

Template Article - Shell Model Project

GIANLUCA SALVIONI¹, INA K. B. KULLMANN², MATTHEW SHELLEY³, and GILHO AHN⁴

¹Department of FILL IN, L^AT_EX University

²Department of Mechanical Engineering, University of Oslo
i.k.b.kullmann@fys.uio.no, youremail@edu.com youremail@edu.com youremail@edu.com

July 18, 2017

Abstract

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Etiam lobortis facilisis sem. Nullam nec mi et neque pharetra sollicitudin. Praesent imperdiet mi nec ante. Donec ullamcorper, felis non sodales commodo, lectus velit ultrices augue, a dignissim nibh lectus placerat pede. Vivamus nunc nunc, molestie ut, ultricies vel, semper in, velit. Ut porttitor. Praesent in sapien. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Duis fringilla tristique neque. Sed interdum libero ut metus. Pellentesque placerat. Nam rutrum augue a leo. Morbi sed elit sit amet ante lobortis sollicitudin. Praesent blandit blandit mauris. Praesent lectus tellus, aliquet aliquam, luctus a, egestas a, turpis. Mauris lacinia lorem sit amet ipsum. Nunc quis urna dictum turpis accumsan semper.

I. INTRODUCTION

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Etiam lobortis facilisis sem. Nullam nec mi et neque pharetra sollicitudin. Praesent imperdiet mi nec ante. Donec ullamcorper, felis non sodales commodo, lectus velit ultrices augue, a dignissim nibh lectus placerat pede. Vivamus nunc nunc, molestie ut, ultricies vel, semper in, velit. Ut porttitor. Praesent in sapien. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Duis fringilla tristique neque. Sed interdum libero ut metus. Pellentesque placerat. Nam rutrum augue a leo. Morbi sed elit sit amet ante lobortis sollicitudin. Praesent blandit blandit mauris. Praesent lectus tellus, aliquet aliquam, luctus a, egestas a, turpis. Mauris lacinia lorem sit amet ipsum. Nunc quis urna dictum turpis accumsan semper.

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Etiam lobortis facilisis sem. Nullam nec mi et neque pharetra sollicitudin. Praesent imperdiet mi nec ante. Donec ullamcorper, felis non sodales commodo, lectus velit ultrices augue, a dignissim nibh lectus placerat pede. Vivamus nunc nunc, molestie ut, ultricies vel, semper in, velit. Ut porttitor. Praesent in sapien. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Duis fringilla tristique neque. Sed interdum libero ut metus. Pellentesque placerat. Nam rutrum augue a leo. Morbi sed elit sit amet ante lobortis sollicitudin. Praesent blandit blandit mauris. Praesent lectus tellus, aliquet aliquam, luctus a, egestas a, turpis. Mauris lacinia lorem sit amet ipsum. Nunc quis urna dictum turpis accumsan semper.

II. PART 1 - RENAME SECTIONS LATER, DO NOT NEED THE NUMBERING OF THE EXERCISES

i. Exe. 1a

Show that the unperturbed Hamiltonian \hat{H}_0 and \hat{V} commute both with \hat{S}_z and \hat{S}^2 .

$$\hat{H}_0 = \sum_{p\sigma} (p-1) a_{p\sigma}^\dagger a_{p\sigma} \hat{S}_z = \frac{1}{2} \sum_{pq\sigma} \sigma a_{p\sigma}^\dagger a_{p\sigma}$$

first rewriting the products:

$$\begin{aligned} \hat{S}_z \hat{H}_0 &= \frac{1}{2} \sum_{p\sigma} \sigma a_{p\sigma}^\dagger a_{p\sigma} \cdot \sum_{p\sigma} (p-1) a_{p\sigma}^\dagger a_{p\sigma} \\ &= \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) a_{p\sigma}^\dagger a_{p\sigma} a_{qb}^\dagger a_{qb} \\ &= \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) a_\alpha^\dagger a_\alpha a_\beta^\dagger a_\beta \\ \hat{H}_0 \hat{S}_z &= \sum_{p\sigma} (p-1) a_{p\sigma}^\dagger a_{p\sigma} \cdot \frac{1}{2} \sum_{p\sigma} \sigma a_{p\sigma}^\dagger a_{p\sigma} \\ &= \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) a_{qb}^\dagger a_{qb} a_{p\sigma}^\dagger a_{p\sigma} \\ &= \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) a_\beta^\dagger a_\beta a_\alpha^\dagger a_\alpha \end{aligned}$$

