

## EUFAR FP7

N6SP - Standards and Protocols

# EGADS Algorithm Handbook

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# Chapter 1

# Introduction

This document contains descriptions of algorithms contained in the EGADS toolbox. Within each algorithm description is the following:

- Algorithm Name name of algorithm as implemented in EGADS.
- Category general category of algorithm. Algorithm can be found in this subdirectory in EGADS .
- Summary short description of what the algorithm does.
- Inputs expected inputs to algorithm. This field includes expected units, and data type of input.
- Outputs outputs produced by algorithm.
- Formula description of formulas or methods behind the algorithm.
- Source person, institution or entity who provided the algorithm.
- References any references to literature, journals or documents with more information on the current algorithm

To aid in algorithm usage and discovery, there is a general naming scheme for EGADS algorithms. Generally, algorithm names are composed as follows:

{measurement}\_{context/detail/instrument}\_{source}

So, for example, an algorithm provided by CNRM to calculate the density of dry air would be named density\_dry\_air\_cnrm.

# $egin{array}{c} ext{Part I} \ ext{Atmospheric} \end{array}$

# Chapter 2

# Thermodynamics



#### 2.1 Pressure altitude

Algorithm name: altitude\_pressure\_cnrm

Category: Thermodynamics

Summary: Calculates pressure altitude using virtual temperature.

#### Inputs:

| $T_v$ Vector        | Virtual temperature [K or °C]                    |
|---------------------|--|
| $P_s$ Vector        | Static pressure [hPa]                            |
| $P_{surface}$ Coeff | Surface pressure [hPa]                           |
| $R_a/g$ Coeff       | Gas constant of air over acceleration of gravity |

#### Outputs:

 $Alt_p$  Vector Pressure altitude [m]

Formula:

$$Alt_p = \frac{R_a}{g} T_v \log \left( \frac{P_{surface}}{P_s} \right)$$

Source: CNRM/GMEI/TRAMM

References:



# 2.2 Density of dry air

Algorithm name: density\_dry\_air\_cnrm

Category: Thermodynamics

Summary: Calculates density of dry air given static temperature and pressure.

#### Inputs:

| $P_s$ | Vector | Static pressure [hPa]        |  |
|-------|--------|------------------------------|--|
| $T_s$ | Vector | Static temperature [K or °C] |  |

#### **Outputs:**

| Ou                | tputs. |                               |
|-------------------|--------|-------------------------------|
| $\overline{\rho}$ | Vector | Density of dry air $[kg/m^3]$ |

#### Formula:

$$\rho = \frac{100 P_s}{R_a T_s}$$

with  $R_a = 287.05 \text{ J kg}^-1 \text{ K}^-1$ 

Density of humid air can be calculated using this same algorithm by using virtual temperature instead of static temperature.

Source: CNRM/GMEI/TRAMM

References: Equation d'état d'un gaz parfait, Triplet-Roche [9], page 34.



## 2.3 Relative humidity from capacitive probe

Algorithm name: hum\_rel\_capacitive\_cnrm

Category: Thermodynamics

Summary: Calculates relative humidity using the measured frequency from a capacitive

probe.

#### Inputs:

| $\overline{Ucapf}$ | Vector | Output frequency of the capacitive probe [Hz] |
|--------------------|--------|---|
| $T_s$              | Vector | Static temperature [K]                        |
| $P_s$              | Vector | Static pressure [hPa]                         |
| $\Delta P$         | Vector | Dynamic pressure [hPa]                        |
| $C_t$              | Coeff. | Temperature correction coefficient [%°C]      |
| $F_{min}$          | Coeff. | Minimal acceptable frequency [Hz]             |
| $C_0$              | Coeff. | 0th degree calibration coefficient            |
| $C_1$              | Coeff. | 1st degree calibration coefficient            |
| $C_2$              | Coeff. | 2nd degree calibration coefficient            |
|                    |        |   |

#### **Outputs:**

 $H_u$  Vector Relative humidity [%]

Formula: If  $Ucapf \leq F_{min}$  then  $Ucapf = F_{min}$ 

$$H_u = \frac{P_s}{P_s + \Delta P} \left[ C_0 + C_1 U cap f + C_2 U cap f^2 + C_t (T_s - 20) \right]$$

with  $T_s$  in  ${}^{\circ}C$ .

Source: CNRM/GMEI/TRAMM

References: CAM note on humidity instrument measurements. [1]



#### 2.4 Pressure and angle of incidence

Algorithm name: pressure\_angle\_incidence\_cnrm

Category: Thermodynamics

**Summary:** Calculates static pressure and dynamic pressure by correction of static error.

Angle of attack and sideslip are calculated from the horizontal and vertical

differential pressures.

#### **Inputs:**

| 1             |           |  |
|---------------|-----------|--|
| $P_{sr}$      | Vector    | Raw static pressure [hPa]                |
| $\Delta P_r$  | Vector    | Raw dynamic pressure [hPa]               |
| $\Delta P_h$  | Vector    | Horizontal differential pressure [hPa]   |
| $\Delta P_v$  | Vector    | Vertical differential pressure [hPa]     |
| $C_{\alpha}$  | Coeff.[2] | Angle of attack calibration coefficients |
| $C_{\beta}$   | Coeff.[2] | Slip calibration coefficients            |
| $C_{errstat}$ | Coeff.[4] | Static error coefficients                |
|               |           |  |

#### **Outputs:**

| -          |        |  |
|------------|--------|--|
| $P_s$      | Vector | Static Pressure [hPa]                              |
| $\Delta P$ | Vector | Dynamic pressure corrected with static error [hPa] |
| $\alpha$   | Vector | Angle of attack [rad]                              |
| $\beta$    | Vector | Sideslip [rad]                                     |

Formula: If  $\Delta P_r > 25$ hPa:

$$Errstat = C_{errstat}[0] + C_{errstat}[1]\Delta P_r + C_{errstat}[2]\Delta P_r^2 + C_{errstat}[3]\Delta P_r^3$$

otherwise:

$$Errstat = \frac{\Delta P_r}{25} \text{ Errstat @ 25 hPa}$$

$$P_s = P_{sr} - Errstat$$

$$\Delta P = \Delta P_r + Errstat$$

$$\alpha = C_{\alpha}[0] + C_{\alpha}[1] \frac{\Delta P_v}{\Delta P}$$

$$\beta = C_{\beta}[0] + C_{\beta}[1] \frac{\Delta P_h}{\Delta P}$$
(2.1)

Source: CNRM/GMEI/TRAMM

References:



## 2.5 Potential Temperature

Algorithm name: temp\_potential\_cnrm

Category: Thermodynamics

Summary: Calculates potential temperature.

#### Inputs:

| $T_s$        | Vector | Static temperature [K or oC]                           |
|--------------|--------|--|
| $P_s$        | Vector | Static pressure [hPa]                                  |
| $R_a/c_{pa}$ | Coeff. | Gas constant of air divided by specific heat of air at |
|              |        | constant pressure                                      |

#### **Outputs:**

 $\theta$  Vector Potential temperature [same unit as  $T_s$ ]

Formula:

$$\theta = T_s \left(\frac{1000}{P_s}\right)^{R_a/c_{pa}}$$

Source: CNRM/GMEI/TRAMM

References: Triplet-Roche [9].



#### 2.6 Equivalent Potential Temperature

Algorithm name: temp\_potential\_equiv\_cnrm

Category: Thermodynamics

Summary: Calculates equivalent potential temperature of air. The equivalent potential

temperature is the temperature a parcel of air would reach if all water vapor in the parcel condensed, and the parcel was brought adiabatially to 1000

hPa.

| inputs |
|--------|
|--------|

| $T_s$    | Vector | Static temperature [K or oC]                  |
|----------|--------|---|
| $\theta$ | Vector | Potential temperature [K or $\circ$ C]        |
| r        | Vector | Vater vapor mixing ratio [g/kg]               |
| $c_{pa}$ | Coeff. | Specific heat of dry air at constant pressure |
| Out      | outs:  |   |

 $\overline{\theta_e}$  Vector Equivalent potential temperature [same units as  $T_s$ ]

Formula:

$$\theta_e = \theta \left( 1 + r \frac{L}{c_{pa} T_s} \right)$$

where  $L = 3136.17 - 2.34T_s$  (for  $T_s$  in K)

Source: CNRM/GMEI/TRAMM

References: From the CAM routine which is identical to the algorithm P. Durand cited

in the formula book created for PYREX.



