

# Sampling networks of ecological interactions

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## Summary

1. Sampling ecological interactions presents similar challenges, problems, potential biases, and constraints as sampling individuals and species in biodiversity inventories. Interactions are just pairwise relationships among individuals of two different species, such as those among plants and their seed dispersers in frugivory interactions or those among plants and their pollinators. Sampling interactions is a fundamental step to build robustly estimated interaction networks, yet few analyses have attempted a formal approach to their sampling protocols.

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2. Robust estimates of the actual number of interactions (links) within diversified ecological networks require adequate sampling effort that needs to be explicitly gauged. Yet we still lack a sampling theory explicitly focusing on ecological interactions.
3. While the complete inventory of interactions is likely impossible, a robust characterization of its main patterns and metrics is probably realistic. We must acknowledge that a sizable fraction of the maximum number of interactions  $I_{max}$  among, say,  $A$  animal species and  $P$  plant species (i.e.,  $I_{max} = AP$ ) is impossible to record due to forbidden links, the restrictions imposed by the organisms life-histories. Thus, the number of observed interactions  $I$  in robustly sampled networks is typically  $I \ll I_{max}$ , resulting in extremely sparse interaction matrices with low connectance.
4. Reasons for forbidden links are multiple but mainly stem from spatial and temporal uncoupling of partner species encounters and from intrinsically low probabilities of interspecific encounter for many of the potential pairwise interactions. Adequately assessing the completeness of a network of ecological interactions thus needs a deep knowledge of the natural history details embedded, so that forbidden links can be “discounted” when addressing sampling effort.
5. Here I provide a review and outline a conceptual framework for interaction sampling by building an explicit analogue to individuals and species sampling, thus extending diversity-monitoring approaches to the characterization of complex networks of ecological interactions. This is crucial to assess the fast-paced and devastating effects of defaunation-driven loss of key ecological

interactions and the services they provide.

## Keywords

complex networks, food webs, frugivory, mutualism, plant-animal interactions, pollination, seed dispersal

## Introduction

Biodiversity sampling is a labour-intensive activity, and sampling is often not sufficient to detect all or even most of the species present in an assemblage. Gotelli & Colwell (2011).

1 Biodiversity assessment aims at sampling individuals in collections and deter-  
2 mining the number of species represented. Given that, by definition, samples are  
3 incomplete, these collections enumerate a lower number of the species actually  
4 present. The ecological literature dealing with robust estimators of species rich-  
5 ness and diversity in collections of individuals is immense, and a number of useful  
6 approaches have been used to obtain such estimates (Magurran, 1988; Gotelli &  
7 Colwell, 2001; Hortal, Borges & Gaspar, 2006; Colwell, 2009; Gotelli & Colwell,  
8 2011). Recent effort has been also focused at defining essential biodiversity vari-  
9 ables (EBV) (Pereira *et al.*, 2013) that can be sampled and measured repeatedly  
10 to complement biodiversity estimates. Yet sampling species or taxa-specific EBVs  
11 is just probing a single component of biodiversity; interactions among species are  
12 another fundamental component, the one that supports the existence of species.

13 For example, the extinction of interactions represents a dramatic loss of biodiver-  
14 sity because it entails the loss of fundamental ecological functions (Valiente-Banuet  
15 *et al.*, 2014). This missed component of biodiversity loss, the extinction of ecolog-  
16 ical interactions, very often accompanies, or even precedes, species disappearance.  
17 Interactions among species are a key component of biodiversity and here I aim to  
18 show that most problems associated to sampling interactions in natural communi-  
19 ties have to do with problems associated to sampling species diversity, even worse.  
20 I consider pairwise interactions among species at the habitat level, in the context of  
21 alpha diversity and the estimation of local interaction richness from sampling data  
22 (Mao & Colwell, 2005). In the first part I provide a succinct overview of previous  
23 work addressing sampling issues for ecological interaction networks. In the second  
24 part, after a short overview of asymptotic diversity estimates (Gotelli & Colwell,  
25 2001), I discuss specific rationales for sampling the biodiversity of ecological inter-  
26 actions. Most of my examples come from the analysis of plant-animal interaction  
27 networks, yet are applicable to other types of species-species interactions.

28 Interactions can be a much better indicator of the richness and diversity of  
29 ecosystem functions than a simple list of taxa and their abundances and/or re-  
30 lated biodiversity indicator variables (EBVs). Thus, sampling interactions should  
31 be a central issue when identifying and diagnosing ecosystem services (e.g., polli-  
32 nation, natural seeding by frugivores, etc.). Fortunately, all the whole battery of  
33 biodiversity-related tools used by ecologists to sample biodiversity (species, *sensu*  
34 *stricto*) can be extended and applied to the sampling of interactions. Analogs  
35 are evident between these approaches (Colwell, Dunn & Harris, 2012). Monitor-  
36 ing interactions is analogous to any biodiversity sampling [i.e., a species inventory  
37 Jordano (1987); Jordano, Vázquez & Bascompte (2009)] and is subject to similar

methodological shortcomings, especially under-sampling (Coddington *et al.*, 2009; Vazquez, Chacoff & Cagnolo, 2009; Dorado *et al.*, 2011; Rivera-Hutinel *et al.*, 2012). For example, when we study mutualistic networks, our goal is to make an inventory of the distinct pairwise interactions that made up the network. We are interested in having a complete list of all the pairwise interactions among species (e.g., all the distinct, species-species interactions, or links, among the pollinators and flowering plants) that can exist in a given community. Sampling these interactions thus entails exactly the same problems, limitations, constraints, and potential biases as sampling individual organisms and species diversity. As Mao & Colwell (2005) put it, these are the workings of Preston’s demon, the moving “veil line” between detected and the undetected interactions as sample size increases (Preston, 1948).

Early efforts to recognize and solve sampling problems in analyses of interactions stem from research on food webs and to determine how undersampling biases food web metrics (Martinez, 1991; Cohen *et al.*, 1993; Martinez, 1993; Bersier, Banasek-Richter & Cattin, 2002; Brose, Martinez & Williams, 2003; Banasek-Richter, Cattin & Bersier, 2004; Wells & O’Hara, 2012). In addition, the myriad of classic natural history studies documenting animal diets, host-pathogen infection records, plant herbivory records, etc., represent efforts to document interactions occurring in nature. All of them share the problem of sampling incompleteness influencing the patterns and metrics reported. Yet, despite the early recognition that incomplete sampling may seriously bias the analysis of ecological networks (Jordano, 1987), only recent studies have explicitly acknowledged it and attempted to determine its influence (Ollerton & Cranmer, 2002; Nielsen & Bascompte, 2007; Vazquez, Chacoff & Cagnolo, 2009; Gibson *et al.*, 2011; Olesen *et al.*, 2011; Cha-

