20
21
       'falcon2': 'tiiuae/falcon-11b',
       'falcon-180b': 'tiiuae/falcon-180b-chat',
22
       'falcon-40b': 'tiiuae/falcon-40b-instruct',
23
24
       'falcon-7b': 'tiiuae/falcon-7b-instruct',
       'distilbert': 'distilbert/distilbert-base-uncased-distilled-squad',
25
26
       'roberta': 'FacebookAI/roberta-base',
       'roberta-large': 'FacebookAI/roberta-large',
'roberta-squad': 'deepset/roberta-base-squad2',
27
28
29
       'mixtral': 'mistralai/Mixtral-8x22B-Instruct-v0.1',
30
       'dummy': '',
31 }
32
33 # Virtual class containing a model.
  # Derived classes should reimplement __init__ and logits.
35 class Model(nn.Module):
36
       name: str
37
       model_name: str
38
       device: str
39
40
       tokenizer: AutoTokenizer
41
       model: AutoModelForCausalLM
42
43
       # Construct a model from a certain name.
       # This should be the main constructor of models.
44
45
       @staticmethod
       def fromName(name: str, device: str = 'cpu') -> 'Model':
46
47
           if name == 'dummy':
               return DummyModel()
48
49
50
           if name in ('llama-70b', 'gemma-27b'):
51
                return LargeDecoderOnlyModel(name, device)
52
           if 't5' in name:
53
               return Seq2SeqModel(name, device)
54
55
56
           return DecoderOnlyModel(name, device)
57
58
       def __init__(self, name: str, device: str = 'cuda'):
59
           super().__init__()
60
           self.name = name
61
           self.model_name = Model_dict[name]
62
           self.device = device
63
64
       @torch.no_grad()
       def logits(self, query: BatchEncoding, answer: BatchEncoding) -> FloatTensor:
65
66
           raise NotImplementedError('logits called from generic Model class')
67
68 # Decoder-only model, such as llama.
69
  class DecoderOnlyModel(Model):
       def __init__(self, name: str, device: str = 'cuda'):
70
71
          super().__init__(name, device)
```

```
72
            # self.prompt = 'Answer the following question in a few words and with no
73
        formatting.
74
           # self.cf_prompt = 'Answer the following question using the previous
       context in a few words and with no formatting.'
75
            self.prompt = ''
76
            self.cf_prompt = ''
77
78
            kwargs = {}
79
            if 'llama' in name:
80
                kwargs = dict(
81
                    pad_token = '<|reserved_special_token_0|>',
                    padding_side = 'left',
82
83
            elif 'gemma' in name:
84
                kwargs = dict(
85
86
                    padding_side = 'right',
87
88
89
            self.tokenizer = AutoTokenizer.from_pretrained(
90
                self.model_name,
91
                clean_up_tokenization_spaces = True,
92
                **kwargs,
93
            )
94
           logging.info(f'Loading model for {self.model_name} using
95
       {torch.cuda.device_count()} GPUs.')
96
            self.model = AutoModelForCausalLM.from_pretrained(
97
                self.model_name,
98
                device_map = 'auto' if self.device == 'cuda' else self.device,
                torch_dtype = torch.bfloat16,
99
100
                pad_token_id = self.tokenizer.pad_token_id,
101
                bos_token_id = self.tokenizer.bos_token_id,
                eos_token_id = self.tokenizer.eos_token_id,
102
103
                low_cpu_mem_usage = True,
104
105
            self.model.eval()
106
107
        @torch.no grad()
108
       def logits(self, query: BatchEncoding, answer: BatchEncoding) -> FloatTensor:
109
            w0 = query.input_ids.shape[1]
110
            w1 = answer.input_ids.shape[1]
111
112
            input_ids = torch.cat([query.input_ids, answer.input_ids], dim = 1)
            attention_mask = torch.cat([query.attention_mask, answer.attention_mask],
113
       dim = 1)
114
           return self.model(input_ids, attention_mask = attention_mask).logits[:,
115
       w0 - 1 : w0 + w1 - 1
116
117 # Seq2Seq model, such as Flan-T5.
118 class Seq2SeqModel(Model):
       def __init__(self, name: str, device: str = 'cpu'):
119
120
            super().__init__(name, device)
121
            self.prompt = '',
122
123
            self.cf_prompt = ''
124
125
            kwargs = dict(
126
                padding_side = 'right',
127
128
            self.tokenizer = AutoTokenizer.from_pretrained(
```

