Sampling networks of ecological interactions

Pedro Jordano*a

 $^{\rm a}$ Integrative Ecology Group, Estación Biológica de Doñana, Consejo Superior de Investigaciones Científicas (EBD-CSIC), Avenida Americo Vespucio s/n, E–41092 Sevilla, Spain

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Summary

- 1. Sampling ecological interactions presents similar challenges, problems, potential biases, and constraints as sampling individuals and species in biodiversity inventories. Robust estimates of the actual number of interactions (links) within diversified ecological networks require adequate sampling effort that needs to be explicitly gauged. Yet we still lack a sampling theory explicitly focusing on ecological interactions.
- 2. While the complete inventory of interactions is likely impossible, a robust characterization of its main patterns and metrics is probably realistic. We

^{*}jordano@ebd.csic.es

must acknowledge that a sizeable fraction of the maximum number of interactions I_{max} among, say, A animal species and P plant species (i.e., $I_{max} = AP$) is impossible to record due to forbidden links, i.e., life-history restrictions. Thus, the number of observed interactions I in robustly sampled networks is typically $I \ll I_{max}$, resulting in sparse interaction matrices with low connectance.

- 3. Here I provide a review and outline a conceptual framework for interaction sampling by building an explicit analogue to individuals and species sampling, thus extending diversity-monitoring approaches to the characterization of complex networks of ecological interactions. Contrary to species inventories, a sizable fraction of non-observed pairwise interactions cannot be sampled, due to biological constraints that forbid their occurrence.
- 4. Reasons for forbidden links are multiple but mainly stem from spatial and temporal uncoupling, size mismatches, and intrinsically low probabilities of interspecific encounter for most potential interactions of partner species. Adequately assessing the completeness of a network of ecological interactions thus needs knowledge of the natural history details embedded, so that forbidden links can be accounted for as a portion of the unobserved links when addressing sampling effort.
- 5. Recent implementations of inference methods for unobserved species or for individual-based data can be combined with the assessment of forbidden links. This can help in estimating their relative importance, simply by the difference between the asymptotic estimate of interaction richness in a robustly-sampled assemblage and the maximum richness I_{max} of interactions.

This is crucial to assess the rapid and devastating effects of defaunationdriven loss of key ecological interactions and the services they provide and the analogous losses related to interaction gains due to invasive species and biotic homogenization.

Keywords

complex networks, food webs, frugivory, mutualism, plant-animal interactions, pollination, seed dispersal

Introduction

Biodiversity sampling is a labour-intensive activity, and sampling is often not sufficient to detect all or even most of the species present in an assemblage.

Gotelli & Colwell (2011).

- Biodiversity species assessment aims at sampling individuals in collections and
- determining the number of species represented. Given that, by definition, samples
- ³ are incomplete, these collections do not enumerate the species actually present.
- 4 The ecological literature dealing with robust estimators of species richness and di-
- 5 versity in collections of individuals is immense, and a number of useful approaches
- 6 have been used to obtain such estimates (Magurran, 1988; Gotelli & Colwell, 2001;
- 7 Colwell et al., 2004; Hortal et al., 2006; Colwell, 2009; Gotelli & Colwell, 2011; Chao
- et al., 2014). Recent effort has been also focused at defining essential biodiversity
- 9 variables (EBV) (Pereira et al., 2013) that can be sampled and measured repeat-

edly to complement biodiversity estimates. Yet sampling species or taxa-specific EBVs is just probing a single component of biodiversity; interactions among species are another fundamental component, one that supports the existence, but in some cases also the extinction, of species. For example, the extinction of interactions represents a dramatic loss of biodiversity because it entails the loss of fundamen-14 tal ecological functions (Valiente-Banuet et al., 2014). This missed component of biodiversity loss, the extinction of ecological interactions, very often accompanies, 16 or even precedes, species disappearance. Interactions among species are thus a key 17 component of biodiversity and here I aim to show that most problems associated 18 with sampling interactions in natural communities relate to, and are even worse than, problems associated with sampling species diversity. I consider pairwise in-20 teractions among species at the habitat level, in the context of alpha diversity and the estimation of local interaction richness from sampling data (Chao et al., 2014). 22 In the first part I provide a succinct overview of previous work addressing sampling issues for ecological interaction networks. In the second part, I discuss specific rationales for sampling the biodiversity of ecological interactions. Finally, I provide 25 a short overview of asymptotic diversity estimates (Gotelli & Colwell, 2001), and a discussion of its application to interaction sampling. Most of the examples come from the analysis of plant-animal interaction networks, yet are applicable to other types of interspecific interactions. 29 Interactions can be a much better indicator of the richness and diversity of 30

Interactions can be a much better indicator of the richness and diversity of ecosystem functions than a simple list of taxa and their abundances and/or related biodiversity indicator variables (EBVs) (Memmott *et al.*, 2006; Valiente-Banuet *et al.*, 2014). Thus, sampling interactions should be a central issue when identifying and diagnosing ecosystem services (e.g., pollination, seeding by frugivores,

etc.). Fortunately, the whole battery of biodiversity-related tools used by ecologists to sample biodiversity (species, sensu stricto) can be extended and applied to the sampling of interactions (see Table 2 in Colwell et al., 2004). Monitoring interactions is a type of biodiversity sampling and is subject to similar methodological shortcomings, especially under-sampling (Jordano, 1987; Jordano et al., 2009; 39 Vázquez et al., 2009; Dorado et al., 2011; Rivera-Hutinel et al., 2012). We are interested in having a complete list of all the pairwise interactions among species 41 (e.g., all the distinct, species-species interactions, or links, among the pollinators 42 and flowering plants) that do actually exist in a given community. Sampling these 43 interactions thus entails exactly the same problems, limitations, constraints, and potential biases as sampling individual organisms and species diversity. As Mao & Colwell (2005) put it, these are the workings of Preston's demon, the moving "veil line" (Preston, 1948) between the detected and the undetected interactions as sample size increases. 48