63 *coff et al.*, 2012; Rivera-Hutinel *et al.*, 2012; Olito & Fox, 2014; Bascompte &  
 64 Jordano, 2014; Vizentin-Bugoni, Maruyama & Sazima, 2014; Frund, McCann &  
 65 Williams, 2015). The sampling approaches have been extended to predict patterns  
 66 of coextinctions in interaction assemblages (e.g., hosts-parasites) (Colwell, Dunn &  
 67 Harris, 2012). Most empirical studies provide no estimate of sampling effort, im-  
 68 plicitly assuming that the reported network patterns and metrics are robust. Yet  
 69 recent evidences point out that number of partner species detected, number of  
 70 actual links, and some aggregate statistics describing network patterns, are prone  
 71 to sampling bias (Nielsen & Bascompte, 2007; Dorado *et al.*, 2011; Olesen *et al.*,  
 72 2011; Chacoff *et al.*, 2012; Rivera-Hutinel *et al.*, 2012; Olito & Fox, 2014; Frund,  
 73 McCann & Williams, 2015). Most of these evidences, however, come from either  
 74 theoretical, simulation, studies (Frund, McCann & Williams, 2015) or from rel-  
 75 atively species-poor assemblages. Even for species-rich, tropical assemblages it  
 76 might be erroneous to conclude that network data routinely come from insuffi-  
 77 ciently sampled datasets (Ollerton & Cranmer, 2002; Chacoff *et al.*, 2012), given  
 78 the extremely sparse nature of these interaction matrices because of the prevalence  
 79 of forbidden links (which, by definition, cannot be documented despite extensive  
 80 sampling effort). However, most certainly, sampling limitations pervade biodiver-  
 81 sity inventories in tropical areas (Coddington *et al.*, 2009) and we might rightly  
 82 expect that frequent interactions may be over-represented and rare interactions  
 83 may be missed entirely in studies of mega-diverse assemblages (Bascompte & Jor-  
 84 dano, 2014); but, to what extent?

## 85 Sampling interactions: methods

86 When we sample interactions in the field we record the presence of two species that  
 87 interact in some way. For example, Snow and Snow(1988) recorded an interaction  
 88 whenever they saw a bird “touching” a fruit on a plant. We observe and record  
 89 feeding observations, visitation, occupancy, presence in pollen loads or in fecal  
 90 samples, etc., of *individual* animals or plants and accumulate pairwise interactions,  
 91 i.e., lists of species partners and the frequencies with which we observe them.  
 92 Therefore, estimating the sampling completeness of pairwise interactions for a  
 93 whole network, requires some gauging of the sampling completeness (i.e., how the  
 94 number (richness) of distinct pairwise interactions accumulates as sampling effort  
 95 is increased) and/or estimating the uncertainty around the missed links (Wells &  
 96 O’Hara, 2012).

97 Most, if not all, types of ecological interactions can be illustrated with bipar-  
 98 tite graphs, with two or more distinct groups of interacting partners (Bascompte  
 99 & Jordano, 2014); for illustration purposes I’ll focus more specifically on plant-  
 100 animal interactions. Sampling interactions requires filling the cells of an inter-  
 101 action matrix with data. The matrix,  $\Delta = AP$ , is a 2D representation of the  
 102 interactions among, say,  $A$  animal species (rows) and  $P$  plant species (columns)  
 103 (Jordano, 1987; Bascompte & Jordano, 2014). The matrix entries illustrate the  
 104 values of the pairwise interactions visualized in the  $\Delta$  matrix, and can be 0 or 1,  
 105 for presence-absence of a given pairwise interaction, or take a quantitative weight  
 106  $w_{ji}$  to represent the interaction intensity or unidirectional effect of species  $j$  on  
 107 species  $i$  (Bascompte & Jordano, 2014; Vazquez *et al.*, 2015). The outcomes of  
 108 most ecological interactions are dependent on frequency of encounters (e.g., visit

rate of pollinators, number of records of ant defenders, frequency of seeds in fecal samples). Thus, a frequently used proxy for interaction intensities  $w_{ji}$  is just how frequent are new interspecific encounters, whether or not appropriately weighted to estimate interaction effectiveness (Vazquez, Morris & Jordano, 2005).

We need to define two basic steps in the sampling of interactions: 1) which type of interactions we sample; and 2) which type of record we get to document the existence of an interaction. In step #1 we need to take into account whether we are sampling the whole community of interactor species (all the animals, all the plants) or just a subset of them, i.e., a sub matrix  $\Delta_{m,n}$  of  $m < A$  animal species and  $n < P$  plant species of the adjacency matrix  $\Delta_{AP}$ . Subsets can be: a) all the potential plants interacting with a subset of the animals (Fig. 1a); b) all the potential animal species interacting with a subset of the plant species (Fig. 1b); c) a subset of all the potential animal species interacting with a subset of all the plant species (Fig. 1c). While some discussion has considered how to establish the limits of what represents a network (Strogatz, 2001) (in analogy to discussion on food-web limits; Cohen, 1978), it must be noted that situations a-c in Fig. 1 do not represent complete interaction networks. As vividly stated by Cohen et al. (1993): “*As more comprehensive, more detailed, more explicit webs become available, smaller, highly aggregated, incompletely described webs may progressively be dropped from analyses of web structure (though such webs may remain useful for other purposes, such as pedagogy)*”. Subnet sampling is generalized in studies of biological networks (e.g., protein interactions, gene regulation), yet it is important to recognize that most properties of subnetworks (even random subsamples) do not represent properties of whole networks (Stumpf, Wiuf & May, 2005).

In step #2 above we face the problem of the type of record we take to sample



134 interactions. This is important because it defines whether we approach the problem  
 135 of filling up the interaction matrix in a “zoo-centric” way or in a “phyto-centric”  
 136 way. Zoo-centric studies directly sample animal activity and document the plants  
 137 ‘touched’ by the animal. For example, analysis of pollen samples recovered from the  
 138 body of pollinators, analysis of fecal samples of frugivores, radio-tracking data, etc.  
 139 Phyto-centric studies take samples of focal individual plant species and document  
 140 which animals ‘arrive’ or ‘touch’ the plants. Examples include focal watches of  
 141 fruiting or flowering plants to record visitation by animals, raising insect herbivores  
 142 from seed samples, identifying herbivory marks in samples of leaves, etc.

143 Most recent analyses of plant-animal interaction networks are phyto-centric;  
 144 just 3.5% of available plant-pollinator ( $N = 58$ ) or 36.6% plant-frugivore ( $N = 22$ )  
 145 interaction datasets are zoo-centric (see Schleuning *et al.*, 2012). Moreover, most  
 146 available datasets on host-parasite or plant-herbivore interactions are “host-centric”  
 147 or phyto-centric (e.g., Thébault & Fontaine, 2010; Eklöf *et al.*, 2013). This maybe  
 148 related to a variety of causes, like preferred methodologies by researchers working  
 149 with a particular group or system, logistic limitations, or inherent taxonomic focus  
 150 of the research questions. A likely result of phyto-centric sampling would be adja-  
 151 cency matrices with large  $A : P$  ratios. In any case we don’t have a clear view of  
 152 the potential biases that taxa-focused sampling may generate in observed network  
 153 patterns, for example by generating consistently asymmetric interaction matrices  
 154 (Dormann *et al.*, 2009). System symmetry has been suggested to influence esti-  
 155 mations of generalization levels in plants and animals when measured as  $I_A$  and  
 156  $I_P$  (Elberling & Olesen, 1999); thus, differences in  $I_A$  and  $I_P$  between networks  
 157 may arise from different  $A : P$  ratios rather than other ecological factors (Olesen  
 158 & Jordano, 2002).

