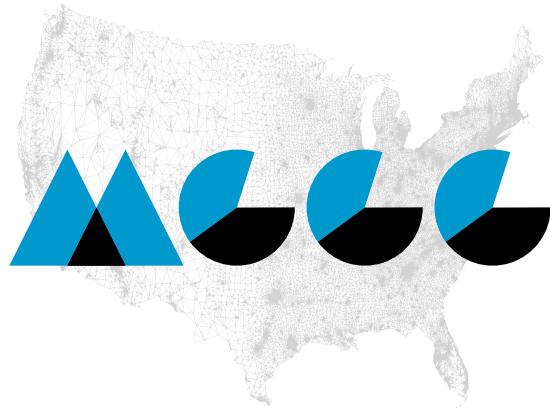


# Analysis of Election Systems for Washington State



MGGG Redistricting Lab

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## Contributors

Amy Becker and Moon Duchin contributed to the study design and analysis in this report. We gratefully acknowledge Talia Blum, Dara Gold, Gabe Schoenbach, and Thomas Weighill for collaboration on ideas, data, and code used here.

## 1 Introduction and Study Questions

Washington State had 6,724,540 residents enumerated in the 2010 Census. Table 1 shows the demographic breakdown of the state by Total Population, Voting Age Population (VAP) and Citizen Voting Age Population (CVAP). We use the term POC (people of color) to refer to residents who are Hispanic or have selected a non-White race in the Census (or both). Other racial group names (Asian, White, etc) denote respondents who identified as non-Hispanic and selected a single racial category. In total the POC share of Washington CVAP is 22.72%. The distribution of POC residents across the state is shown in Figure 1. Breaking down the POC population further, Washington has two individual minority groups that make up more than 5% CVAP share: Hispanic/Latino residents (8.87% of VAP and 7.32% of CVAP) and Asian residents (7.27% of VAP and 6.55% of CVAP).

Race	Share of Total Population	Share of VAP	Share of CVAP
White	72.52%	76.15%	77.28%
POC	27.48%	23.85%	22.72%
Latino	11.24%	8.87%	7.32%
Asian	7.07%	7.27%	6.55%
Black	3.41%	3.27%	3.49%
Other	5.75%	4.44%	5.35%
<b>Total People</b>	<b>6,724,540</b>	<b>5,143,186</b>	<b>5,257,910</b>

**Table 1.** Total population, Voting Age Population (VAP) and Citizen Voting Age Population (CVAP) by race and ethnicity in Washington state. Total population and VAP data is from the 2010 Census, and CVAP data is from the 2018 ACS 5-year rolling average.

Washington is currently divided into 49 state legislative districts, each electing one Senator and two at-large Representatives. State Senators serve 4-year terms; state Representatives serve 2-year terms. All state legislators must reside in the district they represent, and all legislative voting is district-based.

