

Applications of Answer Set Programming

Martin Gebser



University of Klagenfurt

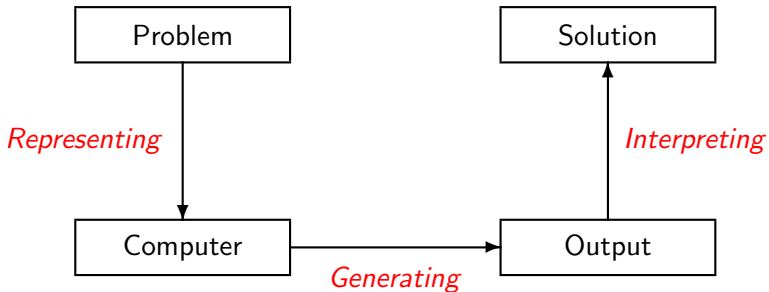
Graz University of Technology



Outline

- 1 Motivation
- 2 ASP in a Nutshell
- 3 Linux Package Configuration
- 4 Conclusion

Computer Programming

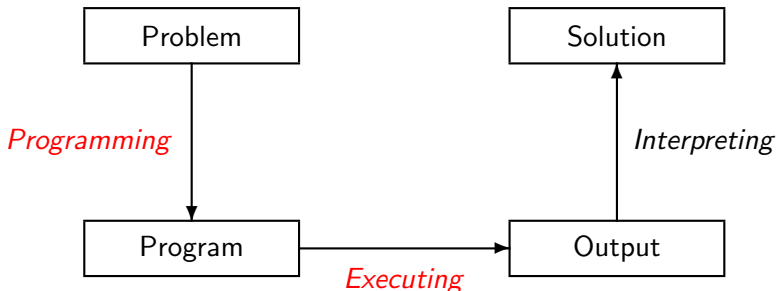


“How to solve the problem?”

versus

“What is the problem?”

“Traditional” Programming

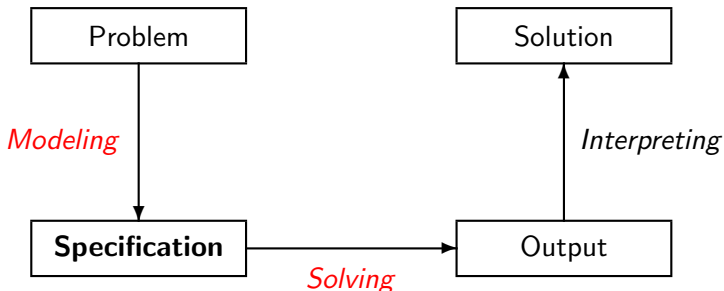


“How to solve the problem?”

versus

“What is the problem?”

Declarative Programming



“How to solve the problem?”

versus

“What is the problem?”

Answer Set Programming (ASP)

- ▶ Attractive tool for Knowledge Representation and Reasoning
 - Integration of deductive database, logic programming, knowledge representation and satisfiability solving techniques
 - Combinatorial search problems in the realm of NP and NP^{NP}
 - decision, optimization and query answering tasks
 - Succinct, elaboration-tolerant problem representations
 - rapid application development tool
 - Easy handling of knowledge-intensive applications
 - data, defaults, exceptions, frame axioms, reachability, etc.
- ▶ Efficient and versatile off-the-shelf solving technology
 - <https://potassco.org/>
 - <https://www.mat.unical.it/DLV2/>
- ▶ ASP has a growing range of applications, and it's good fun!

Answer Set Programming (ASP)

- ▶ Attractive tool for Knowledge Representation and Reasoning
 - Integration of deductive database, logic programming, knowledge representation and satisfiability solving techniques
 - Combinatorial search problems in the realm of NP and NP^{NP}
 - decision, optimization and query answering tasks
 - Succinct, elaboration-tolerant problem representations
 - rapid application development tool
 - Easy handling of knowledge-intensive applications
 - data, defaults, exceptions, frame axioms, reachability, etc.
- ▶ Efficient and versatile off-the-shelf solving technology
 - <https://potassco.org/>
 - <https://www.mat.unical.it/DLV2/>
- ▶ ASP has a growing range of applications, and it's good fun!

Answer Set Programming (ASP)

- ▶ Attractive tool for Knowledge Representation and Reasoning
 - Integration of deductive database, logic programming, knowledge representation and satisfiability solving techniques
 - Combinatorial search problems in the realm of NP and NP^{NP}
 - decision, optimization and query answering tasks
 - Succinct, elaboration-tolerant problem representations
 - rapid application development tool
 - Easy handling of knowledge-intensive applications
 - data, defaults, exceptions, frame axioms, reachability, etc.
- ▶ Efficient and versatile off-the-shelf solving technology
 - <https://potassco.org/>
 - <https://www.mat.unical.it/DLV2/>
- ▶ ASP has a growing range of applications, and it's good fun!

Industrial Applications

- ▶ Airport infrastructure planning
- ▶ Business partner matchmaking
- ▶ Call routing
- ▶ Embedded system design
- ▶ Nurse rostering
- ▶ Production process scheduling
- ▶ Radio spectrum reallocation
- ▶ Safety system configuration
- ▶ Shift planning
- ▶ Software package management
- ▶ Space shuttle maneuvering
- ▶ Train timetabling
- ▶ Vehicle routing
- ▶ Workforce management

Industrial Applications

- ▶ Airport infrastructure planning
- ▶ Business partner matchmaking
- ▶ Call routing
- ▶ Embedded system design
- ▶ Nurse rostering
- ▶ Production process scheduling
- ▶ Radio spectrum reallocation
- ▶ Safety system configuration
- ▶ Shift planning
- ▶ Software package management
- ▶ Space shuttle maneuvering
- ▶ Train timetabling
- ▶ Vehicle routing
- ▶ Workforce management

Call Center Shift Planning

Planning context	"Hard" constraints	"Soft" constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

- ▶ Each solution/shift plan must satisfy all **hard constraints**
- ▶ Soft constraints distinguish/select preferred solutions
 - Successive improvement through "anytime" solving algorithms
 - Guaranteed optimality on termination
- ▶ Monthly shift planning
 - Manual: about **one person-week** of work
 - Automated: "good-quality" shift plans **within one hour**

Call Center Shift Planning

Planning context	"Hard" constraints	"Soft" constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

"The weekly working hours must stay in the legal limit."

Call Center Shift Planning

Planning context	"Hard" constraints	"Soft" constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

- ▶ Each solution/shift plan must satisfy all **hard constraints**
- ▶ Soft constraints distinguish/select preferred solutions
 - Successive improvement through "anytime" solving algorithms
 - Guaranteed optimality on termination
- ▶ Monthly shift planning
 - Manual: about **one person-week** of work
 - Automated: "good-quality" shift plans **within one hour**

Call Center Shift Planning

Planning context	"Hard" constraints	"Soft" constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

- ▶ Each solution/shift plan must satisfy all hard constraints
"Single free days in-between two workdays shall be avoided."

