

# Nonlocal translationally invariant density

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## Abstract

Nonlocal nuclear density is derived from the no-core shell model (NCSM) [1] one-body densities by generalizing the local density operator to a nonlocal form. The translational invariance (trinv) is generated by exactly removing the spurious center of mass (COM) component from the NCSM eigenstates expanded in the harmonic oscillator (HO) basis [2]. This enables the *ab initio* NCSM nuclear structure to be used in intermediate energy nuclear reactions and density functional theory (DFT). The ground state local and nonlocal density of  $^4\text{He}$ ,  $^6\text{He}$ ,  $^{12}\text{C}$  and  $^{16}\text{O}$  are calculated to display the effects of COM removal on predicted nuclear structure. We include nonlocal density in calculations of optical potentials [3] and show more accurate theoretical predictions for the differential cross sections for proton scattering on  $^4\text{He}$ . The results of this work have been published in Ref. [4]. Additionally, we show amplified effects of COM removal in related DFT quantities like kinetic density [5].

## Nuclear density

The general nonlocal nuclear density operator is shown below, where  $\mathbf{r}$  is a coordinate for the final state and  $\mathbf{r}'$  is a separate coordinate for the initial state.

$$\rho_{op}(\vec{r}, \vec{r}') = \sum_{i=1}^A \{|\vec{r}\rangle\langle\vec{r}'|\}^i = \sum_{i=1}^A \delta(\vec{r} - \vec{r}_i) \delta(\vec{r}' - \vec{r}_i)$$

In the NCSM basis, translational invariance of the internal wave function is preserved when the single-particle Slater Determinant (SD) basis is used with  $N_{\text{max}}$  truncation [1]. The factorization of the Jacobi and SD eigenstates allows us to decouple and remove the ground state COM component from the intrinsic part of the wavefunction [2].

$$\langle \vec{r}_1 \cdots \vec{r}_A \vec{\sigma}_1 \cdots \vec{\sigma}_A \vec{\tau}_1 \cdots \vec{\tau}_A | A \lambda J M \rangle_{SD} = \langle \vec{\xi}_1 \cdots \vec{\xi}_{A-1} \vec{\sigma}_1 \cdots \vec{\sigma}_A \vec{\tau}_1 \cdots \vec{\tau}_A | A \lambda J M \rangle \varphi_{000}(\vec{\xi}_0)$$

We construct the local density [2] by taking the diagonal portion of the nonlocal density ( $\vec{r} = \vec{r}'$ ). The local density provides additional confirmation of the effects of COM removal and is useful for studying convergence patterns of the density.

## Microscopic optical potentials

Nonlocal nuclear density is an important input for constructing microscopic optical potentials of nuclear reactions at intermediate energy. These are computed by folding the density with the t-matrix computed using modern high precision two and three nucleon interactions [3].

$$U(\vec{q}, \vec{K}) = \sum_{N=n,p} \int d\vec{P} \eta(\vec{q}, \vec{K}, \vec{P}) t_{pN}(\vec{q}, \vec{K}, \vec{P}) \rho_N(\vec{q}, \vec{P})$$