## 2.7 Static Temperature

Algorithm name: temp\_static\_cnrm

Category: Thermodynamics

Summary: Calculates static temperature of the air from total temperature. This method

applies to probe types such as the Rosemount.

#### Inputs:

| P                   |  |
|---------------------|--|
| $T_t$ Vector        | Measured total temperature [K]                         |
| $\Delta P$ Vector   | Dynamic pressure [hPa]                                 |
| $P_s$ Vector        | Static pressure [hPa]                                  |
| $r_f$ Coeff.        | Probe recovery coefficient                             |
| $R_a/c_{pa}$ Coeff. | Gas constant of air divided by specific heat of air at |
| · ·                 | constant pressure                                      |

#### **Outputs:**

 $T_s$  Vector Static temperature [K]

Formula:

$$T_s = \frac{T_t}{1 + r_f \left( \left( 1 + \frac{\Delta P}{P_s} \right)^{R_a/c_{pa}} - 1 \right)}$$

Source: CNRM/GMEI/TRAMM

References:



## 2.8 Virtual Temperature

Algorithm name: temp\_virtual\_cnrm

Category: Thermodynamics

Summary: Calculates the virtual temperature of air.

**Inputs:** 

| $T_s$ | Vector | Static temperature [K or oc]    |
|-------|--------|---------------------------------|
| r     | Vector | Water vapor mixing ratio [g/kg] |

Outputs:

 $T_v$  Vector Virtual temperature [same units as  $T_s$ ]

Formula:

$$T_v = T_s \frac{1 + (R_v/R_a)r}{1 + r}$$

where  $R_v/R_a = 1.608$ 

Source: CNRM/GMEI/TRAMM

References: Triplet-Roche [9], page 56.



#### 2.9 Mach number

Algorithm name: velocity\_mach\_raf

Category: Thermodynamics

Summary: Calculates the mach number based on dynamic and static pressure.

**Inputs:** 

| $\Delta P$ | Vector | Dynamic pressure [hPa] |
|------------|--------|------------------------|
| $P_s$      | Vector | Static pressure [hPa]  |

**Outputs:** 

M Vector Mach number

Formula:

$$M = \sqrt{\frac{2}{\gamma - 1} \left[ \left( \frac{\Delta P}{P_s} + 1 \right)^{\frac{\gamma - 1}{\gamma}} - 1 \right]}$$

Source: NCAR-EOL

References: NCAR-RAF Bulletin #23 [6]



#### 2.10 True air speed

Algorithm name: velocity\_tas\_cnrm

Category: Thermodynamics

Summary: Calculates true air speed based on static pressure, static temperature and

dynamic pressure using the Barré-St Venant formula.

#### **Inputs:**

| -            |        |  |
|--------------|--------|--|
| $T_s$        | Vector | Static temperature [K]                                 |
| $\Delta P$   | Vector | Dynamic pressure [hPa]                                 |
| $P_s$        | Vector | Static pressure [hPa]                                  |
| $c_{pa}$     | Coeff. | Specific heat of air at constant pressure (for dry air |
|              |        | $1004 \text{ J K}^{-1} \text{ kg}^{-1})$               |
| $R_a/c_{pa}$ | Coeff. | Gas constant of air divided by specific heat of air at |
|              |        | constant pressure                                      |

#### **Outputs:**

 $V_t$  Vector True air speed [m/s]

Formula:

$$V_t^2 = 2c_{pa}T_s \left[ \left( 1 + \frac{\Delta P}{P_s} \right)^{R_a/c_{pa}} - 1 \right]$$

Source: CNRM/GMEI/TRAMM

References: NCAR-RAF Bulletin #23 [6], Méchanique des fluides, Candel [3]



#### 2.11 True air speed

Algorithm name: velocity\_tas\_raf

Category: Thermodynamics

Summary: Calculates true air speed based on Mach number, measured temperature

and thermometer recovery factor. Typical values of the themometer recovery factor range from 0.75-0.9 for platinum wire ratiometer (flush bulb type)

thermometers, and around 1.0 for TAT type thermometers.

**Inputs:** 

| $T_r$ | Vector | Measured temperature [K]    |
|-------|--------|-----------------------------|
| M     | Vector | Mach number                 |
| e     | Coeff. | thermometer recovery factor |
|       |        |                             |

**Outputs:** 

 $V_t$  Vector True air speed [m/s]

Formula:

$$V_t = \sqrt{\frac{R\gamma T_r M^2}{1 + 0.5(\gamma - 1)eM^2}}$$

where the recovery factor e can be determined for a thermometer by comparing its measured temperature with the actual total and static temperature.

$$e \equiv \frac{T_r - T_s}{T_t - T_s}$$

Source: NCAR-EOL

References: NCAR-RAF Bulletin #23 [6]



## 2.12 Longitudinal true airspeed

Algorithm name: velocity\_tas\_longitudinal\_cnrm

Category: Thermodynamics

Summary: Calculates the true air speed along the longitudinal axis of the aircraft.

#### Inputs:

| $\overline{V_t}$ | Vector | True air speed [m/s]  |  |
|------------------|--------|-----------------------|--|
| $\alpha$         | Vector | Angle of attack [rad] |  |
| $\beta$          | Vector | Sideslip angle [rad]  |  |
|                  |        |                       |  |

#### **Outputs:**

 $V_{tx}$  Vector Longitudinal true air speed [m/s]

Formula:

$$V_{tx} = \frac{V_t}{\sqrt{1 + \tan^2 \alpha + \tan^2 \beta}}$$

Source: CNRM/GMEI/TRAMM

**References:** NCAR-RAF Bulletin #23 [6]

# Chapter 3

# Microphysics



#### 3.1 Effective diameter

Algorithm name: diameter\_effective\_dmt

Category: Microphysics

Summary: Calculates effective diameter of a size distribution. In general, this definition

is only meaningful for water clouds, and another form must be used when

in ice clouds.

Inputs:

| $c_i$ | Array[time, bins] | Number concentration of hydrometeors in size cate-                               |
|-------|-------------------|--|
| $d_i$ | Vector[bins]      | gory $i$ [cm <sup>-3</sup> ]<br>Average diameter in size category $i$ [ $\mu$ m] |
| Outp  | outs:             |  |

 $R_e$  Vector[time] Effective diameter [ $\mu$ m]

Formula:

$$D_e = \frac{\sum_{i=1}^{m} c_i d_i^3}{\sum_{i=1}^{m} c_i d_i^2}$$

Source:

References: "Data Analysis User's Guide Chapter I: Single Particle Light Scattering,"

Droplet Measurement Technologies, 30. [4]



#### 3.2 Mean diameter

Algorithm name: diameter\_mean\_raf

Category: Microphysics

Summary: Calculates the arithmetic average of all particle diameters given in a particle

size distribution.

Inputs:

 $n_i$  Array[time, bins] Number of particles in each channel i

 $d_i$  Vector[bins] Channel i size  $[\mu m]$ 

**Outputs:** 

 $\bar{D}$  Vector[time] Mean diameter  $[\mu m]$ 

Formula:

 $\bar{D} = \frac{\sum_{i} n_{i} d_{i}}{N_{t}}$ 

where  $N_t$  is the total number of particles.

Source: NCAR-RAF



#### 3.3 Median Volume Diameter

Algorithm name: diameter\_median\_volume\_dmt

Category: Microphysics

Summary: Calculates the median volume diameter given a size distribution. The

median volume diameter is the size of droplet below which 50% of the total

water volume resides.