Early efforts to recognize and solve sampling problems in analyses of interac-49 tions stem from research on food webs and to determine how undersampling bi-50 ases food web metrics (Martinez, 1991; Cohen et al., 1993; Wells & O'Hara, 2012, 51 among others). In addition, the myriad of classic natural history studies docu-52 menting animal diets, host-pathogen infection records, plant herbivory records, etc., represent efforts to document interactions occurring in nature. All of them share the problem of sampling incompleteness influencing the patterns and metrics reported. Yet, despite the early recognition that incomplete sampling may seri-56 ously bias the analysis of ecological networks (Jordano, 1987), only recent studies 57 have explicitly acknowledged it and attempted to determine its influence (Ollerton 58 & Cranmer, 2002; Nielsen & Bascompte, 2007; Vázquez et al., 2009; Gibson et al.,

2011; Olesen et al., 2011; Chacoff et al., 2012; Rivera-Hutinel et al., 2012; Olito & Fox, 2014; Bascompte & Jordano, 2014; Vizentin-Bugoni et al., 2014, 2016; Frund et al., 2016). The sampling approaches have been extended to predict patterns of 62 coextintions in interaction assemblages (e.g., hosts-parasites) (Colwell et al., 2012). Most empirical studies provide no indication of sampling effort, implicitly assuming that the reported network patterns and metrics are robust. Yet recent evidences point out that number of partner species detected, number of actual links, and 66 some aggregate statistics describing network patterns, are prone to sampling bias 67 (Nielsen & Bascompte, 2007; Dorado et al., 2011; Olesen et al., 2011; Chacoff et al., 68 2012; Rivera-Hutinel et al., 2012; Olito & Fox, 2014; Frund et al., 2016). Most of these evidences, however, come either from simulation studies (Frund et al., 2016) or from relatively species-poor assemblages. Most certainly, sampling limitations pervade biodiversity inventories and we might rightly expect that frequent interactions may be over-represented and rare interactions may be missed entirely in 73 studies of mega-diverse assemblages (Bascompte & Jordano, 2014); but, to what extent? 75

⁷⁶ Sampling interactions: methods

When we sample interactions in the field we record the presence of two species that interact in some way. For example, Snow and Snow(1988) recorded an interaction whenever they saw a bird "touching" a fruit on a plant. We observe and record feeding observations, visitation, occupancy, presence in pollen loads or in fecal samples, etc., of *individual* animals or plants and accumulate pairwise interactions, i.e., lists of species partners and the frequencies with which we observe them. We

assume that the matrix (species numbers) is predefined (i.e., all species interacting are well documented).

Most types of ecological interactions can be illustrated with bipartite graphs, 85 with two or more distinct groups of interacting partners (Bascompte & Jordano, 2014); for illustration purposes I'll focus more specifically on plant-animal inter-87 actions. Sampling interactions requires filling the cells of an interaction matrix with data. The matrix, $\Delta = AP$ (the adjacency matrix for the graph representa-89 tion of the network), is a 2D inventory of the interactions among, say, A animal 90 species (rows) and P plant species (columns) (Jordano, 1987; Bascompte & Jor-91 dano, 2014). The matrix entries illustrate the values of the pairwise interactions visualized in the Δ matrix, and can be 0 or 1, for presence-absence of a given 93 pairwise interaction, or take a quantitative weight w_{ii} to represent the interaction 94 intensity or unidirectional effect of species j on species i (Bascompte & Jordano, 95 2014; Vázquez et al., 2015). The outcomes of most ecological interactions are 96 dependent on frequency of encounters (e.g., visit rate of pollinators, number of 97 records of ant defenders, frequency of seeds in fecal samples). Thus, a frequently 98 used proxy for interaction intensities w_{ji} is just how frequent new interspecific 99 encounters are, whether or not appropriately weighted to estimate interaction ef-100 fectiveness (Vázquez et al., 2005). 101

We need to define two basic steps in the sampling of interactions: 1) which type of interactions we sample; and 2) which type of record we get to document the existence of an interaction. In step #1 we need to take into account whether we are sampling the whole community of interactor species (all the animal and plant species) or just a subset of them, i.e., a sub matrix $\Delta_{m,n}$ of m < A animal species and n < P plant species of the adjacency matrix Δ_{AP} . Subsets can be:

132

a) all the potential plants interacting with a subset of the animals (Fig. 1a); b) 108 all the potential animal species interacting with a subset of the plant species (Fig. 109 1b); c) a subset of all the potential animal species interacting with a subset of all 110 the plant species (Fig. 1c). While some discussion has considered how to establish 111 the limits of what represents a network (Strogatz, 2001) (in analogy to discussion 112 on food-web limits; Cohen, 1978), it must be noted that situations a-c in Fig. 1 113 do not represent complete interaction networks. Subnet sampling is generalized 114 in studies of biological networks (e.g., protein interactions, gene regulation), yet 115 it is important to recognize that most properties of subnetworks (even random 116 subsamples) do not represent properties of whole networks (Stumpf et al., 2005). 117 In step #2 above we face the problem of the type of record we take to sample 118 interactions. This is important because it defines whether we approach the problem 119 of filling up the interaction matrix in a "zoo-centric" way or in a "phyto-centric" 120 way. Zoo-centric studies directly sample animal activity and document the plants 121 'touched' by the animal. For example, analysis of pollen samples recovered from the 122 body of pollinators, analysis of fecal samples of frugivores, radio-tracking data, etc. 123 Phyto-centric studies take samples of focal individual plant species and document 124 which animals 'arrive' or 'touch' the plants. Examples include focal watches of 125 fruiting or flowering plants to record visitation by animals, raising insect herbivores 126 from seed samples, identifying herbivory marks in samples of leaves, etc. 127 Most recent analyses of plant-animal interaction networks are phyto-centric; 128 just 3.5% of available plant-pollinator (N=58) or 36.6% plant-frugivore (N=22) 129 interaction datasets are zoo-centric (see Schleuning et al., 2012). Moreover, most 130 available datasets on host-parasite (parasitoid) or plant-herbivore interactions are 131