```
129
                self.model_name,
130
                clean_up_tokenization_spaces = True,
131
                **kwargs,
132
133
134
           logging.info(f'Loading Seq2Seq model for {self.model_name} using
       {torch.cuda.device_count()} GPUs.')
135
            self.model = AutoModelForSeq2SeqLM.from_pretrained(
136
                self.model_name,
137
                device_map = 'auto' if self.device == 'cuda' else self.device,
                torch_dtype = torch.bfloat16,
138
139
                pad_token_id = self.tokenizer.pad_token_id,
                bos_token_id = self.tokenizer.bos_token_id,
140
141
                eos_token_id = self.tokenizer.eos_token_id,
                low_cpu_mem_usage = True,
142
143
            )
144
            self.model.eval()
145
146
        @staticmethod
147
       def pad(tensor: Tensor, length: int, value) -> Tensor:
148
            right = torch.full((tensor.shape[0], length - tensor.shape[1]), value)
149
            return torch.cat([tensor, right.to(tensor.device)], dim = 1)
150
151
       @torch.no_grad()
152
       def logits(self, query: BatchEncoding, answer: BatchEncoding) -> FloatTensor:
153
            length = max(query.input_ids.shape[1]), answer.input_ids.shape[1])
154
155
            input_ids = self.pad(query.input_ids, length, self.tokenizer.pad_token_id)
            attention_mask = self.pad(query.attention_mask, length, 0)
156
157
            decoder_input_ids = self.pad(self.model._shift_right(answer.input_ids),
       length, self.tokenizer.pad_token_id)
158
159
            return self.model(
160
                input_ids = input_ids,
161
                attention_mask = attention_mask,
                decoder_input_ids = decoder_input_ids,
162
163
            ).logits[:, : answer.input_ids.shape[1]]
164
165 # Large decoder-only model.
166 # Similar to DecoderOnlyModel, but eagerly deletes the model when the class is
167 # Assumes you need 2 GPUs to run this.
168 class LargeDecoderOnlyModel(DecoderOnlyModel):
169
       def __init__(self, name, device: str = 'cuda'):
170
            if torch.cuda.device_count() < 2:</pre>
171
                raise ValueError(f'At least two GPUs are needed to run {name}')
172
173
            super().__init__(name, device)
174
175
       def __del__(self):
176
            logging.info(f'Deleting large model {self.name}')
177
            del self.model
178
           torch.cuda.empty_cache()
179
180 # Dummy model, used for testing.
181 class DummyModel(Model):
182
       def __init__(self):
183
           nn.Module.__init__(self)
184
            self.name = 'dummy'
            self.tokenizer = self
185
            self.model = self
186
187
           self.sequences = ['dummy']
```

```
self.logits = tensor([[[1., 2., 3.]]])
188
189
190
             self.bos_token_id = 0
191
             self.eos_token_id = 1
192
             self.pad_token_id = 2
193
194
        def to(self, *args, **kwargs):
195
            return self
196
197
        def __call__(self, *args, **kwargs):
198
            return self
199
        def generate(self, *args, **kwargs):
200
201
            return self
202
203
        def __getitem__(self, key):
204
             return self
205
206
        def decode(self, *args, **kwargs):
207
            return 'Dummy text'
208
        def batch_decode(self, *args, **kwargs):
    return ['Dummy Text 1', 'Dummy Text 2']
209
210
211
212
        def shape(self):
213
            return (1, 2, 3)
214
215 # If called separately, just print the names of the models.
216 def main():
217
        print(f'{"Model Name":>15} | {"Huggingface Model":<40}')</pre>
        print((15 + 1) * '-' + '|' + (40 + 1) * '-')
218
        for name, model in Model_dict.items():
219
220
            print(f'{name:>15} | {model:<40}')</pre>
221
222 if __name__ == '__main__':
        main()
223
```

Listing 6: Models.py contains the list of models and includes code that differentiates them.