159 Interestingly enough, quite complete analyses of interaction networks can be  
160 obtained when combining both phyto-centric and zoo-centric sampling. For ex-  
161 ample, Bosch *et al.* (2009) showed that the addition of pollen load data on top of  
162 focal-plant sampling of pollinators unveiled a significant number of interactions,  
163 resulting in important network structural changes. Connectance increased 1.43-  
164 fold, mean plant connectivity went from 18.5 to 26.4, and mean pollinator connec-  
165 tivity from 2.9 to 4.1; moreover, extreme specialist pollinator species (singletons  
166 in the adjacency matrix) decreased 0.6-fold. Zoo-centric sampling has recently  
167 been extended with the use of DNA-barcoding, for example with plant-herbivore  
168 (Jurado-Rivera *et al.*, 2009) and plant-frugivore interactions (González-Varo, Ar-  
169 royo & Jordano, 2014). For mutualistic networks we would expect that zoo-centric  
170 sampling could help unveiling interactions for rare species or for relatively common  
171 species which are difficult to sample by direct observation. Future methodologi-  
172 cal work may provide significant advances showing how mixing different sampling  
173 strategies strengthens the completeness of network data. These mixed strategies  
174 may combine, for instance, timed watches at focal plants, spot censuses along  
175 walked transects, pollen load or seed contents analyses, monitoring with camera  
176 traps, and DNA barcoding records. We might expect increased power of these  
177 mixed sampling approaches when combining different methods from both phyto-  
178 and zoo-centric perspectives (Bosch *et al.*, 2009; Bluthgen, 2010). Note also that  
179 the different methods could be applied in different combinations to the two distinct  
180 sets of species. However, there are no tested protocols and/or sampling designs for  
181 ecological interaction studies to suggest an optimum combination of approaches.  
182 Ideally, pilot studies would provide adequate information for each specific study  
183 setting.

## 184 Sampling interactions: rationale

185 The number of distinct pairwise interactions that we can record in a landscape  
 186 (an area of relatively homogeneous vegetation, analogous to the one we would  
 187 use to monitor species diversity) is equivalent to the number of distinct classes in  
 188 which we can classify the recorded encounters among individuals of two different  
 189 species. Yet, individual-based interaction networks have been only recently studied  
 190 (Dupont, Trøjelsgaard & Olesen, 2011; Wells & O’Hara, 2012). The most usual  
 191 approach has been to pool individual-based interaction data into species-based  
 192 summaries, an approach that ignores the fact that only a fraction of individuals  
 193 may actually interact given a per capita interaction effect (Wells & O’Hara, 2012).  
 194 Wells & O’Hara (2012) illustrate the pros and cons of the approach. We walk in  
 195 the forest and see a blackbird  $Tm$  picking an ivy  $Hh$  fruit and ingesting it: we  
 196 have a record for  $Tm - Hh$  interaction. We keep advancing and record again a  
 197 blackbird feeding on hawthorn  $Cm$  fruits so we record a  $Tm - Cm$  interaction;  
 198 as we advance we encounter another ivy plant and record a blackcap swallowing a  
 199 fruit so we now have a new  $Sa - Hh$  interaction, and so on. At the end we have  
 200 a series of classes (e.g.,  $Sa - Hh$ ,  $Tm - Hh$ ,  $Tm - Cm$ , etc.), along with their  
 201 observed frequencies. Bunge & Fitzpatrick (1993) review the main aspects and ap-  
 202 proaches to estimate the number of distinct classes  $C$  in a sample of observations.  
 203 Our main problem then turns to estimate the number of true missed links, i.e.,  
 204 those that can’t be accounted for by biological constraints and that might suggest  
 205 undersampling. Thus, the sampling of interactions in nature, as the sampling of  
 206 species, is a cumulative process. In our analysis, we are not re-sampling individ-  
 207 uals, but interactions, so we made interaction-based accumulation curves. If an

interaction-based curve points towards a robust sampling, it does mean that no new interactions are likely to be recorded, irrespectively of the species, as it is a whole-network sampling approach (N. Gotelli, pers. com.). We add new, distinct, interactions recorded as we increase sampling effort (Fig. 2). We can obtain an Interaction Accumulation Curve (*IAC*) analogous to a Species cumulating Curve (*SAC*) (see Supplementary Online Material): the observed number of distinct pairwise interactions in a survey or collection as a function of the accumulated number of observations or samples (Colwell, 2009).

Our sampling above would have resulted in a vector  $n = [n_1 \dots n_C]'$  where  $n_i$  is the number of records in the  $i^{th}$  class. As stressed by Bunge & Fitzpatrick (1993), however, the  $i^{th}$  class would appear in the sample if and only if  $n_i > 0$ , and we don't know *a priori* which  $n_i$  are zero. So,  $n$  is not observable. Rather, what we get is a vector  $c = [c_1 \dots c_n]'$  where  $c_j$  is the number of classes represented  $j$  times in our sampling:  $c_1$  is the number of singletons (interactions recorded once),  $c_2$  is the number of twin pairs (interactions wkth just two records),  $c_3$  the number of triplets, etc. The problem thus turns to be estimating the number of distinct classes  $C$  from the vector of  $c_j$  values and the frequency of unobserved interactions (see "The real missing links" below).

Estimating the number of interactions with resulting robust estimates of network parameters is a central issue in the study of ecological interaction networks (Jordano, 1987; Bascompte & Jordano, 2014). In contrast with traditional species diversity estimates, sampling networks has the paradox that despite the potentially interacting species being present in the sampled assemblage (i.e., included in the  $A$  and  $P$  species lists), some of their pairwise interactions are impossible to be recorded. The reason is forbidden links. Independently of whether we sample full

communities of subset communities we face a problem: some of the interactions that we can visualize in the empty adjacency matrix  $\Delta$  will simply not occur. Thus, independently of the sampling effort we put, we'll never document these pairwise interactions. With a total of  $AP$  "potential" interactions, a fraction of them are impossible to record, because they are forbidden (Jordano, Bascompte & Olesen, 2003; Olesen *et al.*, 2011). Forbidden links are non-occurrences of pairwise interactions that can be accounted for by biological constraints, such as spatio-temporal uncoupling (Jordano, 1987), size or reward mismatching, foraging constraints (e.g., accessibility) (Moré *et al.*, 2012), and physiological-biochemical constraints (Jordano, 1987). We still have extremely reduced information about the frequency of forbidden links in natural communities (Jordano, Bascompte & Olesen, 2003; Stang *et al.*, 2009; Vazquez, Chacoff & Cagnolo, 2009; Olesen *et al.*, 2011; Ibanez, 2012; Maruyama *et al.*, 2014; Vizentin-Bugoni, Maruyama & Sazima, 2014) (Table 1). Forbidden links are thus represented as structural zeroes in the interaction matrix, i.e., matrix cells that cannot get a non-zero value. So, we need to account for the frequency of these structural zeros in our matrix before proceeding. For example, most measurements of connectance  $C = I/(AP)$  implicitly ignore the fact that by taking the full product  $AP$  in the denominator they are underestimating the actual connectance value, i.e., the fraction of actual interactions  $I$  relative to the *biologically possible* ones, not to the total maximum  $I_{max} = AP$ .