Inputs:

| $c_i$   | Array[time, bins]     | Number concentration of hydrometeors in size cate-                 |
|---------|-----------------------|--|
|         |                       | gory $i \text{ [cm}^{-3}]$   |
| $d_i$   | Vector[bins]          | Average diameter of size category $i [\mu m]$                      |
| $ ho_i$ | Vector[bins],Optional | Density of hydrometeor in size category $i$ [g cm <sup>-3</sup> ]. |
|         |                       | Default is $\rho_w = 1.0 \text{ g cm}^-3$                          |
|         |                       |  |

**Outputs:** 

 $D_{mvd}$  Vector[time] Median volume diameter [ $\mu$ m]

Formula: Step 1: Compute liquid water content

$$W = \frac{\pi \rho_w}{6} \sum_{i=1}^m c_i d_i^3$$

Step 2: Beginning at the first size channel, calculate the accumulated mass  $S_n = w_1 + w_2 + ... w_n$  where  $w_1$  is the mass of water in channel 1, and  $w_n$  is the channel where the accumulated mass is greater than or equal to 0.5W, i.e. greater than or equal to 50% of the total LWC.

Step 3: Compute the median volume diameter,  $D_{mvd}$  by interpolating linearly between the channels that bracket where the accumulated mass exceeded the total LWC:

$$D_{mvd} = D_{n-1} + (0.5 - S_{n-1}/S_n)(D_n - D_{n-1})$$

Source:

References: "Data Analysis User's Guide Chapter I: Single Particle Light Scattering,"

Droplet Measurement Technologies, 33. [4]



## 3.4 Extinction Coefficient

Algorithm name: extinction\_coeff\_dmt

Category: Microphysics

Summary: Calculates extinction coefficient given a particle size distribution.

#### Inputs:

| $c_i$ | Array[time, bins]      | Number conentration of hydrometeors in size category |  |
|-------|------------------------|--|--|
|       |                        | $i  [\text{cm}^{-3}]$                                |  |
| $d_i$ | Vector[bins]           | Average diameter of size category $i [\mu m]$        |  |
| $Q_e$ | Vector[bins], Optional | Extinction efficiency; default is $Q_e = 2$          |  |
|       |                        |  |  |
| 04    | Outrocker              |  |  |

#### Outputs:

| $B_e$ | Vector[time] | Extinction coefficient [ | $\mathrm{km}^{-1}$ |  |
|-------|--------------|--------------------------|--------------------|--|

#### Formula:

$$B_e = \frac{\pi}{4} \sum_{i=1}^m Q_e c_i d_i^2$$

Source:

References: "Data Analysis User's Guide Chapter I: Single Particle Light Scattering,"

Droplet Measurement Technologies, 30.~[4]



#### 3.5 Mass Concentration

Algorithm name: mass\_conc\_dmt

Category: Microphysics

Summary: Calculates mass concentration given a size distribution. Can be used to

calculate liquid or ice water content depending on the types of hydrometeors

being sampled.

| Inputs | : |
|--------|---|
|        |   |

| PG      |                    |   |
|---------|--------------------|---|
| $c_i$   | Array[time, bins]  | Number concentration of hydrometeors in size cate-                  |
|         |                    | gory $i \text{ [cm}^{-3}]$  |
| $d_i$   | Vector[bins]       | Average diameter of size category $i \ [\mu m]$                     |
| $s_i$   | Array[time, bins]  | Shape factor of the hydrometeor of size category $i$ to             |
|         |                    | account for asphericity   |
| $ ho_i$ | Vector[time, bins] | Density of the hydrometeor in size category $i \text{ [g cm}^{-3}]$ |
|         |                    |   |

#### **Outputs:**

M Vector[time] Mass concentration [g cm<sup>-3</sup>]

Formula:

$$M = \frac{\pi}{6} \sum_{i=1}^{m} s_i \rho_i c_i d_i^3$$

Source:

References: "Data Analysis User's Guide Chapter I: Single Particle Light Scattering,"

Droplet Measurement Technologies, 30. [4]



## 3.6 Total Number Concentration (DMT)

Algorithm name: number\_conc\_total\_dmt

Category: Microphysics

Summary: Calculation of total number concentration given distribution of particle

counts from a particle sampling probe.

Inputs:

 $c_i$  Array[time, bins] Number concentration of hydrometeors in size category i [cm<sup>-3</sup>]

**Outputs:** 

N Vector[time] Total number concentration [cm<sup>-3</sup>]

Formula:

$$N = \sum_{i=1}^{m} c_i$$

Source:

References: "Data Analysis User's Guide Chapter I: Single Particle Light Scattering,"

Droplet Measurement Technologies, 30. [4]



#### 3.7 Total Number Concentration

Algorithm name: number\_conc\_total\_raf

Category: Microphysics

Summary: Calculation of total number concentration for a particle probe.

Inputs:

 $n_i$  Array Number of particles in each channel i SV Array Sample volume [m<sup>3</sup>]

Outputs:

 $N_t$  Vector Total number concentration [m<sup>-3</sup>]

Formula:

 $N_t = \frac{\sum_i n_i}{SV}$ 

Source: NCAR-RAF



#### 3.8 Sample area for imaging probes

Algorithm name: sample\_area\_oap\_all\_in\_raf

Category: Microphysics

Summary: Calculation of 'all in' sample area size for OAP probes such as the 2DC,

2DP, CIP, etc. This sample area varies by number of shadowed diodes. This

routine calculates a sample area per bin.

| Inputs: |
|---------|
|---------|

| )•     |                                      |
|--------|--------------------------------------|
| Coeff. | Laser wavelength [nm]                |
| Coeff. | Distance between probe arm tips [mm] |
| Coeff. | Diode diameter $[\mu m]$             |
| Coeff. | Probe magnification factor           |
| Coeff. | Number of diodes in array            |
|        |                                      |
| its:   |                                      |
| Vector | Sample area [m <sup>2</sup> ]        |
|        | Coeff. Coeff. Coeff. Coeff. Coeff.   |

# Formula:

$$DOF_{i} = \frac{6R_{i}^{2}}{\lambda}$$

$$R_{i} = i\frac{dD}{2}$$

$$X = 1 N$$
(3.1)

where DOF must be less than  $D_{arms}$ . The parameter i ranges from 1 to N.

$$ESW_i = \frac{dD(N - X_i - 1)}{M}$$

A value for  $ESW_i$  (effective sample width) is calculated for each X.

$$SA_i = (DOF_i)(ESW_i)$$

Source: NCAR-RAF



#### 3.9 Sample area for imaging probes

Algorithm name: sample\_area\_oap\_center\_in\_raf

Category: Microphysics

Summary: Calculation of 'center in' sample area size for OAP probes such as the 2DC,

2DP, CIP, etc. This sample area varies by number of shadowed diodes. This

routine is intended to calculate a sample area per bin.

Inputs:

| Inpatis                | •      |                                      |
|------------------------|--------|--------------------------------------|
| λ                      | Coeff. | Laser wavelength [nm]                |
| $D_{arms}$             | Coeff. | Distance between probe arm tips [mm] |
| $\mathrm{d}\mathrm{D}$ | Coeff. | Diode diameter $[\mu m]$             |
| M                      | Coeff. | Probe magnification factor           |
| N                      | Coeff. | Number of diodes in array            |
|                        |        |                                      |
| Outpu                  | ts:    |                                      |

Sample area [m<sup>2</sup>]  $\overline{SA}$ Vector

Formula:

$$DOF_{i} = \frac{6R_{i}^{2}}{\lambda}$$

$$R_{i} = X\frac{dD}{2}$$

$$X = 1 N$$
(3.2)

where DOF must be less than  $D_{arms}$ . The parameter i ranges from 1 to N.

$$ESW = NdD$$

$$SA_i = (DOF_i)(ESW)$$

Source: NCAR-RAF



## 3.10 Sample area for scattering probes

Algorithm name: sample\_area\_scattering\_raf

Category: Microphysics

Summary: Calculation of sample area for scattering probes such as the FSSP, CAS,

etc.