"host-centric" or phyto-centric (e.g., Thébault & Fontaine, 2010; Morris et al.,

2013; Eklöf et al., 2013). This may be related to a variety of causes, like preferred 133 methodologies by researchers working with a particular group or system, logistic limitations, or inherent taxonomic focus of the research questions. A likely result 135 of phyto-centric sampling would be adjacency matrices with large A: P ratios. In 136 contrast, zoo-centric samplings might be prone to detect plants from outside the 137 habitat, complicating the definition of network boundaries. In any case we don't 138 have a clear view of the potential biases that taxa-focused sampling may generate 139 in observed network patterns, for example by generating consistently asymmetric 140 interaction matrices (Dormann et al., 2009). 141

Reasonably complete analyses of interaction networks can be obtained when 142 combining both phyto-centric and zoo-centric sampling. For example, Bosch et 143 (2009) showed that the addition of pollen load data on top of focal-plant 144 sampling of pollinators unveiled a significant number of interactions, resulting in 145 important network structural changes. Olesen et al. (2011) identified pollen loads 146 on sampled insects and added the new links to an observation-based visitation ma-147 trix, with an extra 5% of links representing the estimated number of missing links 148 in the pollination network. The overlap between observational and pollen-load 149 recorded links was only 33%, underscoring the value of combining methodolog-150 ical approaches. Zoo-centric sampling has recently been extended with the use 151 of DNA-barcoding, for example with plant-herbivore (Jurado-Rivera et al., 2009), 152 host-parasiotid (Wirta et al., 2014; Evans et al., 2016), and plant-frugivore inter-153 actions (González-Varo et al., 2014). For mutualistic networks we would expect 154 that zoo-centric sampling could help unveiling interactions of the animals with 155 rare plant species or for relatively common plants species which are difficult to 156 sample by direct observation. Future methodological work may provide significant advances showing how mixing different sampling strategies strengthens the completeness of network data. These mixed strategies may combine, for instance, timed watches at focal plants, spot censuses along walked transects, pollen load or seed contents analyses, monitoring with camera traps, and DNA barcoding records. However, there are no tested protocols and/or sampling designs for ecological interaction studies to suggest an optimum combination of approaches. Ideally, pilot studies would provide adequate information for each specific study setting.

Sampling interactions: rationale

The number of distinct pairwise interactions that we can record in a landscape (an 166 area of relatively homogeneous vegetation) is equivalent to the number of distinct 167 classes in which we can classify the recorded encounters among individuals of 168 two different species. Yet, individual-based interaction networks have been only 169 recently studied (Dupont et al., 2011; Wells & O'Hara, 2012). The most usual 170 approach has been to pool individual-based interaction data into species-based 171 summaries, an approach that ignores the fact that only a fraction of individuals 172 may actually interact given a per capita interaction effect (Wells & O'Hara, 2012). 173 Wells & O'Hara (2012) illustrate the pros and cons of the approach. We walk in 174 the forest and see a blackbird Tm picking an ivy Hh fruit and ingesting it: we 175 have a record for Tm - Hh interaction. We keep advancing and record again a 176 blackbird feeding on hawthorn Cm fruits so we record a Tm - Cm interaction; 177 as we advance we encounter another ivy plant and record a blackcap swallowing a fruit so we now have a new Sa - Hh interaction, and so on. At the end we have 179 a series of classes (e.g., Sa - Hh, Tm - Hh, Tm - Cm, etc.), along with their

observed frequencies.

182

times in our sampling: c_1 is the number of singletons (interactions recorded once), 183 c_2 is the number of twin pairs (interactions with just two records), c_3 the number 184 of triplets, etc. The problem thus turns to be estimating the number of distinct 185 classes C from the vector of c_j values and the frequency of unobserved interactions 186 (see "The real missing links" below). 187 More specifically, we usually obtain a type of reference sample (Chao et al., 188 2014) for interactions: a series of repeated samples (e.g., observation days, 1h 189 watches, etc.) with quantitative information, i.e., recording the number of in-190 stances of each interaction type on each day. This replicated abundance data, 191 can be treated in three ways: 1) Abundance data within replicates: the counts 192 of interactions, separately for each day; 2) Pooled abundance data: the counts of 193 interactions, summed over all days (the most usual approach); and 3) Replicated 194 incidence data: the number of days on which we recorded each interaction. As-195 suming a reasonable number of replicates, replicated incidence data is considered 196 to be the most robust statistically, as it takes account of heterogeneity among days 197 (Colwell et al., 2004, 2012; Chao et al., 2014). Thus, both presence-absence and 198 weighted information on interactions can be accommodated for this purpose. 199

We get a vector $c = [c_1...c_n]'$ where c_j is the number of classes represented j

$_{200}$ The species assemblage

When we consider an observed and recorded sample of interactions on a particular assemblage of A_{obs} and P_{obs} species (or a set of replicated samples) as a reference sample (Chao *et al.*, 2014) we may have three sources of undersampling error.

These sources are ignored if we treat the reference sample as a true representation 204 of the interactions in a well-defined assemblage: 1) some animal species are actually 205 present but not observed (zero abundance or incidence in the interactions in the 206 reference sample), A_0 ; 2) some plant species are actually present but not observed (zero abundance or incidence in the interactions in the reference sample), P_0 ; 3) 208 some unobserved links (the zeroes in the adjacency matrix, UL) may actually 209 occur but not recorded. Thus a first problem is determining if A_{obs} and P_{obs} truly 210 represent the actual species richness interacting in the assemblage. To this end 211 we might use the replicated reference samples to estimate the true number of 212 interacting animal A_{est} and plant P_{est} species as in traditional diversity estimation 213 analysis (Chao et al., 2014). If there are no uniques (species seen on only one day), 214 then A_0 and P_0 will be zero (based on the Chao2 formula), and we have A_{obs} and 215 P_{obs} as robust estimates of the actual species richness of the assemblage. If A_0 216 and P_0 are not zero they estimate the minimum number of undetected animal and 217 plant species that can be expected with a sufficiently large number of replicates, 218 taken from the same assemblage/locality by the same methods in the same time 219 period. We can use extrapolation methods (Colwell et al., 2012) to estimate how 220 many additional replicate surveys it would take to reach a specified proportion q221 of A_{est} and P_{est} .