Adjacency matrices are frequently sparse, i.e., they are densely populated with zeroes, with a fraction of them being structural (unobservable interactions) (Bascompte & Jordano, 2014). It would be thus a serious interpretation error to attribute the sparseness of adjacency matrices for bipartite networks to undersampling. The actual typology of link types in ecological interaction networks is thus

258 more complex than just the two categories of observed and unobserved interactions  
 259 (Table 1). Unobserved interactions are represented by zeroes and belong to two  
 260 categories. Missing interactions may actually exist but require additional sampling  
 261 or a variety of methods to be observed. Forbidden links, on the other hand, arise  
 262 due to biological constraints limiting interactions and remain unobservable in na-  
 263 ture, irrespectively of sampling effort (Table 1). Forbidden links *FL* may actually  
 264 account for a relatively large fraction of unobserved interactions *UL* when sam-  
 265 pling taxonomically-restricted subnetworks (e.g., plant-hummingbird pollination  
 266 networks) (Table 1). Phenological unmatching is also prevalent in most networks,  
 267 and may add up to explain ca. 25–40% of the forbidden links, especially in highly  
 268 seasonal habitats, and up to 20% when estimated relative to the total number  
 269 of unobserved interactions (Table 2). In any case, we might expect that a frac-  
 270 tion of the missing links *ML* would be eventually explained by further biological  
 271 reasons, depending on the knowledge of natural details of the particular systems.  
 272 Our goal as naturalists would be to reduce the fraction of *UL* which remain as  
 273 missing links; to this end we might search for additional biological constraints or  
 274 increase sampling effort. For instance, habitat use patterns by hummingbirds in  
 275 the Arima Valley network (Table 2; Snow & Snow, 1972) impose a marked pattern  
 276 of microhabitat mismatches causing up to 44.5% of the forbidden links. A myr-  
 277 iad of biological causes beyond those included as *FL* in Table 2 may contribute  
 278 explanations for *UL*: limits of color perception and or partial preferences, pres-  
 279 ence of secondary metabolites in fruit pulp and leaves, toxins and combinations  
 280 of monosaccharides in nectar, etc. However, it is surprising that just the limited  
 281 set of forbidden link types considered in Table 1 explain between 24.6–77.2% of  
 282 the unobserved links. Notably, the Arima Valley, Santa Virg nia, and Hato Rat n

networks have  $> 60\%$  of the unobserved links explained, which might be related to the fact that they are subnetworks (Arima Valley, Santa Virgínia) or relatively small networks (Hato Ratón). All this means that empirical networks may have sizable fractions of structural zeroes. Ignoring this biological fact may contribute to wrongly infer undersampling of interactions in real-world assemblages.

To sum up, two elements of inference are required in the analysis of unobserved interactions in ecological interaction networks: first, detailed natural history information on the participant species that allows the inference of biological constraints imposing forbidden links, so that structural zeroes can be identified in the adjacency matrix; second, a critical analysis of sampling robustness and a robust estimate of the actual fraction of missing links,  $M$ , and thus, a robust estimate of  $I$ . In the next sections I explore these elements of inference. The basic proposal is to use *IACs* to assess the robustness of interaction sampling, then scale the asymptotic estimate of interactions richness to account for the unrealizable  $FL$ .

## Asymptotic diversity estimates

Let's assume a sampling of the diversity in a specific locality, over relatively homogeneous landscape where we aim at determining the number of species present for a particular group of organisms. To do that we carry out transects or plot samplings across the landscape, adequately replicated so we obtain a number of samples. Briefly,  $S_{obs}$  is the total number of species observed in a sample, or in a set of samples.  $S_{est}$  is the estimated number of species in the community represented by the sample, or by the set of samples, where *est* indicates an estimator. With abundance data, let  $S_k$  be the number of species each represented by exactly

$k$  individuals in a single sample. Thus,  $S_0$  is the number of undetected species (species present in the community but not included in the sample),  $S_1$  is the number of singleton species (represented by just one individual),  $S_2$  is the number of doubleton species (species with two individuals), etc. The total number of individuals in the sample would be:

$$n = \sum_{k=1}^{S_{obs}} S_k$$

298

299 A frequently used asymptotic, bias corrected, non-parametric estimator is  $S_{Chao}$   
 300 (Hortal, Borges & Gaspar, 2006; Chao, 2005; Colwell, 2013):

$$S_{Chao} = S_{obs} + \frac{S_1(S_1 - 1)}{2(S_2 + 1)}$$

301 Another frequently used alternative is the Chao2 estimator,  $S_{Chao2}$  (Gotelli &  
 302 Colwell, 2001), which has been reported to have a limited bias for small sample  
 303 sizes (Colwell & Coddington, 1994; Chao, 2005):

$$S_{Chao2} = S_{obs} + \frac{S_1^2}{2S_2}$$

304 A plot of the cumulative number of species recorded,  $S_n$ , as a function of some  
 305 measure of sampling effort (say,  $n$  samples taken) yields the species accumulation  
 306 curve (SAC) or collector's curve (Colwell & Coddington, 1994). Such a curve even-  
 307 tually reaches an asymptote converging with  $S_{est}$ . In an analogous way, interaction  
 308 accumulation curves (IAC), analogous to SACs, can be used to assess the robust-  
 309 ness of interactions sampling for plant-animal community datasets (Jordano, 1987;



Jordano, Vázquez & Bascompte, 2009; Olesen *et al.*, 2011). For instance, a random accumulator function (e.g., library `vegan` in the R Package, R Development Core Team, 2010) which finds the mean IAC and its standard deviation from random permutations of the data, or subsampling without replacement (Gotelli & Colwell, 2001) can be used to estimate the expected number of distinct pairwise interactions included in a given sampling of records (Jordano, Vázquez & Bascompte, 2009; Olesen *et al.*, 2011). This is analogous to a biodiversity sampling matrix with species as rows and sampling units (e.g., quadrats) as columns (Jordano, Vázquez & Bascompte, 2009). In this way we effectively extend sampling theory developed for species diversity to the sampling of ecological interactions. Yet future theoretical work will be needed to formally assess the similarities and differences in the two approaches and developing biologically meaningful null models of expected interaction richness with added sampling effort.