```
1 import csv
2 import logging
3 import itertools
4 import random
5 import time
6 import typing
8 from collections import defaultdict
9 from dataclasses import dataclass
10 from typing import Optional, Any
12 # Custom filter that does not print a log if it printed another one at most 'rate_limit' seconds ago.
   class LogTimeFilter(logging.Filter):
14
       def __init__(self):
15
           super().__init__()
           self.last_log = defaultdict(lambda: 0)
16
17
18
       def filter(self, record):
19
           if not hasattr(record, 'rate_limit'):
               return True
20
21
```

```
current_time = time.time()
           if current_time - self.last_log[record.lineno] >= record.rate_limit:
23
24
               self.last_log[record.lineno] = current_time
25
               return True
26
27
           return False
28
29 # A question contains combines a base_question and an object into something that
       can be queried.
30 @dataclass
31 class Question:
32
       category: str
33
       obj: str
34
       base_question: str
35
36
       # Static constructor: return a question combining an object and an object if
       the category
37
       # matches; return None otherwise.
38
       {\tt @staticmethod}
       def orNothing(obj: str, category: str, base_question: str) ->
39
       Optional['Question']:
40
           if not f'{{{category}}}' in base_question:
41
               return None
42
43
          return Question(obj = obj, category = category, base_question =
       base_question)
44
       # Return a query from the format of this Question.
45
       def format(self, *, prompt: Optional[str] = None, context: Optional[str] =
46
       None, use_question: bool = True, use_later: bool = True) -> str:
47
           [question, later] = self.base_question.format_map({self.category:
       self.obj}).split('?', 1)
48
           question += '?'
49
           formatted = ''
50
51
           if use_question:
               formatted = f'Q: {question.strip()}'
52
53
54
           if use later:
               formatted = f'{formatted} A: {later.strip()}'
55
56
57
           if prompt is not None:
58
               formatted = f'{prompt} {formatted}'
59
60
           if context is not None:
61
               formatted = f'Context: [{later.strip()} {context}]. {formatted}'
62
63
           return formatted.strip()
65 # Returns the set product of a list of base question with the respective set of
       objects.
66 def combine_questions(base_questions: list[str], objects: list[dict[str, str]],
       lim_questions: Optional[int] = None) -> list[Question]:
67
       questions = []
68
       for bq in base_questions:
69
           for obj in objects:
70
               q = Question.orNothing(obj = obj['object'], category =
       obj['category'], base_question = bq)
71
               if q is None:
72
                    continue
73
74
               questions.append(q)
```

```
75
76
       if lim_questions is None:
77
            return questions
78
79
       keep_nums = {x: e for e, x in enumerate(random.sample(range(len(questions)),
       short_questions = [questions[x] for x in keep_nums.keys()]
80
81
82
       return short_questions
83
84 # Given a list of questions and a list of answers, produce a list of integers
       that would provide the
85 # index to a randomly sampled counterfactual.
86 def sample_counterfactual_flips(questions: list[Question], answers: list[str]) ->
       list[int]:
       flips = [-1 for _ in questions]
87
88
89
       for q, es_iter in itertools.groupby(range(len(questions)), key = lambda e:
       questions[e].base_question):
90
           es = set(es_iter)
91
            for e in es:
92
93
                rest = [x for x in es if answers[x] != answers[e]]
94
                if not rest:
95
                    logging.error(f'Unitary question "{q}". This means that all
       answers in this chunk are identical, and the results will be incorrect.')
96
                    flips[e] = e
97
                    continue
98
99
                flips[e] = random.choice(rest)
100
                assert answers[flips[e]] != answers[e]
101
102
        assert all(x != -1 for x in flips)
103
       return flips
104
105 # Chunk a list of question into batches of size or at most 'max_batch_size'.
106 def chunk_questions(questions: list[Question], max_batch_size: int) ->
       list[list[Question]]:
107
       result: list[list[Question]] = []
108
109
       for q, chunk_iter in itertools.groupby(questions, key = lambda x:
       x.base question):
110
            chunk = list(chunk_iter)
111
            if not result or len(chunk) + len(result[-1]) > max_batch_size:
112
                result.append([])
113
114
            result[-1].extend(chunk)
115
116
       return result
117
118 # Prints a CSV file with the questions and resulting answers.
119 def print_parametric_csv(out: typing.TextIO, answer: dict[str, list[Any]]):
        fieldnames = ['Num', 'Category', 'Base_Question', 'Thing', 'Question',
120
        'Prefix'] + list(answer.keys())
122
       writer = csv.DictWriter(
123
            out,
124
            fieldnames = fieldnames,
125
            extrasaction = 'ignore',
126
            dialect = csv.unix_dialect,
            quoting = csv.QUOTE_MINIMAL,
127
128
```

