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# Leveraging High Performance Computing for Salvo Exchange Simulations

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- Introduction to Salvo Models
- Simulation Concept
- Salvo Models App Workflow
  - Streamlit Interface
  - DOE Modifications
  - Paramiko for HPC Connection
  - Batch Simulations in HPC
  - Large Data Preprocessing
  - Visualizations
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- The salvo model was originally developed by CAPT Wayne Hughes in 1986 to provide insight into modern naval missile engagements, where traditional continuous-fire models were inadequate.
- The model provides a way to compare naval forces by analyzing offensive, defensive, and staying power during naval combat.
- The salvo model analyzes combat as simultaneous volleys instead of continuous fire, which captures the impact of high-damage, high-risk exchanges.
- Salvo models aid in designing ships and strategies by assessing the balance of offensive, defensive, and staying power in naval engagements.



## The Basic Model:

$$\Delta B = \frac{\alpha A - b_3 B}{b_1} \quad \Delta A = \frac{\beta B - a_3 A}{a_1} \quad (1)$$

Calculates combat work achieved by a single salvo at any time step (ships out of action)

Combat Power:  $P_a$  or  $P_b$  measured in hits that damage target force.

$A$  = # of units in force A

$B$  = # of units in force B

$\alpha$  = # of well-aimed missiles fired by each A unit

$\beta$  = # of well-aimed missiles fired by each B unit

$a_1$  = # of hits by B's missiles needed to put one A out of action

$b_1$  = # of hits by A's missiles needed to put one B out of action

$a_3$  = # of well-aimed missiles destroyed by each A

$b_3$  = # of well-aimed missiles destroyed by each B

$\Delta A$  = # of units in force A out of action from B's salvo

$\Delta B$  = # of units in force B out of action from A's salvo





Previous calculation highlights the concept of instability for weak staying power vs strong combat power.

$$\Delta B = \frac{\alpha A - b_3 B}{b_1} \quad \Delta A = \frac{\beta B - a_3 A}{a_1} \quad (1)$$

If staying power cannot be easily and affordably added, then instability is only restored through adding more units (A's and B's of affordable attributes)

This type of instability heavily favors circumstances for unanswered strikes and calls for superior scouting for the first effective attack (embellished model).



**“Fire effectively first.”**  
– The Great Wayne P. Hughes Jr.

A simple salvo model demonstrating such instability implies limited value of specific and detailed studies until we better understand the **general** nature of warship characteristics and modern combat.

Focus on combat power alone increases risk of investing too much capability into a single package. Must consider factors of greater numbers and staying power.



The Embellished Model:

$$\Delta B = \frac{(\alpha' A - b_3' B) b_4}{b_1} \quad \Delta A = \frac{(\beta' B - a_3' A) a_4}{a_1}$$

where

$\alpha'$  = fighting power in hits of an attacking unit of side A modified for scouting and training deficiencies and the effect of defender B's distraction chaff

$\beta'$  = fighting power in hits of an attacking unit of side B modified for scouting and training deficiencies and the effect of defender A's distraction chaff

$a_3'$  = hits denied to A by defender counterfire of B, degraded for defender alertness and training deficiencies

$b_3'$  = hits denied to B by defender counterfire of A, degraded for defender alertness and training deficiencies

$a_4$  = A's effectiveness in employing seduction chaff to cause otherwise accurate well aimed B missiles to miss after counterfire has failed

$b_4$  = B's effectiveness in employing seduction chaff to cause otherwise accurate well aimed A missiles to miss after counterfire has failed

Combat Power  $P_a$  or  $P_b$  are now based on partial offensive and defensive effectiveness

This model incorporates values for combat features that are difficult to capture quantitatively



## Modified Combat Effectiveness:

$$\alpha' = \sigma_a \tau_a \rho_b \alpha$$

$$b_3' = \delta_b \tau_b b_3$$

$$\beta' = \sigma_b \tau_b \rho_a \beta$$

$$a_3' = \delta_a \tau_a a_3$$

$\tau$  is present in both offensive and defensive effectiveness for both sides

These additional factors can only degrade combat effectiveness, not enhance

where

$\sigma$  = *Scouting effectiveness*. Takes values between 0 and 1 that measure the extent to which striking power is diminished due to less than perfect targeting and distribution of fire against the target force

$\delta$  = *Defender alertness*. Takes values between 0 and 1 that measure the extent to which counterfire is diminished due to less than perfect readiness or fire control designation to destroy the missiles of an enemy attack