## Assessing sampling effort when recording interactions

The basic method we can propose to estimate sampling effort and explicitly show the analogues with rarefaction analysis in biodiversity research is to vectorize the interaction matrix  $AP$  so that we get a vector of all the potential pairwise interactions ( $I_{max}$ , Table 1) that can occur in a community of  $A$  animal species and  $P$  plant species. The new “species” we aim to sample are the pairwise interactions (Table 3). So, if we have in our community *Turdus merula* ( $Tm$ ) and *Rosa canina* ( $Rc$ ) and *Prunus mahaleb* ( $Pm$ ), our problem will be to sample 2 new

332 “species”:  $Tm - Rc$  and  $Tm - Pm$ . In general, if we have  $A = 1...i$ , animal  
 333 species and  $P = 1...j$  plant species, we’ll have a vector of “new” species to sample:  
 334  $A_1P_1, A_1P_2, ...A_2P_1, A_2P_2, ...A_iP_j$ . We can represent the successive samples where  
 335 we can potentially get records of these interactions in a matrix with the vectorized  
 336 interaction matrix and columns representing the successive samples we take (Table  
 337 3). This is simply a vectorized version of the interaction matrix.

338 Rarefaction analysis and diversity-accumulation analysis (Magurran, 1988; Hor-  
 339 tal, Borges & Gaspar, 2006) come up immediately with this type of dataset. This  
 340 procedure plots the accumulation curve for the expected number of distinct pair-  
 341 wise interactions recorded with increasing sampling effort (Jordano, Vázquez &  
 342 Bascompte, 2009; Olesen *et al.*, 2011). Asymptotic estimates of interaction rich-  
 343 ness and its associated standard errors and confidence intervals can thus be ob-  
 344 tained (Hortal, Borges & Gaspar, 2006) (see Supplementary Online Material). It  
 345 should be noted that the asymptotic estimate of interaction richness implicitly  
 346 ignores the fact that, due to forbidden links, a number of pairwise interactions  
 347 among the  $I_{max}$  number specified in the adjacency matrix  $\Delta$  cannot be recorded,  
 348 irrespective of sampling effort. Therefore, the asymptotic value most likely is an  
 349 overestimate of the actual maximum number of links that can be present in an  
 350 assemblage. If forbidden links are taken into account, the asymptotic estimate  
 351 should be lower. Yet, to the best of my knowledge, there is no theory developed  
 352 to estimate this “biologically real” asymptotic value. Not unexpectedly, most re-  
 353 cent analyses of sampling effort in ecological network studies found evidences of  
 354 undersampling (Chacoff *et al.*, 2012). This needs not to be true, especially when  
 355 interaction subwebs are studied (Olesen *et al.*, 2011; Vizentin-Bugoni, Maruyama  
 356 & Sazima, 2014), and once the issue of structural zeroes in the interaction matrices

is effectively incorporated in the estimates.

For example, mixture models incorporating detectabilities have been proposed to effectively account for rare species (Mao & Colwell, 2005). In an analogous line, mixture models could be extended to samples of pairwise interactions, also with specific detectability values. These detection rate/odds could be variable among groups of interactions, depending on their specific detectability. For example, detectability of flower-pollinator interactions involving bumblebees could have a higher detectability than flower-pollinator pairwise interactions involving, say, nitidulid beetles. These more homogeneous groupings of pairwise interactions within a network define modules (Bascompte & Jordano, 2014), so we might expect that interactions of a given module (e.g., plants and their hummingbird pollinators; Fig. 1a) may share similar detectability values, in an analogous way to species groups receiving homogeneous detectability values in mixture models (Mao & Colwell, 2005). Such sampling, in its simplest form, would result in a sample with multiple pairwise interactions detected, in which the number of interaction events recorded for each distinct interaction found in the sample is recorded (i.e., a column vector in Table 3, corresponding to, say, a sampling day). The number of interactions recorded for the  $i_{th}$  pairwise interaction (i.e.,  $A_i P_j$  in Table 3),  $Y_i$  could be treated as a Poisson random variable with a mean parameter  $\lambda_i$ , its detection rate. Mixture models (Mao & Colwell, 2005) include estimates for abundance-based data (their analogous in interaction sampling would be weighted data), where  $Y_i$  is a Poisson random variable with detection rate  $\lambda_i$ . This is combined with the incidence-based model, where  $Y_i$  is a binomial random variable (their analogous in interaction sampling would be presence/absence records of interactions) with detection odds  $\lambda_i$ . Let  $T$  be the number of samples in an incidence-based data set.

382 A Poisson/binomial density can be written as (Mao & Colwell, 2005):

$$g(y; \lambda) = \begin{cases} \frac{\lambda^y}{y!e^\lambda} & [1] \\ \binom{T}{y} \frac{\lambda^y}{(1+\lambda)^T} & [2] \end{cases}$$

383 where [1] corresponds to a weighted network, and [2] to a qualitative network.

384 The detection rates  $\lambda_i$  depend on the relative abundances  $\phi_i$  of the interactions,  
 385 the probability of a pairwise interaction being detected when it is present, and the  
 386 sample size (the number of interactions recorded), which, in turn, is a function  
 387 of the sampling effort. Unfortunately, no specific sampling model has been de-  
 388 veloped along these lines for species interactions and their characteristic features.  
 389 For example, a complication factor might be that interaction abundances,  $\phi_i$ , in  
 390 real assemblages are a function of the abundances of interacting species, that de-  
 391 termine interspecific encounter rates; yet they also depend on biological factors  
 392 that ultimately determine if the interaction occurs when the partner species are  
 393 present. For example,  $\lambda_i$  should be set to zero for all  $FL$ . In its simplest form,  $\phi_i$   
 394 could be estimated from just the product of partner species abundances, an ap-  
 395 proach recently used as a null model to assess the role of biological constraints in  
 396 generating forbidden links and explaining interaction patterns (Vizentin-Bugoni,  
 397 Maruyama & Sazima, 2014). Yet more complex models (e.g., Wells & O'hara  
 398 2012) should incorporate not only interspecific encounter probabilities, but also  
 399 interaction detectabilities, phenotypic matching and incidence of forbidden links.

## 400 The *real* missing links

401 Given that a fraction of unobserved interactions can be accounted for by for-  
 402 bidden links, what about the remaining missing interactions? We have already  
 403 discussed that some of these could still be related to unaccounted constraints, and  
 404 still others would be certainly attributable to insufficient sampling. Would this  
 405 always be the case? Multispecific assemblages of distinct taxonomic relatedness,  
 406 whose interactions can be represented as bipartite networks (e.g., host-parasite,  
 407 plant-animal mutualisms, plant-herbivore interactions- with two distinct sets of  
 408 unrelated higher taxa), are shaped by interspecific encounters among individuals  
 409 of the partner species (Fig. 2). A crucial ecological aspect limiting these inter-  
 410 actions is the probability of interspecific encounter, i.e., the probability that two  
 411 individuals of the partner species actually encounter each other in nature.