Call Center Shift Planning

Planning context	"Hard" constraints	"Soft" constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

- ▶ Each solution/shift plan must satisfy all hard constraints
- ▶ **Soft constraints** distinguish/select preferred solutions
 - Successive improvement through "anytime" solving algorithms
 - Guaranteed optimality on termination
- ▶ Monthly shift planning
 - Manual: about **one person-week** of work
 - Automated: "good-quality" shift plans **within one hour**

Call Center Shift Planning

Planning context	“Hard” constraints	“Soft” constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

- ▶ Each solution/shift plan must satisfy all hard constraints
- ▶ **Soft constraints** distinguish/select preferred solutions
 - Successive improvement through **“anytime” solving algorithms**
 - Guaranteed **optimality** on termination
- ▶ Monthly shift planning
 - Manual: about **one person-week** of work
 - Automated: **“good-quality” shift plans within one hour**

Call Center Shift Planning

Planning context	“Hard” constraints	“Soft” constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

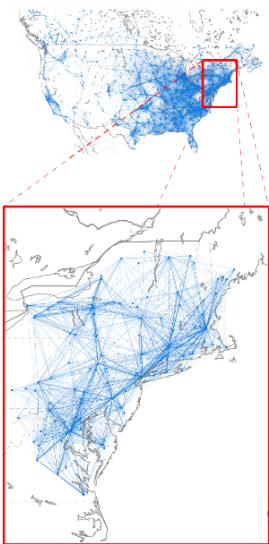
- ▶ Each solution/shift plan must satisfy all hard constraints
- ▶ Soft constraints distinguish/select preferred solutions
 - Successive improvement through “anytime” solving algorithms
 - Guaranteed optimality on termination
- ▶ Monthly shift planning
 - Manual: about **one person-week** of work
 - Automated: “good-quality” shift plans **within one hour**

Call Center Shift Planning

Planning context	“Hard” constraints	“Soft” constraints
Workload	4	1
Shift sequence	6	1
Times of absence	2	2
Quality of service	0	3
Free days	0	5
Total	12	12

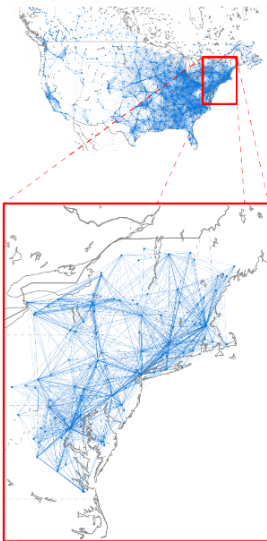
- ▶ Each solution/shift plan must satisfy all hard constraints
- ▶ Soft constraints distinguish/select preferred solutions
 - Successive improvement through “anytime” solving algorithms
 - Guaranteed optimality on termination
- ▶ Monthly shift planning
 - Manual: about one person-week of work
 - Automated: “good-quality” shift plans within one hour

Radio Spectrum Reallocation



- Complex incentive auction by the US Federal Communications Commission
 - ~ 3000 sending stations
 - ~ 3 million interference restrictions

Radio Spectrum Reallocation



► Complex incentive auction by the US Federal Communications Commission

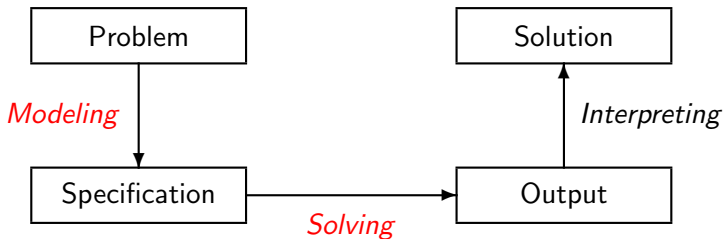
- ~ 3000 sending stations
- ~ 3 million interference restrictions

Over 13 months in 2016–17 the **US Federal Communications Commission** conducted an “incentive auction” to repurpose radio spectrum from broadcast television to wireless internet. In the end, the auction yielded **\$19.8 billion**, \$10.05 billion of which was paid to 175 broadcasters for voluntarily relinquishing their licenses across 14 UHF channels. Stations that continued broadcasting were assigned potentially new channels to fit as densely as possible into the channels that remained. The government netted more than **\$7 billion** (used to pay down the national debt) after covering costs. A crucial element of the auction design was the construction of a **solver**, dubbed SATFC, **that determined whether sets of stations could be “repacked” in this way; it needed to run every time a station was given a price quote.** This

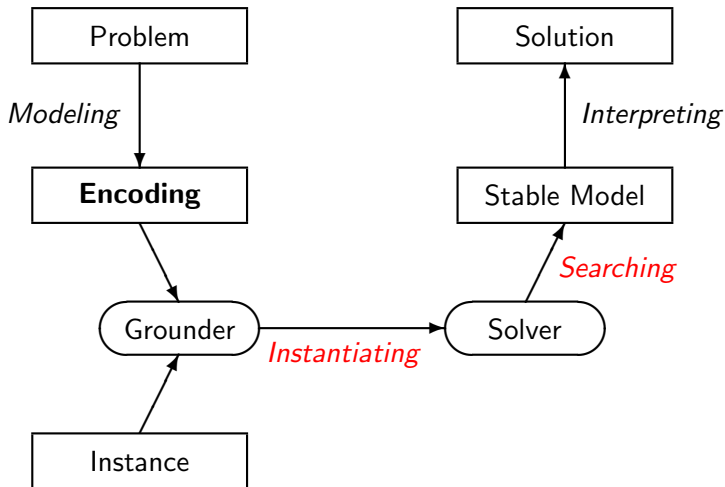
Outline

- 1 Motivation
- 2 ASP in a Nutshell
- 3 Linux Package Configuration
- 4 Conclusion

Basic Workflow



Basic Workflow



Modeling Language

- ▶ **Facts** $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) \text{ :- } p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
- ▶ Integrity constraints $\text{ :- } p(3).$
- ▶ Default negation $\text{ :- not } p(2).$
- ▶ First-order variables $q(X) \text{ :- } p(X).$
- ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
- ▶ Conjunctions $s(X) \text{ :- } q(X), r(X).$
- ▶ Aggregates $t(N) \text{ :- } \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} \text{ :- } t(N).$
- ▶ Optimization $\text{ :- } \sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $\perp :- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ **First-order variables** $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts p(0).
 - ▶ Normal rules p(1) :- p(0).
 - ▶ Choice rules {p(2); p(3)} = 1 :- p(1).
 - ▶ Integrity constraints :- p(3).
 - ▶ Default negation :- not p(2).
 - ▶ First-order variables q(X) :- p(X).
- Instantiation
- q(0) :- p(0).
q(1) :- p(1).
q(2) :- p(2).
q(3) :- p(3).