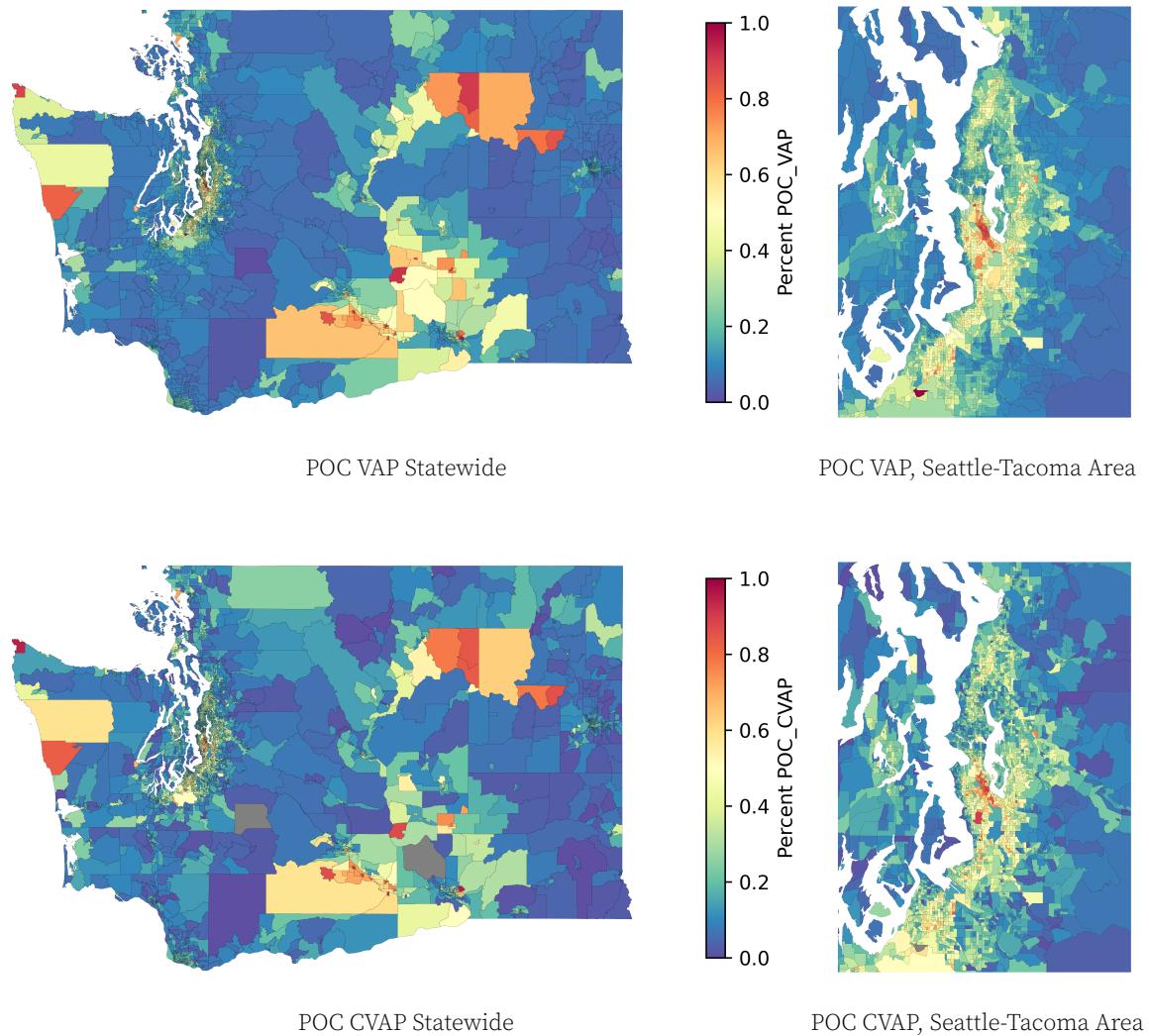
Even though POC residents comprise over a quarter of the state's population (and almost a quarter of the state's CVAP), they are fairly dispersed, rarely achieving high concentrations in any legislative districts. High levels of racially polarized voting or low POC voter turnout could therefore lead to the near-complete exclusion of POC-preferred candidates from office.<sup>1</sup> Furthermore, the at-large system used to elect two House members is also known to be unfavorable to minority representation.

The POC share of the overall population is 27.48%, so the proportional share of the total 147 state legislators (counting Senators and Representatives) would be roughly 40.4. Currently, Washington is well below that mark with only 28 POC state legislators. It is natural to ask whether some of this disparity could be reduced by changes to the state's election system or to the electoral districts.

The Washington State Constitution dictates that "the house of representatives shall be composed of not less than sixty-three nor more than ninety-nine members [and] the number of senators shall not be more than one-half nor less than one-third of the number of members of the house of rep-

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<sup>1</sup>We will take care to distinguish between POC-preferred candidates, who may be from any racial group, and candidates or representatives who are themselves people of color—these groups often, but not always, coincide.