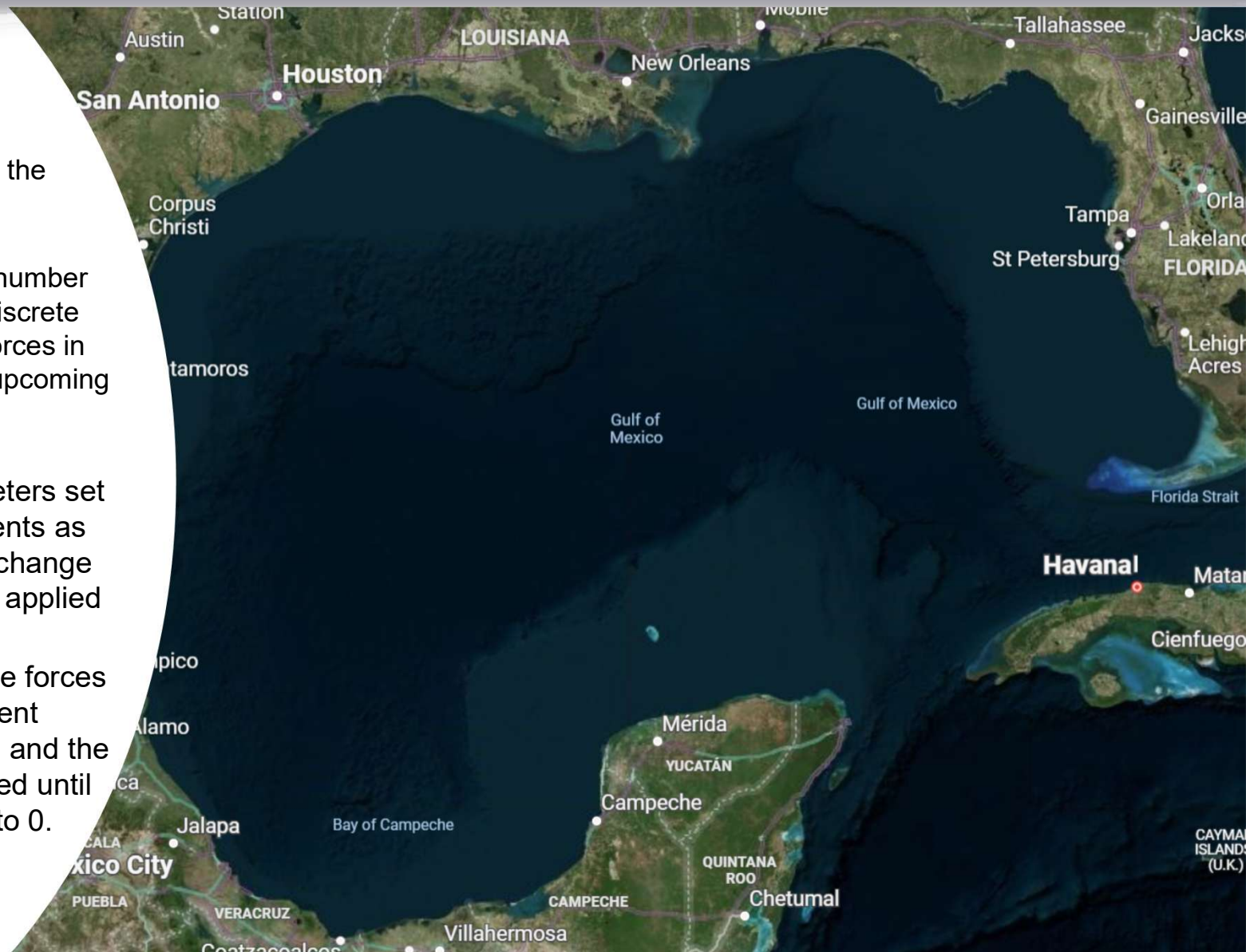
$\rho$  = *Distraction Chaff*. Multiplier between 0 and 1 that reduces the number of accurate shots that must be destroyed by counterfire. Distracts each enemy shot with a fixed probability.

$\tau$  = *Skillfulness/Training multiplier*. Multiplier between 0 and 1, the degree to which a firing or target unit fails to achieve its full combat potential due to inadequate training, organization, or motivation.





- $A_0$  and  $B_0$  set at the start of the simulation.
- Half of each side are in the engagement area and the number of forces is selected by a discrete random uniform (1 – # of forces in engagement area) for the upcoming exchange.
- Exchange dynamics are dependent on the parameters set by the design of experiments as the inputs to the salvo exchange equations and losses are applied to the number of forces.
- Reserves are added to the forces available in the engagement area, forces are selected, and the salvo exchange is repeated until one of the sides is equal to 0.







