

NAME

bisimulator – on-the-fly equivalence/preorder checking

SYNOPSIS

bcg.open [*bcg_opt*] *lts1*[**.bcg**] [*cc_opt*] **bisimulator** [*bisimulator_opt*] *lts2*[**.bcg**]

or:

exp.open [*exp_opt*] *lts1*[**.exp**] [*cc_opt*] **bisimulator** [*bisimulator_opt*] *lts2*[**.bcg**]

or:

fsp.open [*fsp_opt*] *lts1*[**.lts**] [*cc_opt*] **bisimulator** [*bisimulator_opt*] *lts2*[**.bcg**]

or:

lnt.open [*lnt_opt*] *lts1*[**.lnt**] [*cc_opt*] **bisimulator** [*bisimulator_opt*] *lts2*[**.bcg**]

or:

lotos.open [*lotos_opt*] *lts1*[**.lotos**] [*cc_opt*] **bisimulator** [*bisimulator_opt*] *lts2*[**.bcg**]

or:

seq.open [*seq_opt*] *lts1*[**.seq**] [*cc_opt*] **bisimulator** [*bisimulator_opt*] *lts2*[**.bcg**]

DESCRIPTION

bisimulator takes as inputs two Labelled Transition Systems (LTSs), the first one being represented either as a BCG graph *lts1*.**bcg**, a composition expression *lts1*.**exp**, an FSP program *lts1*.**lts**, an LNT program *lts1*.**lnt**, a LOTOS program *lts1*.**lotos**, or a sequence file *lts1*.**seq**, and the second one being represented as a BCG graph *lts2*.**bcg**. Traditionally, *lts1* represents the behaviour of a *protocol* and *lts2* represents the behaviour of its *service*.

bisimulator performs an on-the-fly comparison of the two LTSs *lts1* and *lts2* modulo a given equivalence/preorder relation (see EQUIVALENCE RELATIONS below). The result of this verification (TRUE or FALSE) is displayed on the standard output, possibly accompanied by a diagnostic (see OPTIONS below).

Note: The verification method underlying the current version of **bisimulator** is based upon a translation of the equivalence/preorder checking problem into the resolution of a Boolean Equation System (BES), which is performed on-the-fly using the algorithms provided by the **caesar_solve_1**(LOCAL) library of OPEN/CAESAR (see the corresponding manual page and the article [Mat06] for details).

OPTIONS

The options *bcg_opt*, if any, are passed to **bcg_lib**(LOCAL).

The options *exp_opt*, if any, are passed to **exp.open**(LOCAL).

The options *fsp_opt*, if any, are passed to **fsp.open**(LOCAL).

The options *lnt_opt*, if any, are passed to **lnt.open**(LOCAL).

The options *lotos_opt*, if any, are passed to **caesar**(LOCAL) and to **caesar.adt**(LOCAL).

The options *seq_opt*, if any, are passed to **seq.open**(LOCAL).

The options *cc_opt*, if any, are passed to the C compiler.

The options *bisimulator_opt* currently available are described below.

The options below specify the equivalence relation used for comparing *lts1* and *lts2*.

-branching

Use branching equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Not a default option.

-observational

Use observational equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Not a default option.

-safety Use safety equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Not a default option.

-strong Use strong equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Default option.

-taustar

Use *tau*.a* equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Not a default option.

-trace Use trace equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Not a default option.

-weaktrace

Use weak trace equivalence (resp. its corresponding preorder) as equivalence (resp. preorder) relation for comparing *lts1* and *lts2*. Not a default option.

The options below specify the kind of comparison between *lts1* and *lts2*.

-smaller

Check whether *lts1* is included in *lts2* modulo the preorder corresponding to the equivalence relation considered (if the two LTSs are equivalent, they are also included one into the other modulo the corresponding preorder). Not a default option.

-equal Check whether *lts1* is equivalent to *lts2* modulo the equivalence relation considered. Default option.

-greater

Check whether *lts2* is included in *lts1* modulo the preorder corresponding to the equivalence relation considered (if the two LTSs are equivalent, they are also included one into the other modulo the corresponding preorder). Not a default option.

The options below specify the algorithm used for comparing *lts1* and *lts2*.

- bfs** Compare *lts1* and *lts2* using a breadth-first search algorithm. Compared to **-dfs**, this option is generally slower, but produces counterexamples of smaller depth. Not a default option.
- dfs** Compare *lts1* and *lts2* using a depth-first search algorithm. Compared to **-bfs**, this option produces counterexamples of greater depth, but is generally faster and consumes less memory if *lts2* is deterministic (for strong equivalence) and has no invisible actions (for weak equivalences). Default option.