412 Given log-normally distributed abundances of the two species groups, the ex-  
 413 pected “neutral” probabilities of interspecific encounter (*PIE*) would be simply the  
 414 product of the two lognormal distributions. Thus, we might expect that for low  
 415 *PIE* values, pairwise interactions would be either extremely difficult to sample, or  
 416 just simply non-occurring in nature. Consider the Nava de las Correhuelas inter-  
 417 action web (NCH, Table 2), with  $A = 36$ ,  $P = 25$ ,  $I = 181$ , and almost half of the  
 418 unobserved interactions not accounted for by forbidden links, thus  $M = 53.1\%$ .  
 419 Given the robust sampling of this network (Jordano, Vázquez & Bascompte, 2009),  
 420 a sizable fraction of these possible but missing links would be simply not occurring  
 421 in nature, most likely by extremely low *PIE*, in fact asymptotically zero. Given  
 422 the vectorized list of pairwise interactions for NCH, I computed the *PIE* values for  
 423 each one by multiplying element wise the two species abundance distributions. The

424  $PIE_{max} = 0.0597$ , being a neutral estimate, based on the assumption that interac-  
 425 tions occur in proportion to the species-specific local abundances. With  $PIE_{median}$   
 426  $< 1.4 \cdot 10^{-4}$  we may safely expect (note the quantile estimate  $Q_{75\%} = 3.27 \cdot 10^{-4}$ ) that  
 427 a sizable fraction of these missing interactions may simply not occur according to  
 428 this neutral expectation (Jordano, 1987; Olesen *et al.*, 2011) (neutral forbidden  
 429 links, *sensu* Canard *et al.*, 2012). Which is the expected frequency for pairwise  
 430 interactions? and, which is the expected probability for unobserved interactions?  
 431 More specifically, which is the probability of missing interactions,  $M$  (i.e., the  
 432 unobserved ones that cannot be accounted for as forbidden links)?

433 When we consider the vectorized interaction matrix, enumerating all pairwise  
 434 interactions for the  $AP$  combinations, the expected probabilities of finding a given  
 435 interaction can be estimated with a Good-Turing approximation (Good, 1953).  
 436 The technique, developed by Alan Turing and I.J. Good with applications to lin-  
 437 guistics and word analysis (Gale & Sampson, 1995) has been recently applied in  
 438 ecology (Chao *et al.*, 2015), estimates the probability of recording an interaction  
 439 of a hitherto unseen pair of partners, given a set of past records of interactions  
 440 between other species pairs. Let a sample of  $N$  interactions so that  $n_r$  distinct  
 441 pairwise interactions have exactly  $r$  records. All Good-Turing estimators obtain  
 442 the underlying frequencies of events as:

$$P(X) = \frac{(N_X + 1)}{T} \left(1 - \frac{E(1)}{T}\right) \quad (1)$$

443 where  $X$  is the pairwise interaction,  $N_X$  is the number of times interaction  $X$   
 444 is recorded,  $T$  is the sample size (number of distinct interactions recorded) and  
 445  $E(1)$  is an estimate of how many different interactions were recorded exactly once.

Strictly speaking Equation (1) gives the probability that the next interaction type recorded will be  $X$ , after sampling a given assemblage of interacting species. In other words, we scale down the maximum-likelihood estimator  $\frac{n}{T}$  by a factor of  $\frac{1-E(1)}{T}$ . This reduces all the probabilities for interactions we have recorded, and makes room for interactions we haven't seen. If we sum over the interactions we have seen, then the sum of  $P(X)$  is  $1 - \frac{1-E(1)}{T}$ . Because probabilities sum to one, we have the left-over probability of  $P_{new} = \frac{E(1)}{T}$  of seeing something new, where new means that we sample a new pairwise interaction.

Note, however, that Good-Turing estimators, as the traditional asymptotic estimators, do not account in our case for the forbidden interactions. To account for these  $FL$  I re-scaled the asymptotic estimates, so that a more meaningful estimate could be obtained (Table 4). The scaling was calculated as  $[Chao1*(I+ML)]/AP$ , just correcting for the  $FL$  frequency, given that  $I+ML$  represent the total *feasible* interactions when discounting the forbidden links (Table 1). After scaling, observed  $I$  values (Table 2) are within the *Chao1* and *ACE* asymptotic estimates but below the *ACE* estimates for Hato Ratón and Zackenberg (Table 4). Thus, even after re-scaling for  $FL$ , it is likely that adequate characterization of most interaction networks will require intensive sampling effort.

## Discussion

Recent work has inferred that most data available for interaction networks are incomplete due to undersampling, resulting in a variety of biased parameters and network patterns (Chacoff *et al.*, 2012). It is important to note, however, that in practice, many surveyed networks to date have been subnets of much larger

networks. This is true for protein interaction, gene regulation, and metabolic networks, where only a subset of the molecular entities in a cell have been sampled (Stumpf, Wiuf & May, 2005). Despite recent attempts to document whole ecosystem meta-networks (Pocock, Evans & Memmott, 2012), it is likely that most ecological interaction networks will illustrate just major ecosystem compartments. Due to their high generalization, high temporal and spatial turnover, and high complexity of association patterns, adequate sampling of ecological interaction networks requires extremely large sampling effort. Undersampling of ecological networks may originate from the analysis of assemblage subsets (e.g., taxonomically or functionally defined), and/or from logistically-limited sampling effort. It is extremely hard to robustly sample the set of biotic interactions even for relatively simple, species-poor assemblages; yet, concluding that all ecological network datasets are undersampled would be unrealistic. The reason stems from a biological fact: a sizeable fraction of the maximum, potential links that can be recorded among two distinct sets of species is simply unobservable, irrespective of sampling effort (Jordano, 1987).

Missing links are a characteristic feature of all plant-animal interaction networks, and likely pervade other ecological interactions. Important natural history details explain a fraction of them, resulting in unrealizable interactions (i.e., forbidden interactions) that define structural zeroes in the interaction matrices and contribute to their extreme sparseness. Sampling interactions is a way to monitor biodiversity beyond the simple enumeration of component species and to develop efficient and robust inventories of functional interactions. Yet no sampling theory for interactions is available. Some key components of this sampling are analogous to species sampling and traditional biodiversity inventories; however, there



are important differences. Focusing just on the realized interactions or treating missing interactions as the expected unique result of sampling bias would miss important components to understand how mutualisms coevolve within complex webs of interdependence among species.

Contrary to species inventories, a sizable fraction of non-observed pairwise interactions cannot be sampled, due to biological constraints that forbid their occurrence. A re-scaling of traditional asymptotic estimates for interaction richness can be applied whenever the knowledge of natural history details about the study system is sufficient to estimate at least the main causes of forbidden links. Moreover, recent implementations of inference methods for unobserved species (Chao *et al.*, 2015) or for individual-based data (Wells & O’Hara, 2012) can be combined with the forbidden link approach, yet they do not account either for the existence of these ecological constraints.

Ecological interactions provide the wireframe supporting the lives of species, and they also embed crucial ecosystem functions which are fundamental for supporting the Earth system. Yet we still have a limited knowledge of the biodiversity of ecological interactions, but they are being lost (extinct) at a very fast pace, frequently preceding species extinctions (Valiente-Banuet *et al.*, 2014). We urgently need robust techniques to assess the completeness of ecological interactions networks because this knowledge will allow the identification of the minimal components of their ecological complexity that need to be restored to rebuild functional ecosystems after perturbations.