## Half of the Total Force is Available for each Engagement

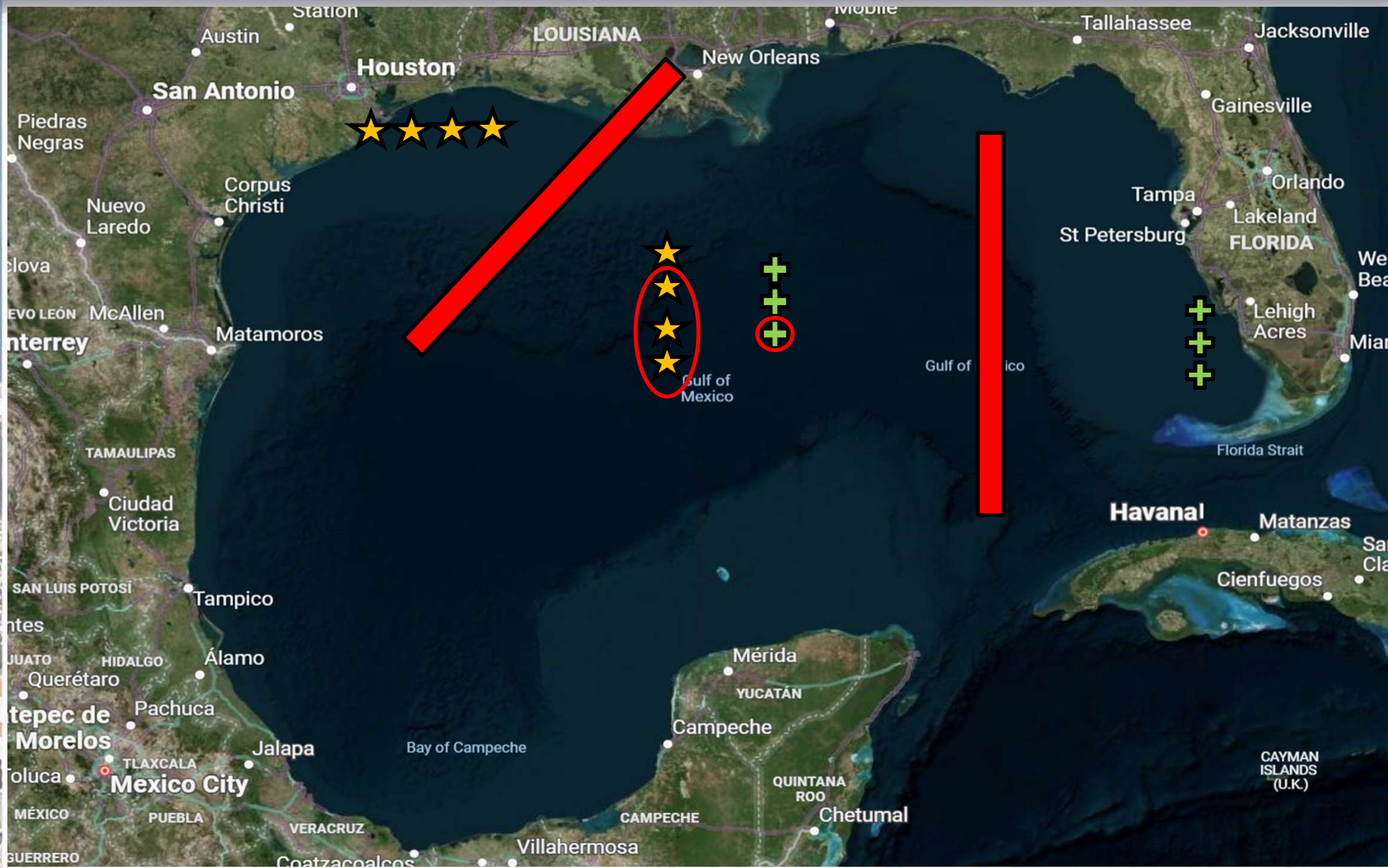






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## Forces are Randomly Selected for the Exchange