The options below specify various features available in addition to the comparison of *lts1* and *lts2*.

-bes [*file*[**.bes**][*.ext*]]

Print in *file*[**.bes**] or, if the file name argument is missing, in file **bisimulator.bes**, a textual description of the BES corresponding to the comparison of *lts1* and *lts2* modulo the equivalence/preorder relation considered. If present, the extension *.ext* must correspond to a known file compression format (e.g., *.Z*, *.gz*, *.bz2*, etc.). In this case, the file containing the BES is compressed according to the corresponding format. The list of currently supported extensions and compression formats is given by the **\$CADP/src/com/cadp_zip** shell-script. This option does not influence the comparison between the two LTSs. Not a default option.

-diag [**-minimal**] [*diag*[**.bcg**]]

When the comparison of *lts1* and *lts2* yields FALSE, generate a diagnostic (counterexample) in BCG format (see the **bcg(LOCAL)** manual page for details) explaining this result. The diagnostic is generated in the file *diag.bcg* or, if the file name argument is missing, in file **bisimulator.bcg**. This option has no effect when the comparison of *lts1* and *lts2* yields TRUE, since in this case the diagnostic would be larger than *lts1* and *lts2*, and would not bring any useful information. The BCG file containing the diagnostic can be visualized using the **bcg_draw(LOCAL)** and **bcg_edit(LOCAL)** tools of CADP (see respective manual pages for details).

The diagnostic is a directed acyclic graph included (modulo the preorder corresponding to the equivalence relation considered) both in *lts1* and *lts2*. Each state *p* of the diagnostic corresponds to a couple of states (*q*, *r*) belonging to *lts1* and *lts2*, respectively; the portion of diagnostic going out of *p* illustrates why the two corresponding states *q* and *r* are not equivalent. The terminal states of the diagnostic have additional "error" outgoing transitions with labels of the form "Present in *lts2.bcg*: *b*" or "Absent in *lts2.bcg*: *b*", indicating that the action *b* does not occur either in *lts1*, or in *lts2*, respectively (*b* can be either a visible action, or the invisible action *tau*, see EQUIVALENCE RELATIONS below for naming conventions). Intuitively, all transition sequences contained in the diagnostic lead, when executed simultaneously in *lts1* and *lts2*, to states which are unrelated modulo the equivalence/preorder relation considered. Note that for weak equivalences, any transition *p1*--*b*-->*p2* in the diagnostic may correspond to sequences of the form *q1*--*tau**.*b*-->*q2* and *r1*--*tau**.*b*-->*r2* contained in *lts1* and *lts2*, respectively. Also, any transition *p1*--*tau*-->*p2* in the diagnostic may correspond to a sequence *q1*--*tau*-->*q2* contained in *lts1* and possibly to a sequence *r1*--*tau**-->*r2* contained in *lts2*, or vice-versa.

In the case of branching equivalence, the diagnostic may also contain some transitions of the form *p1*--*b*-->*p2* leading to sink states. Considering that *p1* corresponds to the couple of states (*q1*, *r1*), such a transition indicates the existence of two sequences of the form *q1*--*tau**-->*q2*--*b*-->*q3* and *r1*--*tau**-->*r2*--*b*-->*r3* in *lts1* and *lts2*, respectively, such that the states *q2* and *r2* are not branching equivalent. For each transition *p1*--*b*-->*p2* leading to a sink state in the diagnostic, the remainder of the diagnostic going out of *p1* illustrates the non equivalence of the states *q2* and *r2*. This

specific handling of branching equivalence is due to the nature of this relation, which (at the opposite of other relations, such as strong, observational, $\tau a^*.a$, and safety) requires that not only the target states of transitions, but also their source states are equivalent.

If the additional option **-minimal** is specified, a small-depth diagnostic is generated (the depth is guaranteed to be minimal only when the diagnostic is a tree).

If the diagnostic is a sequence of transitions, it will also be displayed on standard output using the SEQ format (see the **seq(LOCAL)** manual page for the definition of this format). Not a default option.

-stat Display statistical information about the resolution of the BES corresponding to the comparison of *lts1* and *lts2* modulo the equivalence/preorder relation considered. Not a default option.

-tauconfluence

Reduce *lts1* on-the-fly modulo tau-confluence (a form of partial order reduction that preserves branching equivalence) while performing the comparison with *lts2*. This option can be used only in conjunction with options **-branching** and **-observational**, and in some cases it may improve speed and memory consumption significantly. Not a default option.