Inputs:

| DOF | Coeff. | Depth of field [m] |
|-----|--------|--------------------|
| BD  | Coeff. | Beam diameter [m]  |

Outputs:

SA Coeff. Sample area [m<sup>2</sup>]

Formula:

SA = (DOF)(BD)

Source: NCAR-RAF



# 3.11 Sample Volume

Algorithm name: sample\_volume\_general\_raf

Category: Microphysics

Summary: Calculates sample volume for microphysics probes (1D, 2D, FSSP, etc).

| Ι | nı | οι | $\mathbf{it}$ | s: |
|---|----|----|---------------|----|
|   |    |    |               |    |

| $V_t$ | Vector | True air speed [m/s]            |
|-------|--------|---------------------------------|
| SA    | Coeff. | Sample area of probe $[m^2]$    |
| $t_s$ | Coeff. | Sample rate [s]                 |
|       |        |                                 |
| Outp  | outs:  |                                 |
| SV    | Vector | Sample volume [m <sup>3</sup> ] |

Formula:

$$SV = V_t t_s SA$$

Source: NCAR-RAF



#### 3.12 Surface Area Concentration

Algorithm name: surface\_area\_conc\_dmt

Category: Microphysics

Summary: Calculation of surface area concentration given size distribution from particle

probe.

Inputs:

| $c_i$ | Array[time, bins] | Number concentration of hydrometeors in size cate-        |
|-------|-------------------|---|
|       |                   | gory $i  [\mathrm{cm}^{-3}]$                              |
| $d_i$ | Vector[bins]      | Average diameter of size category $i [\mu m]$             |
| $s_i$ | Array[time, bins] | Shape factor of hydrometeor in size category $i$ , to ac- |
|       |                   | count for asphericity                                     |

**Outputs:** 

S Vector[time] Surface area concentration  $[\mu m^2 \text{ cm}^{-3}]$ 

Formula:

$$S = \pi \sum_{i=1}^{m} s_i c_i d_i^2$$

Source:

References: "Data Analysis User's Guide Chapter I: Single Particle Light Scattering,"

Droplet Measurement Technologies, 30. [4]

# Chapter 4

# Radiation



#### 4.1 Solar Vector Computation

Algorithm name: solar\_vector\_blanco

Category: Radiation

Summary: This algorithm comuptes the current solar vector, given current date, time,

latitude and longitude. Algorithm is most accurate between 1999-2005, but calculations out to 2015 show the solar vector can be determined with an

error of less than 0.5 minutes of arc.

#### Inputs:

| -               |  |
|-----------------|--|
| Date_tim\vector | ISO String of current date/time in UTC [yyyymmd- |
|                 | dThhmmss]  |
| lat Vector      | Latitude [degrees]                               |
| long Vector     | Longitude [degrees]                              |

#### **Outputs:**

| $\overline{ra}$ | Vector | Right ascension [radians] |
|-----------------|--------|---------------------------|
| $\delta$        | Vector | Delcination [radians]     |
| $	heta_z$       | Vector | Solar Zenith [radians]    |
| $\gamma$        | Vector | Solar Azimuth [radians]   |

#### Formula:

$$jd = \frac{1461}{4}(y + 4800 + (m - 14)/12) + \frac{367}{12}(m - 2 - 12((m - 14)/12))$$
$$-\frac{3}{4}(y + 4900 + (m - 14)/12)/100 + d - 32075 - 0.5 + hour/24.0$$
$$jd = (1461(y + 4800 + (m - 14)/12))/4 + (367(m - 2 - 12((m - 14)/12)))/12$$
$$-(3((y + 4900 + (m - 14)/12)/100))/4 + d + 32075 - 0.5 + hour/24.0$$

where y is the year, m is the month, d is the day of the month and hour is the current hour in decimal format, i.e. with minutes and seconds as fractions of an hour. Note that all divisions in this calculation are integer divisions except the last.

The ecliptic coordinates of the sun are computed from the Julian Day by:

$$n=jd-2451545.0$$
 
$$\Omega=2.1429-0.0010394594n$$
 
$$L \ (\text{mean longitude}) = 4.8950630+0.017202791698n$$
 
$$g \ (\text{mean anomaly}) = 6.2400600+0.0172019699n$$
 
$$l \ (\text{ecliptic longitude}) = L+0.03341607\sin g+0.00034894\sin 2g-0.0001134-0.0000203\sin \Omega$$
 
$$ep \ (\text{obliquity of the ecliptic}) = 0.4090928-6.2140\times 10^{-9}n+0.0000396\cos \Omega$$



The conversion from ecliptic coordinates to celestial coordinates is computed by:

$$ra ext{ (right ascension)} = \tan^{-1} \left[ \frac{\cos ep \sin l}{\cos l} \right]$$
  
 $\delta ext{ (declination)} = \sin^{-1} [\sin ep \sin l]$ 

where ra must be between 0 and  $2\pi$ .

The conversion between celestial coordinates to horizontal coordinates is then computed by the following equations:

$$gmst = 6.6974243242 + 0.0657098283n + hour$$
 
$$lmst = \frac{pi}{180}(15gmst + long)$$
 
$$\omega \text{ (hour angle)} = lmst - ra$$
 
$$\theta_z = \cos^{-1}[\cos lat \cos \omega \cos \delta + \sin \delta \sin lat]$$
 
$$\gamma = \tan^{-1}\left[\frac{-\sin \omega}{\tan \delta \cos lat - \sin lat \cos \omega}\right]$$
 
$$Parallax = \frac{EarthMeanRadius}{AstronomicalUnit}\sin \theta_z$$
 
$$\theta_z = \theta_z + Parallax$$

where: EarthMeanRadius = 6371.01 km and AstronomicalUnit = 149597890 km

#### Source:

References: Manuel Blanco-Muriel, et al., "Computing the Solar Vector," Solar Energy

70 (2001): 436-38. [2]



#### 4.2 Solar Vector Calculation (Reda-Andreas)

Algorithm name: solar\_vector\_reda

Category: Radiation

Summary: This algorithm calculates the current solar vector based on time, latitude and

longitude inputs. It accepts optional pressure and temperature arguments to correct for atmospheric refraction effects. The zenith and azimuth angle calculated by this algorithm have uncertainties equal to  $\pm 0.0003^{\circ}$  in the

period from the year -2000 to 6000.

Inputs:

| 1      |                  |  |
|--------|------------------|--|
| Date_t | tim\vector       | ISO String of current date/time in UTC [yyyymmd- |
|        |                  | dThhmmss]  |
| lat    | Vector           | Latitude [degrees]                               |
| long   | Vector           | Longitude [degrees]                              |
| E      | Vector           | Elevation [m]                                    |
| P      | Vector, Optional | Local pressure [hPa]                             |
| T      | Vector, Optional | Local temperature [°C]                           |
|        |                  |  |

#### **Outputs:**

|          | -      |                         |
|----------|--------|-------------------------|
| $\theta$ | Vector | Solar Zenith [degrees]  |
| $\Phi$   | Vector | Solar Azimuth [degrees] |

#### Formula:

- 1. Calculate Julian and Julian Ephemeris Day, Century and Millenuim:
  - (a) Calculate Julian Day (JD):

$$JD = INT(365.25(Y + 4716)) + INT(30.6001(M + 1)) + D + B - 1524.5$$

where:

- INT is the integer of the calculated terms (e.g. 8.7 = 8, 8.2 = 8, etc)
- $\bullet$  Y is the year
- M is the month of the year. If  $M \le 2$  then Y = Y 1 and M = M + 12
- D is the day of the month with decimal time (i.e. with fractions of the day being represented after the decimal point.)
- B is equal to 0 for the Julian Calendar, and equal to (2 A + INT(A/4)) for the Gregorian calendar, where A = INT(Y/100)
- (b) Calculate Julian Ephemeris Day (*JDE*):

$$JDE = JD + \frac{\Delta T}{86400}$$

Where  $\Delta T$  is the difference between the Earth rotation time and the Terrestrial Time. It is reported yearly in the Astronomical Almanac [?].



