

### Computer Implementation 1.4 (*Matlab*) Assembly procedure (p. 25)

The assembly process is conceptually straight-forward but is clearly tedious and thus error prone when performing computations by hand. Fortunately it is fairly easy to establish a *Mathematica* or *Matlab* based procedure to assemble equations for any finite element model. The process in *Matlab* is illustrated here. The global system is  $10 \times 10$ . We start the process by defining a  $10 \times 10$  matrix  $\mathbf{K}$  and a  $10 \times 1$  vector  $\mathbf{R}$  using the Table command as follows.

MatlabFiles\Chap1\AssemblyEx.m

The global system is  $10 \times 10$ . We start the process by defining a  $10 \times 10$  matrix  $\mathbf{K}$  and a  $10 \times 1$  vector  $\mathbf{R}$  using the Table command as follows.

```
K=zeros(10); R = zeros(10,1);
```

Consider assembly of element 1 whose  $\mathbf{k}$  matrix and  $\mathbf{r}$  vector are as follows.

```
k = [111,201,301; 201,222,232; 301,232,333]
r = [11; 12; 13]
```

This element contributes to 1, 2 and 5 degrees of freedom. We define a vector  $\mathbf{lm}$  (element assembly location vector) to indicate the degrees of freedom to which this element contributes.

```
lm = [1, 2, 5]
```

For assembling  $\mathbf{r}$  into the global  $\mathbf{R}$  vector, the appropriate locations are those given in the  $\mathbf{lm}$  vector. Thus we must extract elements 1, 2 and 5 of the  $\mathbf{R}$  vector and add the  $\mathbf{r}$  vector to them. The *Matlab* syntax  $\mathbf{R}(\mathbf{lm})$  accomplishes the task of extracting the required elements. Thus we can assemble  $\mathbf{r}$  into global  $\mathbf{R}$  as follows.

```
R(lm) = R(lm) + r
>>
R =

    11
    12
     0
     0
    13
     0
     0
     0
     0
     0
```

For assembling  $\mathbf{k}$  into the global  $\mathbf{K}$ , the appropriate locations are combinations of entries given in the  $\mathbf{lm}$  vector. *Matlab* generates these combinations automatically if arguments for extracting elements are two lists. Thus we can assemble  $\mathbf{k}$  into global  $\mathbf{K}$  as follows.

```
K(lm, lm) = K(lm, lm) + k
>>
K =

    111    201     0     0    301     0     0     0     0     0
    201    222     0     0    232     0     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
    301    232     0     0    333     0     0     0     0     0
```

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

Now consider the assembly of element 2 whose  $\mathbf{k}$  matrix and  $\mathbf{r}$  vector are as follows.

```
k = [77,80,90; 80,88,100; 90,100,99]
r = [21; 22; 23]
```

This element contributes to 2, 6 and 5 degrees of freedom and thus we define the  $\mathbf{lm}$  vector for this element as follows.

```
lm = [2, 6, 5]
```

The assembly of  $\mathbf{r}$  into global  $\mathbf{R}$  is as follows.

```
R(lm) = R(lm) + r
>>
R =

    11
    33
     0
     0
    36
    22
     0
     0
     0
     0
```

The assembly of  $\mathbf{k}$  into global  $\mathbf{K}$  is as follows.

```
K(lm, lm) = K(lm, lm) + k
>>
K =

    111    201     0     0    301     0     0     0     0     0
    201    299     0     0    322    80     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
    301    322     0     0    432   100     0     0     0     0
     0     80     0     0    100    88     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
     0     0     0     0     0     0     0     0     0     0
```

Clearly all elements can easily be assembled using this procedure. As will be illustrated in later examples, the process can be streamlined even further by using the *for* loop function in *Matlab*.

---