EQUIVALENCE RELATIONS

An LTS is a quadruple $M = (Q, A, T, q0)$, where: Q is the set of *states*, A is the set of *actions* (transition labels), T included in $Q * A * Q$ is the *transition relation*, and $q0$ is the *initial state*. The set A contains the invisible action τ , which denotes internal (unobservable) activity. A transition (p, a, q) in T (also noted $p \xrightarrow{a} q$) means that the system can evolve from state p to state q by performing action a . If L is a language included in A^* , then $p \xrightarrow{L} q$ denotes a transition sequence $p \xrightarrow{a_1} q_2 \xrightarrow{a_2} \dots \xrightarrow{a_n} q$ such that the word $a_1 a_2 \dots a_n$ belongs to L . All states q of Q are assumed to be reachable from the initial state $q0$ via sequences of transitions in T (i.e., $q0 \xrightarrow{A^*} q$). In the sequel, visible actions of A are denoted by a , and (both visible and invisible) actions of A are denoted by b . The transitive and reflexive closure of T is denoted by T^* .

Two LTSs $M1 = (Q1, A, T1, q01)$ and $M2 = (Q2, A, T2, q02)$ are related modulo an equivalence relation R (noted $M1 R M2$) if and only if their initial states are related modulo R (noted $q01 R q02$). The equivalence relations currently supported by **bisimulator** are defined below. For each equivalence R_{equ} , the corresponding preorder relation L_{equ} , which indicates whether a state p is “simulated” by a state q (resp. q is “simulated” by p) is obtained by keeping only condition 1 (resp. 2) in the definition of R_{equ} .

Strong equivalence [Par81]

This is the largest relation R_{str} such that two states p and q are related modulo strong equivalence ($p R_{str} q$) if and only if:

1. for each transition $p \xrightarrow{b} p'$ in $T1$
there is a transition $q \xrightarrow{b} q'$ in $T2$
such that $p' R_{str} q'$
2. for each transition $q \xrightarrow{b} q'$ in $T2$
there is a transition $p \xrightarrow{b} p'$ in $T1$
such that $p' R_{str} q'$

Branching equivalence [GW89]

This is the largest relation R_{bra} such that two states p and q are related modulo branching equivalence ($p R_{bra} q$) if and only if:

1. for each transition $p \xrightarrow{b} p'$ in $T1$

- a. either $b = \tau$ and $p' R_{bra} q$, or
- b. there is a sequence $q \xrightarrow{\tau^*} q' \xrightarrow{b} q''$ in $T2^*$ such that $p R_{bra} q'$ and $p' R_{bra} q''$
- 2. for each transition $q \xrightarrow{b} q'$ in $T2$
 - a. either $b = \tau$ and $p R_{bra} q'$, or
 - b. there is a sequence $p \xrightarrow{\tau^*} p' \xrightarrow{b} p''$ in $T1^*$ such that $p' R_{bra} q$ and $p'' R_{bra} q'$

Observational equivalence [Mil89]

This is the largest relation R_{obs} such that two states p and q are related modulo observational equivalence ($p R_{obs} q$) if and only if:

- 1. a. for each transition $p \xrightarrow{\tau} p'$ in $T1$ there is a sequence $q \xrightarrow{\tau^*} q'$ in $T2^*$ such that $p' R_{obs} q'$
- b. for each transition $p \xrightarrow{a} p'$ in $T1$ there is a sequence $q \xrightarrow{\tau^*} q' \xrightarrow{a} q''$ in $T2^*$ such that $p' R_{obs} q''$
- 2. a. for each transition $q \xrightarrow{\tau} q'$ in $T2$ there is a sequence $p \xrightarrow{\tau^*} p'$ in $T1^*$ such that $p' R_{obs} q'$
- b. for each transition $q \xrightarrow{a} q'$ in $T2$ there is a sequence $p \xrightarrow{\tau^*} p' \xrightarrow{a} p''$ in $T1^*$ such that $p' R_{obs} p''$

 $\tau^*.a$ equivalence [FM91]

This is the largest relation $R_{\tau a}$ such that two states p and q are related modulo $\tau^*.a$ equivalence ($p R_{\tau a} q$) if and only if:

- 1. for each sequence $p \xrightarrow{\tau^*.a} p'$ in $T1^*$ there is a sequence $q \xrightarrow{\tau^*.a} q'$ in $T2^*$ such that $p' R_{\tau a} q'$
- 2. for each transition $q \xrightarrow{\tau^*.a} q'$ in $T2^*$ there is a sequence $p \xrightarrow{\tau^*.a} p'$ in $T1^*$ such that $p' R_{\tau a} q'$

Safety equivalence [BFG+91]

This is the largest relation R_{saf} such that two states p and q are related modulo safety equivalence ($p R_{saf} q$) if and only if:

- 1. $p I_{\tau a} q$
- 2. $q I_{\tau a} p$

Safety equivalence is defined in terms of the $\tau^*.a$ preorder $I_{\tau a}$. It is a *simulation equivalence* rather than a *bisimulation* (e.g., like $\tau^*.a$ equivalence), because it only requires that states p and q are included one into the other modulo $I_{\tau a}$, and does not require that each $\tau^*.a$ -successor of p (resp. q) is equivalent to a corresponding $\tau^*.a$ -successor of q (resp. p). Therefore, safety equivalence is weaker than $\tau^*.a$ equivalence (see the note below), but it has the same associated preorder (i.e., $I_{saf} = I_{\tau a}$).

Trace equivalence (a.k.a. language equivalence)

This is the largest relation R_{tra} such that two states p and q are related modulo trace equivalence

$(p R_{tra} q)$ if and only if:

1. for each sequence $p \xrightarrow{b1...bn} p'$ in $T1^*$
there is a sequence $q \xrightarrow{b1...bn} q'$ in $T2^*$
2. for each sequence $q \xrightarrow{b1...bn} q'$ in $T2^*$
there is a sequence $p \xrightarrow{b1...bn} p'$ in $T1^*$

Weak trace equivalence [BHR84]

Two states p and q are related modulo weak trace equivalence $(p R_{wtr} q)$ if and only if:

1. for each sequence $p \xrightarrow{\tau^*.a1...tau^*.an} p'$ in $T1^*$
there is a sequence $q \xrightarrow{\tau^*.a1...tau^*.an} q'$ in $T2^*$
2. for each sequence $q \xrightarrow{\tau^*.a1...tau^*.an} q'$ in $T2^*$
there is a sequence $p \xrightarrow{\tau^*.a1...tau^*.an} p'$ in $T1^*$

Note: A relation $R1$ is said to be *stronger* than another relation $R2$ (noted $R1 \leq R2$) iff $p R1 q$ implies $p R2 q$ for any states p, q . The relations above are ordered w.r.t. their strength as follows:

$$R_{str} \leq R_{bra} \leq R_{obs} \leq R_{saf} \leq R_{wtr}$$

$$R_{str} \leq R_{tra} \leq R_{wtr}$$

$$R_{bra} \leq R_{tau} \leq R_{saf}$$

As opposed to R_{str} and R_{tra} (the strong and trace equivalences), which handle all transition labels in the same way, the relations R_{bra} , R_{obs} , R_{tau} , R_{saf} , and R_{wtr} are called *weak* equivalences, since each of them performs a kind of abstraction over invisible actions.

Note: To obtain maximal performance, it is recommended to put the “bigger” LTS (the protocol) in argument *lts1* and the “smaller” LTS (the service) in argument *lts2*. In addition, the service LTS *lts2* can be minimized before comparison, either modulo strong equivalence (when strong equivalence is considered for comparing *lts1* and *lts2*), or modulo branching equivalence (if a weak equivalence is considered) using the **bcg_min**(LOCAL) tool of CADP (see the corresponding manual page for details). This restriction will be eliminated in a future version of **bisimulator**.

EXIT STATUS

Exit status is 0 if everything is alright, 1 otherwise.

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AUTHORS

Radu Mateescu, with the help of Damien Bergamini (both at INRIA/VASY), who implemented a first version of the encoding of branching equivalence in terms of boolean equation systems.

OPERANDS

<i>lts1.bcg</i>	BCG graph (input)
<i>lts1.exp</i>	network of communicating LTSs (input)
<i>lts1.lts</i>	FSP specification (input)
<i>lts1.lnt</i>	LNT specification (input)
<i>lts1.lotot</i>	LOTOS specification (input)
<i>lts1.seq</i>	sequence file (input)
<i>lts2.bcg</i>	BCG graph (input)
<i>diag.bcg</i>	diagnostic in BCG format (output)
<i>file.bes</i>	BES in textual format (output)

FILES

The binary code of **bisimulator** is available in \$CADP/bin./arch/bisimulator.a

SEE ALSO

bcg(LOCAL), **bcg.open**(LOCAL), **exp**(LOCAL), **exp.open**(LOCAL), **fsp.open**(LOCAL), **lnt.open**(LOCAL), **lotot.open**(LOCAL), **seq**(LOCAL), **seq.open**(LOCAL)

Additional information is available from the CADP Web page located at <http://cadp.inria.fr>

Directives for installation are given in files \$CADP/INSTALLATION_*.

Recent changes and improvements to this software are reported and commented in file \$CADP/HISTORY.

BUGS

Please report bugs to Radu.Mateescu@inria.fr