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ **Arithmetics** $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
 - ▶ Normal rules $p(1) \text{ :- } p(0).$
 - ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
 - ▶ Integrity constraints $\text{ :- } p(3).$
 - ▶ Default negation $\text{ :- not } p(2).$
 - ▶ First-order variables $q(X) \text{ :- } p(X).$
 - ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
- Instantiation
- $r(1) \text{ :- } p(0).$
 $r(2) \text{ :- } p(1).$
 $r(3) \text{ :- } p(2).$
 $r(4) \text{ :- } p(3).$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ **Conjunctions** $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts `p(0).`
 - ▶ Normal rules `p(1) :- p(0).`
 - ▶ Choice rules `{p(2); p(3)} = 1 :- p(1).`
 - ▶ Integrity constraints `:- p(3).`
 - ▶ Default negation `:- not p(2).`
 - ▶ First-order variables `q(X) :- p(X).`
 - ▶ Arithmetics `r(X+1) :- p(X).`
 - ▶ Conjunctions `s(X) :- q(X), r(X).`
- (Relevant) Instantiation `s(1) :- q(1), r(1).`
- `s(2) :- q(2), r(2).`
- `s(3) :- q(3), r(3).`

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) \text{ :- } p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
- ▶ Integrity constraints $\text{ :- } p(3).$
- ▶ Default negation $\text{ :- not } p(2).$
- ▶ First-order variables $q(X) \text{ :- } p(X).$
- ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
- ▶ Conjunctions $s(X) \text{ :- } q(X), r(X).$
- ▶ **Aggregates** $t(N) \text{ :- } \text{\#sum}\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} \text{ :- } t(N).$
- ▶ Optimization $\text{ :- } \sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$

(Relevant) Instantiation

```
t(0) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 0.  
t(1) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 1.  
t(2) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 2.  
t(3) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 3.  
t(4) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 4.  
t(5) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 5.  
t(6) :- #sum{1 : s(1); 2 : s(2); 3 : s(3)} = 6.
```

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) \text{ :- } p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
- ▶ Integrity constraints $\text{ :- } p(3).$
- ▶ Default negation $\text{ :- not } p(2).$
- ▶ First-order variables $q(X) \text{ :- } p(X).$
- ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
- ▶ Conjunctions $s(X) \text{ :- } q(X), r(X).$
- ▶ Aggregates $t(N) \text{ :- } \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} \text{ :- } t(N).$
- ▶ Optimization $\text{ :- } \sim u(X). [X]$

Modeling Language

- ▶ Facts p(0).
- ▶ Normal rules p(1) :- p(0).
- ▶ Choice rules $\{p(2); p(3)\} = 1$:- p(1).
- ▶ Integrity constraints :- p(3).
- ▶ Default negation :- not p(2).
- ▶ First-order variables q(X) :- p(X).
- ▶ Arithmetics r(X+1) :- p(X).
- ▶ Conjunctions s(X) :- q(X), r(X).
- ▶ Aggregates t(N) :- #sum{X : s(X)} = N.
- ▶ Conditional literals $\{u(X) : r(X), X < N\}$:- t(N).

(Relevant) Instantiation

```

{u(1) : r(1)} :- t(2).
{u(1) : r(1); u(2) : r(2)} :- t(3).
{u(1) : r(1); u(2) : r(2); u(3) : r(3)} :- t(4).
{u(1) : r(1); u(2) : r(2); u(3) : r(3); u(4) : r(4)} :- t(5).
{u(1) : r(1); u(2) : r(2); u(3) : r(3); u(4) : r(4)} :- t(6).

```

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ Optimization $:\sim u(X). [X]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) \text{ :- } p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
- ▶ Integrity constraints $\text{ :- } p(3).$
- ▶ Default negation $\text{ :- not } p(2).$
- ▶ First-order variables $q(X) \text{ :- } p(X).$
- ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
- ▶ Conjunctions $s(X) \text{ :- } q(X), r(X).$
- ▶ Aggregates $t(N) \text{ :- } \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} \text{ :- } t(N).$
- ▶ Optimization $\text{ :- } \sim u(X). [X]$
 - (Relevant) Instantiation $\text{ :- } \sim u(1). [1]$
 - $\text{ :- } \sim u(2). [2]$
 - $\text{ :- } \sim u(3). [3]$
 - $\text{ :- } \sim u(4). [4]$

Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) \text{ :- } p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
- ▶ Integrity constraints $\text{ :- } p(3).$
- ▶ Default negation $\text{ :- not } p(2).$
- ▶ First-order variables $q(X) \text{ :- } p(X).$
- ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
- ▶ Conjunctions $s(X) \text{ :- } q(X), r(X).$
- ▶ Aggregates $t(N) \text{ :- } \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} \text{ :- } t(N).$
- ▶ Optimization $\text{ : } \sim u(X). [X]$

Optimum

$\{p(0), p(1), p(2), q(0), \dots, s(1), s(2), t(3)\}$

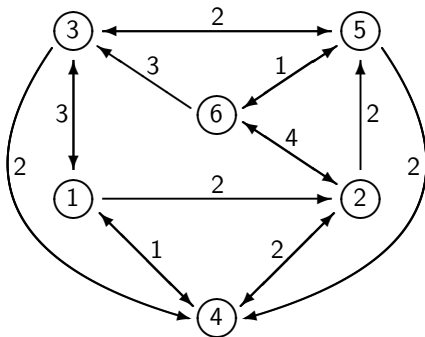
Modeling Language

- ▶ Facts $p(0).$
- ▶ Normal rules $p(1) :- p(0).$
- ▶ Choice rules $\{p(2); p(3)\} = 1 :- p(1).$
- ▶ Integrity constraints $:- p(3).$
- ▶ Default negation $:- \text{not } p(2).$
- ▶ First-order variables $q(X) :- p(X).$
- ▶ Arithmetics $r(X+1) :- p(X).$
- ▶ Conjunctions $s(X) :- q(X), r(X).$
- ▶ Aggregates $t(N) :- \#sum\{X : s(X)\} = N.$
- ▶ Conditional literals $\{u(X) : r(X), X < N\} :- t(N).$
- ▶ **Multi-criteria** Optimization $:\sim u(X). [X\textcolor{red}{0}1]$
 $:\sim \#count\{X : u(X)\} = 0. [1\textcolor{red}{0}2]$

Modeling Language

- ▶ Facts $p(0).$
 - ▶ Normal rules $p(1) \text{ :- } p(0).$
 - ▶ Choice rules $\{p(2); p(3)\} = 1 \text{ :- } p(1).$
 - ▶ Integrity constraints $\text{ :- } p(3).$
 - ▶ Default negation $\text{ :- not } p(2).$
 - ▶ First-order variables $q(X) \text{ :- } p(X).$
 - ▶ Arithmetics $r(X+1) \text{ :- } p(X).$
 - ▶ Conjunctions $s(X) \text{ :- } q(X), r(X).$
 - ▶ Aggregates $t(N) \text{ :- } \#sum\{X : s(X)\} = N.$
 - ▶ Conditional literals $\{u(X) : r(X), X < N\} \text{ :- } t(N).$
 - ▶ Multi-criteria Optimization $\text{ :}\sim u(X). [X@1]$
 $\text{ :}\sim \#count\{X : u(X)\} = 0. [1@2]$
- Optimum** $\{p(0), p(1), p(2), q(0), \dots, s(1), s(2), t(3), u(1)\}$

Traveling Salesperson (TSP) Example



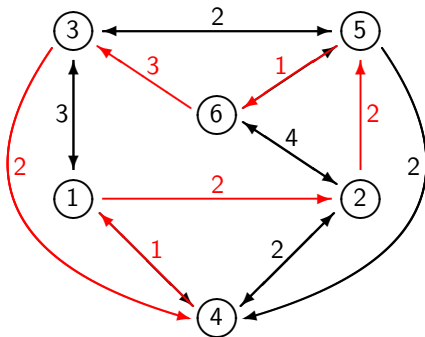
Total Cost: 11

Instance Representation

```
node(1). node(2). node(3).  
node(4). node(5). node(6).
```

```
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1).  
edge(2,4,2). edge(4,2,2).  
edge(2,5,2).  
edge(2,6,4). edge(6,2,4).  
edge(3,4,2).  
edge(3,5,2). edge(5,3,2).  
edge(5,4,2).  
edge(5,6,1). edge(6,5,1).  
edge(6,3,3).
```