223 The interactions

We are then faced with assessing the sampling of interactions I. Table 1 summarizes the main components and targets for estimation of interaction richness. In contrast with traditional species diversity estimates, sampling networks has the

241

paradox that despite the potentially interacting species being present in the sam-227 pled assemblage (i.e., included in the A_{obs} and P_{obs} species lists), some of their pairwise interactions are impossible to record. The reason is forbidden links. In-229 dependently of whether we sample full communities or subset communities we face a problem: some of the interactions that we can visualize in the empty adjacency 231 matrix Δ will simply not occur. With a total of $A_{obs}P_{obs}$ "potential" interactions 232 (eventually augmented to $A_{est}P_{est}$ in case we have undetected species), a fraction 233 of them are impossible to record, because they are forbidden (Jordano et al., 2003; 234 Olesen et al., 2011). 235 Our goal is to estimate the true number of non-null AP interactions, including 236 interactions that actually occur but have not been observed (I_0) from the repli-237 cated incidence frequencies of interaction types: $I_{est} = I_{obs} + I_0$. Note that I_0 238 estimates the minimum number of undetected plant-animal interactions that can 239 be expected with a sufficiently large number of replicates, taken from the same 240 assemblage/locality by the same methods in the same time period. Therefore we

have two types of non-observed links: UL* and UL, corresponding to the real 242 assemblage species richness and to the observed assemblage species richness, re-243 spectively (Table 1). 244 Forbidden links are non-occurrences of pairwise interactions that can be ac-245 counted for by biological constraints, such as spatio-temporal uncoupling (Jor-246 dano, 1987), size or reward mismatching, foraging constraints (e.g., accessibility) 247 (Moré et al., 2012), and physiological-biochemical constraints (Jordano, 1987). We 248

communities (Jordano et al., 2003; Stang et al., 2009; Vázquez et al., 2009; Olesen 250

still have very little information about the frequency of forbidden links in natural

et al., 2011; Ibanez, 2012; Maruyama et al., 2014; Vizentin-Bugoni et al., 2014)

(Table 1). Forbidden links are thus represented as structural zeroes in the interaction matrix, i.e., matrix cells that cannot get a non-zero value. Therefore, we need to account for the frequency of these structural zeros in our matrix before proceeding.

Our main problem then turns to estimate the number of true missed links, 256 i.e., those that can't be accounted for by biological constraints and that might 257 suggest undersampling. Thus, the sampling of interactions in nature, as the sam-258 pling of species, is a cumulative process. In our analysis, we are not re-sampling 259 individuals, but interactions, so we built interaction-based accumulation curves. 260 We add new, distinct, interactions recorded as we increase sampling effort (Fig. 2, 261 and Supplementary Online Material). We can obtain an Interaction Accumulation 262 Curve (IAC) analogous to a Species Curve (SAC) (see Supporting Information in 263 the online data availability repository): the observed number of distinct pairwise 264 interactions in a survey or collection as a function of the accumulated number of 265 observations or samples (Colwell, 2009). 266

²⁶⁷ Empirical data on Forbidden Links

Adjacency matrices are frequently sparse, i.e., they are densely populated with zeroes, with a fraction of them being structural (unobservable interactions) (Bascompte & Jordano, 2014). Thus, it would be a serious interpretation error to attribute the sparseness of adjacency matrices for bipartite networks to just the result of undersampling. The actual typology of link types in ecological interaction networks is thus more complex than just the two categories of observed and unobserved interactions (Table 1). Unobserved interactions are represented by

zeroes and belong to two categories. Missing interactions may actually exist but 275 require additional sampling or a variety of methods to be observed. Forbidden links, on the other hand, arise due to biological constraints limiting interactions 277 and remain unobservable in nature, irrespectively of sampling effort (Table 1). Forbidden links FL may actually account for a relatively large fraction of unob-279 served interactions UL when sampling taxonomically-restricted subnetworks (e.g., 280 plant-humming bird pollination networks) (Table 1). Phenological uncoupling is 281 also prevalent in most networks, and may add up to explain ca. 25-40% of the for-282 bidden links, especially in highly seasonal habitats, and up to 20% when estimated 283 relative to the total number of unobserved interactions (Table 2). In any case, we 284 might expect that a fraction of the missing links ML would be eventually explained 285 by further biological reasons, depending on the knowledge of natural details of the 286 particular systems. Our goal as naturalists would be to reduce the fraction of UL287 which remain as missing links; to this end we might search for additional biological 288 constraints or increase sampling effort. For instance, habitat use patterns by hum-289 mingbirds in the Arima Valley network (Table 2; Snow & Snow, 1972) impose a 290 marked pattern of microhabitat mismatches causing up to 44.5% of the forbidden 291 links. A myriad of biological causes beyond those included as FL in Table 1 may 292 contribute explanations for UL: limits of color perception, presence of secondary 293 metabolites in fruit pulp and leaves, toxins and combinations of monosaccharides 294 in nectar, etc. For example, aside from FL, some pairwise interactions may sim-295 ply have an asymptotically-zero probability of interspecific encounter between the 296 partner species, if they are very rare. However, it is surprising that just the limited 297 set of forbidden link types considered in Table 1 explain between 24.6-77.2\% of 298 the unobserved links. Notably, the Arima Valley, Santa Virgínia, and Hato Ratón

networks have > 60% of the unobserved links explained, which might be related to the fact that they are subnetworks (Arima Valley, Santa Virgínia) or relatively small networks (Hato Ratón). All this means that empirical networks may have sizable fractions of structural zeroes. Ignoring this biological fact may contribute to wrongly inferring undersampling of interactions in real-world assemblages.