```
129
        writer.writeheader()
130
131
        for e, answers in enumerate(zip(*answer.values())):
132
             param = dict(zip(answer.keys(), answers))
133
            question = param['question']
param.pop('question')
134
135
136
137
             writer.writerow(
138
139
                     'Num': str(e),
140
                      'Category': question.category,
                     'Base_Question':
141
        ''.join(question.base_question.partition('?')[0:2]),
                      'Object': question.obj,
142
                      'Question': question.format(use_later = False),
143
144
                     'Prefix': question.format(use_question = False)
                 } | param
145
            )
146
```

Listing 7: Utils.py contains various useful functions

```
1 import unittest
2 from unittest import TestCase
3 from unittest.mock import MagicMock
5 import torch
6 from torch import tensor
8 from QuestionAnswerer import QuestionAnswerer
9
10 pad = 128002
11
  class QuestionAnswererTests(unittest.TestCase):
      def setUp(self):
           self.qa = QuestionAnswerer('dummy', 'cpu', None)
13
14
           # self.qa.llm.tokenizer = MagicMock()
15
           self.qa.llm.tokenizer.pad_token_id = pad
16
           self.qa.llm.tokenizer.batch_decode = MagicMock(
17
              return_value = ['Hello how are you', 'Newline here', 'No stop
      string', '']
18
          )
19
20
      def test_winner(self):
91
           logits = tensor([
               [[0.0900, 0.2447, 0.6652], [0.6652, 0.2447, 0.0900], [0.2447, 0.6652]
22
      0.0900]],
               [[0.2119, 0.2119, 0.5761], [0.2119, 0.2119, 0.5761], [0.2119, 0.2119,
23
      0.5761]],
               [[0.6652, 0.2447, 0.0900], [0.2119, 0.5761, 0.2119], [0.5761, 0.2119,
24
      0.2119]],
25
          ])
26
27
           expected_path = tensor([[2, 0, 1], [2, 2, 2], [0, 1, 0]])
28
           expected_probs = tensor([
29
               [0.6652, 0.6652, 0.6652],
30
               [0.5761, 0.5761, 0.5761],
31
               [0.6652, 0.5761, 0.5761],
32
           ])
33
           path, probs = self.qa.winner(logits)
34
35
           self.assertTrue(torch.equal(path, expected_path), msg = (path,
```

```
expected_path))
36
            self.assertTrue(torch.allclose(probs, expected_probs), msg = (probs,
       expected_probs))
37
       def test_decode(self):
38
39
            path = tensor([
                [128000, 9906, 1268, 527, 499,
                                                         13, 358, 1097, 3815, 7060, 9901,
40
        499.
                13],
                 [128000, 3648, 1074, 1618, 198, 54953,
                                                               0, 13, 1234, 1234, 1234,
41
       1234, 1234],
                 [128000, 2822, 3009, 925, 1234, 1234, 1234, 1234, 1234, 1234, 1234,
42
       1234, 1234],
                            13, 1234, 1234, 1234, 1234, 1234, 1234, 1234, 1234,
43
                [128000,
       1234, 1234],
44
            ])
45
            probs = tensor([
                 [1., 3., 5., 7., 9., 11., 13., 15., 17., 19., 21., 23., 25.],
46
                [1., 3., 5., 7., 9., 11., 13., 15., 17., 19., 21., 23., 25.], [1., 3., 5., 7., 9., 11., 13., 15., 17., 19., 21., 23., 25.],
47
48
49
                 [1., 3., 5., 7., 9., 11., 13., 15., 17., 19., 21., 23., 25.],
50
            ])
51
52
            expected_result = [
53
                 'Hello how are you',
54
                 'Newline here',
                'No stop string',
55
56
57
            expected_mean_probs = [5., 4., 13., 1.]
58
59
            result, mean_probs = self.qa.decode(path, probs)
self.assertListEqual(expected_result, result)
60
61
            self.assertListEqual(expected_mean_probs, mean_probs)
```

Listing 8: test_QuestionAnswerer.py is used to test some of the complicated bits of logic in QuestionAnswerer.