# Conduct Salvo Exchange Based on Design Point Parameters



Gulf of Mexico

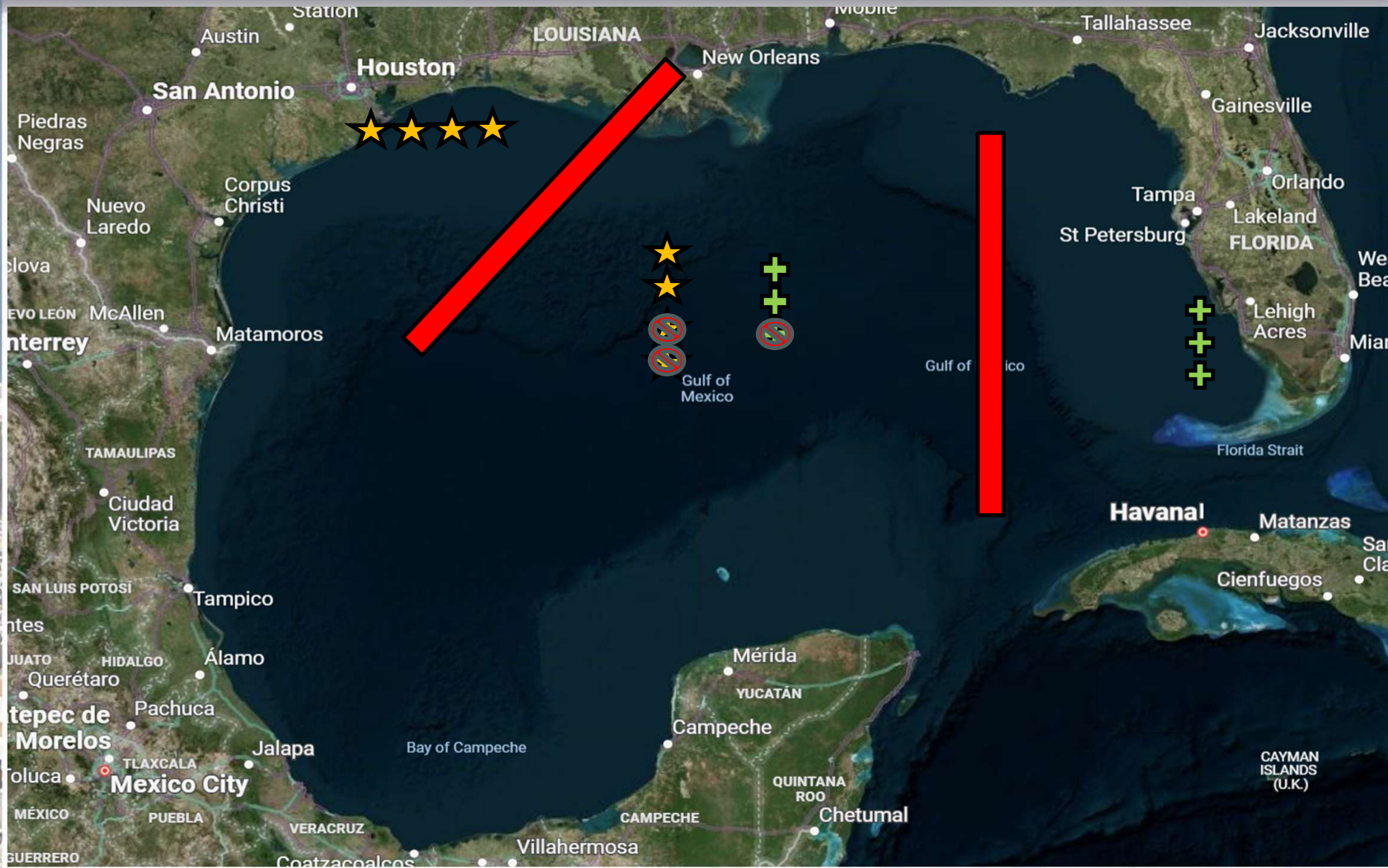


Gulf of Mexico





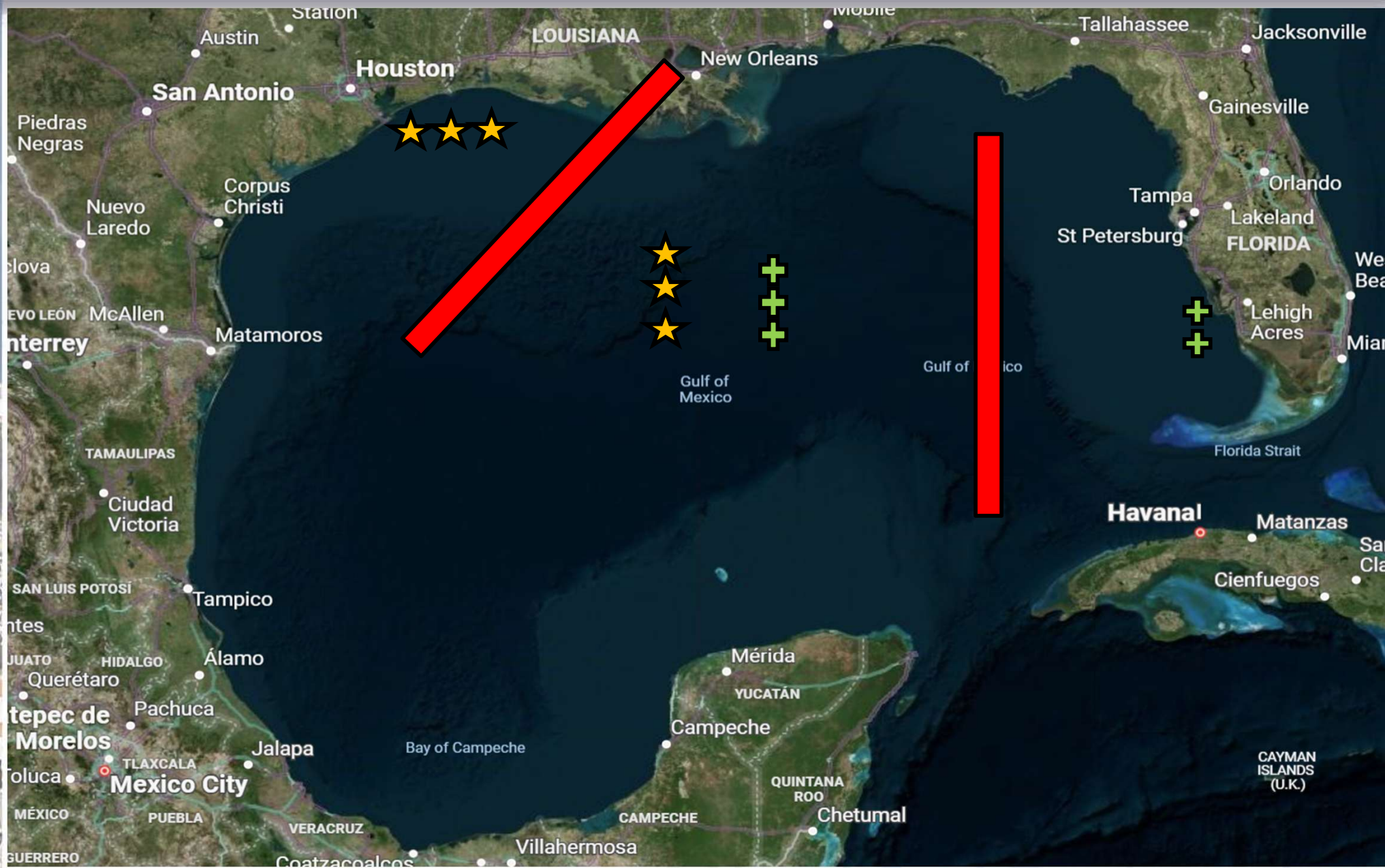
# Forces are Replaced and Half of the Total Force is Available for Next Exchange







