Computer Implementation 6.2 (*Matlab*) Mapping areas (p. 405)

The calculations for mapping areas can easily be performed in *Matlab*. Consider finding mapping for a curved quadrilateral area. All four sides are curved and are defined by three points on each side for a total of 8 points. The master element has eight nodes as shown in the figure.

MatlabFiles\Chap6\TwoDMappingEx.m

```
% Mapping for a quadrilateral defined by the following eight points
pts = [0.5, 0.5; 1.1, 1.6; 1.7, 2.1; 1.5, 2.5; 1.1, 2.8;
   .75, 2.5; .5,2.5; .25, 1.5];
xn=pts(:,1); yn=pts(:,2);
map=[];
for s=-1:1/10:1
  for t=-1:1/10:1
     % 8 node serendipity interpolation functions
     n = [-((-1 + s)^*(-1 + t)^*(1 + s + t))/4, ...
           ((-1 + s^2)^*(-1 + t))/2, ...
           ((-1 + t)*(1 - s^2 + t + s*t))/4,...
           -((1 + s)*(-1 + t^2))/2, ...
           ((1 + s)*(1 + t)*(-1 + s + t))/4, ...
           -((-1 + s^2)^*(1 + t))/2, ...
           ((-1 + s)*(1 + s - t)*(1 + t))/4,...
           ((-1 + s)*(-1 + t^2))/2;
     dns = [-((-1 + t)*(2*s + t))/4, s*(-1 + t), ...
           ((-1 + t)*(-2*s + t))/4,...
           (1 - t^2)/2, ((1 + t)^*(2^*s + t))/4, ...
           -(s^*(1+t)), ((2*s-t)^*(1+t))/4, ...
           (-1 + t^2)/2];
     dnt = [((-1 + s)^*(s + 2^*t))/4, (-1 + s^2)/2, ...
           -((1 + s)*(s - 2*t))/4,...
           -((1 + s)*t), ((1 + s)*(s + 2*t))/4, ...
           (1 - s^2)/2, ...
           ((-1 + s)*(s - 2*t))/4, (-1 + s)*t];
     x = n*xn; y=n*yn;
     dxs=dns*xn; dxt=dnt*xn;
     dys=dns*yn; dyt=dnt*yn; J=[dxs, dxt; dys, dyt]; detJ = det(J);
     map=[map; [s, t, x, y, detJ]];
  end
end
detJ=[]; x=[]; y=[];
for i=1:21:length(map)
  x = [x, map(i:i+20,3)];
  y = [y, map(i:i+20,4)];
  detJ = [detJ, map(i:i+20,5)];
```

```
end
% Plot quadrilateral from mapped coordinates
% The surface plot shows detJ values
clf
hold on
mesh(x,y, zeros(length(x)));
mesh(x,y, detJ)
title('Jacobian over mapped element')
xlabel('x'); ylabel('y'); zlabel('detJ')
hold off
```

A plot of the actual element can be generated from the mapping by taking a series of points on the master element and generating x and y coordinates from the mapping. Comparing this plot to the actual element plot, it is visually clear that the mapping is valid.