



# Design, Implementation and Evaluation of an Incremental Nonlinear Dynamic Inversion Controller for a Nano-Quadrotor

Entwurf, Implementierung und Evaluierung eines Inkrementellen Nichtlinearen Dynamischen Inversionsreglers für einen Nano-Quadrotor

# Semesterarbeit

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# **Statutory Declaration**

I, Evghenii Volodscoi, declare on oath towards the Institute of Flight System Dynamics of Technische Universität München, that I have prepared the present Semester Thesis independently and with the aid of nothing but the resources listed in the bibliography.

This thesis has neither as-is nor similarly been submitted to any other university.

Garching,



# Kurzfassung

Deutsche Kurzfassung der Arbeit.

#### **Abstract**

English abstract of the thesis.



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# **Table of Acronyms**

**Acronym Description** 

ADF Automatic Direction Finder
ADI Automatic Direction Indicator



# **Table of Symbols**

#### **Latin Letters**

Symbol	Unit Description	
F	N	Force
g	$m/s^2$	Gravitational acceleration

#### **Greek Letters**

Symbol	Unit	Description
$\alpha$	rad	Angle of attack
ζ	_	Damping of a linear second order system
Indices		

## Symbol Unit Description

m Variable related to pitch moment

W Wind



- 1 Introduction
- 1.1 Motivation
- 1.2 Contribution of the Thesis
- 1.3 Structure of the Thesis



## 2 Theoretical Background

#### 2.1 General Equations of Motion

#### General:

- Linear Momentum
- Angular Momentum
- Attitude differential equations
- Position differential equations
- External forces and moments

with some of the used assumptions

### 2.2 Nonlinear Dynamic Inversion

- Theory from Sieberling paper.

#### 2.3 Incremental Nonlinear Dynamic Inversion

- Here only the general principle is provided, next subsections show the full derivation of the two controller loops.

#### 2.3.1 INDI inner loop

- Derivation of the inner INDI loop (detailed equations).

#### 2.3.2 INDI outer loop

- Derivation of the outer INDI loop (detailed equations).



## 3 Implementation

#### 3.1 Research Quadrotor

- Some facts about Crazyflie hardware (foto, uC frequency, weight, length)

#### 3.2 Simulink Model

#### 3.2.1 Purpose

- Estimation of relevant components (Matrices...)
- Testing of the PD-gains
- Testing the filter

#### 3.2.2 Structure

- Parameters
- Actuator dynamics
- Filter
- Images of the Simulink model

#### 3.2.3 Simulation Results

# 3.3 Implementation on Hardware

#### 3.3.1 Structure of the Code

#### 3.3.2 Testing with contact Forces and Moments



# 4 Results



# 5 Discussion



# **Appendix**