Traveling Salesperson (TSP) Example



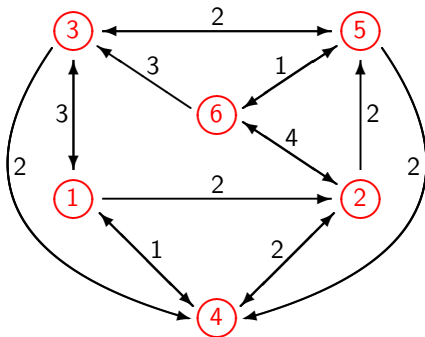
Total Cost: 11

Instance Representation

```
node(1). node(2). node(3).  
node(4). node(5). node(6).
```

```
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1).  
edge(2,4,2). edge(4,2,2).  
edge(2,5,2).  
edge(2,6,4). edge(6,2,4).  
edge(3,4,2).  
edge(3,5,2). edge(5,3,2).  
edge(5,4,2).  
edge(5,6,1). edge(6,5,1).  
edge(6,3,3).
```

Traveling Salesperson (TSP) Example



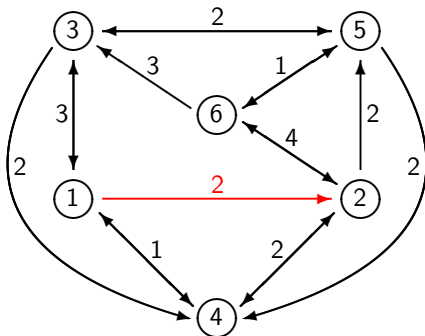
Total Cost: 11

Instance Representation

```
node(1). node(2). node(3).  
node(4). node(5). node(6).
```

```
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1).  
edge(2,4,2). edge(4,2,2).  
edge(2,5,2).  
edge(2,6,4). edge(6,2,4).  
edge(3,4,2).  
edge(3,5,2). edge(5,3,2).  
edge(5,4,2).  
edge(5,6,1). edge(6,5,1).  
edge(6,3,3).
```

Traveling Salesperson (TSP) Example



Total Cost: 11

Instance Representation

```
node(1). node(2). node(3).  
node(4). node(5). node(6).
```

```
edge(1,2,2).
```

```
edge(1,3,3). edge(3,1,3).
```

```
edge(1,4,1). edge(4,1,1).
```

```
edge(2,4,2). edge(4,2,2).
```

```
edge(2,5,2).
```

```
edge(2,6,4). edge(6,2,4).
```

```
edge(3,4,2).
```

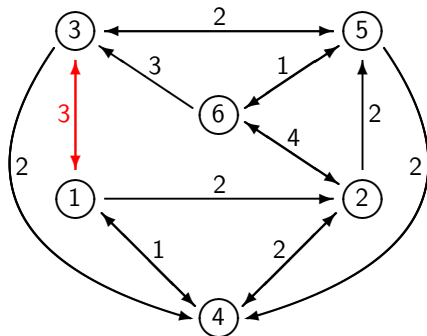
```
edge(3,5,2). edge(5,3,2).
```

```
edge(5,4,2).
```

```
edge(5,6,1). edge(6,5,1).
```

```
edge(6,3,3).
```

Traveling Salesperson (TSP) Example



Total Cost: 11

Instance Representation

```
node(1). node(2). node(3).  
node(4). node(5). node(6).
```

```
edge(1,2,2).
```

```
edge(1,3,3). edge(3,1,3).
```

```
edge(1,4,1). edge(4,1,1).
```

```
edge(2,4,2). edge(4,2,2).
```

```
edge(2,5,2).
```

```
edge(2,6,4). edge(6,2,4).
```

```
edge(3,4,2).
```

```
edge(3,5,2). edge(5,3,2).
```

```
edge(5,4,2).
```

```
edge(5,6,1). edge(6,5,1).
```

```
edge(6,3,3).
```


TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one **incoming** edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes **reached from (arbitrary) start node**
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 **Minimum sum of edge costs**

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

TSP Solution Specification

- 1 Exactly one outgoing edge per node
- 2 Exactly one incoming edge per node
- 3 All nodes reached from (arbitrary) start node
- 4 Minimum sum of edge costs

Problem Encoding

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X,Y]
```



More encoding “optimization” feasible

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(X).  
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,Y) : edge(1,Y,C)} = 1 :- node(1).  
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).
```

```
edge(1,2,2).
```

```
edge(1,3,3). edge(3,1,3).
```

```
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,Y) : edge(1,Y,C)} = 1.
```

```
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.
```

```
reached(Y) :- cycle(X,Y), reached(X).
```

```
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1.  
{cycle(X,Y) : edge(X,Y,C)} = 1 :- node(Y).
```

```
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...  
  
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1.  
{cycle(X,1) : edge(X,1,C)} = 1 :- node(1).  
  
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1.  
{cycle(3,1); cycle(4,1)} = 1.
```

```
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...  
  
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...  
  
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...  
  
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...  
  
reached(X) :- #min{Y : node(Y)} = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```


(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(X) :- #min{1 : ; 2 : ; 3 : ; 4 : ; 5 : ; 6 : } = X.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1) :- #min{1 : ; 2 : ; 3 : ; 4 : ; 5 : ; 6 : } = 1.  
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).
```

```
reached(Y) :- cycle(X,Y), reached(X).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).  
reached(Y) :- cycle(1,Y), reached(1).  
:- node(Y), not reached(Y).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).  
reached(Y) :- cycle(1,Y), reached(1).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1).  
:- node(Y), not reached(Y).
```

```
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1). ...  
:- node(Y), not reached(Y).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...  
  
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...  
  
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1). ...  
:- node(Y), not reached(Y).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```


(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1). ...  
:- not reached(1). ... :- not reached(6).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...  
  
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...  
  
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1). ...  
:- not reached(1). ... :- not reached(6).  
  
:~ cycle(X,Y), edge(X,Y,C). [C,X]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...  
  
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...  
  
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1). ...  
:- not reached(1). ... :- not reached(6).  
  
:~ cycle(1,2). [2,1] ... :~ cycle(1,4). [1,1]
```

(Intelligent) Grounding

Ground Instantiation

```
node(1). node(2). node(3). node(4). node(5). node(6).  
edge(1,2,2).  
edge(1,3,3). edge(3,1,3).  
edge(1,4,1). edge(4,1,1). ...
```

```
{cycle(1,2); cycle(1,3); cycle(1,4)} = 1. ...  
{cycle(3,1); cycle(4,1)} = 1. ...
```

```
reached(1).  
reached(2) :- cycle(1,2), reached(1).  
reached(3) :- cycle(1,3), reached(1).  
reached(4) :- cycle(1,4), reached(1). ...  
:- not reached(1). ... :- not reached(6).  
  
:~ cycle(1,2). [2,1] ... :~ cycle(1,4). [1,1] ...
```