(c) Calculate Julian Century (JC) and the Julian Ephemeris Century (JCE) for the 2000 standard epoch:

$$JC = \frac{JD - 2451545}{36525}$$
 
$$JCE = \frac{JDE - 2451545}{36525}$$

(d) Calculate the Julian Ephemeris Millenium (JME) for the 2000 standard epoch:

$$JME = \frac{JCE}{10}$$

- 2. Calculate Earth heliocentric longitude, latitude and radius vector (L, B, and R):
  - (a) Calculate  $L0_i$  and L0:

$$L0_{i} = A_{i} \cos(B_{i} + C_{i} \times JME)$$

$$L0 = \sum_{i=0}^{n} L0_{i}$$

Where the terms  $A_i$ ,  $B_i$  and  $C_i$  are based on values found in table A4.2 of the algorithm literature [8].

- (b) Calculate the terms L1, L2, L3, L4 and L5 by using these same equations, but using the appropriate terms from the table.
- (c) Calculate the Earth heleocentric longitude (in radians):

$$L = 10^{-8} (L0 + L1 \times JME + L2 \times JME^{2} + L3 \times JME^{3} + L4 \times JME^{4} + L5 \times JME^{5})$$

- (d) Convert L to degrees and limit between  $0^{\circ}$  and  $360^{\circ}$ .
- (e) Calculate the Earth heliocentric latitude B by using table A4.2 and repeating steps (a)-(c) using the appropriate values. Then convert B to degrees. Note that there are no B2 through B5.
- (f) Calculate the Earth radius vector R (in AU) in a similar manner by repeating steps (a)-(c) and using the appropriate values from table A4.2.
- 3. Calculate the geocentric longitude and latitude ( $\Theta$  and  $\beta$ ):

$$\Theta = L + 180$$
$$\beta = -B$$

Where  $\Theta$  must be limited between  $0^{\circ}$  and  $360^{\circ}$ .

- 4. Calculate the nutation in logitude and obliquity ( $\Delta \psi$  and  $\Delta \epsilon$ ):
  - (a) Calculate the mean elongation of the moon from the sun (in degrees):

$$X_0 = 297.85036 + 445267.11480JCE - 0.0019142JCE^2 + \frac{JCE^3}{189474}$$



(b) Calculate the mean anomaly of the sun (in degrees):

$$X_1 = 357.52772 + 35999.050340JCE - 0.0001603JCE^2 - \frac{JCE^3}{3000000}$$

(c) Calculate the mean anomaly of the moon (in degrees):

$$X_2 = 134.96298 + 477198.867398JCE + 0.0086972JCE^2 + \frac{JCE^3}{56250}$$

(d) Calculate the moon's argument of latitude (in degrees):

$$X_3 = 93.27191 + 483202.017538JCE - 0.0036825JCE^2 + \frac{JCE^3}{327270}$$

(e) Caluclate the longitude of the ascending node of the moon's mean orbit on the ecliptic, measured from the mean equinox of the date (in degrees):

$$X_4 = 125.04452 - 1934.136261JCE + 0.0020708JCE^2 + \frac{JCE^3}{450000}$$

(f) For each row in table A4.3, calculate the terms  $\Delta \psi$  and  $\Delta \epsilon$  (in 0.0001 of arc seconds):

$$\Delta \psi_i = (a_i + b_i JCE) \sin \left( \sum_{j=0}^4 X_j Y_{i,j} \right)$$
$$\Delta \epsilon_i = (c_i + d_i JCE) \cos \left( \sum_{j=0}^4 X_j Y_{i,j} \right)$$

where:

- $a_i$ ,  $b_i$ ,  $c_i$  and  $d_i$  are the values listed in the *i*th row and columns a, b c and d in Table A4.3.
- $X_i$  are the X values calculated above
- $Y_{i,j}$  are the values in row i and jth Y column in table A4.3.
- (g) Calculate the nutation in longitude and obliquity (in degrees):

$$\Delta \psi = \frac{\sum_{i=0}^{63} \Delta \psi_i}{36000000}$$

$$\Delta \epsilon = \frac{\sum_{i=0}^{63} \Delta \epsilon_i}{36000000}$$

5. Calculate the true obliquity of the ecliptic (in degrees):

$$U = JME/10$$

$$\epsilon_0 = 84381.448 - 4680.93U - 1.55U^2 + 1999.25U^3 - 51.38U^4$$

$$- 249.67U^5 - 39.05U^6 + 7.12U^7 + 27.87U^8 + 5.79U^9 + 2.45U^{10}$$

$$\epsilon = \epsilon_0/3600 + \Delta \epsilon$$



6. Calculate the aberration correction (in degrees):

$$\Delta \tau = -\frac{20.4898}{3600R}$$

7. Calculate the apparent sun longitude (in degrees):

$$\lambda = \Theta + \Delta \psi + \Delta \tau$$

8. Calculate the apparent sidereal time at Greenwich at any given time (in degrees):

$$\nu_0 = 280.46061837 + 360.98564736629(JD - 2451545) + 0.000387933JC^2 - \frac{JC^3}{38710000}$$
$$\nu = \nu_0 + \Delta\psi\cos\epsilon$$

where  $\nu_0$  must be limited to the range from  $0^{\circ}$  to  $360^{\circ}$ .

9. Calculate the geocentric sun right ascension (in degrees):

$$\alpha = \frac{180}{\pi} \tan^{-1} \left( \frac{\sin \lambda \cos \epsilon - \tan \beta \sin \epsilon}{\cos \lambda} \right)$$

where, as before,  $\alpha$  must be limited to the range from  $0^{\circ}$  to  $360^{\circ}$ .

10. Calculate the geocentric sun declination  $\delta$  (in degrees):

$$\delta = \frac{180}{\pi} \sin^{-1}(\sin \beta \cos \epsilon + \cos \beta \sin \epsilon \sin \lambda)$$

11. Calculate the observer local hour angle (in degrees):

$$H = \nu + long - \alpha$$

Limit H from  $0^{\circ}$  to  $360^{\circ}$ , and note that in this algorithm H is measured westward from south.

- 12. Calculate the topocentric sun right ascension and declination (in degrees):
  - (a) Calculate the equatorial horizontal parallax of the sun (in degrees):

$$\xi = \frac{8.794}{3600R}$$

(b) Calculate the terms u (in radians), x and y:

$$u = \tan^{-1}(0.99664719 \tan lat)$$

$$x = \cos u + \frac{E}{6378140} \cos lat$$

$$y = 0.99664719 \sin u + \frac{E}{6378140} \sin lat$$



(c) Calculate the parallax in the sun right ascension (in degrees):

$$\Delta \alpha = \frac{180}{\pi} \tan^{-1} \left( \frac{-x \sin \xi \sin H}{\cos \delta - x \sin \xi \cos H} \right)$$

(d) Calculate the topocentric sun right ascension and declination (in degrees):

$$\alpha' = \alpha + \Delta \alpha$$
$$\delta' = \tan^{-1} \left( \frac{(\sin \delta - y \sin \xi) \cos \Delta \alpha}{\cos \delta - x \sin \xi \cos H} \right)$$

13. Calculate the topocentric local hour angle (in degrees):

$$H' = H - \Delta \alpha$$

- 14. Calculate the topocentric zenith angle (in degrees):
  - (a) Calculate the topocentric elevation angle without atmospheric correction (in degrees):

$$e_0 = \frac{180}{\pi} \sin^{-1}(\sin lat \sin \delta' + \cos lat \cos \delta' \cos H')$$

(b) Calculate the atmospheric refraction correction (in degrees):

$$\Delta e = \frac{P}{1010} \frac{283}{(T+273)} \frac{1.02}{60 \tan \left(e_0 + \frac{10.3}{e_0 + 5.11}\right)}$$

Note that this step is skipped if temperature and pressure are not provided by the user. Also note that the argument for the tangent is computed in degrees. A conversion to radians may be needed if required by your computer or calculator.