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## Data accessibility

This review does not use new raw data, but includes some re-analyses of previously published material. All the original data supporting the paper, R code, supplementary figures, and summaries of analytical protocols is available at the author's GitHub repository ([https://github.com/pedroj/MS\\_Network-Sampling](https://github.com/pedroj/MS_Network-Sampling)), with DOI: 10.5281/zenodo.29437.

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## Figure captions

**Figure 1.** Sampling ecological interaction networks (e.g., plant-animal interactions) usually focus on different types of subsampling the full network, yielding submatrices  $\Delta[m, n]$  of the full interaction matrix  $\Delta$  with  $A$  and  $P$  animal and plant species. a) all the potential plants interacting with a subset of the animals (e.g., studying just the hummingbird-pollinated flower species in a community); b) all the potential animal species interacting with a subset of the plant species (e.g., studying the frugivore species feeding on figs *Ficus* in a community); and c) sampling a subset of all the potential animal species interacting with a subset of all the plant species (e.g., studying the plant-frugivore interactions of the rainforest understory).

**Figure 2.** Sampling species interactions in natural communities. Suppose an assemblage with  $A = 3$  animal species (red, species 1–3 with three, two, and 1 individuals, respectively) and  $P = 3$  plant species (green, species a-c with three individuals each) (colored balls), sampled with increasing effort in steps 1 to 6 (panels). In Step 1 we record animal species 1 and plant species 1 and 2 with a total of three interactions (black lines) represented as two distinct interactions:  $1 - a$  and  $1 - b$ . As we advance our sampling (panels 1 to 6, illustrating e.g., additional sampling days) we record new distinct interactions. Note that we actually sample and record interactions among individuals, yet we pool the data across species to get a species by species interaction matrix. Few network analyses have been carried out on individual data (Dupont *et al.*, 2014).

744 **Figures**

Figure 1:

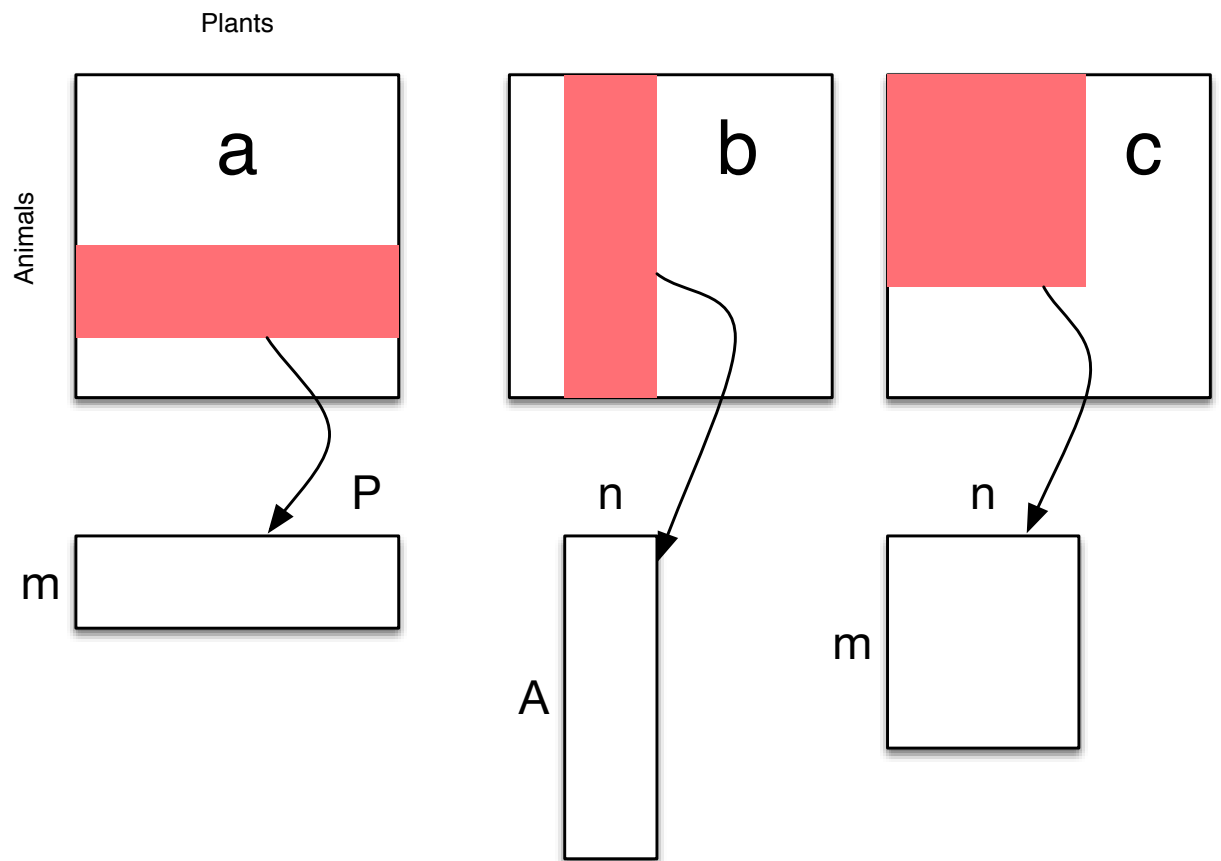
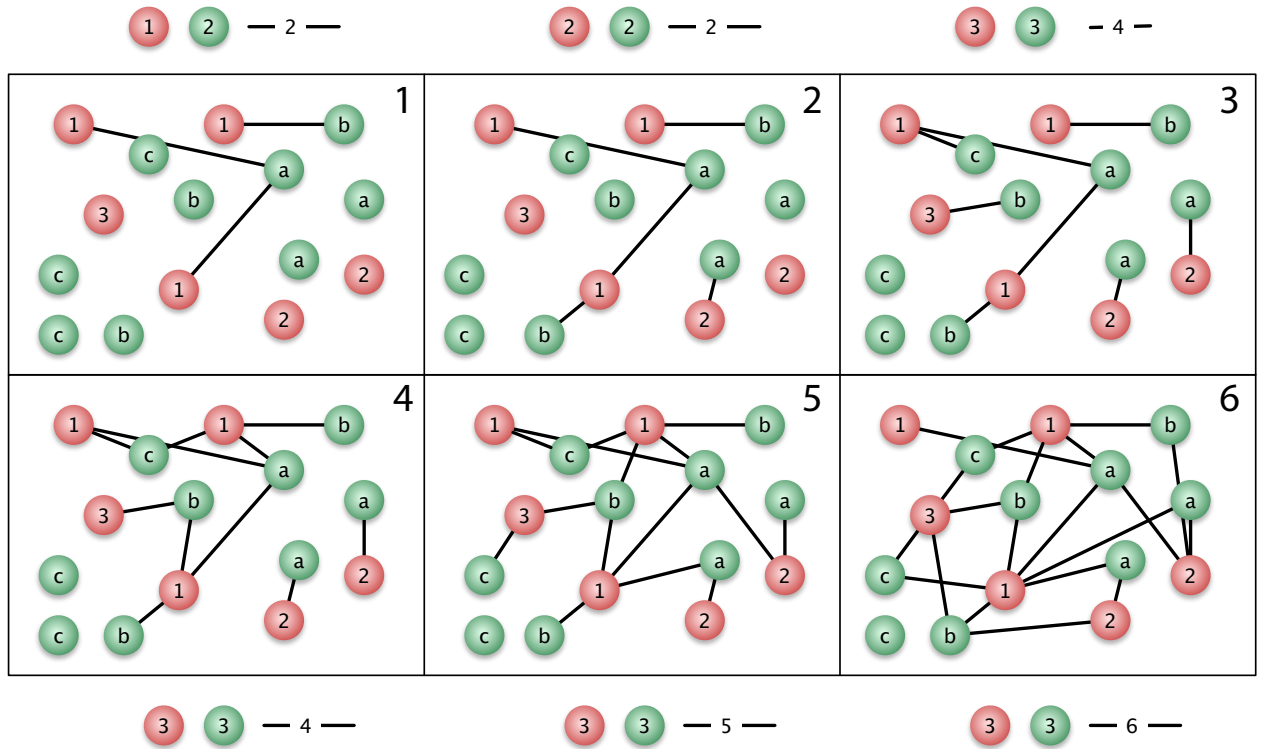