so that the commutation relation becomes:

$$\begin{aligned} [\hat{S}_z, \hat{H}_0] &= \hat{S}_z \hat{H}_0 - \hat{H}_0 \hat{S}_z \\ &= \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) a_\alpha^\dagger a_\alpha a_\beta^\dagger a_\beta - \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) a_\beta^\dagger a_\beta a_\alpha^\dagger a_\alpha \\ &= \frac{1}{2} \sum_{p\sigma} \sum_{qb} \sigma (q-1) (a_\alpha^\dagger a_\alpha a_\beta^\dagger a_\beta - a_\beta^\dagger a_\beta a_\alpha^\dagger a_\alpha) \end{aligned}$$

which can only be zero if

$$a_\alpha^\dagger a_\alpha a_\beta^\dagger a_\beta - a_\beta^\dagger a_\beta a_\alpha^\dagger a_\alpha = 0$$

we can use the relations

$$\begin{aligned} \hat{a}_i^\dagger \hat{a}_j^\dagger &= -\hat{a}_j^\dagger \hat{a}_i^\dagger \\ \hat{a}_i \hat{a}_j &= -\hat{a}_j \hat{a}_i \\ \{\hat{a}_i^\dagger, \hat{a}_j\} &= \hat{a}_i^\dagger \hat{a}_j + \hat{a}_j \hat{a}_i^\dagger = \delta_{ij} \\ \Rightarrow \hat{a}_i^\dagger \hat{a}_j &= -\hat{a}_j \hat{a}_i^\dagger, i \neq j \end{aligned}$$

Table 1: *Example table*

Name		
First name	Last Name	Grade
John	Doe	7.5
Richard	Miles	2

to rewrite the first expression

$$\begin{aligned}
 a_{\alpha}^{\dagger}a_{\alpha}a_{\beta}^{\dagger}a_{\beta} &= a_{\alpha}^{\dagger}a_{\beta}^{\dagger}a_{\alpha}a_{\beta} \\
 &= -a_{\beta}^{\dagger}a_{\alpha}^{\dagger}a_{\alpha}a_{\beta} \\
 &= -a_{\beta}^{\dagger}a_{\alpha}^{\dagger}(-a_{\beta}a_{\alpha}) \\
 &= a_{\beta}^{\dagger}a_{\alpha}^{\dagger}a_{\beta}a_{\alpha} \\
 &\Rightarrow a_{\alpha}^{\dagger}a_{\alpha}a_{\beta}^{\dagger}a_{\beta} - a_{\beta}^{\dagger}a_{\beta}a_{\alpha}^{\dagger}a_{\alpha} = 0 \\
 &\Rightarrow [\hat{S}_z, \hat{H}_0] = 0
 \end{aligned}$$

hmmm is this really a proof? indices

ii. Exe. 1b - simple model

We are only including two lowest single-particle levels and totally two particles. We want to construct the Hamiltonian matrix using second quantization and Wick's theorem for a system with no broken pairs and $S = 0$, $S_z = 0$

In this model we can only excite two particles at the same time, so we can define the ground state and the excited state which are the only two possible states:

(also include a figure with the states drawn?)

III. METHODS

Text requiring further explanation¹.

IV. RESULTS

V. DISCUSSION

REFERENCES

[Figueredo and Wolf, 2009] Figueredo, A. J. and Wolf, P. S. A. (2009). Assortative pairing and life history strategy - a cross-cultural study. *Human Nature*, 20:317–330.

¹Example footnote