(c) Calculate the topocentric elevation angle (in degrees):

$$e = e_0 + \Delta e$$

(d) Calculate the topocentric zenith angle (in degrees):

$$\theta = 90 - e$$

15. Calculate the topocentric azimuth angle (in degrees):

$$\Phi = \frac{180}{\pi} \tan^{-1} \left( \frac{\sin H'}{\cos H' \sin lat - \tan \delta' \cos lat} \right) + 180$$

Limit  $\Phi$  from  $0^{\circ}$  to  $360^{\circ}$ . Note that  $\Phi$  is measured eastward from north.

#### Source:

References: Reda and Andreas, "Solar Position Algorithm for Solar Radiation Applications," National Renewable Energy Laboratory, Revised 2008, accessed February 14, 2012, http://www.nrel.gov/docs/fy08osti/34302.pdf. [8]

# Chapter 5

## Corrections



#### 5.1 Simple correction of spikes

Algorithm name: correction\_spike\_simple\_cnrm

Category: Corrections

Summary: Detection of spikes which exceed a specified threshold. The detected value

is replaced with the mean of the surrounding values.

This algorithm does not apply well to variables that are naturally discontinuous.

| рu | $\mathbf{ts}$ |
|----|---------------|
|    |               |
|    | pu            |

| 1              |        |   |
|----------------|--------|---|
| $\overline{X}$ | Vector | Parameter for analysis                                  |
| $S_0$          | Coeff  | Spike detection threshold (same units as $X$ , and must |
|                |        | be positive)  |

#### Outputs:

 $X_c$  Vector Parameter with corrections applied

Formula: The *i*th term is considered a spike if:

$$||X[i] - X[i-1]|| > S_0 (5.1)$$

$$||X[i] - X[i+1]|| > S_0 \tag{5.2}$$

$$(X[i] - X[i-1])(X[i] - X[i+1]) > 0 (5.3)$$

with

$$X_c[i] = \frac{X[i+1]+X[i-1]}{2}$$

Otherwise,  $X_c[i] = X[i]$ 

Source: CNRM/GMEI/TRAMM

References:

# $\begin{array}{c} {\rm Part~II} \\ {\rm Hyperspectral} \end{array}$

Chapter 6

Biophysics



#### 6.1 NDVI

**Algorithm name:** biophys\_indices (NDVI is one index calculated within the overall program)

Category: Biophysics - broad band VIS

Summary: Calculation of Normalised Difference Vegetation index (NDVI)

**Inputs:** Multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 671nm and 864nm.

Outputs: Single band with NDVI values

Formula:

$$NDVI = \frac{R_{864} - R_{671}}{R_{864} + R_{671}}$$

Source: DLR-DFD

References: Rouse, J. W., Haas, R. H., Schell, J. A. and Deering, J. A. (1973). Moni-

toring vegetation systems in the great plains with erts. In: Proceedings of the Third Symposium on Significant Results Obtained with ERTS Vol. 1,

p. 309317



#### 6.2 RVI

Algorithm name: biophys\_indices (RVI is one index calculated within the overall

program)

Category: Biophysics - broad band VIS

Summary: Calculation of Ratio Vegetation index (RVI)

**Inputs:** Multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 671nm and 864nm.

Outputs: Single band with RVI values

Formula:

$$RVI = \frac{R_{864}}{R_{671}}$$

Source: DLR-DFD

References: Pearson, R. L., and L. D. Miller, 1972, Remote mapping of standing

crop biomass for estimation of the productivity of the short-grass Prairie, Pawnee National Grassland, Colorado: 8th international symposium on

remote sensing of environment, p. 1357-1381



#### 6.3 MCARI

**Algorithm name:** biophys\_indices (MCARI is one index calculated within the overall program)

Category: Biophysics - narrow band chlorophyll indices

Summary: Calculation of Modified Chlorophyll absorption in Reflectance Index (MCARI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 550nm, 670nm and 701nm.

Outputs: Single band with MCARI values

Formula:

$$MCARI = ((R_{701} - R_{670}) - 0.2 * (R_{701} - R_{550})) * \frac{R_{701}}{R_{670}}$$

Source: DLR-DFD

References: Daughtry, C.S.T., Walthall, C.L., Kim, M.S., Brown de Colstoun, E.,

McMurtrey, J.E. III (2000): Estimating corn leaf chlorophyll concentration from leaf and canopy reflectance. In: Remote Sensing of Environment, 74,

p.229-239.



#### 6.4 LCI

Algorithm name: biophys\_indices (LCI is one index calculated within the overall

program)

Category: Biophysics - narrow band chlorophyll indices

Summary: Calculation of Leaf Chlorophyll Index (LCI)

**Inputs:** Multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 710nm and 850nm.

Outputs: Single band with LCI values

Formula:

$$LCI = \frac{R_{850} - R_{710}}{R_{850} + R_{710}}$$

Source: DLR-DFD

References:



#### 6.5 SR705

**Algorithm name:** biophys\_indices (SR705 is one index calculated within the overall program)

Category: Biophysics - narrow band chlorophyll indices

Summary: Calculation of Chlorophyll-Index SR705 // Linear regression

**Inputs:** Multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 705nm and 750nm.

Outputs: Single band with SR705 values

Formula:

$$SR705 = \frac{R_{750}}{R_{705}}$$

Source: DLR-DFD

References: Sims, D.A., Gamon, J.A., 2002, Relationships between leaf pigment content

and spectral reflectance across a wide range of species, leaf structures and developmental stages. In: Remote Sensing of Environment, p. 337-354



#### 6.6 mND705

**Algorithm name:** biophys\_indices (mND705 is one index calculated within the overall program)

Category: Biophysics - narrow band chlorophyll indices

Summary: Calculation of Chlorophyll-Index mND705 // hyperbolic regression

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 445nm, 705nm and 750nm.

Outputs: Single band with mND705 values

Formula:

$$mND705 = \frac{R_{750} - R_{705}}{R_{750} + R_{705} - 2R_{445}}$$

Source: DLR-DFD

References: Sims, D.A., Gamon, J.A. (2002): Relationships between leaf pigment con-

tent and spectral reflectance across a wide range of species, leaf structures and developmental stages. In: Remote Sensing of Environment, 81, p.337-

354.



#### 6.7 GI

**Algorithm name:** biophys\_indices (GI is one index calculated within the overall program)

Category: Biophysics - narrow band chlorophyll indices

Summary: Calculation of Greenness Index (GI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 549nm and 671nm.

Outputs: Single band with GI values

Formula:

$$GI = \frac{R_{671}}{R_{549}}$$

Source: DLR-DFD

References: Zarco Tejada, P.J., Berjon, A., Lopez Lozano, R., Miller, J.R., Martin,

P., Cachorro, V., Gonzalez, M.R., de Frutos, A. (2005): Assessing vineyard condition with hyperspectral indices: Leaf and canopy reflectance simulation in a row-structured discontinuous canopy. In: remote Sensing of

Environment, 99, p.271 287



#### 6.8 PRI

Algorithm name: biophys\_indices (PRI is one index calculated within the overall

program)

Category: Biophysics - narrow band chlorophyll indices

Summary: Calculation of Photochemical Reflectance Index (PRI), also Carotenoid/chlorophyll

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 529nm and 569nm.

Outputs: Single band with PRI values

Formula:

$$PRI = \frac{R_{529} - R_{569}}{R_{529} + R_{569}}$$

Source: DLR-DFD

References: Sims, D.A., Gamon, J.A. (2002): Relationships between leaf pigment con-

tent and spectral reflectance across a wide range of species, leaf structures and developmental stages. In: Remote Sensing of Environment, 81, p.337-

354.



#### **6.9** REIP

**Algorithm name:** biophys\_indices (REIP is one index calculated within the overall program)

Category: Biophysics - red edge parametrisation

Summary: Calculation of red edge infliction point (REIP), method 1

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 671nm, 701nm, 740nm and 780nm.

Outputs: Single band with REIP values

Formula:

$$REIP = 700 + 40 * \frac{0.5 * (R_{671} + R_{780}) - R_{701}}{R_{740} - R_{701}}$$

Source: DLR-DFD

References: Guyot, G., Baret, F. and Major, D. J. (1988). High spectral resolution:

determination of spectral shifts between the red and the near infrared. In: International Archives of Photogrammetry and Remote Sensing 11, p.