(Pseudo-)Boolean Optimization

Model-guided Approach

```
$ clingo <instance> <encoding>
```

```
Answer: 1
```

```
cycle(1,4) cycle(4,2) cycle(2,6) cycle(6,5) cycle(5,3) cycle(3,1)
```

```
Optimization: 13
```

```
Answer: 2
```

```
cycle(1,4) cycle(4,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,1)
```

```
Optimization: 12
```

```
Answer: 3
```

```
cycle(1,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,4) cycle(4,1)
```

```
Optimization: 11
```

```
Time : 0.002s
```

```
Conflicts : 12
```

(Pseudo-)Boolean Optimization

Model-guided Approach

```
$ clingo <instance> <encoding>
```

Answer: 1

```
cycle(1,4) cycle(4,2) cycle(2,6) cycle(6,5) cycle(5,3) cycle(3,1)
```

Optimization: 13

Answer: 2

```
cycle(1,4) cycle(4,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,1)
```

Optimization: 12

Answer: 3

```
cycle(1,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,4) cycle(4,1)
```

Optimization: 11

Time : 0.002s

Conflicts : 12

(Pseudo-)Boolean Optimization

Model-guided Approach

```
$ clingo <instance> <encoding>
```

```
Answer: 1
```

```
cycle(1,4) cycle(4,2) cycle(2,6) cycle(6,5) cycle(5,3) cycle(3,1)
```

```
Optimization: 13
```

```
Answer: 2
```

```
cycle(1,4) cycle(4,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,1)
```

```
Optimization: 12
```

```
Answer: 3
```

```
cycle(1,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,4) cycle(4,1)
```

```
Optimization: 11
```

```
Time : 0.002s
```

```
Conflicts : 12
```

(Pseudo-)Boolean Optimization

Core-guided Approach

```
$ clingo <instance> <encoding> --opt-strategy=usc
```

```
Progression : [3;inf]
```

```
Progression : [5;inf]
```

```
Progression : [6;inf]
```

```
Progression : [7;inf]
```

```
Progression : [8;inf]
```

```
Progression : [9;inf]
```

```
Progression : [10;inf]
```

```
Progression : [11;inf]
```

```
Answer: 1
```

```
cycle(1,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,4) cycle(4,1)
```

```
Optimization: 11
```

```
Time : 0.002s
```

```
Conflicts : 10
```


(Pseudo-)Boolean Optimization

Core-guided Approach

```
$ clingo <instance> <encoding> --opt-strategy=usc
```

```
Progression : [3;inf]
```

```
Progression : [5;inf]
```

```
Progression : [6;inf]
```

```
Progression : [7;inf]
```

```
Progression : [8;inf]
```

```
Progression : [9;inf]
```

```
Progression : [10;inf]
```

```
Progression : [11;inf]
```

```
Answer: 1
```

```
cycle(1,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,4) cycle(4,1)
```

```
Optimization: 11
```

```
Time : 0.002s
```

```
Conflicts : 10
```

(Pseudo-)Boolean Optimization

Core-guided Approach

```
$ clingo <instance> <encoding> --opt-strategy=usc
```

```
Progression : [3;inf]
```

```
Progression : [5;inf]
```

```
Progression : [6;inf]
```

```
Progression : [7;inf]
```

```
Progression : [8;inf]
```

```
Progression : [9;inf]
```

```
Progression : [10;inf]
```

```
Progression : [11;inf]
```

Answer: 1

```
cycle(1,2) cycle(2,5) cycle(5,6) cycle(6,3) cycle(3,4) cycle(4,1)
```

Optimization: 11

```
Time : 0.002s
```

```
Conflicts : 10
```

Outline

- 1 Motivation
- 2 ASP in a Nutshell
- 3 Linux Package Configuration
- 4 Conclusion

Free and Open Source Software Management

- ▶ Maintaining packages in modern Linux distributions is difficult
 - Complex dependencies
 - Large package repositories
 - Ever changing in view of software development
- ▶ Challenges for package configuration tools
 - Large problem size
 - Soft (and hard) constraints
 - Multiple optimization criteria



Targeted in the EU research project *Mancoosi*

- ▶ Contributions of ASP
 - Uniform modeling by encoding plus instances
 - Solving techniques for (multi-criteria) optimization



*Instead of the **standard** `apt-get install libreoffice` that **failed to propose a decent upgrade**, as detailed later, I typed `apt-get --solver aspcud install libreoffice` that returned this pretty good solution ...*

Free and Open Source Software Management

- ▶ Maintaining packages in modern Linux distributions is difficult
 - Complex dependencies
 - Large package repositories
 - Ever changing in view of software development
- ▶ Challenges for package configuration tools
 - Large problem size
 - Soft (and hard) constraints
 - Multiple optimization criteria



Targeted in the EU research project *Mancoosi*

- ▶ Contributions of ASP
 - Uniform modeling by encoding plus instances
 - Solving techniques for (multi-criteria) optimization



*Instead of the **standard** `apt-get install libreoffice` that **failed to propose a decent upgrade**, as detailed later, I typed `apt-get --solver aspcud install libreoffice` that returned this pretty good solution ...*

Free and Open Source Software Management

- ▶ Maintaining packages in modern Linux distributions is difficult
 - Complex dependencies
 - Large package repositories
 - Ever changing in view of software development
- ▶ Challenges for package configuration tools
 - Large problem size
 - Soft (and hard) constraints
 - Multiple optimization criteria



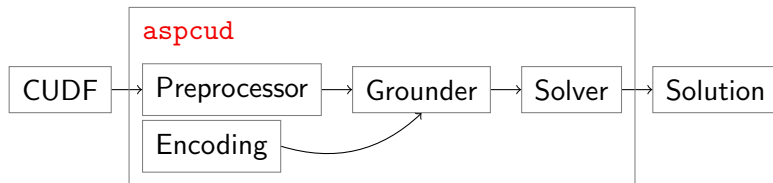
Targeted in the EU research project *Mancoosi*

- ▶ Contributions of ASP
 - Uniform modeling by encoding plus instances
 - Solving techniques for (multi-criteria) optimization



Instead of the *standard* `apt-get install libreoffice` that *failed to propose a decent upgrade*, as detailed later, I typed `apt-get --solver aspcud install libreoffice` that *returned this pretty good solution* ...

