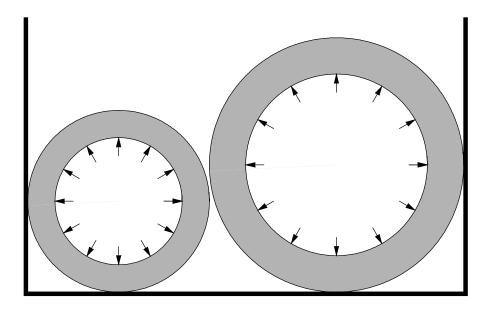
CHAPTER TEN

Contact Problems

Tension Plate Example: Hyperelastic material (p. 513)

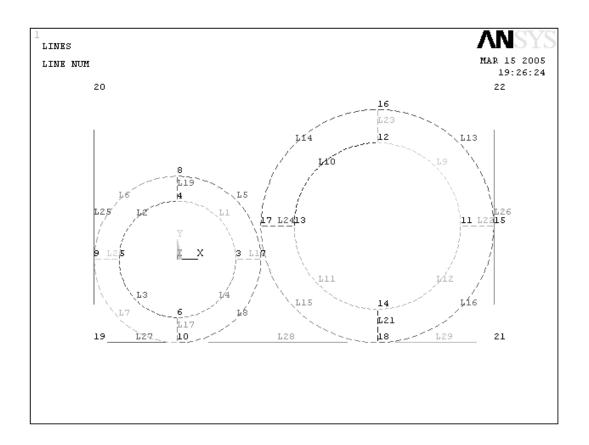
Consider the two cylinders problem shown in Figure. The smaller cylinder has inner and outer radii of 35 mm and 50 mm respectively. The larger cylinder has inner and outer radii of 50 mm and 70 mm respectively. Assume $E = 2000 \, N/\text{mm}^2$ and v = 0.2. The coefficient of friction between all contact surfaces is assumed to be 0.2. The walls and the base of box in which the cylinders are placed are considered rigid. Both cylinders are subjected to inside pressure of $100 \, N/\text{mm}^2$.



The global coordinate system is defined with the origin at the center of the left cylinder. The center of the right cylinder is located at (120,20). The model is created by defining several key points and lines as shown in the following Figure. To prevent rigid body motion both horizontal and vertical displacements at key points 9, 10, 15, and 18 are set to zero. The following contactor-target pairs are defined.

Contactor	Target
L13 and L16	L26 (Right rigid wall)
L15 and L16	L28 and L29 (Bottom rigid wall)
L7 and L8	L27 (Bottom rigid wall)
L5 and L7	L25 (Left rigid wall)
L5	L15

Key points and lines used to create model



$An sys Files \verb|\Chap10| cyliders Contact.txt|$

/PREP7

۱*

ET,1,PLANE42

|*

KEYOPT,1,1,0

KEYOPT,1,2,0

KEYOPT,1,3,2

KEYOPT,1,5,0

KEYOPT,1,6,0

!*

```
!*
MPTEMP,,,,,,
MPTEMP,1,0
MPDATA, EX, 1,, 2000
MPDATA,PRXY,1,,.2
!* Define key points, lines and areas
K,1,,,,
K,2,120,20,,
CIRCLE,1, 35, , ,360, ,
CIRCLE, 1, 50, , , 360, ,
CIRCLE,2,50, , ,360, ,
CIRCLE,2,70, , ,360, ,
LSTR,
         10,
                6
LSTR,
               7
          3,
LSTR,
          4,
               8
LSTR,
               9
          5,
LSTR,
         18,
               14
LSTR,
         11,
               15
LSTR,
         12,
                16
LSTR,
         13,
               17
AL,17,8,18,4
AL,18,5,19,1
AL,19,6,20,2
AL,20,7,17,3
AL,21,16,22,12
AL,22,13,23,9
AL,23,14,24,10
AL,24,15,21,11
!* Create mesh
ESIZE,5
MSHKEY,1
AMESH,ALL
!* Create key points and lines for defining
!* rigid walls and base
K,19,-50,-50,,
K,20,-50,100,,
K,21,190,-50,,
K,22,190,100,,
```