750760



#### 6.10 DGVI1

**Algorithm name:** biophys\_indices (DGVI1 is one index calculated within the overall program)

Category: Biophysics - red edge parametrisation

Summary: Calculation of Derivative-based Green Vegetation Index (DGVI). Surface

under curve of first derivative between 626nm and 795nm.

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 626nm and 795nm.

Outputs: Single band with DGVI1 values

Formula:

$$DGVI1 = \int_{\lambda_1 = 626nm}^{\lambda_2 = 795nm} \mid \frac{d\rho}{d\lambda} \mid d\lambda$$

Source: DLR-DFD

References: Elvidge, C.D., Chen, Z.(1995): Comparison of Broad-Band and Narrow-

Band Red and Near-Infrared Vegetation indices. In: Remote Sensing of

Environment, 54, p.38-48.



#### 6.11 DGVI2

**Algorithm name:** biophys\_indices (DGVI2 is one index calculated within the overall program)

Category: Biophysics - red edge parametrisation

Summary: Calculation of Derivative-based Green Vegetation Index (DGVI). Surface

under curve of second derivative between 626nm and 795nm.

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 626nm and 795nm.

Outputs: Single band with DGVI2 values

Formula:

$$DGVI2 = \int_{\lambda_1 = 626nm}^{\lambda_2 = 795nm} \mid \frac{d\rho}{d^2\lambda} \mid d\lambda$$

Source: DLR-DFD

References: Elvidge, C.D., Chen, Z.(1995): Comparison of Broad-Band and Narrow-

Band Red and Near-Infrared Vegetation indices. In: Remote Sensing of

Environment, 54, p.38-48.



#### 6.12 NDNI

**Algorithm name:** biophys\_indices (NDNI is one index calculated within the overall program)

Category: Biophysics - dry vegetation (stress) indices

Summary: Calculation of Normalized Difference Nitrogen Index (NDNI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 1510nm and 1680nm.

Outputs: Single band with NDNI values

Formula:

$$NDNI = \frac{\log \frac{1}{R_{1510}} - \log \frac{1}{R_{1680}}}{\log \frac{1}{R_{1510}} + \log \frac{1}{R_{1680}}}$$

Source: DLR-DFD

References: Serrano, L., Penuelas, J., Ustin, L.S. (2002): Remote sensing of nitrogen

and lignin in Mediterranean vegetaion from AVIRIS data: Decomposing biochemical from structural signals. In: Remote Sensing of Environment,

81, p.355-364



#### 6.13 NDLI

**Algorithm name:** biophys\_indices (NDLI is one index calculated within the overall program)

Category: Biophysics - dry vegetation (stress) indices

Summary: Calculation of Normalized Difference Lignin Index (NDLI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 1754nm and 1680nm.

Outputs: Single band with NDLI values

Formula:

$$NDLI = \frac{\log \frac{1}{R_{1754}} - \log \frac{1}{R_{1680}}}{\log \frac{1}{R_{1754}} + \log \frac{1}{R_{1680}}}$$

Source: DLR-DFD

References: Serrano, L., Penuelas, J., Ustin, L.S. (2002): Remote sensing of nitrogen

and lignin in Mediterranean vegetaion from AVIRIS data: Decomposing biochemical from structural signals. In: Remote Sensing of Environment,

81, p.355-364



#### 6.14 CAI

Algorithm name: biophys\_indices (CAI is one index calculated within the overall

program)

Category: Biophysics - dry vegetation (stress) indices

Summary: Calculation of Cellulose Absorption Index (CAI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 2000nm, 2100nm and 2200nm.

Outputs: Single band with CAI values

Formula:

$$CAI = 0.5 * (R_{2000} + R_{2200}) - R_{2100}$$

Source: DLR-DFD

References: Nagler, P.L., Daughtry, C.S.T., Goward, S.N. (2000): Plant Litter and Soil

Reflectance. In: Remote Sensing of Environment, 71, P.207-215.



#### 6.15 CSI2

Algorithm name: biophys\_indices (CSI2 is one index calculated within the overall

program)

Category: Biophysics - dry vegetation (stress) indices

Summary: Calculation of Carter stress index 2 (CSI2)

Inputs: Narrow band multi- or hyperspectral imagery (ENVI standard image data)

including channels close to the wavelengths of 695nm and 760nm.

Outputs: Single band with CSI2 values

Formula:

$$CSI2 = \frac{R_{695}}{R_{760}}$$

Source: DLR-DFD

References: Carter et al., 1994/6



#### 6.16 NDWI

**Algorithm name:** biophys\_indices (NDWI is one index calculated within the overall program)

Category: Biophysics - water (stress) indices

Summary: Calculation of Normalized Difference Water Index (NDWI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 864nm and 1245nm.

Outputs: Single band with NDWI values

Formula:

$$NDWI = \frac{R_{864} - R_{1245}}{R_{864} + R_{1245}}$$

Source: DLR-DFD

References: Gao, Bo-Cai (1996): NDWI A Normalized Difference Water Index for

Remote Sensing of Vegetation liquid Water from Space. In: Remote Sensing

of Environment, 58, p.257-266



#### 6.17 NDWI\_MIR

**Algorithm name:** biophys\_indices (NDWI\_MIR is one index calculated within the overall program)

Category: Biophysics - water (stress) indices

Summary: Calculation of Normalized Difference Water Index - Mid Infrared (NDWI\_MIR)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 864nm and 2161nm.

Outputs: Single band with NDWI\_MIR values

Formula:

$$NDWI\_MIR = \frac{R_{864} - R_{2161}}{R_{864} + R_{2161}}$$

Source: DLR-DFD

References:



#### 6.18 LWVI1

**Algorithm name:** biophys\_indices (LWVI1 is one index calculated within the overall program)

Category: Biophysics - water (stress) indices

Summary: Calculation of Leaf Water Vegetation Index (LWVI-1)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 983nm and 1094nm.

Outputs: Single band with LWVI1 values

Formula:

$$LWVI1 = \frac{R_{1094} - R_{983}}{R_{1094} + R_{983}}$$

Source: DLR-DFD

References: Galvao, L.S., Formaggio, A.R., Tisot, D.A. (2005): Discriminating of

sugarcane varieties in Southeastern Brazil with EO-1 Hyperion data. In:

Remote Sensing of Environment, 94, p.523-534



#### 6.19 LWVI2

**Algorithm name:** biophys\_indices (LWVI2 is one index calculated within the overall program)

Category: Biophysics - water (stress) indices

Summary: Calculation of Leaf Water Vegetation Index (LWVI-2)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 1094nm and 1205nm.

Outputs: Single band with LWVI2 values

Formula:

$$LWVI2 = \frac{R_{1094} - R_{1205}}{R_{1094} + R_{1205}}$$

Source: DLR-DFD

References: Galvao, L.S., Formaggio, A.R., Tisot, D.A. (2005): Discriminating of

sugarcane varaieties in Southeastern Brazil with EO-1 Hyperion data. In:

Remote Sensing of Environment, 94, p.523-534



#### 6.20 DWSI5

**Algorithm name:** biophys\_indices (DWSI5 is one index calculated within the overall program)

Category: Biophysics - water (stress) indices

Summary: Calculation of Disease Water Stress Index (DWSI-5)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 549nm, 680nm, 803nm and 1659nm.

Outputs: Single band with DWSI5 values

Formula:

$$DWSI5 = \frac{R_{803} + R_{549}}{R_{1659} + R_{680}}$$

Source: DLR-DFD

References: Apan et al., 2003



#### **6.21 SWIRVI**

**Algorithm name:** biophys\_indices (SWIRVI is one index calculated within the overall program)

Category: Biophysics - cover indices

Summary: Calculation SWIR index: green (SWIRVI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 2090nm, 2210nm and 2280nm.