To sum up, two elements of inference are required in the analysis of unobserved 305 interactions in ecological interaction networks: first, detailed natural history infor-306 mation on the participant species that allows the inference of biological constraints 307 imposing forbidden links, so that structural zeroes can be identified in the adja-308 cency matrix. Second, a critical analysis of sampling robustness and a robust 309 estimate of the actual fraction of missing links, M, resulting in a robust estimate 310 of I. In the next sections we explore these elements of inference, using IACs as 311 analogs to SACs to assess the robustness of interaction sampling. 312

Assessing sampling effort when recording interactions: asymptotic diversity estimates

A plot of the cumulative number of species recorded, S_n , as a function of some measure of sampling effort (say, n samples taken) yields the species accumulation curve (SAC) or collector's curve (Colwell & Coddington, 1994). Similarly, interaction accumulation curves (IAC), analogous to SACs (Gotelli & Colwell, 2001; Hortal et al., 2006; Chao, 2005; Colwell, 2013), can be used to assess the robustness of interactions sampling for plant-animal community datasets (Jordano, 1987; Jordano et al., 2009; Olesen et al., 2011; Chacoff et al., 2012).

The basic method to estimate sampling effort and explicitly show the analogues 322 with rarefaction analysis in biodiversity research is to vectorize the interaction matrix AP so that we get a vector of all the potential pairwise interactions (I_{max} , 324 Table 1) that can occur in the observed assemblage with A_{obs} animal species and 325 P_{obs} plant species. The new "species" we aim to sample are the pairwise interactions 326 (Table 3), as previously discussed. In general, if we have A = 1...i, animal species 327 and P = 1...j plant species (assuming a complete list of species in the assemblage), 328 we'll have a vector of "new" species to sample: $A_1P_1, A_1P_2, ...A_2P_1, A_2P_2, ...A_iP_j$. 329 We can represent the successive samples where we can potentially get records of 330 these interactions in a matrix with the vectorized interaction matrix and columns 331 representing the successive samples we take (Table 3). This is simply a vectorized 332 version of the interaction matrix Δ . This is analogous to a biodiversity sam-333 pling matrix with species as rows and sampling units (e.g., quadrats) as columns 334 (Jordano et al., 2009). The package EstimateS (Colwell, 2013) includes a com-335 plete set of functions for estimating the mean IAC and its unconditional standard 336 deviation from random permutations of the data, or subsampling without replace-337 ment (Gotelli & Colwell, 2001); it further reports asymptotic estimators for the 338 expected number of distinct pairwise interactions included in a given reference 339 sample of interaction records (see also the specaccum function in library vegan 340 of the R Package) (R Development Core Team, 2010; Jordano et al., 2009; Olesen 341 et al., 2011). In particular, we may take advantage of replicated incidence data, 342 as it takes account of heterogeneity among samples (days, censuses, etc.; R.K Col-343 well, pers. comm.) (see also Colwell et al., 2004, 2012; Chao et al., 2014). Future theoretical work will be needed to formally assess the similarities and differences 345 between the species vs. interactions sampling approaches and developing biologically meaningful null models of expected interaction richness with added sampling effort.

Diversity-accumulation analysis (Magurran, 1988; Hortal et al., 2006) comes 349 up immediately with this type of dataset. This procedure plots the accumulation curve for the expected number of distinct pairwise interactions recorded with in-351 creasing sampling effort (Jordano et al., 2009; Olesen et al., 2011). Asymptotic 352 estimates of interaction richness and its associated standard errors and confidence 353 intervals can thus be obtained (Hortal et al., 2006) (see Table 4 and Supplemen-354 tary Online Material). The characteristic feature of interaction datasets is that, 355 due to forbidden links, a number of pairwise interactions among the I_{max} number 356 specified in the Δ adjacency matrix cannot be recorded, irrespective of sampling 357 effort. 358

We may expect undersampling specially in moderate to large sized networks with multiple modules (i.e., species subsets requiring different sampling strategies)

(Jordano, 1987; Olesen et al., 2011; Chacoff et al., 2012); adequate sampling may be feasible when interaction subwebs are studied (Olesen et al., 2011; Vizentin-Bugoni et al., 2014), typically with more homogeneous subsets of species (e.g., bumblebee-pollinated flowers).

Mixture models incorporating detectabilities have been proposed to effectively
account for rare species (Mao & Colwell, 2005). In an analogous line, mixture
models could be extended to samples of pairwise interactions, also with specific
detectability values. These detection rate/odds could be variable among groups of
interactions, depending on their specific detectability. For example, detectability of
flower-pollinator interactions involving bumblebees could have a higher detectability than flower-pollinator pairwise interactions involving, say, nitidulid beetles.

These more homogeneous groupings of pairwise interactions within a network de-372 fine modules (Bascompte & Jordano, 2014), so we might expect that interactions of a given module (e.g., plants and their humming bird pollinators; Fig. 1a) may 374 share similar detectability values, in an analogous way to species groups receiving homogeneous detectability values in mixture models (Mao & Colwell, 2005). In 376 its simplest form, this would result in a sample with multiple pairwise interactions 377 detected, in which the number of interaction events recorded for each distinct 378 interaction found in the sample is recorded (i.e., a column vector in Table 3, cor-379 responding to, say, a sampling day). The number of interactions recorded for the 380 i_{th} pairwise interaction (i.e., A_iP_j in Table 3), Y_i could be treated as a Poisson 381 random variable with a mean parameter λ_i , its detection rate. Mixture models 382 (Mao & Colwell, 2005) include estimates for abundance-based data (their analogs 383 in interaction sampling would be weighted data), where Y_i is a Poisson random 384 variable with detection rate λ_i . This is combined with the incidence-based model, 385 where Y_i is a binomial random variable (their analogous in interaction sampling 386 would be presence/absence records of interactions) with detection odds λ_i . Let 387 T be the number of samples in an incidence-based data set. A Poisson/binomial 388 density can be written as (Mao & Colwell, 2005):

$$g(y;\lambda) = \begin{cases} \frac{\lambda^y}{y!e^{\lambda}} & [1] \\ \binom{T}{y} \frac{\lambda^y}{(1+\lambda)^T} & [2] \end{cases}$$

where [1] corresponds to a weighted network, and [2] to a qualitative network.