Linux Package Configurator aspcud



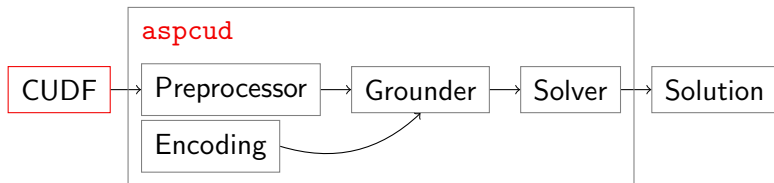
Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Linux Package Configurator aspcud : Input



Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Common Upgradability Description Format (CUDF)

► Language to represent package interdependencies

- Conflicts
- Dependencies
- Recommendations

► and user goals

- Installation
- Removal
- Upgrade

► subject to optimization

- Package deletions
- Package additions
- Package recommendations
- Version changes
- Version up-to-dateness
- Version coherence
- Installation size

CUDF Input

```
package:      firefox
version:      3
conflicts:    firefox
depends:       xserver > 2

recommends:   thunderbird

request:
install:      firefox
remove:       firefox < 3

upgrade:      firefox > 2
```

Common Upgradability Description Format (CUDF)

► Language to represent package interdependencies

- Conflicts
- Dependencies
- Recommendations

► and user goals

- Installation
- Removal
- Upgrade

► subject to optimization

- Package deletions
- Package additions
- Package recommendations
- Version changes
- Version up-to-dateness
- Version coherence
- Installation size

CUDF Input

```
package:      firefox
version:      3
conflicts:    firefox
depends:       xserver > 2

recommends:   thunderbird

request:
install:      firefox
remove:       firefox < 3

upgrade:      firefox > 2
```

Common Upgradability Description Format (CUDF)

► Language to represent package interdependencies

- Conflicts
- Dependencies
- Recommendations

► and user goals

- Installation
- Removal
- Upgrade

► subject to optimization

- Package deletions
- Package additions
- Package recommendations
- Version changes
- Version up-to-dateness
- Version coherence
- Installation size

CUDF Input

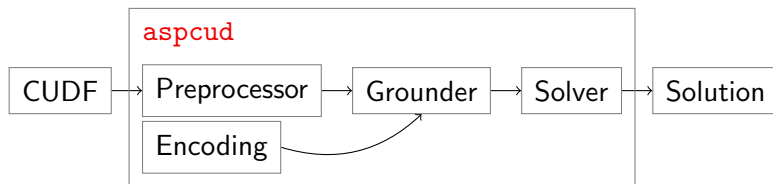
```
package:      firefox
version:      3
conflicts:    firefox
depends:       xserver > 2

recommends:   thunderbird

request:
install:      firefox
remove:       firefox < 3

upgrade:      firefox > 2
```

Linux Package Configurator aspcud



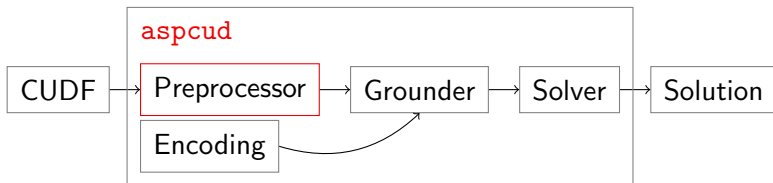
Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Linux Package Configurator aspcud : Preprocessor



Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Setting the Focus

Scenario

- ▶ Modern Linux distributions are large (50K packages or more)
- 👉 Problem representation and search space are of significant size

Observations

- ▶ Some packages can't be installed (remove or upgrade goals)
- ▶ An empty installation is conflict-free and thus valid
- 👉 Packages to install should serve (hard) `install` or `upgrade` goals, or satisfy (soft) constraints

Approach

- ① Identify packages whose installation may be of direct use
- ② Saturate such packages wrt. dependencies and soft constraints
- ③ Restrict the ASP instance to closure of “interesting” packages
- ④ (Greedy) partition these packages into mutual conflict cliques

Setting the Focus

Scenario

- ▶ Modern Linux distributions are large (50K packages or more)
- ☞ Problem representation and search space are of significant size

Observations

- ▶ Some packages can't be installed (remove or upgrade goals)
- ▶ An empty installation is conflict-free and thus valid
- ☞ Packages to install should serve (hard) `install` or `upgrade` goals, or satisfy (soft) constraints

Approach

- ① Identify packages whose installation may be of direct use
- ② Saturate such packages wrt. dependencies and soft constraints
- ③ Restrict the ASP instance to closure of “interesting” packages
- ④ (Greedy) partition these packages into mutual conflict cliques

Setting the Focus

Scenario

- ▶ Modern Linux distributions are large (50K packages or more)
- 👉 Problem representation and search space are of significant size

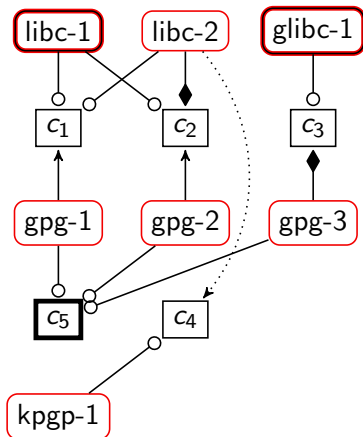
Observations

- ▶ Some packages can't be installed (remove or upgrade goals)
- ▶ An empty installation is conflict-free and thus valid
- 👉 Packages to install should serve (hard) `install` or `upgrade` goals, or satisfy (soft) constraints

Approach

- ① Identify packages whose installation may be of direct use
- ② Saturate such packages wrt. dependencies and soft constraints
- ③ Restrict the ASP instance to closure of “interesting” packages
- ④ (Greedy) partition these packages into mutual conflict cliques

Instance Representation



Installable Packages

```
package(libc,1).
```

```
package(libc,2).
```

```
package(glibc,1).
```

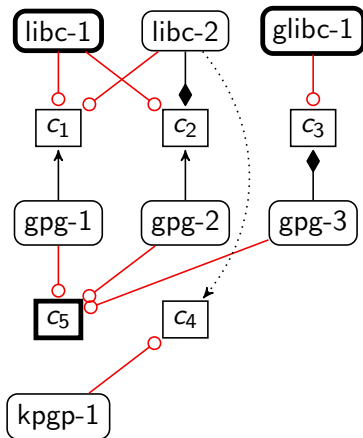
```
package(gpg,1).
```

```
package(gpg,2).
```

```
package(gpg,3).
```

```
package(kpgp,1).
```

Instance Representation



Package Conditions

```
satisfies(libc,1,c1).  
satisfies(libc,2,c1).
```

```
satisfies(libc,1,c2).
```

```
satisfies(glibc,1,c3).
```

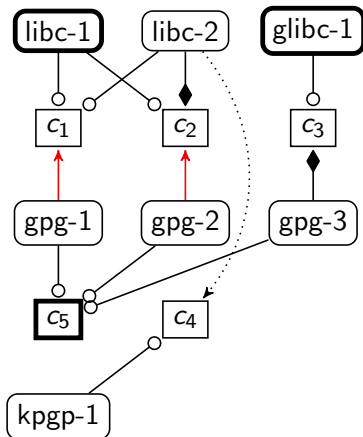
```
satisfies(kpgp,1,c4).
```

```
satisfies(gpg,1,c5).
```

```
satisfies(gpg,2,c5).
```

```
satisfies(gpg,3,c5).
```