**Figure 1.** POC VAP and POC CVAP by block group across Washington with insets for the Seattle-Tacoma area.

resentatives.<sup>2</sup> These criteria allow a considerable amount of flexibility in the design of the system and the districts. We will also consider possibilities outside of the Constitutional specifications to see whether even more flexibility could afford more opportunity for POC voters. Our focus will be identifying options for the design of districts that are suitable for use in combination with ranked choice voting (RCV), with the aim of maximizing the opportunities for people of color to approach proportional levels of representation in Washington's state legislature.

We consider five alternative setups: (1) 49 districts, each electing three Senators and six House members; (2) 33 districts, each electing one Senator and three House members; (3) 7 districts, each electing seven Senators and subdivided into two House districts, each electing seven House members; (4) 150 districts, each electing one legislator (unicameral); and (5) 200 districts, each electing one legislator (unicameral). As noted above, some of these alternatives would require constitutional amendments—only (2) and (3) fall within the current constraints.

	<b>System 1</b>	<b>System 2</b>	<b>System 3</b>	<b>System 4</b>	<b>System 5</b>
Number of Senate Districts	49	33	7	150	200
Number of House Districts	49	33	14		
District Relation	Coincide	Coincide	Nested	Unicameral	Unicameral
Number of Senators per Senate District	3	1	7	1	1
Number of Representatives per House District	6	3	7		
Total Number of Senators	147	33	49	150	200
Total Number of Representatives	294	99	98		
Ratio of Senators to Representatives	0.5	0.33	0.5		
Total Number of Legislators	441	132	147	150	200

**Table 2.** Summary of the electoral system design alternatives assessed in this report.

## 2 Experimental Design

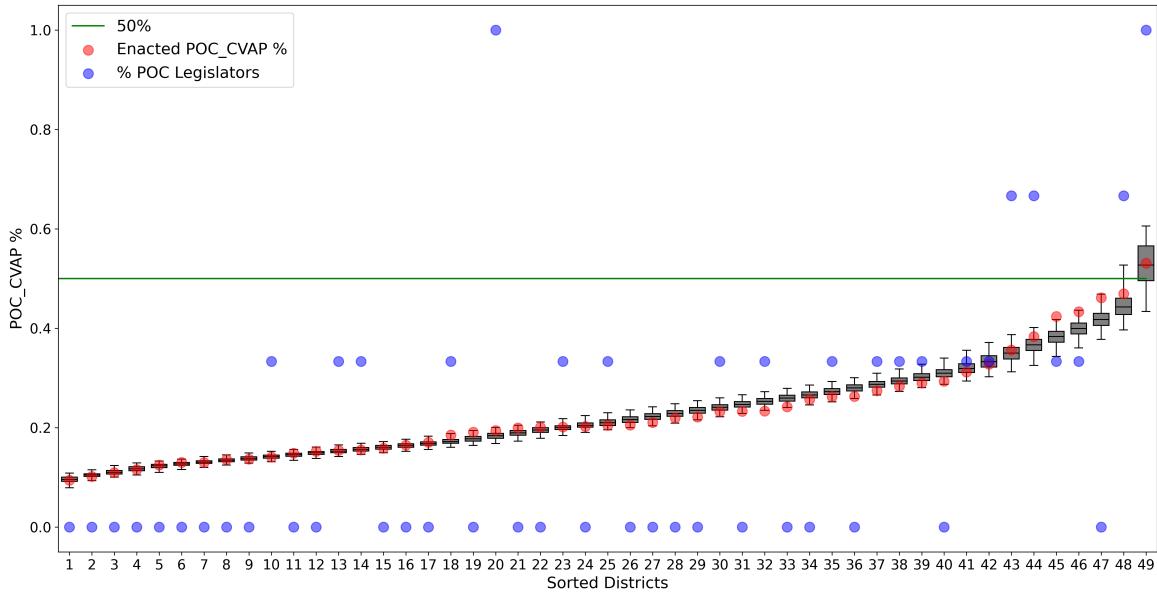
### 2.1 Ensembles of Alternative Districting Plans

A central technique in this study is a random process for generating alternative valid districting plans. We use an algorithm that produces large numbers of plans while maintaining population balance, contiguity, and reasonable compactness.<sup>3</sup> From each run, we collected a sample of 500,000 valid districting plans, which we will call an *ensemble* of plans.