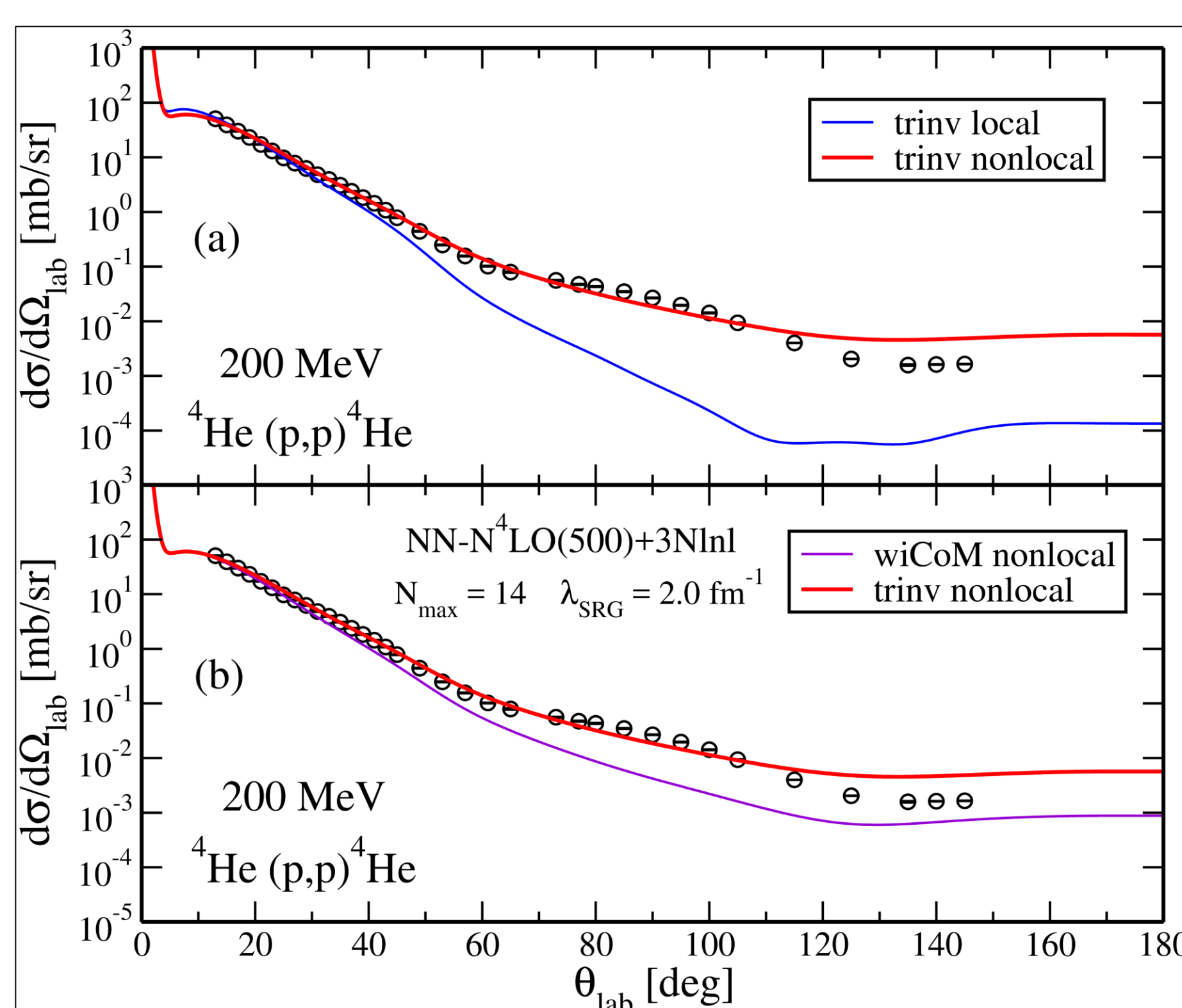


Figure 3: Comparisons between the wiCOM and trinv local density and nonlocal density calculations for the differential cross section of  $^4\text{He}$

See the talk titled “Microscopic optical potential for proton elastic scattering off light exotic nuclei” by Matteo Vorabbi for explicit discussion of the microscopic optical potentials.

