Computer Implementation 3.1 (*Matlab*) Heat flow through fins (p. 198)

The tedious calculations to solve the previous heat flow problem can be conveniently carried out using *Matlab* functions presented earlier. Using these functions, and following procedures discussed in Chapter 1, the global equations for the four quadratic element model can be developed and assembled as follows.

MatlabFiles\Chap3\FinHeatFlowEx.m

```
% Heat flow through a fin
kx=237;w=3;t=0.3/100;A=w*t;h=30;L=20/100.;P=2*(w+t);Tinf=25;
alpha=-h*A/(kx*A); beta=h*A*Tinf/(kx*A);
k=kx*A; p=-h*P; q=h*P*Tinf;
nodes = [0:L/8:L];n=length(nodes);
K=zeros(n); R = zeros(n,1);
% Generate equations for each element and assemble them.
for i=1:4
  Im=[2*(i-1)+1,2*(i-1)+2,2*(i-1)+3];
  [ke, re] = BVP1DQuadElement(k,p,q, nodes(lm));
  K(Im, Im) = K(Im, Im) + ke;
  R(Im) = R(Im) + re;
end
% Adjust for NBC
K(n,n)=K(n,n)-alpha*k
R(n)=R(n)+beta*k
% Nodal solution and reactions
d = NodalSoln(K, R, [1], [100])
plot(nodes,d),title('Temperature distribution'), xlabel('x'),ylabel('T')
>> FinHeatFlowEx
K =
 Columns 1 through 7
                                          0
                                                       0
 100.7412 -113.1594 13.9197
                                                0
-113.1594 232.3248 -113.1594
                                    0
                                          0
                                                       0
  13.9197 -113.1594 201.4824 -113.1594 13.9197
           0 -113.1594 232.3248 -113.1594
     0
     0
            0 13.9197 -113.1594 201.4824 -113.1594 13.9197
     0
                         0 -113.1594 232.3248 -113.1594
     0
           0
                  0
                         0 13.9197 -113.1594 201.4824
     0
           0
                  0
                         0
                               0
                                      0 -113.1594
                                      0 13.9197
                  0
```

Columns 8 through 9

```
0 0
0 0
0 0
0 0
0 0
0 0
-113.1594 13.9197
232.3248 -113.1594
-113.1594 101.0112
```

R =

37.5375 150.1500 75.0750 150.1500 75.0750 150.1500 75.0750 150.1500 44.2875

d =

100.0000 85.4383 74.0844 65.3306 58.7175 53.8905 50.5968 48.6592 47.9772