The detection rates λ_i depend on the relative abundances ϕ_i of the interactions,

the probability of a pairwise interaction being detected when it is present, and the

sample size (the number of interactions recorded), which, in turn, is a function 393 of the sampling effort. Unfortunately, no specific sampling model has been developed along these lines for species interactions and their characteristic features. For 395 example, a complication factor might be that interaction abundances, ϕ_i , in real assemblages are a function of the abundances of interacting species that determine 397 interspecific encounter rates; yet they also depend on biological factors that ulti-398 mately determine if the interaction occurs when the partner species are present. 399 For example, λ_i should be set to zero for all FL. It its simplest form, ϕ_i could be 400 estimated from just the product of partner species abundances, an approach re-401 cently used as a null model to assess the role of biological constraints in generating 402 forbidden links and explaining interaction patterns (Vizentin-Bugoni et al., 2014). 403 Yet more complex models (e.g., Wells & O'hara 2012; 2016) should incorporate not 404 only interspecific encounter probabilities, but also interaction detectabilities, phe-405 notypic matching and incidence of forbidden links. Mixture models are certainly 406 complex and for most situations of evaluating sampling effort better alternatives 407 include the simpler incidence-based rarefaction and extrapolation (Colwell et al., 408 2012; Chao et al., 2014).

The real missing links

Given that a fraction of unobserved interactions can be accounted for by forbidden links, what about the remaining missing interactions? We have already discussed that some of these could still be related to unaccounted constraints, and still others would be certainly attributable to insufficient sampling. Would this always be the case? A crucial ecological aspect limiting interactions within multispecific assemblages of distinct taxonomic relatedness (Fig. 2) is the probability of interspecific encounter, i.e., the probability that two individuals of the partner species actually encounter each other in nature.

Given log-normally distributed abundances of the two species groups, the ex-419 pected probabilities of interspecific encounter (PIE) would be simply the product 420 of the two lognormal distributions. Thus, we might expect that for very low PIE 421 values, pairwise interactions would be either extremely difficult to sample, or sim-422 ply do not occur in nature. Consider the Nava de las Correhuelas interaction 423 web (NCH, Table 2, 4), with A = 36, P = 25, I = 181, and almost half of the 424 unobserved interactions not accounted for by forbidden links, thus M = 53.1%425 (Jordano et al., 2009). A sizable fraction of these possible but missing links would 426 be simply not occurring in nature, most likely due to extremely low PIE, in fact 427 asymptotically zero. Given the vectorized list of pairwise interactions for NCH, I 428 computed the PIE values for each one by multiplying element-wise the two species 429 abundance distributions. The $PIE_{max} = 0.0597$, being a neutral estimate, based 430 on the assumption that interactions occur in proportion to the species-specific local 431 abundances. With $PIE_{median} < 1.4 \ 10^{-4}$ we may safely expect (note the quantile 432 estimate $Q_{75\%} = 3.27 \ 10^{-4}$) that a sizable fraction of these missing interactions 433 may not occur according to this neutral expectation (Jordano, 1987; Olesen et al., 434 2011) (neutral forbidden links, sensu Canard et al., 2012). 435

When we consider the vectorized interaction matrix, enumerating all pairwise interactions for the *AP* combinations, the expected probabilities of finding a given interaction can be estimated with a Good-Turing approximation (Good, 1953). The technique, developed by Alan Turing and I.J. Good with applications to linguistics and word analysis (Gale & Sampson, 1995) has been recently extended in

novel ways for ecological analyses (Chao et al., 2015). In our present context it estimates the probability of recording an interaction of a hitherto unseen pair of partners, given a set of past records of interactions between other species pairs. Let a sample of N interactions so that n_r distinct pairwise interactions have exactly r records. All Good-Turing estimators obtain the underlying frequencies of events as:

$$P(X) = \frac{(N_X + 1)}{T} \left(1 - \frac{E(1)}{T}\right) \tag{1}$$

where X is the pairwise interaction, N_X is the number of times interaction X 447 is recorded, T is the sample size (number of distinct interactions recorded) and E(1) is an estimate of how many different interactions were recorded exactly once. 449 Strictly speaking Equation (1) gives the probability that the next interaction type recorded will be X, after sampling a given assemblage of interacting species. In 451 other words, we scale down the maximum-likelihood estimator $\frac{n}{T}$ by a factor of $\frac{1-E(1)}{T}$. This reduces all the probabilities for interactions we have recorded, and 453 makes room for interactions we haven't seen. If we sum over the interactions we 454 have seen, then the sum of P(X) is $1 - \frac{1 - E(1)}{T}$. Because probabilities sum to one, 455 we have the left-over probability of $P_{new} = \frac{E(1)}{T}$ of seeing something new, where new means that we sample a new pairwise interaction. 457