# Forces are Replaced and Half of the Total Force is Available for Next Exchange





## Basic Random Selection Model

- **A**: initial number of units in force A
- **B**: initial number of units in force B
- $\alpha$  : number of **well aimed** missiles fired by each A unit.
- $\beta$  : number of **well aimed** missiles fired by each B unit.
- $a_1$  : number of hits by B's missiles needed to put one A unit out of action.
- $b_1$  : number of hits by A's missiles needed to put one B unit out of action.
- $a_3$  : number of **well aimed** missiles **destroyed** by each A.
- $b_3$  : number of **well aimed** missiles **destroyed** by each B.

## Stochastic Basic Model

- **A**: initial number of units in force A
- **B**: initial number of units in force B
- $\alpha$  : number of missiles fired by each A unit.
- $\beta$  : number of missiles fired by each B unit.
- $a_1$  : number of hits by B's missiles needed to put one A unit out of action.
- $b_1$  : number of hits by A's missiles needed to put one B unit out of action.
- $a_3$  : number of missiles that can be destroyed by each A.
- $b_3$  : number of missiles that can be destroyed by each B.
- $P(\mathbf{A_{Well-Aimed Missile}})$  : probability that an A unit fires a missile that can hit a B unit
- $P(\mathbf{B_{Well-Aimed Missile}})$  : probability that a B unit fires a missile that can hit an A unit
- $P(\mathbf{A_{Destroy Well-Aimed Missile}})$  : probability that an A unit can destroy a missile that can hit an A unit
- $P(\mathbf{B_{Destroy Well-Aimed Missile}})$  : probability that a B unit can destroy a missile that can hit a B unit



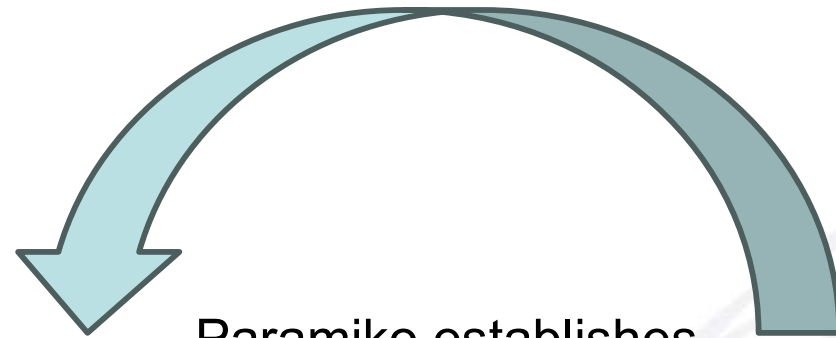


## Modified Random Selection Model

- **A**: initial number of units in force A
- **B**: initial number of units in force B
- $\alpha$ : number of **well aimed** missiles fired by each A unit.
- $\beta$ : number of **well aimed** missiles fired by each B unit.
- $a_1$ : number of hits by B's missiles needed to put one A unit out of action.
- $b_1$ : number of hits by A's missiles needed to put one B unit out of action.
- $a_3$ : **number of well aimed missiles destroyed** by each A.
- $b_3$ : **number of well aimed missiles destroyed** by each B.
- $a_4$ : probability that accurate shots miss an A unit after their counterfire has failed.
- $b_4$ : probability that accurate shots miss a B unit after their counterfire has failed.
- $\sigma_A$ : scouting effectiveness due to less than perfect targeting of A units.
- $\sigma_B$ : scouting effectiveness due to less than perfect targeting of B units.
- $\tau_A$ : training effectiveness of A units.
- $\tau_B$ : training effectiveness of B units.
- $\delta_A$ : alertness of unit A's defense that is degraded by less than perfect readiness or fire control.
- $\delta_B$ : alertness of unit B's defense that is degraded by less than perfect readiness or fire control.
- $\rho_A$ : effectiveness of unit A chaff that draws off shots before its counterfire against B's missiles.
- $\rho_B$ : effectiveness of unit B chaff that draws off shots before its counterfire against A's missiles.