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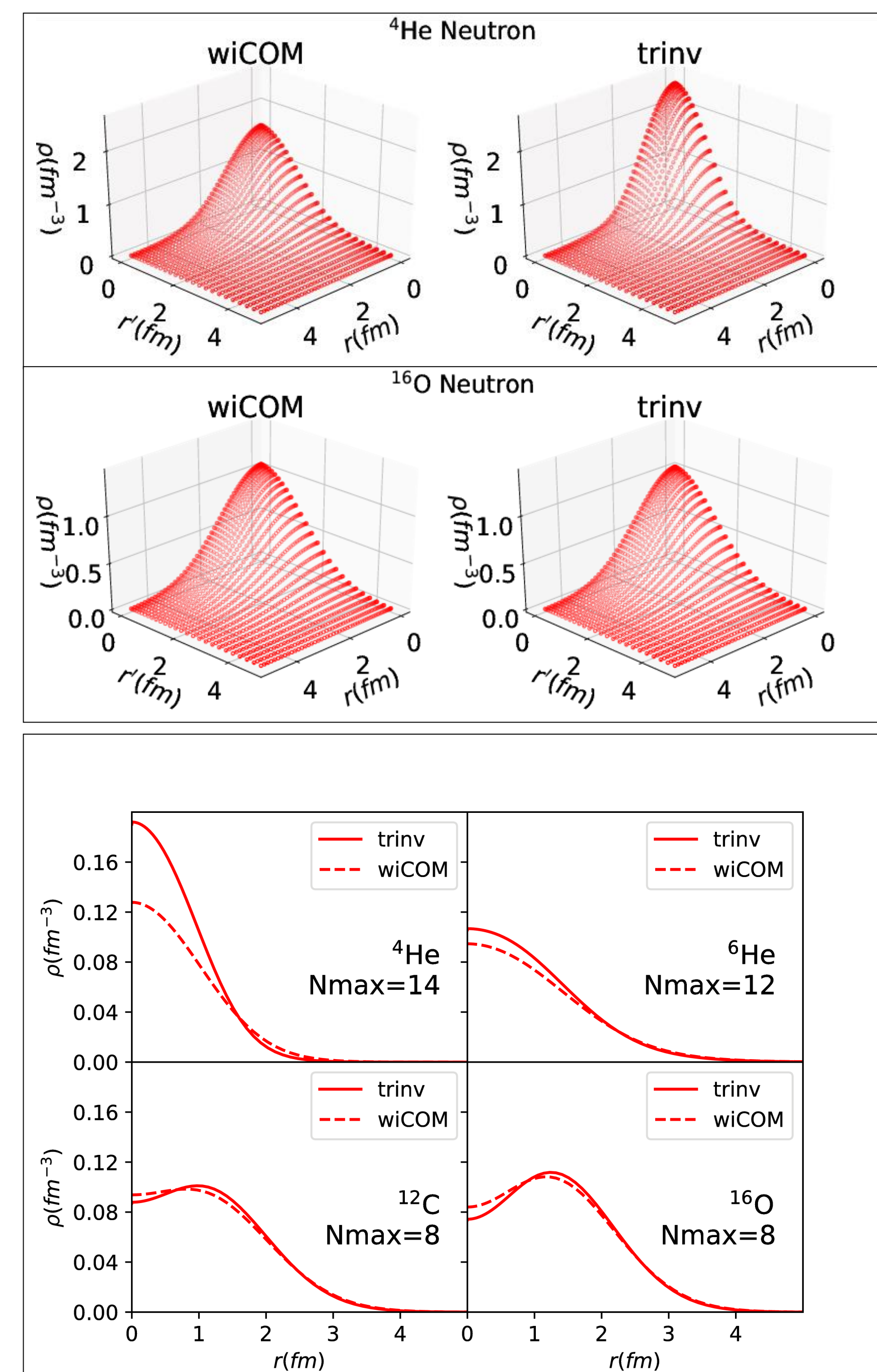


Figure 1: Comparisons between wiCOM and trinv nuclear density for  $^4\text{He}$  and  $^{16}\text{O}$

Figure 2: Comparisons of local wiCOM and trinv densities of  $^4\text{He}$ ,  $^6\text{He}$ ,  $^{12}\text{C}$  and  $^{16}\text{O}$ .

## Kinetic density

The kinetic density is an example of one object in DFT [5] we can compute using *ab initio* wavefunctions. The kinetic density is given by the following relation,

$$\tau_N(\vec{r}) = (\vec{\nabla} \cdot \vec{\nabla}' \rho_N(\vec{r}, \vec{r}'))|_{\vec{r}=\vec{r}'}$$

The Laplacian-like operator is applied on the nonlocal density and should amplify effects of COM removal, the results of which are shown for  $^4\text{He}$ ,  $^6\text{He}$ ,  $^{12}\text{C}$ , and  $^{16}\text{O}$ .