58 Discussion

Recent work has inferred that most data available for interaction networks are incomplete due to undersampling, resulting in a variety of biased parameters and

network patterns (Chacoff et al., 2012). It is important to note, however, that in 461 practice, most surveyed networks to date have been subnets of much larger networks. This is also true for protein interaction, gene regulation, and metabolic 463 networks, where only a subset of the molecular entities in a cell have been sampled (Stumpf et al., 2005). Despite recent attempts to document whole ecosystem 465 meta-networks (Pocock et al., 2012), it is likely that most ecological interaction networks will illustrate just major ecosystem compartments. Due to their high 467 generalization, high temporal and spatial turnover, and high complexity of associ-468 ation patterns, adequate sampling of ecological interaction networks is challenging 469 and requires extremely large sampling effort. Undersampling of ecological networks may originate from the analysis of assemblage subsets (e.g., taxonomically 471 or functionally defined), and/or from logistically-limited sampling effort. It is ex-472 tremely hard to robustly sample the set of biotic interactions even for relatively 473 simple, species-poor assemblages; thus, we need to assess how robust is the char-474 acterization of the adjacency matrix Δ . Concluding that an ecological network 475 dataset is undersampled just by its sparseness would be unrealistic. The reason 476 stems from a biological fact: a sizeable fraction of the maximum, potential links 477 that can be recorded among two distinct sets of species is simply unobservable, irrespective of sampling effort (Jordano, 1987). In addition, sampling effort needs 479 to be explicitly gauged because of its potential influence on parameter estimates 480 for the network. 481

Missing links are a characteristic feature of all plant-animal interaction networks, and likely pervade other ecological interactions. Important natural history details explain a fraction of them, resulting in unrealizable interactions (i.e., forbidden interactions) that define structural zeroes in the interaction matrices and contribute to their extreme sparseness. Sampling interactions is a way to monitor biodiversity beyond the simple enumeration of component species and to develop efficient and robust inventories of functional interactions. Yet no sampling theory for interactions is available. Focusing just on the realized interactions or treating missing interactions as the expected unique result of sampling bias would miss important components to understand how all sorts of interactions coevolve within complex webs of interdependence among species.

Contrary to species inventories, a sizable fraction of non-observed pairwise 493 interactions cannot be sampled, due to biological constraints that forbid their 494 occurrence. Moreover, recent implementations of inference methods for unobserved 495 species (Chao et al., 2015) or for individual-based data (Wells & O'Hara, 2012) 496 can be combined with the forbidden link approach. They do not account either 497 for the existence of these ecological constraints, but can help in estimating their 498 relative importance, simply by the difference between the asymptotic estimate of 499 interaction richness in a robustly-sampled assemblage and the maximum richness 500 I_{max} of interactions. 501

Ecological interactions provide the wireframe supporting the lives of species, 502 and they also embed crucial ecosystem functions which are fundamental for sup-503 porting the Earth system. We still have a limited knowledge of the biodiversity 504 of ecological interactions, and they are being lost (extinct) at a very fast pace, 505 frequently preceding species extinctions (Valiente-Banuet et al., 2014). We ur-506 gently need robust techniques to assess the completeness of ecological interactions 507 networks because this knowledge will allow the identification of the minimal components of their ecological complexity that need to be restored to rebuild functional 509 ecosystems after perturbations.

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Data accessiblity

This review does not use new raw data, but includes some re-analyses of previously published material. All the original data supporting the paper, R code, supplementary figures, and summaries of analytical protocols is available at the author's GitHub repository (https://github.com/pedroj/MS_Network-Sampling), with DOI: 10.5281/zenodo.29437.

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24 Figure captions

735

Figure 1. Sampling ecological interaction networks (e.g., plant-animal interac-725 tions) usually focus on different types of subsampling the full network, yielding 726 submatrices $\Delta[m,n]$ of the full interaction matrix Δ with A and P animal and 727 plant species. a) all the potential plants interacting with a subset of the animals 728 (e.g., studying just the humming bird-pollinated flower species in a community); 729 b) all the potential animal species interacting with a subset of the plant species 730 (e.g., studying the frugivore species feeding on figs Ficus in a community); and c) 731 sampling a subset of all the potential animal species interacting with a subset of all 732 the plant species (e.g., studying the plant-frugivore interactions of the rainforest 733 understory). 734

Figure 2. Sampling species interactions in natural communities. Suppose an 736 assemblage with A=3 animal species (red, species 1-3 with three, two, and 1 737 individuals, respectively) and P=3 plant species (green, species a-c with three individuals each) (colored balls), sampled with increasing effort in steps 1 to 6 739 (panels). In Step 1 we record a total of three interactions (black lines) for animal species 1 and plant species a and b, represented as two distinct pairwise interac-741 tions: 1-a and 1-b. As we advance our sampling (panels 1 to 6, illustrating e.g., additional sampling days) we record new distinct interactions. Note that we 743 actually sample and record interactions among individuals, yet we pool the data across species to get a species by species interaction matrix. Few network analyses 745 have been carried out on individual data (e.g., Dupont et al., 2014). Above and below each panel are the cumulative number of distinct species and interactions $_{748}$ $\,$ sampled, so that panel 6 illustrates the final network.

749

Figures Figures

Figure 1:



Figure 2:

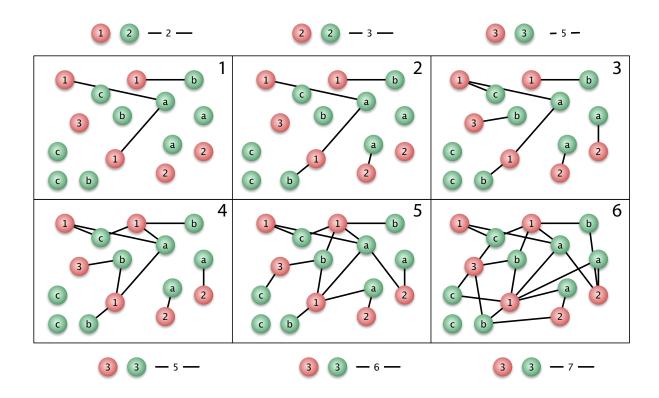


Table captions

Table 1. A taxonomy of link types for ecological interactions (Olesen *et al.* 2011). A_{obs} , number of animal species; P_{obs} , number of plant species; I_{obs} , number of observed links; FL, number of forbidden links; and ML, number of missing links.

As natural scientists, our ultimate goal is to eliminate ML from the equation FL = AP - I - ML, which probably is not feasible given logistic sampling limitations. When we, during our study, estimate ML to be negligible, we cease observing and estimate I and FL.