Figure 2 shows the POC CVAP percentages of the 49 enacted state legislative districts in comparison to the range of POC CVAP percentages observed in the ensemble. The fact that the red dots fall close to the boxes indicates that the current plan is unremarkable in its POC distribution: the comparison suggests no intention to create more (or fewer) majority-minority districts than would be present purely by chance.

<sup>2</sup>[https://leg.wa.gov/CodeReviser/Pages/WAConstitution.aspx#ARTICLE\\_II](https://leg.wa.gov/CodeReviser/Pages/WAConstitution.aspx#ARTICLE_II)

<sup>3</sup>Specifically, we use the ReCom Markov chain implementation designed by the MGGG Redistricting Lab. See <https://mggg.org/uploads/ReCom.pdf>. We required all districts to be within 5% of ideal district population, and we ensured district nesting in System 3 by building Senate districts first, then using spanning tree methods to randomly subdivide those into House districts.



**Figure 2.** POC CVAP shares by Senate district (in sorted order from least POC share to highest). The box and whiskers are drawn from a large random sample of possible Senate plans. The POC CVAP percents of the currently enacted Senate districts are overlaid in red dots. Blue dots show how many of the three representatives of each district (one Senate, two House) are themselves POC identified. Note that six of the seven districts with over 1/3 POC CVAP share have at least one POC representative.

For a random sub-sample of 10,000 plans from the ensemble, we simulated an RCV election in each district in the plan. Our methods of simulating elections require several specifications: (a) a choice of model for voter ranking behavior, (b) a candidate pool, (c) a candidate strength scenario, and (d) a level of racial polarization in the electorate. In order to approximate the complexity of real-world elections, we randomize these parameters and use them in conjunction with the actual POC CVAP share of each district. By repeating these trials many times, we obtain an overview of the variability in outcomes that might reasonably be expected if the system were implemented.

Adding up the projections over the districts in a plan, we can make some bottom-line comparisons of likely representation across the electoral system design alternatives. In the next section, we provide more details of the ranked choice study design

## 2.2 Ranked Choice Voting (RCV) Models and Parameters

In our RCV study, we implement the standard single transferable vote (STV) system: if a district has magnitude  $m$  (i.e., elects  $m$  representatives), then the threshold for election is  $\frac{1}{m+1}$  first-place votes. For instance, if there are  $m = 3$  seats, then 1/4, or 25%, of the first-place votes suffices for a candidate to be immediately elected. Due to transferred votes, a candidate with 10-15% of the first-place votes (or even fewer) can easily be elected in subsequent rounds of counting if they are

frequently ranked second or third by enough voters. Since 22.72% of the state's CVAP (and 23.85% of the state's VAP) is POC, there are excellent prospects for representation in multimember districts with 3 or more seats.

Because RCV is not currently used for many elections in the Pacific Northwest, we are not able to estimate RCV outcomes using ranking data from past elections.<sup>4</sup> Instead, our analysis uses generative models of ranked choice voting behavior—that is, models that produce a set of ballots—to simulate how RCV *could* perform in various scenarios.

### 2.2.1 Ranking models

We use four different generative models to create simulated ballots which will be tabulated by ranked choice voting systems. All four models begin with three input values: the support from POC voters for POC candidates; the support from White voters for POC candidates; and the estimated POC share of the electorate. The Plackett-Luce (PL) and Bradley-Terry (BT) models rely on classical probabilistic forms of ranking, using what is called a Dirichlet distribution to allocate support to candidates within each group. The Alternating Crossover (AC) and Cambridge Sampler (CS) models are simple alternatives designed for this application. For these, we use estimated probabilities to determine whether a voter will rank a White or POC candidate first, then rely on specific assumptions on how the rest of the ballot will be completed. The AC model assumes that voters are either bloc voters or else alternate between blocs in their support. For instance, a POC voter can only be assigned a ballot of type CCCWWW, ranking all candidates of color above all White candidates, or else WCWCWC. The CS model uses ballot data from a decade's worth of ranked choice city council ballots in Cambridge, MA. Each voter's first choice is determined by classic RPV methods, and then their subsequent ballot is drawn at random from the observed ballot types in Cambridge that have a matching candidate at the top of the ballot.<sup>5</sup>