## Stochastic Modified Model

- **A**: initial number of units in force A
- **B**: initial number of units in force B
- $\alpha$ : number of missiles fired by each A unit.
- $\beta$ : number of missiles fired by each B unit.
- $a_1$ : number of hits by B's missiles needed to put one A unit out of action.
- $b_1$ : number of hits by A's missiles needed to put one B unit out of action.
- $a_3$ : number of missiles that can be destroyed by each A.
- $b_3$ : number of missiles that can be destroyed by each B.
- $a_4$ : probability that accurate shots miss an A unit after their counterfire has failed.
- $b_4$ : probability that accurate shots miss a B unit after their counterfire has failed.
- $\sigma_A$ : scouting effectiveness due to less than perfect targeting of A units.
- $\sigma_B$ : scouting effectiveness due to less than perfect targeting of B units.
- $\tau_A$ : training effectiveness of A units.
- $\tau_B$ : training effectiveness of B units.
- $\delta_A$ : alertness of unit A's defense that is degraded by less than perfect readiness or fire control.
- $\delta_B$ : alertness of unit B's defense that is degraded by less than perfect readiness or fire control.
- $\rho_A$ : effectiveness of unit A chaff that draws off shots before its counterfire against B's missiles.
- $\rho_B$ : effectiveness of unit B chaff that draws off shots before its counterfire against A's missiles.
- $P(A_{\text{Well-Aimed Missile}})$ : probability that an A unit fires a missile that can hit a B unit
- $P(B_{\text{Well-Aimed Missile}})$ : probability that a B unit fires a missile that can hit an A unit
- $P(A_{\text{Destroy Well-Aimed Missile}})$ : probability that an A unit can destroy a missile that can hit an A unit
- $P(B_{\text{Destroy Well-Aimed Missile}})$ : probability that a B unit can destroy a missile that can hit a B unit



Paramiko establishes a secure shell to NPS Hamming, allowing bash commands to run transparently in the background of the streamlit app, and provide the user updates







- User selects the model
  - Basic, Basic Stochastic, Modified, Modified Stochastic
- User selects minimum and maximum values that they are interested in studying
- Slide bars were used for user functionality
- A<sub>0</sub> and B<sub>0</sub> range of values were too large for the user to control the values selection

## Hughes' Salvo Equations Modeler

C:\Users\jheber\Documents\OA3802\_Comp\_MethodsIII\WebData\Interactive\_Viz\OA3802\_strea

### Model Selection

Choose the model you want to run.

Choose the salvo model you want to run:

Salvo\_Basic

### Enter Model Inputs

Input all of the necessary values of the model you intend to run.

#### Force A

Initial A Force Min

10

- +

Initial A Force Max

20

- +

Well aimed missiles fired by A

4 10

0

100

number of hits by B's missiles needed to put one A unit out of action

3 6

#### Force B

Initial B Force Min

10

- +

Initial B Force Max

20

- +

Well aimed missiles fired by B

4 10

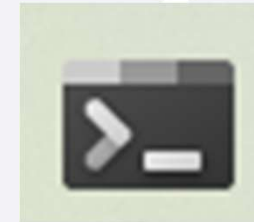
0

100

number of hits by A's missiles needed to put one B unit out of action

3 6

- User requires an account for NPS HPC
- App is designed to be run with no coding necessary once it is launched
- App must be launched from a terminal.
- This is important for running the model seamlessly since file management can get complicated.
- Absolute Paths with modular variables.



```
(base) C:\Users\jeber\Documents\OA3802_Comp_MethodsIII\WebData\Interactive_Viz\OA3802_streamlit_exercise_20241021153925112\OA3802_streamlit_exercise\OA3802_streamlit_SSH_PE\Salvo\Salvo>streamlit run Hughes_Salvo_App_V2.py
```

```
f"{present_dir}/{model}_HPC.py", f"/home/{username}/Salvo_outputs/{model}_HPC.py")
```



## Connect to HPC

Connect to NPS HPC Hamming platform at hostname `hamming-sub1.uc.nps.edu` to access and run Hughes' Lanchester model.

Enter NPS HPC Username

john.berner

Enter NPS HPC Password



Generate DOE

Run Model

```
if st.button('Generate DOE'):  
    if connected:  
        generate_DOE(A_val, alpha, a1_val, a3_val,  
    else:  
        st.write('Connect to HPC and try again.')
```

User logs in with their own NPS HPC account info. Username is stored for use in bash commands

User then inputs all required variables for their selected model using input boxes and sliding bars.

Code assumes user can run Python on HPC already

## Enter Model Inputs

Input all of the necessary values of the model you intend to run

### Force A

Initial A Force Min

10

- +

Initial A Force Max

20

- +

Well aimed missiles fired by A



```
if st.button('Run Model'):  
    if connected:  
        prep_model(model, client, username)  
        run_model(present_dir, model, client, username)  
        run_robust(present_dir, model, client, username)  
        clear_outputs(present_dir, model, client, username)  
    else:  
        st.write('Connect to HPC and try again.')
```



- 

[illegible]





