### **CHAPTER TWO**

# **Analysis of Elastic Solids**

### **Example 2.1 p. 51**

Determine stresses in a tetrahedral shaped solid made of concrete shown in Figure 2.2. Assume the base (side on the xy plane) is completely fixed and the solid is subjected to a temperature increase of  $50^{\circ}$ C. Use the following data.

$$E = 22 \text{ GPa}; \quad v = 0.15; \quad \alpha = 11 \times 10^{-6} / ^{\circ}\text{C}$$

Nodal coordinates:  $\{10, 0, 0\}, \{40, 0, 0\}, \{25, 25, 0\}, \{25, 0, 25\}$ 

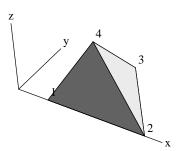


Figure 2.2. A tetrahedral solid subjected to temperature change

#### ■ One element solution for comparison with text

AnsysFiles\Chap02\Ex21.txt

```
!* Example 2.1 (p. 51)
!* One tetrahedral element
/PREP7
! *
ET,1,SOLID45
! *
KEYOPT, 1, 1, 1
KEYOPT, 1, 2, 0
KEYOPT, 1, 4, 0
KEYOPT, 1, 5, 0
KEYOPT, 1, 6, 0
! *
! *
MPTEMP,,,,,,,,
MPTEMP, 1, 0
MPDATA, EX, 1,, 22000
MPDATA, PRXY, 1, , 0.15
MPTEMP,,,,,,,,
MPTEMP, 1, 0
UIMP, 1, REFT, , ,
MPDATA, CTEX, 1,, 11*10**(-6)
N,1,10000,,,,,
N,2,40000,,,,,
N,3,25000,25000,,,,
N,4,25000,0,25000,,,,
e,1,2,3,3,4,4,4,4
D,1, , , , , , ALL, , , , ,
D,2, , , , , , ALL, , , , ,
D,3, , , , , , ALL, , , , ,
TUNIF,50,
FINISH
/SOL
/STATUS, SOLU
SOLVE
FINISH
/POST1
! *
PRNSOL, DOF
PRESOL, S, PRIN
```

```
PRINT U
       NODAL SOLUTION PER NODE
 ***** POST1 NODAL DEGREE OF FREEDOM LISTING *****
               1 SUBSTEP=
 LOAD STEP=
                             1
  TIME= 1.0000 LOAD CASE=
                                 0
 THE FOLLOWING DEGREE OF FREEDOM RESULTS ARE IN GLOBAL COORDINATES
   NODE
           UZ
        0.0000
      1
        0.0000
      2
      3
         0.0000
        18.603
MAXIMUM ABSOLUTE VALUES
NODE
             4
VALUE
       18.603
PRINT S PRIN ELEMENT SOLUTION PER ELEMENT
***** POST1 ELEMENT NODAL STRESS LISTING *****
 LOAD STEP= 1 SUBSTEP=
                             1
  TIME= 1.0000
                 LOAD CASE=
 THE FOLLOWING X,Y,Z VALUES ARE IN GLOBAL COORDINATES
 ELEMENT=
              1
                      SOLID45
   NODE S1
                    S2
                               S3
                                          SINT
                                                     SEOV
                                                   5EQ.
14.235
      DE S1 S2 S3 SINT
1 0.0000 -14.235 -14.235 14.235
2 0.0000 -14.235 -14.235 14.235
                                                     14.235
                                          14.235
        0.0000
                   -14.235
                             -14.235
                                                     14.235
      3
        0.0000
                   -14.235
                              -14.235
                                          14.235
                                                     14.235
      3
        0.0000
                   -14.235
                              -14.235
                                          14.235
                                                     14.235
      4
                                          14.235
      4
        0.0000
                   -14.235
                             -14.235
                                                     14.235
                                         14.235
        0.0000
                   -14.235
                             -14.235
                                                     14.235
```

-14.235 14.235

14.235

#### ■ Solution with default Ansys mesh

0.0000

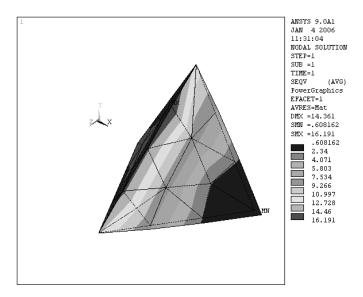
-14.235

AnsysFiles\Chap02\Ex21Mesh.txt

```
!* Example 2.1 (p. 51)
!* Using a reasoable mesh
/PREP7
!*
ET,1,SOLID45
!*
KEYOPT,1,1,1
KEYOPT,1,2,0
```

```
KEYOPT, 1, 4, 0
KEYOPT, 1, 5, 0
KEYOPT, 1, 6, 0
MPTEMP,,,,,,,,
MPTEMP, 1, 0
MPDATA, EX, 1,, 22000
MPDATA, PRXY, 1,, 0.15
MPTEMP,,,,,,,,
MPTEMP, 1, 0
UIMP, 1, REFT, , ,
MPDATA, CTEX, 1,, 11*10**(-6)
K,1,10000,,,,,
K,2,40000,,,,,
K,3,25000,25000,,,,
K,4,25000,0,25000,,,,
V,1,2,3,4
MSHKEY, 0
MSHAPE, 1, 3d
CM,_Y,VOLU
VSEL, , , ,
                    1
CM,_Y1,VOLU
CHKMSH, 'VOLU'
CMSEL,S,_Y
! *
VMESH,_Y1
! *
{\tt CMDELE, \_Y}
CMDELE,_Y1
CMDELE,_Y2
! *
FLST, 2, 1, 5, ORDE, 1
FITEM, 2, 4
! *
/GO
DA, P51X, ALL,
TUNIF, 50,
FINISH
/SOL
/STATUS, SOLU
SOLVE
FINISH
/POST1
! *
PRNSOL, DOF
PRESOL, S, PRIN
```