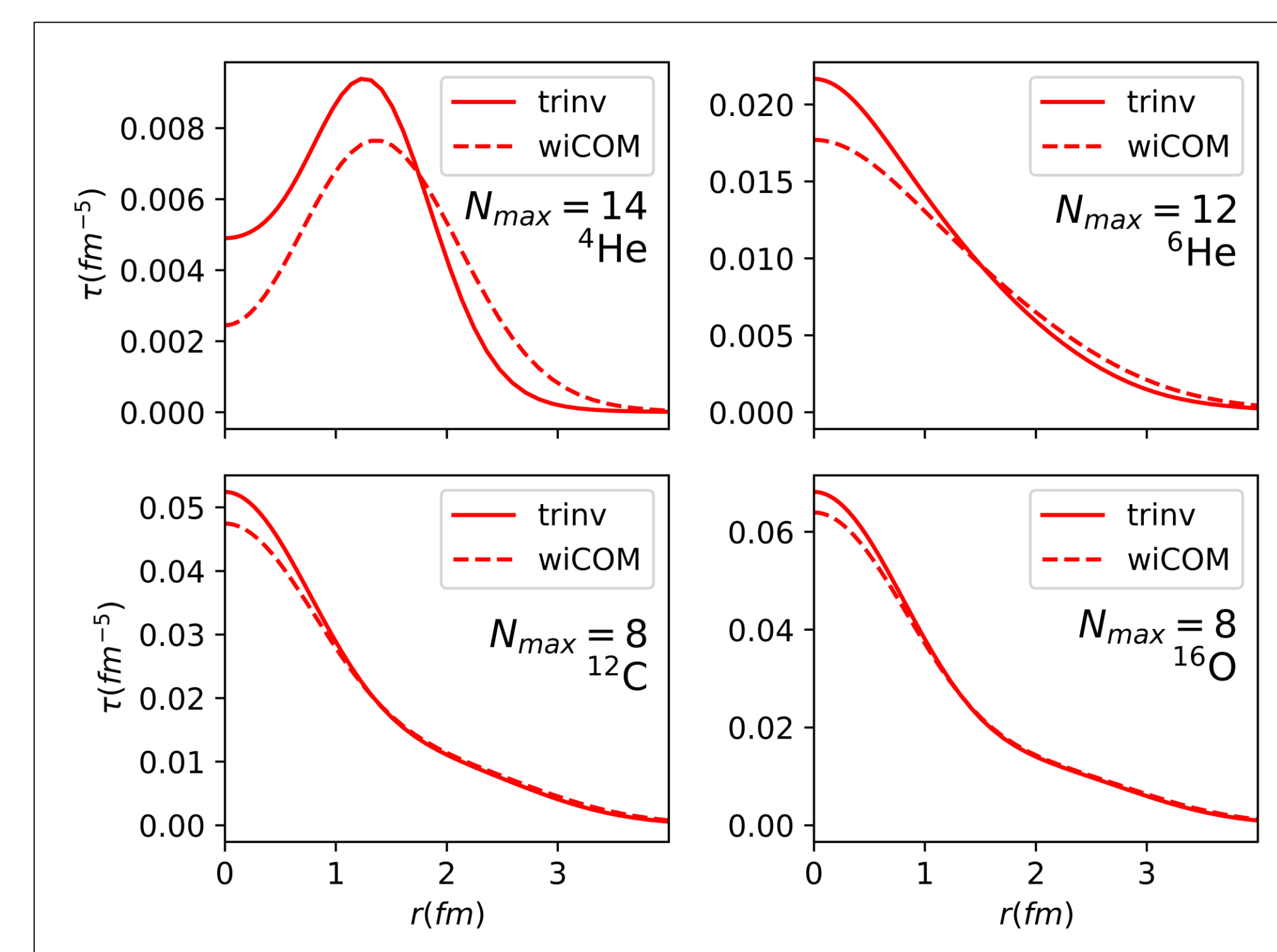


Figure 4: Comparison between the neutron wiCOM and trinv kinetic densities

## References

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