LSTR,19,20

```
LSTR,21,22
LSTR,19,10
LSTR,10,18
LSTR,18,21
!* Fix initial contact points between
!* rigid walls and cylinders
DK,10, , , ,0,UX, , , , , ,
DK,10, , , ,0,UY, , , , ,
DK,18, , , ,0,UX, , , , , ,
DK,18, , , ,0,UY, , , , ,
DK,9, , , ,0,UX, , , , , ,
DK,9,,,,0,UY,,,,,,
DK,15, , , ,0,UX, , , , ,
DK,15, , , ,0,UY, , , , ,
!* Apply pressure
SFL,1,PRES,100,
SFL,2,PRES,100,
SFL,3,PRES,100,
SFL,4,PRES,100,
SFL,9,PRES,100,
SFL,10,PRES,100,
SFL,11,PRES,100,
SFL,12,PRES,100,
/COM, CONTACT PAIR CREATION - START
!* Contact between two cylinders
MP,MU,1,0.2
MAT,1
R,3
REAL,3
ET,2,169
ET,3,175
R,3,,,1.0,0.1,0,
RMORE,,,1.0E20,0.0,1.0,
RMORE, 0.0, 0, 1.0, , 1.0, 0.5
RMORE,0,1.0,1.0,0.0,,1.0
RMORE,10.0
KEYOPT,3,3,0
KEYOPT,3,4,0
KEYOPT,3,5,0
```