#### Plot of vonMises stresses



## Cantilever bracket p. 75

The left end of the bracket is fixed. The top face is subjected to a pressure of 10MPa. The material properties are  $E = 200 \,\text{GPa}$  and v = 0.3. The nodal coordinates are as follows.

	x (mm)	y (mm)	z (mm)
1	0	0	0
2	400	100	0
3	400	200	0
4	0	200	0
5	0	0	100
6	400	100	100
7	400	200	100
8	0	200	100

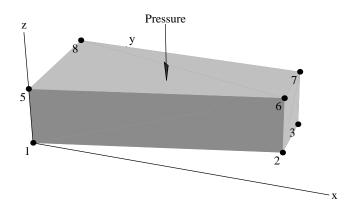


Figure 2.7. One 8 node solid element model of a cantilever bracket

### ■ One element solution for comparison with text

 $An sysFiles \ \ Chap 02 \ \ Cantilever Bracket p 75.txt$ 

```
!* Cantilever bracket (p. 75)
!* One 8 node solid element
/PREP7
! *
ET,1,SOLID45
! *
KEYOPT, 1, 1, 1
KEYOPT, 1, 2, 0
KEYOPT, 1, 4, 0
KEYOPT, 1, 5, 0
KEYOPT, 1, 6, 0
! *
MPTEMP,,,,,,,,
MPTEMP, 1, 0
MPDATA, EX, 1,, 200000
MPDATA, PRXY, 1,, 0.3
N,1,,,,,,
N,2,400,100,,,,
N,3,400,200,,,,
N,4,0,200,0,,,,
N,5,0,0,100,,,
N,6,400,100,100,,,,
N,7,400,200,100,,,,
N,8,0,200,100,,,,
e,1,2,3,4,5,6,7,8
D,1, , , , , , ALL, , , , ,
D,4, , , , , , ALL, , , , ,
D,5, , , , , , ALL, , , , ,
D,8, , , , , ALL, , , ,
SFE,1,6,PRES, ,10, , ,
FINISH
/SOL
/STATUS, SOLU
SOLVE
FINISH
/POST1
! *
PRNSOL, DOF
! *
PRESOL, S, PRIN
 PRINT U
           NODAL SOLUTION PER NODE
  ***** POST1 NODAL DEGREE OF FREEDOM LISTING *****
  LOAD STEP=
                 1 SUBSTEP=
   TIME= 1.0000
                         LOAD CASE=
```

THE FOLLOWING DEGREE OF FREEDOM RESULTS ARE IN GLOBAL COORDINATES

```
NODE
          UZ
    1 0.0000
     2 -0.27802
     3 -0.27986
     4 0.0000
     5 0.0000
     6 -0.28187
     7 -0.28371
     8 0.0000
MAXIMUM ABSOLUTE VALUES
VALUE -0.28371
PRINT S PRIN ELEMENT SOLUTION PER ELEMENT
***** POST1 ELEMENT NODAL STRESS LISTING *****
LOAD STEP= 1 SUBSTEP=
 TIME= 1.0000 LOAD CASE=
 THE FOLLOWING X,Y,Z VALUES ARE IN GLOBAL COORDINATES
```

ELEMENT=	1	SOLID45			
NODE	S1	S2	S3	SINT	SEQV
1	29.792	-16.052	-78.876	108.67	94.492
2	5.6325	2.2015	-48.543	54.175	52.544
3	9.5786	-2.8866	-55.348	64.926	59.678
4	28.695	-16.965	-80.851	109.55	95.306
5	81.444	16.574	-28.967	110.41	96.106
6	40.533	-2.4245	-16.742	57.274	51.627
7	46.967	1.1917	-19.638	66.606	59.015
8	83.242	17.393	-28.019	111.26	96.896

#### ■ Solution with default Ansys mesh

AnsysFiles\Chap02\CantileverP75Mesh.txt

```
!* Cantilever bracket (p. 75)
!* Using Ansys default mesh
/PREP7
!*
ET,1,SOLID45
!*
KEYOPT,1,1,1
KEYOPT,1,2,0
KEYOPT,1,4,0
KEYOPT,1,5,0
KEYOPT,1,6,0
```

```
! *
! *
MPTEMP,,,,,,,,
MPTEMP, 1, 0
MPDATA, EX, 1,, 200000
MPDATA, PRXY, 1, , 0.3
k,1,,,,,,
k,2,400,100,,,,
k,3,400,200,,,,
k,4,0,200,0,,,,
k,5,0,0,100,,,,
k,6,400,100,100,,,,
k,7,400,200,100,,,,
k,8,0,200,100,,,,
v,1,2,3,4,5,6,7,8
MSHKEY, 0
MSHAPE, 1, 3d
CM, Y, VOLU
VSEL, , , ,
CM,_Y1,VOLU
CHKMSH, 'VOLU'
{\tt CMSEL,S,\_Y}
VMESH,_Y1
CMDELE,_Y
CMDELE,_Y1
CMDELE,_Y2
! *
DA,5,ALL,
SFA, 6, 1, PRES, 10
FINISH
/SOL
/STATUS, SOLU
SOLVE
FINISH
/POST1
! *
PRNSOL, DOF
! *
PRESOL, S, PRIN
```

Plot of vonMises stresses

