

Computer Implementation 6.5 (Matlab) 3D numerical integration (p. 420)

Consider evaluation of the following integral using Gauss quadrature.

$$I = \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (400 t^5 + 675 t^3 - 900 s^4 - 200 s^2 + 25 r + 0.2) dr ds dt$$

MatlabFiles\Chap6\ThreeDGaussQuadratureEx.m

```
% Integration over a cube using 1x2x3 Gaussian quadrature
gaussPoints=[0., -0.5773502691896257, -0.7745966692414834;
 0., -0.5773502691896257, 0.;
 0., -0.5773502691896257, 0.7745966692414834;
 0., 0.5773502691896257, -0.7745966692414834;
 0., 0.5773502691896257, 0.;
 0., 0.5773502691896257, 0.7745966692414834];

gaussWeights=[1.111111111111111, 1.777777777777777, ...
 1.111111111111111, 1.111111111111111, ...
 1.777777777777777, 1.111111111111111];
int=0;
for i=1:length(gaussWeights)
    r = gaussPoints(i,1); s = gaussPoints(i,2); t = gaussPoints(i,3);
    frst = 0.2 + 25*r - 200*s^2 + 675*t^3 - 900*s^4 + 400*t^5;
    int = int + gaussWeights(i)*frst;
end
int

>> ThreeDGaussQuadratureEx

int =

-1.3317e+003
```