KEYOPT,3,7,0

KEYOPT,3,8,0

KEYOPT,3,9,1

KEYOPT,3,10,1

KEYOPT,3,11,0

KEYOPT,3,12,0

KEYOPT,3,2,0

! Generate the target surface

LSEL,S,,,14

LSEL,A,,,15

CM,_TARGET,LINE

TYPE,2

NSLL,S,1

ESLN,S,0

ESURF

! Generate the contact surface

LSEL,S,,,5

LSEL,A,,,8

CM,_CONTACT,LINE

TYPE,3

NSLL,S,1

ESLN,S,0

ESURF

ALLSEL

ESEL,ALL

ESEL,S,TYPE,,2

ESEL,A,TYPE,,3

ESEL,R,REAL,,3

/PSYMB,ESYS,1

/PNUM,TYPE,1

/NUM,1

EPLOT

ESEL,ALL

/COM, CONTACT PAIR CREATION - START

!* Contact between large cylinder and right wall

CM,_NODECM,NODE

CM,_ELEMCM,ELEM

CM,_KPCM,KP

CM,_LINECM,LINE

CM,_AREACM,AREA

CM,_VOLUCM,VOLU

/GSAV,cwz,gsav,,temp

MP,MU,1,0.2

MAT,1

R,4

REAL,4

ET,4,169

ET,5,175

KEYOPT,5,9,0

KEYOPT,5,10,1

R,4,

RMORE,

RMORE,,0

RMORE,0

! Generate the target surface

LSEL,S,,,26

CM,_TARGET,LINE

TYPE,4

LATT,-1,4,4,-1

TYPE,4

LMESH,ALL

! Generate the contact surface

LSEL,S,,,13

LSEL,A,,,16

CM,_CONTACT,LINE

TYPE,5

NSLL,S,1

ESLN,S,0

ESURF

*SET,_REALID,4

ALLSEL

ESEL,ALL

ESEL,S,TYPE,,4

ESEL,A,TYPE,,5

ESEL,R,REAL,,4

LSEL,S,REAL,,4

/PSYMB,ESYS,1

/PNUM,TYPE,1

/NUM,1

EPLOT

! Reverse target normals

CM,_Y,LINE

LSEL,,,, 26

CM,_YEL,ELEM

CM,_YND,NODE

NSLL,S,1

ESLN,S,1

ESEL,R,REAL,,_REALID

ESURF,,REVERSE

CMSEL,S,_Y

CMSEL,S,_YEL

CMSEL,S,_YND

CMDELE,_Y

CMDELE,_YEL

CMDELE,_YND

/REPLOT

!*

ESEL,ALL

ESEL,S,TYPE,,4

ESEL,A,TYPE,,5

ESEL,R,REAL,,4

LSEL,S,REAL,,4

/PSYMB,ESYS,1

/PNUM,TYPE,1

/NUM,1

EPLOT

ESEL,ALL

ESEL,S,TYPE,,4

ESEL,A,TYPE,,5

ESEL,R,REAL,,4

LSEL,S,REAL,,4

CMSEL,A,_NODECM

CMDEL,_NODECM

CMSEL,A,_ELEMCM

CMDEL,_ELEMCM

CMSEL,S,_KPCM

CMDEL,_KPCM

```
CMSEL,S,_LINECM
CMDEL,_LINECM
CMSEL,S,_AREACM
CMDEL,_AREACM
CMSEL,S,_VOLUCM
CMDEL,_VOLUCM
/GRES,cwz,gsav
CMDEL,_TARGET
CMDEL,_CONTACT
/COM, CONTACT PAIR CREATION - END
!*
!*
/COM, CONTACT PAIR CREATION - START
!* Contact between large cylinder and base
CM,_NODECM,NODE
CM,_ELEMCM,ELEM
CM,_KPCM,KP
CM,_LINECM,LINE
CM,_AREACM,AREA
CM,_VOLUCM,VOLU
/GSAV,cwz,gsav,,temp
MP,MU,1,0.2
MAT,1
R,5
REAL,5
ET,6,169
ET,7,175
KEYOPT,7,9,0
KEYOPT,7,10,1
R,5,
RMORE,
RMORE,,0
RMORE,0
! Generate the target surface
LSEL,S,,,28
LSEL,A,,,29
CM,_TARGET,LINE
TYPE,6
```

LATT,-1,5,6,-1

TYPE,6

LMESH,ALL

! Generate the contact surface

LSEL,S,,,15

LSEL,A,,,16

CM,_CONTACT,LINE

TYPE,7

NSLL,S,1

ESLN,S,0

ESURF

*SET,_REALID,5

ALLSEL

ESEL,ALL

ESEL,S,TYPE,,6

ESEL,A,TYPE,,7

ESEL,R,REAL,,5

LSEL,S,REAL,,5

/PSYMB,ESYS,1

/PNUM,TYPE,1

/NUM,1

EPLOT

! Reverse target normals

FLST,5,2,4,ORDE,2

FITEM,5,28

FITEM,5,-29

CM,_Y,LINE

 $\mathsf{LSEL},\,,\,,\,\mathsf{,P51X}$

CM,_YEL,ELEM

CM,_YND,NODE

NSLL,S,1

ESLN,S,1

ESEL,R,REAL,,_REALID

ESURF,,REVERSE

CMSEL,S,_Y

CMSEL,S,_YEL

CMSEL,S,_YND

CMDELE,_Y

CMDELE,_YEL

CMDELE,_YND

```
/REPLOT
!*
ESEL,ALL
ESEL,S,TYPE,,6
ESEL,A,TYPE,,7
ESEL,R,REAL,,5
LSEL,S,REAL,,5
/PSYMB,ESYS,1
/PNUM,TYPE,1
/NUM,1
EPLOT
ESEL,ALL
ESEL,S,TYPE,,6
ESEL,A,TYPE,,7
ESEL,R,REAL,,5
LSEL,S,REAL,,5
CMSEL,A,_NODECM
CMDEL,_NODECM
CMSEL,A,_ELEMCM
CMDEL,_ELEMCM
CMSEL,S,_KPCM
CMDEL,_KPCM
CMSEL,S,_LINECM
CMDEL,_LINECM
CMSEL,S,_AREACM
CMDEL,_AREACM
CMSEL,S,_VOLUCM
CMDEL,_VOLUCM
/GRES,cwz,gsav
CMDEL,_TARGET
CMDEL,_CONTACT
/COM, CONTACT PAIR CREATION - END
!*
!*
/COM, CONTACT PAIR CREATION - START
!* Contact between small cylinder and left wall
CM,_NODECM,NODE
CM,_ELEMCM,ELEM
CM,_KPCM,KP
```