759

Table 2. Frequencies of different type of forbidden links in natural plant-animal 760 interaction assemblages. AP, maximum potential links, I_{max} ; I, number of ob-761 served links; UL, number of unobserved links; FL, number of forbidden links; 762 FL_P , phenology constraints; FL_S , size restrictions; FL_A , accessibility constraints; 763 FL_O , other types of restrictions; ML, unknown causes (missing links). Relative 764 frequencies (in parentheses) calculated over I_{max} for I and UL; those for FL, and ML, over UL; for all forbidden links types (FL_P, FL_S, FL_A, FL_O) , calculated 766 over FL. Data for Hato Ratón and Nava Correhuelas include interactions with bird and mammal frugivores. References, from left to right: Olesen et al. 2008; 768 Olesen & Myrthue unpubl.; Snow & Snow 1972 and Jordano et al. 2006; Vizentin-Bugoni et al. 2014; Jordano et al. 2009; Olesen et al. 2011. 770

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Table 3. A vectorized interaction matrix corresponding to the sampling shown in Figure 2. All the possible distinct pairwise interactions (cells of the adjacency matrix) between animal species (A) 1, 2, and 3 and plant species (P) a, b and c

can be potentially recorded in any of the six sampling periods (panels in figure 1). For each sampling period, N is the cumulative number of records and I is the cumulative number of distinct pairwise interactions recorded (1's in the binary adjacency matrix).

779

Table 4. Sampling statistics for three plant-animal interaction networks (Olesen et al. 2011). Symbols as in Table 1; N, number of records; Chao1 and ACE are asymptotic estimators for the number of distinct pairwise interactions I (Hortal et al. 2006), and their standard errors; C, sample coverage for rare interactions (Chao & Jost 2012). Scaled asymptotic estimators and their confidence intervals (CI) were calculated by weighting Chao1 and ACE with the observed frequencies of forbidden links. Data for Hato Ratón and Nava Correhuelas include only plant-bird interactions.

788

Tables

Table 1:

Link type	Formulation	Definition
Potential links	$I_{max} = A_{obs} P_{obs}$	Size of observed network matrix, i.e. maximum number of potentially observable interactions; A_{obs} and P_{obs} , numbers of interacting animal and plant species, respectively. These might be below the real numbers of animal and plant species, A_{est} and P_{est} .
Observed links	I_{obs}	Total number of observed links in the network given a sufficient sampling effort. Number of ones in the adjacency matrix.
True links	I_{est}	Total number of links in the network given a sufficient sampling effort; expected for the augmented $A_{est}P_{est}$ matrix.
Unobserved links	$UL = I_{max} - I_{obs}$	Number of zeroes in the adjacency matrix.
True unobserved links	$UL* = I_{max} - I_{obs}$	Number of zeroes in the augmented adjacency matrix that, eventually, includes unobserved species.
Forbidden links	FL	Number of links, which remain unobserved because of linkage constraints, irrespectively of sufficient sampling effort.
Observed Missing links	$ML = A_{obs}P_{obs} - I_{obs} - FL$	Number of links, which may exist in nature but need more sampling effort and/or additional sampling methods to be observed.
True Missing links	$ML* = A_{est}P_{est} - I_{est} - FL$	Number of links, which may exist in nature but need more sampling effort and/or additional sampling methods to be observed. Augments ML for the $A_{est}P_{est}$ matrix.

Table 2:

		Pollination			Seed dispersal	
Link type	Zackenberg	g Grundvad		Sta. Virginia	Hato Ratón	Nava Correhuelas
I_{max}	1891	646	522	423	320	900
I	384 (0.2031)	212 (0.3282)	185 (0.3544)	86 (0.2033)	151 (0.4719)	181 (0.2011)
UL	1507 (0.7969)	$ 434 \\ (0.6718) $	337 (0.6456)	337 (0.7967)	$ \begin{array}{c} 169 \\ (0.5281) \end{array} $	719 (0.7989)
FL	530 (0.3517)	107 (0.2465)	218 (0.6469)		118 (0.6982)	320 (0.4451)
FL_P	530 (1.0000)	94 (0.8785)	$\cdots (\cdots)$		67 (0.5678)	195 (0.6094)
FL_S	$\cdots (\cdots)$		30 (0.1376)			46 (0.1438)
FL_A	$\cdots (\cdots)$		$150 (0.6881)^a$		20 (0.1695)	79 (0.2469)
FL_O	$\cdots (\cdots)$	$\cdots (\cdots)$	$38 (0.1743)^b$	$\cdots (\cdots)$	$\cdots (\cdots)$	$\cdots (\cdots)$
ML		327 (0.7535)				

^a, Lack of accessibility due to habitat uncoupling, i.e., canopy-foraging species vs.

understory species. b , Colour restrictions, and reward per flower too small relative to the size of the bird. Dots indicate no data available for the FL type.

Table 3:

Interaction	Sample 1	Sample 2	Sample 3	Sample 4	Sample 5	Sample 6
1-a	2	2	2	3	3	5
1-b	1	2	2	3	4	4
1-c	0	0	1	2	2	2
2-a	0	1	2	2	3	3
2-b	0	0	0	0	0	2
2-c	0	0	0	0	0	0
3-a	0	0	0	0	0	0
3-b	0	0	1	1	1	2
3-с	0	0	0	0	1	2
\overline{N}	3	5	8	11	14	20
I	2	3	5	5	6	7

Table 4:

	Hato Ratón	Nava Correhuelas	Zackenberg
\overline{A}	17	33	65
P	16	25	31
I_{max}	272	825	1891
N	3340	8378	1245
I	151	181	268
Chao1	263.1 ± 70.9	231.4 ± 14.2	509.6 ± 54.7
ACE	240.3 ± 8.9	241.3 ± 7.9	566.1 ± 14.8
$\% \ unobserved^a$	8.33	15.38	47.80

 $[^]a,$ estimated with library Jade (R
 Core Development Team 2010, Chao $\it et~\it al.~2015)$