Figure 2:



Jordano - Figure 1

## Table captions

**Table 1.** A taxonomy of link types for ecological interactions (Olesen et al. 2011).

$A$ , number of animal species;  $P$ , number of plant species;  $I$ , number of observed links;  $C = 100I/(AP)$ , connectance;  $FL$ , number of forbidden links; and  $ML$ , number of missing links. As natural scientists, our ultimate goal is to eliminate  $ML$  from the equation  $FL = AP - I - ML$ , which probably is not feasible given logistic sampling limitations. When we, during our study, estimate  $ML$  to be negligible, we cease observing and estimate  $I$  and  $FL$ .

**Table 2.** Frequencies of different type of forbidden links in natural plant-animal interaction assemblages.  $AP$ , maximum potential links,  $I_{max}$ ;  $I$ , number of observed links;  $UL$ , number of unobserved links;  $FL$ , number of forbidden links;  $FL_P$ , phenology;  $FL_S$ , size restrictions;  $FL_A$ , accessibility;  $FL_O$ , other types of restrictions;  $ML$ , unknown causes (missing links). Relative frequencies (in parentheses) calculated over  $I_{max} = AP$  for  $I$ ,  $ML$ , and  $FL$ ; for all forbidden links types, calculated over  $FL$ . References, from left to right: Olesen et al. 2008; Olesen & Myrthue unpubl.; Snow & Snow 1972 and Jordano et al. 2006; Vizentin-Bugoni et al. 2014; Jordano et al. 2009; Olesen et al. 2011.

**Table 3.** A vectorized interaction matrix.

**Table 4.** Sampling statistics for three plant-animal interaction networks (Olesen et al. 2011). Symbols as in Table 1;  $N$ , number of records;  $Chao1$  and  $ACE$  are asymptotic estimators for the number of distinct pairwise interactions  $I$  (Hortal

769 et al. 2006), and their standard errors;  $C$ , sample coverage for rare interactions  
770 (Chao & Jost 2012). Scaled asymptotic estimators and their confidence intervals  
771 ( $CI$ ) were calculated by weighting  $Chao1$  and  $ACE$  with the observed frequencies  
772 of forbidden links.

773



774 **Tables**

Table 1:

Link type	Formulation	Definition
Potential links	$I_{max} = AP$	Size of network matrix, i.e. maximum number of potentially observable interactions; $A$ and $P$ , numbers of interacting animal and plant species, respectively.
Observed links	$I$	Total number of observed links in the network given a sufficient sampling effort. Number of ones in the adjacency matrix.
Unobserved links	$UL = I_{max} - I$	Number of zeroes in the adjacency matrix.
Forbidden links	$FL$	Number of links, which remain unobserved because of linkage constraints, irrespectively of sufficient sampling effort.
Missing links	$ML = AP - I - FL$	Number of links, which may exist in nature but need more sampling effort and/or additional sampling methods to be observed.

Table 2:

Link type	Pollination			Seed dispersal		
	Zackenberg	Grundvad	Arima Valley	Sta. Virginia	Hato Ratón	Nava Correhuelas
$I_{max}$	1891	646	522	423	272	825
$I$	268 (0.1417)	212 (0.3282)	185 (0.3544)	86 (0.1042)	151 (0.4719)	181 (0.2194)
$UL$	1507 (0.7969)	434 (0.6718)	337 (0.6456)	337 (0.4085)	169 (0.5281)	644 (0.7806)
$FL$	530 (0.3517)	107 (0.2465)	218 (0.6469)	260 (0.7715)	118 (0.6982)	302 (0.4689)
$FL_P$	530 (1.0000)	94 (0.2166)	0 (0.0000)	120 (0.1624)	67 (0.3964)	195 (0.3028)
$FL_S$	$\dots(\dots)$	8 (0.0184)	30 (0.0890)	140 (0.1894)	31 (0.1834)	46 (0.0714)
$FL_A$	$\dots(\dots)$	5 (0.0115)	150 (0.445) <sup>a</sup>	$\dots(\dots)$	20 (0.1183)	61 (0.0947)
$FL_O$	$\dots(\dots)$	$\dots(\dots)$	38 (0.1128) <sup>b</sup>	$\dots(\dots)$	$\dots(\dots)$	363 (0.5637)
$ML$	977 (0.6483)	327 (0.7535)	119 (0.3531)	77 (0.1042)	51 (0.3018)	342 (0.5311)

<sup>a</sup>, Lack of accessibility due to habitat uncoupling, i.e., canopy-foraging species vs. understory species.

<sup>b</sup>, Colour restrictions, and reward per flower too small relative to the size of the bird.

Table 3:

Interaction	Sample 1	Sample 2	Sample 3	...	Sample $i$
A1 - P2	12	2	0	...	6
A1 - P2	0	0	0	...	1
...	...	...	...	...	...
A5 - P3	5	0	1	...	18
A5 - P4	1	0	1	...	3
...	...	...	...	...	...
A <sub>i</sub> - P <sub>i</sub>	1	0	1	...	2

Table 4:

	Hato Ratón	Nava Correhuelas	Zackenberg
$A$	17	33	65
$P$	16	25	31
$I_{max}$	272	825	1891
$N$	3340	8378	1245
$I$	151	181	268
$C$	0.917	0.886	0.707
$Chao1$	$263.1 \pm 70.9$	$231.4 \pm 14.2$	$509.6 \pm 54.7$
$ACE$	$240.3 \pm 8.9$	$241.3 \pm 7.9$	$566.1 \pm 14.8$
$Scaled\ Chao$	195.4	162.7	308.4
$CI$	[124.5–266.3]	[148.5–176.9]	[253.6–363.1]
$Scaled\ ACE$	178.5	169.7	342.6
$CI$	[169.5–187.4]	[161.8–177.6]	[327.8–357.4]
% <i>unobserved</i> <sup>a</sup>	8.33	15.38	47.80

<sup>a</sup>, estimated with library Jade (R Core Development Team 2010, Chao et al. 2015)