

# Deflation results with MCMC

February 18, 2021

## 1 Constant preconditioners

### 1.1 Block Jacobi (bJ)

### 1.2 Algebraic multigrid (AMG)

### 1.3 Low rank (LORASC)

### 1.4 Neumann-Neumann (NN)

## 2 Deflation results

### 2.1 Weak scaling

Results in Tab. 1 are \*.

Table 1: Weak scaling results of deflation for a constant bJ preconditioner with  $spdim = \lfloor 2.5 \times nb \rfloor$ .

n	nb	pcg iter	spdim	eigdefpcg iter	eipcg iter	defpcg iter
20,000	8	$10 \pm 2$	20	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
40,000	16	$10 \pm 2$	40	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
80,000	32	$10 \pm 2$	80	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
160,000	64	$10 \pm 2$	160	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
320,000	128	$10 \pm 2$	320	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$

Table 2: Weak scaling results of deflation for a constant LORASC preconditioner with  $\varepsilon = 0.01$  and  $spdim = \lfloor 2.5 \times ndom \rfloor$ .

n	ndom	pcg iter	spdim	eigdefpcg iter	eipcg iter	defpcg iter
20,000	8	$10 \pm 2$	20	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
40,000	16	$10 \pm 2$	40	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
80,000	32	$10 \pm 2$	80	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
160,000	64	$10 \pm 2$	160	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
320,000	128	$10 \pm 2$	320	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$

Table 3: Weak scaling results of deflation for a constant LORASC preconditioner with  $\varepsilon = 0$  and  $spdim = \lfloor 2.5 \times ndom \rfloor$ .

n	ndom	pcg iter	spdim	eigdefpcg iter	eipcg iter	defpcg iter
20,000	8	$10 \pm 2$	20	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
40,000	16	$10 \pm 2$	40	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
80,000	32	$10 \pm 2$	80	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
160,000	64	$10 \pm 2$	160	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
320,000	128	$10 \pm 2$	320	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$

Table 4: Weak scaling results of deflation for a constant AMG preconditioner.

n	pcg iter	spdim	eigdefpcg iter	eipcg iter	defpcg iter
20,000	$10 \pm 2$	20	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
40,000	$10 \pm 2$	40	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
80,000	$10 \pm 2$	80	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
160,000	$10 \pm 2$	160	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
320,000	$10 \pm 2$	320	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$

### 2.1.1 Condensed linear system

Table 5: Weak scaling results of deflation for a constant NN preconditioner with  $spdim = \lfloor 2.5 \times ndom \rfloor$ .

$n_\Gamma$	ndom	pcg iter	spdim	eigdefpcg iter	eipcg iter	defpcg iter
20,000	8	$10 \pm 2$	20	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
40,000	16	$10 \pm 2$	40	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
80,000	32	$10 \pm 2$	80	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
160,000	64	$10 \pm 2$	160	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
320,000	128	$10 \pm 2$	320	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$

## 2.2 Strong scaling results

### 2.2.1 Condensed linear system

Table 6: Strong scaling results of deflation for a constant LORASC preconditioner with  $\varepsilon = 0.01$  and  $spdim = \lfloor 2.5 \times ndom \rfloor$ .

n	ndom	pcg iter	spdim	eigdefpcg iter	eipcg iter	defpcg iter
20,000	8	$10 \pm 2$	20	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
40,000	16	$10 \pm 2$	40	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
80,000	32	$10 \pm 2$	80	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
160,000	64	$10 \pm 2$	160	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$
320,000	128	$10 \pm 2$	320	$10 \pm 2$	$10 \pm 2$	$10 \pm 2$