Outputs: Single band with SWIRVI values

Formula:

$$SWIRVI = 37.72 * (R_{2210} - R_{2090}) + 26.27 * (R_{2280} - R_{2090}) + 0.57$$

Source: DLR-DFD

References: Lobell, D.B., Asner, G.P., Law, B.E., Treuhaft R.N. (2001): Subpixel

can opy cover estimation of coniferous forests in Oregon using SWIR imaging spectrometry. In: Journal of geophysical research, 106, p.5151-5160



#### 6.22 SWIRLI

**Algorithm name:** biophys\_indices (SWIRLI is one index calculated within the overall program)

Category: Biophysics - cover indices

Summary: Calculation SWIR index: litter (SWIRLI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 2090nm, 2210nm and 2280nm.

Outputs: Single band with SWIRLI values

Formula:

$$SWIRLI = 3.87 * (R_{2210} - R_{2090}) - 27.51 * (R_{2280} - R_{2090}) - 0.20$$

Source: DLR-DFD

References: Lobell, D.B., Asner, G.P., Law, B.E., Treuhaft R.N. (2001): Subpixel

can opy cover estimation of coniferous forests in Oregon using SWIR imaging spectrometry. In: Journal of geophysical research, 106, p.5151-5160



#### **6.23** SWIRSI

**Algorithm name:** biophys\_indices (SWIRSI is one index calculated within the overall program)

Category: Biophysics - cover indices

Summary: Calculation SWIR index: soil (SWIRSI)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 2090nm, 2210nm and 2280nm.

Outputs: Single band with SWIRSI values

Formula:

$$SWIRSI = -41.59 * (R_{2210} - R_{2090}) + 1.24 * (R_{2280} - R_{2090}) + 0.64$$

Source: DLR-DFD

References: Lobell, D.B., Asner, G.P., Law, B.E., Treuhaft R.N. (2001): Subpixel

can opy cover estimation of coniferous forests in Oregon using SWIR imaging spectrometry. In: Journal of geophysical research, 106, p.5151-5160



#### 6.24 clay\_1

**Algorithm name:** biophys\_indices (clay\_1 is one index calculated within the overall program)

Category: Biophysics - soil indices

Summary: Calculation of clay ratio (clay\_1)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 2136nm, 2195nm and 2240nm.

Outputs: Single band with clay\_1 values

Formula:

$$clay_{-1} = 0.5 * (R_{2136} + R_{2240}) - R_{2195}$$

Source: DLR-DFD

References:



#### 6.25 iron<sub>-1</sub>

**Algorithm name:** biophys\_indices (iron\_1 is one index calculated within the overall program)

Category: Biophysics - soil indices

Summary: Calculation of iron ratio (iron\_1)

**Inputs:** Narrow band multi- or hyperspectral imagery (ENVI standard image data) including channels close to the wavelengths of 780nm, 920nm and 1245nm.

Outputs: Single band with iron\_1 values

Formula:

$$iron_{-1} = 0.5 * (R_{780} + R_{1245}) - R_{920}$$

Source: DLR-DFD

References:

## Chapter 7

# **Quality Control**



#### 7.1 Check navigation data for inconsistencies

Algorithm name: nav\_chk

Category: Quality Control

Summary: Tests navigation file (position and attitude) for inconsistencies and corrects

them. The code is based on a HyMap \*gps File.

**Inputs:** \*.gps file plus the number of image lines according to the ENVI header of the related image data. The \*.gps file is a multi-column ASCII file derived by HyVista Corp. proprietary software, which synchronises times and generates an output which is indexed by scan line number. The table below shows the list of parameters.

| Parameters   | Example              | Description                                |
|--------------|----------------------|--|
| Line         | 1                    | Scan line number                           |
| UTC Time     | 48835.0462/20/5/2004 | Time of day in seconds/day/month/year      |
| VME Time     | 929386852.0          | Internal computer tick time in microsec-   |
|              |                      | onds                                       |
| IMU Time     | 2048825953.1         | Internal IMU time in microseconds          |
| Latitude     | 48.03321015          | Decimal degrees (positive = north, nega-   |
|              |                      | tive = south)                              |
| Longitude    | 11.28140200          | Decimal degrees (positive = east, negative |
|              |                      | = west)                                    |
| Altitude     | 2970.79892155        | Meters above MSL                           |
| Pitch        | 0.22235917           | Decimal degrees (positive = nose up)       |
| Roll         | 0.54269902           | Decimal degrees (positive = right wing     |
|              |                      | up)  |
| Heading      | 0.37774316           | Decimal degrees (positive = N-E-S direc-   |
|              |                      | tion, negative = $N-W-S$ direction)        |
| True Track   | 1.00507651           | Decimal degrees (0 to 360)                 |
| Ground Speed | 72.90907700          | Meters / second                            |
| Sat          | 5                    | Number of satellites being received        |
| DGPS         | 1                    | DGPS status: $1 = DGPS$ being received     |
|              |                      | 0 = no DGPS received                       |

Outputs: status file → template+'\_status'

If applicable: corrected gps file

backup of original .gps  $\rightarrow$  filename.gps\_original

Formula: test & correct the following

• point or colon - separator in .gps =; error catched in hymap\_read\_gps.pro corrected when re-writing the .gps-file anyway



• #lines in image = #lines in gps if too many gps-lines: truncate lines at beginning (like Hyvista does) if too few gps-lines: adding extrapolated lines at end

• invalid start / end time: calculating average timestep & using last relieable line

• data gaps (indicated by identical time): interpolate info

Source: DLR-DFD

References: EUFAR FP7 - DJ2.2.2 - Quality Layers for VITO, DLR, INTA and PML



# 7.2 Additional consistency check & QA for navigation data (no correction!)

Algorithm name: nav\_const

Category: Quality Control

Summary: Tests navigation file (position and attitude) for consistency. The code is

based on a HyMap \*gps File.

This check can be performed after nav\_chk.pro.

**Inputs:** \*.gps file. The \*.gps file is a multi-column ASCII file derived by HyVista Corp. proprietary software, which synchronises times and generates an output which is indexed by scan line number. The table below shows the list of parameters.

| Parameters   | Example              | Description  |
|--------------|----------------------|--|
| Line         | 1                    | Scan line number   |
| UTC Time     | 48835.0462/20/5/2004 | Time of day in seconds/day/month/year                                    |
| VME Time     | 929386852.0          | Internal computer tick time in microseconds                              |
| IMU Time     | 2048825953.1         | Internal IMU time in microseconds  |
| Latitude     | 48.03321015          | Decimal degrees (positive = north, negative = south)                     |
| Longitude    | 11.28140200          | Decimal degrees (positive = east, negative = west)                       |
| Altitude     | 2970.79892155        | Meters above MSL   |
| Pitch        | 0.22235917           | Decimal degrees (positive = nose up)                                     |
| Roll         | 0.54269902           | Decimal degrees (positive = right wing up)                               |
| Heading      | 0.37774316           | Decimal degrees (positive = N-E-S direction, negative = N-W-S direction) |
| True Track   | 1.00507651           | Decimal degrees (0 to 360)   |
| Ground Speed | 72.90907700          | Meters / second  |
| Sat          | 5                    | Number of satellites being received                                      |
| DGPS         | 1                    | DGPS status: $1 = DGPS$ being received                                   |
|              |                      | 0 = no DGPS received   |

Outputs: if (KEYWORD\_SET(gps\_err\_array)) → QC array otime, lat, lon, alt, pit, rol, heading, track, speed, sat, dgps Values: 0:OK 1:minor problem 2:major problem if (KEYWORD\_SET(gps\_data)) → gps data as array otime, lat, lon, alt, pit, rol, heading, track, speed, sat, dgps

Formula: test & report the following

• if data range is not plausible



• if change between steps > threshold: latlon, alt, pit, rol, heading, track, speed

• uncorrectable errors in: time, latlon, alt, pit, rol, heading, track, speed, sat, dgps

Source: DLR-DFD

References: EUFAR FP7 - DJ2.2.2 - Quality Layers for VITO, DLR, INTA and PML

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