# High Performance Computer (HPC)

- Each batch job will execute a .py file for the corresponding model that will run (2000) simulations
- The batch job will run multiple iterations of the .py file and the random seed is set based on the iteration of the batch job.
- The number of units lost by each force and the winner of each observation of each design point is recorded in a .json file and saved under a data outputs directory
- We executed 500 iterations for each design point and the number of simulations would take an extensive amount of time to complete without HPC
  - The memory required for each model's outputs was estimated to take 4.5 GB

```
1  {"remaining_A": 208,  
2  "remaining_B": 0,  
3  "delta_A": 27,  
4  "delta_B": 65,  
5  "total_wins_A": 8,  
6  "total_wins_B": 2,  
7  "total_exchanges": 10,  
8  "winner_A": 1,  
9  "winner_B": 0,  
10 "tie": 0}
```

```
1  #!/bin/sh  
2  #SBATCH --job-name=Basic  
3  #SBATCH --array=1-500  
4  #SBATCH -N 5  
5  #SBATCH --mem-per-cpu=2048M  
6  #SBATCH --cpus-per-task=5  
7  #SBATCH --output=print_outputs/Basic/DP%a.txt  
8  
9  . /etc/profile  
10 module load lang/python  
11 source /smallwork/$USER/comp3/bin/activate  
12  
13 python Salvo_Basic_HPC.py ${SLURM_ARRAY_TASK_ID}  
14
```



# High Performance Computer (HPC) Continued

- The data from each simulation needed to be processed to calculate the means and standard deviations for the units lost by each force, and the proportion of wins for either side.
- Due to the size of the folder, the memory that was required to execute these calculations was too large for the user's local machine

```
for filename in os.listdir('./data_output/Salvo_Basic/'):
    if filename.endswith(".json"):
        DP = int(filename.split('_')[0][2:])
        obs_number = int(filename.split('_')[1].split('.')[0][4:])

        with open(os.path.join('./data_output/Salvo_Basic/', filename), 'r') as f:
            json_data = json.load(f)
        try:
            data_dict[DP]['remaining_A'].append(json_data['remaining_A'])
            data_dict[DP]['remaining_B'].append(json_data['remaining_B'])
            data_dict[DP]['delta_A'].append(json_data['delta_A'])
            data_dict[DP]['delta_B'].append(json_data['delta_B'])
            data_dict[DP]['total_wins_A'].append(json_data['total_wins_A'])
            data_dict[DP]['total_wins_B'].append(json_data['total_wins_B'])
            data_dict[DP]['total_exchanges'].append(json_data['total_exchanges'])
            data_dict[DP]['winner_A'].append(json_data['winner_A'])
            data_dict[DP]['winner_B'].append(json_data['winner_B'])
            data_dict[DP]['tie'].append(json_data['tie'])
        except:
            data_dict[DP] = {
                'remaining_A': [json_data['remaining_A']],
                'remaining_B': [json_data['remaining_B']],
                'delta_A': [json_data['delta_A']],
                'delta_B': [json_data['delta_B']],
                'total_wins_A': [json_data['total_wins_A']],
                'total_wins_B': [json_data['total_wins_B']],
                'total_exchanges': [json_data['total_exchanges']],
                'winner_A': [json_data['winner_A']],
                'winner_B': [json_data['winner_B']],
                'tie': [json_data['tie']]
            }
```

```
for DP in data_dict.keys():
    data = {
        'index': DP,
        'avg_remaining_A': statistics.mean(data_dict[DP]['remaining_A']),
        'sd_remaining_A': statistics.stdev(data_dict[DP]['remaining_A']),
        'avg_remaining_B': statistics.mean(data_dict[DP]['remaining_B']),
        'sd_remaining_B': statistics.stdev(data_dict[DP]['remaining_B']),
        'avg_delta_A': statistics.mean(data_dict[DP]['delta_A']),
        'sd_delta_A': statistics.stdev(data_dict[DP]['delta_A']),
        'avg_delta_B': statistics.mean(data_dict[DP]['delta_B']),
        'sd_delta_B': statistics.stdev(data_dict[DP]['delta_B']),
        'FER': FER_across_DP(data_dict, DP),
        'avg_total_wins_A': statistics.mean(data_dict[DP]['total_wins_A']),
        'sd_total_wins_A': statistics.stdev(data_dict[DP]['total_wins_A']),
        'avg_total_wins_B': statistics.mean(data_dict[DP]['total_wins_B']),
        'sd_total_wins_B': statistics.stdev(data_dict[DP]['total_wins_B']),
        'avg_total_exchanges': statistics.mean(data_dict[DP]['total_exchanges']),
        'sd_total_exchanges': statistics.stdev(data_dict[DP]['total_exchanges']),
        'prop_A_wins_exchanges': sum(data_dict[DP]['total_wins_A'])/sum(data_dict[DP]['total_exchanges']),
        'prop_B_wins_exchanges': sum(data_dict[DP]['total_wins_B'])/sum(data_dict[DP]['total_exchanges']),
        'prop_A_wins_overall': sum(data_dict[DP]['winner_A'])/len(data_dict[DP]['winner_A']),
        'prop_B_wins_overall': sum(data_dict[DP]['winner_B'])/len(data_dict[DP]['winner_B']),
        'prop_tie_overall': sum(data_dict[DP]['tie'])/len(data_dict[DP]['tie'])
    }
    outputs.append(data)

df_DOE = pd.read_csv('sim_DOE.csv')
df_DOE.index += 1
df = pd.DataFrame(outputs)
merged_df = df_DOE.merge(df, left_index=True, right_on='index', how='left')

merged_df.to_csv('sim_DOE_results_Salvo_Basic.csv', header=True, index=False)
```



