

Computer Implementation 1.13 (*Matlab*) Complete solution of a heat flow problem (p. 53)

By combining procedures discussed in earlier implementations, here we present a complete *Matlab* based solution for the heat flow model. This implementation can be used as template to analyze any other two dimensional heat flow problem.

MatlabFiles\Chap1\SquareDuctHeatEx.m

```
% Heat flow through a square duct example
kx=1.4; ky=1.4; Q=0;
nodes=[0,0; 20,0; 20,30; 0,10; 10,10]/100;
lmm = [1,2,5; 2,3,5; 3,4,5; 1,5,4];

K=zeros(5); R = zeros(5,1);
% Generate equations for each element and assemble them.
for i=1:4
    lm = lmm(i,:);
    [k, r] = HeatTriElement(kx, ky, Q, nodes(lm,:));
    K(lm, lm) = K(lm, lm) + k;
    R(lm) = R(lm) + r;
end
% Add the term beacuse of convection on side 1 of element 2
h=27;Tinf=20; lm = lmm(2,:);
[kh, rh] = ConvectionTerm(1,h,Tinf,nodes(lm,:));
K(lm, lm) = K(lm, lm) + kh
R(lm) = R(lm) + rh

% Nodal solution and reactions
[d, reactions] = NodalSoln(K, R, [1,4], [300; 300])
results=[];
for i=1:4
    results = [results; HeatTriResults(nodes(lmm(i,:),:), d(lmm(i,:)))];
end
results

>> SquareDuctHeatEx

K =

    1.4         0         0    -0.7    -0.7
         0    4.5667    1.5833         0    -2.1
         0    1.5833    3.5167    0.35    -1.4
   -0.7         0     0.35    3.15    -2.8
   -0.7    -2.1    -1.4    -2.8         7

R =

     0
    81
    81
     0
     0

d =

    300
```

93.547
23.844
300
182.83

reactions =

82.017
231.41

results =

192.13	-1032.3	-139.41
100.07	-1125.2	-232.34
168.89	-1171.7	-209.11
260.94	-1171.7	0