Instance Representation

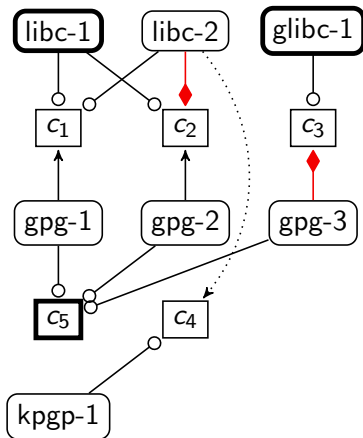


Package Dependencies

`depends (gpg, 1, c1) .`

`depends (gpg, 2, c2) .`

Instance Representation

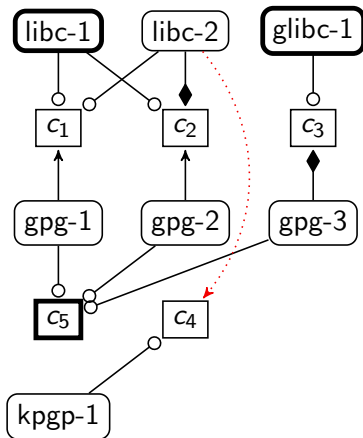


Package Conflicts

```
conflicts(libc,2,c2).
```

```
conflicts(gpg,3,c3).
```

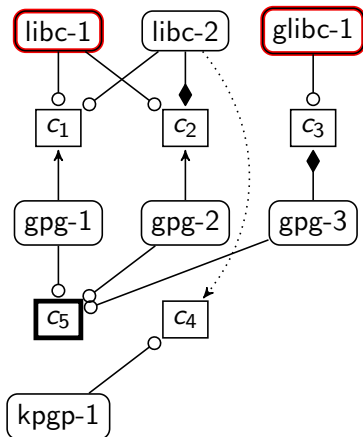
Instance Representation



Package Recommendations

```
recommends(libc,2,c4) .
```

Instance Representation

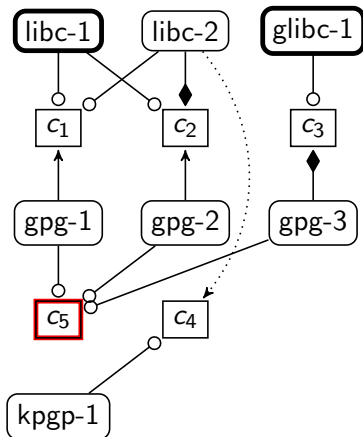


Installed Packages

```
installed(libbc,1).
```

```
installed(glibc,1).
```

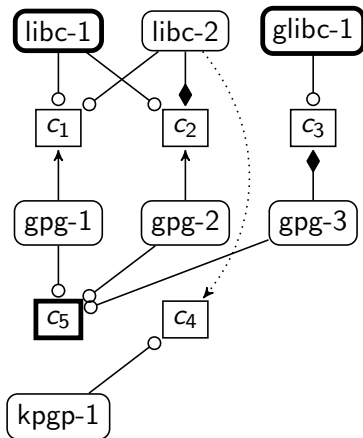
Instance Representation



User Goals

request(c5).

Instance Representation

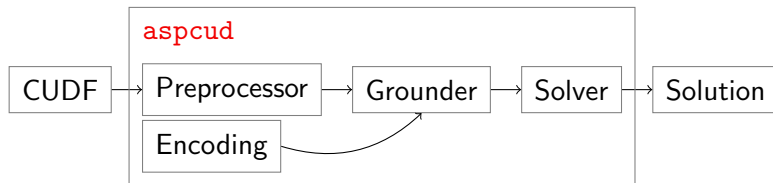


Optimization Criteria

`utility(delete,1).`

`utility(change,2).`

Linux Package Configurator aspcud



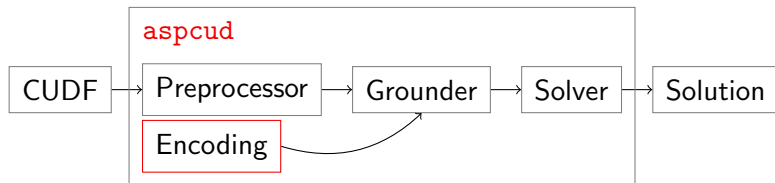
Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Linux Package Configurator aspcud : Encoding



Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Hard Constraints

- 1 Can install any installable package
- 2 Excluded, included, and satisfied conditions (packages) follow
- 3 Respective conditions and user goals must be fulfilled

Problem Encoding

```
{install(P,V)} :- package(P,V).
```

```
exclude(C) :- install(P,V), conflicts(P,V,C).
```

```
include(C) :- install(P,V), depends(P,V,C).
```

```
satisfy(C) :- install(P,V), satisfies(P,V,C).
```

```
:- exclude(C),      satisfy(C).
```

```
:- include(C), not satisfy(C).
```

```
:- request(C), not satisfy(C).
```

Hard Constraints

- 1 Can install any **installable package**
- 2 Excluded, included, and satisfied conditions (packages) follow
- 3 Respective conditions and user goals must be fulfilled

Problem Encoding

```
{install(P,V)} :- package(P,V).
```

```
exclude(C) :- install(P,V), conflicts(P,V,C).
```

```
include(C) :- install(P,V), depends(P,V,C).
```

```
satisfy(C) :- install(P,V), satisfies(P,V,C).
```

```
:- exclude(C),      satisfy(C).
```

```
:- include(C), not satisfy(C).
```

```
:- request(C), not satisfy(C).
```

Hard Constraints

- 1 Can install any installable package
- 2 **Excluded, included, and satisfied conditions** (packages) follow
- 3 Respective conditions and user goals must be fulfilled

Problem Encoding

```
{install(P,V)} :- package(P,V).
```

```
exclude(C) :- install(P,V), conflicts(P,V,C).
```

```
include(C) :- install(P,V), depends(P,V,C).
```

```
satisfy(C) :- install(P,V), satisfies(P,V,C).
```

```
:- exclude(C),      satisfy(C).
```

```
:- include(C), not satisfy(C).
```

```
:- request(C), not satisfy(C).
```

Hard Constraints

- 1 Can install any installable package
- 2 Excluded, included, and satisfied conditions (packages) follow
- 3 Respective **conditions and user goals** must be fulfilled

Problem Encoding

```
{install(P,V)} :- package(P,V).
```

```
exclude(C) :- install(P,V), conflicts(P,V,C).
```

```
include(C) :- install(P,V), depends(P,V,C).
```

```
satisfy(C) :- install(P,V), satisfies(P,V,C).
```

```
:- exclude(C),      satisfy(C).
```

```
:- include(C), not satisfy(C).
```

```
:- request(C), not satisfy(C).
```

Soft Constraints

- 1 Package additions and deletions
- 2 Version changes

Problem Encoding (ctd)

```
install(P)    :- install(P,V).  
installed(P)  :- installed(P,V).
```

```
violate(newpkg,L,P) :-  
    utility(newpkg,L), install(P), not installed(P).  
violate(delete,L,P) :-  
    utility(delete,L), installed(P), not install(P).  
violate(change,L,P) :-  
    utility(change,L), installed(P,V), not install(P,V).  
violate(change,L,P) :-  
    utility(change,L), install(P,V), not installed(P,V).  
  
:~ violate(U,L,T). [1@L,U,T]
```

Soft Constraints

- 1 Package **additions** and deletions
- 2 Version changes

Problem Encoding (ctd)

```
install(P)    :- install(P,V).  
installed(P)  :- installed(P,V).
```

```
violate(newpkg,L,P) :-  
    utility(newpkg,L), install(P), not installed(P).  
violate(delete,L,P) :-  
    utility(delete,L), installed(P), not install(P).  
violate(change,L,P) :-  
    utility(change,L), installed(P,V), not install(P,V).  
violate(change,L,P) :-  
    utility(change,L), install(P,V), not installed(P,V).  
  
:~ violate(U,L,T). [1@L,U,T]
```