# Results



# Visualizations

Streamlit app hosts four variable heatmaps with dropdown selectors:

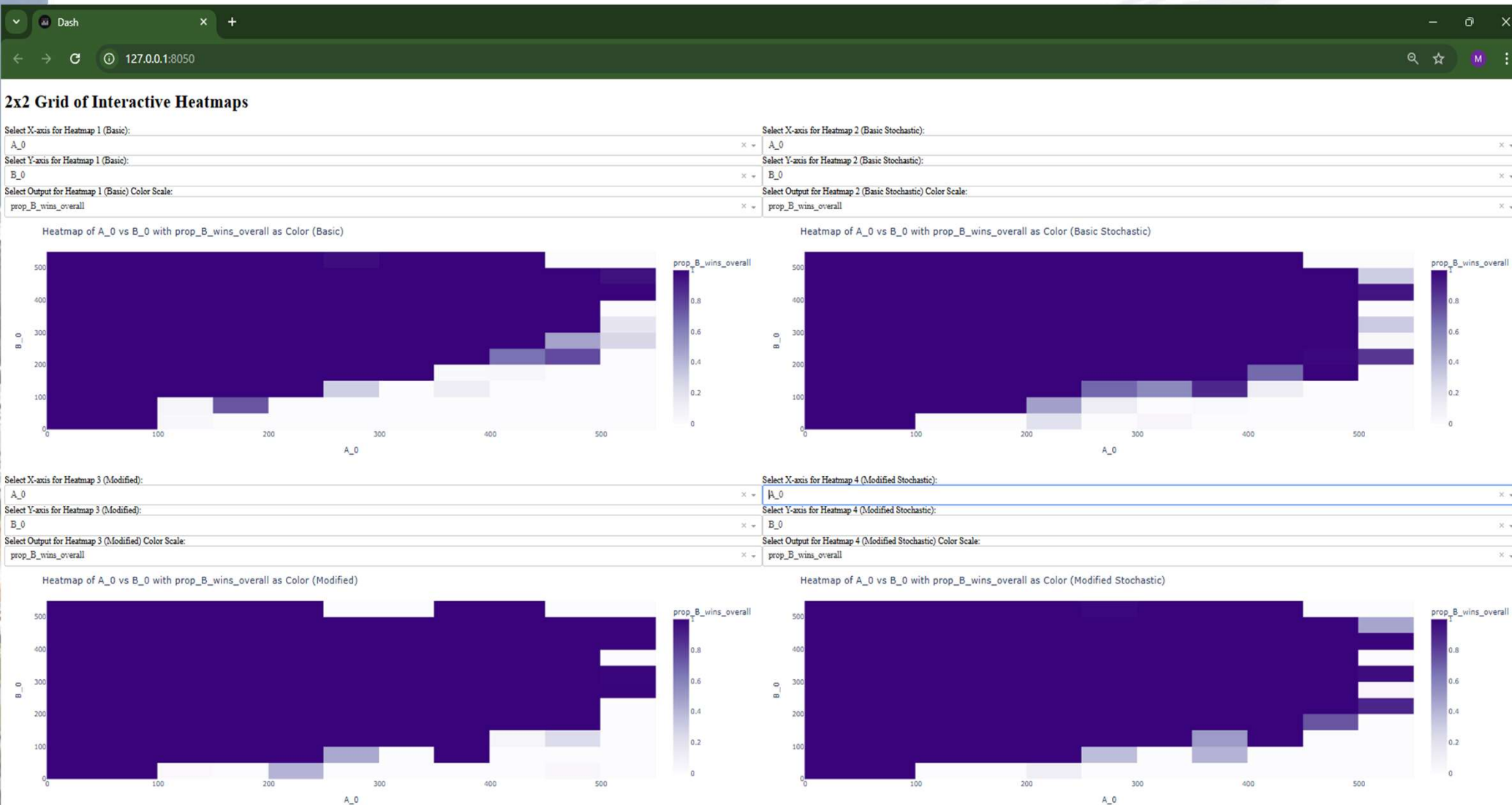
- x and y (Input parameters)
- Output (specific simulation result) dictates color

Here we have:

x: A\_0 (initial A forces)

y: B\_0 (initial B forces)

Output: Proportion B wins overall







## **Comp 3 Takeaways:**

- Not all HPC tunnels are created equal
  - MobaXTerm vs. Paramiko vs. Other solutions
- Dashboards are helpful, but too much going on in the background can get complicated
- Output management: SQL vs. Other data storage methods (pandas, .csv, .json)
  - Don't reinvent the wheel
- File paths and file permissions are easy ways for code to break
- Scouting is the key to success and survival. This applies to delivering weapons at range and disrupting the enemies sensing and C2
- Maximum fighting strength (regardless of how it is achieved) is the proper warship design goal. Further research is needed comparing the relative worth of offensive and defensive power with the number of warships and staying power

## **Future Work:**

- Build out the model repository with other Salvo equations
- Further develop “immediate analysis” aids (think mini-STORMMiner) in Dash



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# Questions?

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