CM,_LINECM,LINE

CM,_AREACM,AREA

CM,_VOLUCM,VOLU

/GSAV,cwz,gsav,,temp

MP,MU,1,0.2

MAT,1

R,6

REAL,6

ET,8,169

ET,9,175

KEYOPT,9,9,0

KEYOPT,9,10,1

R,6,

RMORE,

RMORE,,0

RMORE,0

! Generate the target surface

LSEL,S,,,25

CM,_TARGET,LINE

TYPE,8

LATT,-1,6,8,-1

TYPE,8

LMESH,ALL

! Generate the contact surface

LSEL,S,,,6

LSEL,A,,,7

CM,_CONTACT,LINE

TYPE,9

NSLL,S,1

ESLN,S,0

ESURF

*SET,_REALID,6

ALLSEL

ESEL,ALL

ESEL,S,TYPE,,8

ESEL,A,TYPE,,9

ESEL,R,REAL,,6

LSEL,S,REAL,,6

/PSYMB,ESYS,1

```
/NUM,1
EPLOT
ESEL,ALL
ESEL,S,TYPE,,8
ESEL,A,TYPE,,9
ESEL,R,REAL,,6
LSEL,S,REAL,,6
CMSEL,A,_NODECM
CMDEL,_NODECM
CMSEL,A,_ELEMCM
CMDEL,_ELEMCM
CMSEL,S,_KPCM
CMDEL,_KPCM
CMSEL,S,_LINECM
CMDEL,_LINECM
CMSEL,S,_AREACM
CMDEL,_AREACM
CMSEL,S,_VOLUCM
CMDEL,_VOLUCM
/GRES,cwz,gsav
CMDEL,_TARGET
CMDEL,_CONTACT
/COM, CONTACT PAIR CREATION - END
!*
!*
/COM, CONTACT PAIR CREATION - START
!* Contact between small cylinder and base
CM,_NODECM,NODE
CM,_ELEMCM,ELEM
CM,_KPCM,KP
CM,_LINECM,LINE
CM,_AREACM,AREA
CM,_VOLUCM,VOLU
/GSAV,cwz,gsav,,temp
MP,MU,1,0.2
MAT,1
R,7
```

/PNUM,TYPE,1

REAL,7

ET,10,169

ET,11,175

KEYOPT,11,9,0

KEYOPT,11,10,1

R,7,

RMORE,

RMORE,,0

RMORE,0

! Generate the target surface

LSEL,S,,,27

CM,_TARGET,LINE

TYPE,10

LATT,-1,7,10,-1

TYPE,10

LMESH,ALL

! Generate the contact surface

LSEL,S,,,7

LSEL,A,,,8

CM,_CONTACT,LINE

TYPE,11

NSLL,S,1

ESLN,S,0

ESURF

*SET,_REALID,7

ALLSEL

ESEL,ALL

ESEL,S,TYPE,,10

ESEL,A,TYPE,,11

ESEL,R,REAL,,7

LSEL,S,REAL,,7

/PSYMB,ESYS,1

/PNUM,TYPE,1

/NUM,1

EPLOT

! Reverse target normals

CM,_Y,LINE

LSEL, , , , 27

CM,_YEL,ELEM

CM,_YND,NODE

NSLL,S,1

ESLN,S,1

ESEL,R,REAL,,_REALID

ESURF,,REVERSE

CMSEL,S,_Y

CMSEL,S,_YEL

CMSEL,S,_YND

CMDELE,_Y

CMDELE,_YEL

CMDELE,_YND

/REPLOT

!*

ESEL,ALL

ESEL,S,TYPE,,10

ESEL,A,TYPE,,11

ESEL,R,REAL,,7

LSEL,S,REAL,,7

/PSYMB,ESYS,1

/PNUM,TYPE,1

/NUM,1

EPLOT

ESEL,ALL

ESEL,S,TYPE,,10

ESEL,A,TYPE,,11

ESEL,R,REAL,,7

LSEL,S,REAL,,7

CMSEL,A,_NODECM

CMDEL,_NODECM

CMSEL,A,_ELEMCM

CMDEL,_ELEMCM

CMSEL,S,_KPCM

CMDEL,_KPCM

CMSEL,S,_LINECM

CMDEL,_LINECM

CMSEL,S,_AREACM

CMDEL,_AREACM

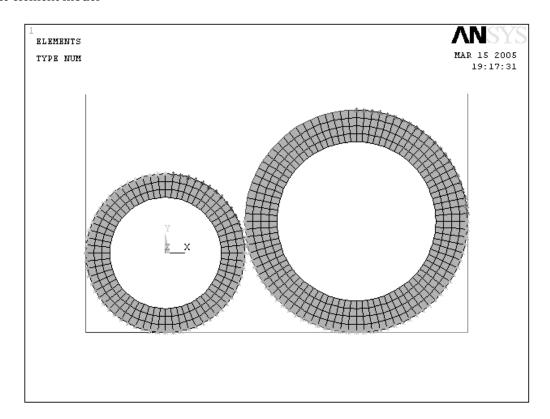
CMSEL,S,_VOLUCM

CMDEL,_VOLUCM

/GRES,cwz,gsav

CMDEL,_TARGET
CMDEL,_CONTACT
/COM, CONTACT PAIR CREATION - END
FINISH
!* Solution and post processing
/SOL
/STATUS,SOLU
NSUBST,100,0,0
SOLVE
FINISH
/POST1
/DSCALE,1,1.0
PLDISP,1

Finite element model



vonMises stresses shown on deformed shape