Soft Constraints

- 1 Package additions and deletions
- 2 Version changes

Problem Encoding (ctd)

```
install(P)    :- install(P,V).
installed(P)  :- installed(P,V).

violate(newpkg,L,P) :-
    utility(newpkg,L), install(P), not installed(P).
violate(delete,L,P) :-
    utility(delete,L), installed(P), not install(P).
violate(change,L,P) :-
    utility(change,L), installed(P,V), not install(P,V).
violate(change,L,P) :-
    utility(change,L), install(P,V), not installed(P,V).

:~ violate(U,L,T). [1@L,U,T]
```

Soft Constraints

- 1 Package additions and deletions
- 2 Version changes

Problem Encoding (ctd)

```
install(P)    :- install(P,V).  
installed(P)  :- installed(P,V).
```

```
violate(newpkg,L,P) :-  
    utility(newpkg,L), install(P), not installed(P).  
violate(delete,L,P) :-  
    utility(delete,L), installed(P), not install(P).  
violate(change,L,P) :-  
    utility(change,L), installed(P,V), not install(P,V).  
violate(change,L,P) :-  
    utility(change,L), install(P,V), not installed(P,V).
```

```
:~ violate(U,L,T). [1@L,U,T]
```

Soft Constraints

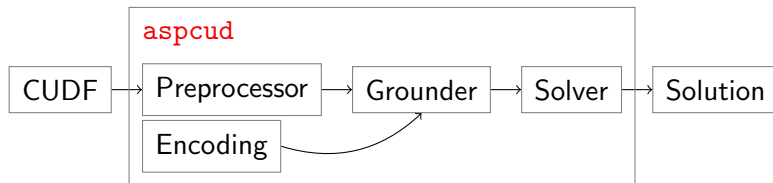
- 1 Package additions and deletions
- 2 Version changes

Problem Encoding (ctd)

```
install(P)    :- install(P,V).
installed(P)  :- installed(P,V).

violate(newpkg,L,P) :-
    utility(newpkg,L), install(P), not installed(P).
violate(delete,L,P) :-
    utility(delete,L), installed(P), not install(P).
violate(change,L,P) :-
    utility(change,L), installed(P,V), not install(P,V).
violate(change,L,P) :-
    utility(change,L), install(P,V), not installed(P,V).
...
:~ violate(U,L,T). [1@L,U,T]
```

Linux Package Configurator aspcud



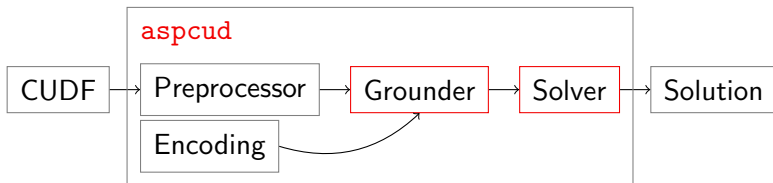
Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Linux Package Configurator aspcud : Reasoning



Preprocessor Converts CUDF input to ASP instance

Encoding First-order problem specification

Grounder Instantiates first-order variables

Solver Searches for (optimal) answer sets

Mancoosi International Solver Competition (MISC)

► Encoding using conflict cliques and core-guided optimization

➤ **Track: paranoid**

Category	aspcud-paranoid-1.7	aspuncud-paranoid-1.7	cudf_fumax_p-0.1	p2cudf-paranoid-1.15
paranoid	104 (683.49)	98 (542.51)	154 (743.19)	248 (1161.00)
Total	104 (683.49)	98 (542.51)	154 (743.19)	248 (1161.00)

Criterion	aspcud-paranoid-1.7	aspuncud-paranoid-1.7	cudf_fumax_p-0.1	p2cudf-paranoid-1.15
paranoid	104 (683.49)	98 (542.51)	154 (743.19)	248 (1161.00)
Total	104 (683.49)	98 (542.51)	154 (743.19)	248 (1161.00)

Paranoid Track (details)

➤ **Track: basic**

Category	aspcud-basic-1.7	aspuncud-basic-1.7	cudf_fumax_bu-0.1	p2cudf-basic-1.15
paranoid-size	138 (8619.43)	98 (1013.50)	233 (7601.23)	294 (4094.53)
embedded	153 (7952.31)	98 (1053.80)	359 (6850.86)	280 (915.45)
Total	291 (16571.73)	193 (3467.23)	592 (14452.09)	574 (5009.98)

Criterion	aspcud-basic-1.7	aspuncud-basic-1.7	cudf_fumax_bu-0.1	p2cudf-basic-1.15
paranoid-size	138 (8619.43)	98 (1013.50)	233 (7601.23)	294 (4094.53)
embedded	153 (7952.31)	98 (1053.80)	359 (6850.86)	280 (915.45)
Total	291 (16571.73)	193 (3467.23)	592 (14452.09)	574 (5009.98)

Basic User Track (details)

➤ **Track: full**

Category	aspcud-full-1.7	aspuncud-full-1.7	p2cudf-full-1.15
trendy-size	292 (32003.38)	135 (4247.64)	293 (8308.43)
dist-upgrade	130 (2912.62)	129 (1592.38)	500 (34449.24)
upgrade	131 (2935.91)	129 (1594.91)	497 (34396.18)
slowlink	239 (24293.00)	126 (3117.77)	264 (16364.54)
Total	792 (62144.90)	522 (10552.71)	1554 (93518.40)

Criterion	aspcud-full-1.7	aspuncud-full-1.7	p2cudf-full-1.15
trendy-size	292 (32003.38)	135 (4247.64)	293 (8308.43)
dist-upgrade	130 (2912.62)	129 (1592.38)	500 (34449.24)
upgrade	131 (2935.91)	129 (1594.91)	497 (34396.18)
slowlink	239 (24293.00)	126 (3117.77)	264 (16364.54)
Total	792 (62144.90)	522 (10552.71)	1554 (93518.40)

Full User Track (details)

Outline

- 1 Motivation
- 2 ASP in a Nutshell
- 3 Linux Package Configuration
- 4 Conclusion

Further Remarks

- ▶ Virtually all application problems require **optimization**
 - objective functions
 - lexicographic (multi-)criteria
- ▶ Complex criteria like \subseteq -minimality or Pareto efficiency by
 - meta-programming (disjunctive ASP)
 - asprin framework
- ▶ Multi-shot solving, domain heuristics and theory reasoning
 - clingo
 - clingo[DL]
 - clingo[LP]
 - clingcon
 - DLV2
 - dlvhex
 - EZCSP
 - EZSMT
 - IDP
 - wasp
 - ASP tools (by Aalto SCI)

Further Remarks

- ▶ Virtually all application problems require **optimization**
 - objective functions
 - lexicographic (multi-)criteria
- ▶ Complex criteria like \subseteq -minimality or Pareto efficiency by
 - meta-programming (disjunctive ASP)
 - asprin framework
- ▶ Multi-shot solving, domain heuristics and theory reasoning
 - clingo
 - clingo[DL]
 - clingo[LP]
 - clingcon
 - DLV2
 - dlvhex
 - EZCSP
 - EZSMT
 - IDP
 - wasp
 - ASP tools (by Aalto SCI)

Thanks!

- ▶ to Roland Kaminski and Torsten Schaub for part of the slides
- ▶ to **you** for your attention and ...

Questions?