#### Models

- **Plackett-Luce:** each position is filled with a random draw;
- **Bradley-Terry:** each ballot is filled using probabilities of pairwise comparisons;
- **Alternating Crossover:** every voter either bloc-votes or alternates;
- **Cambridge Sampler:** ballots are drawn from historical ranking data in Cambridge, MA.

### 2.2.2 Election parameters

There are four more election parameters that can vary: the number of seats being elected, the makeup of the candidate pool, the existence of strong candidates, and the polarization level of the voters.

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<sup>4</sup>To date, the only known election to use RCV in the Pacific Northwest was the November 2020 County Commissioner race in Benton County, Oregon (<https://www.oregonrcv.org/rcv-in-oregon/benton-county/>).

<sup>5</sup>For more information about the models, see <https://mggg.org/STV>.

### Number of seats and candidate pool

- **1 seat:**
  - (Balanced Pool): 2 POC candidates and 2 White candidates run for office
  - (Unbalanced Pool): 1 POC candidates and 2 White candidates run for office
- **3 seats:**
  - (Balanced Pool): 3 POC candidates and 3 White candidates run for office
  - (Unbalanced Pool): 2 POC candidates and 3 White candidates run for office
- **6 seats:**
  - (Balanced Pool): 6 POC candidates and 6 White candidates run for office
  - (Unbalanced Pool): 3 POC candidates and 6 White candidates run for office
- **7 seats:**
  - (Balanced Pool): 7 POC candidates and 7 White candidates run for office
  - (Unbalanced Pool): 3 POC candidates and 7 White candidates run for office

We also consider five scenarios of how voters divide or concentrate their support, intended to capture the possibility of elections with consensus strong candidates versus instances with more “spread” in the voting patterns.

### Candidate strength scenarios

- **Scenario A: Unanimous Order.** All voters agree on strongest candidates in each group.
- **Scenario B: POC vary POC.** POC voters vary preferences among POC candidates.
- **Scenario C: All Vary Order.** No agreement on strongest candidates.
- **Scenario D: White Vary Order.** White voters don’t agree on strongest candidates.
- **Scenario E: Generic.** All levels of agreement equally likely.

As mentioned above, these RCV models require estimates for the rate at which POC and White voters support POC candidates. Typically, we would want to use local single-winner elections to estimate these levels of support. However, precise estimates (with a high degree of confidence) are not always available—especially for districts with low turnout and a small number of precincts. We consider four hypothetical levels of polarization.

### Polarization levels

- **Category 1 Polarization:** POC 95% and White 5% support for POC-preferred candidates;
- **Category 2 Polarization:** POC 90% and White 20% support for POC-preferred candidates;
- **Category 3 Polarization:** POC 75% and White 20% support for POC-preferred candidates; and

- **Category 4 Polarization:** POC 60% and White 40% support for POC-preferred candidates.

Finally, the RCV models require estimates for the proportions of POC and White voters as an input. We use CVAP to estimate these proportions. That is, we assume that the proportion of POC voters is roughly equivalent to the proportion of POC citizens of voting age in each district. This estimate makes the implicit assumption that voter turnout is comparable for White and POC voters, which may or may not reflect actual voting behaviors in Washington.

For every combination of model, number of district seats (i.e., district magnitude), candidate pool, candidate strength scenario, we use the actual district-level CVAP share to simulate 100 ranked choice elections. From the outputs, we count how many POC-preferred candidates are elected in each trial, and compute the average across elections.

### 3 Findings

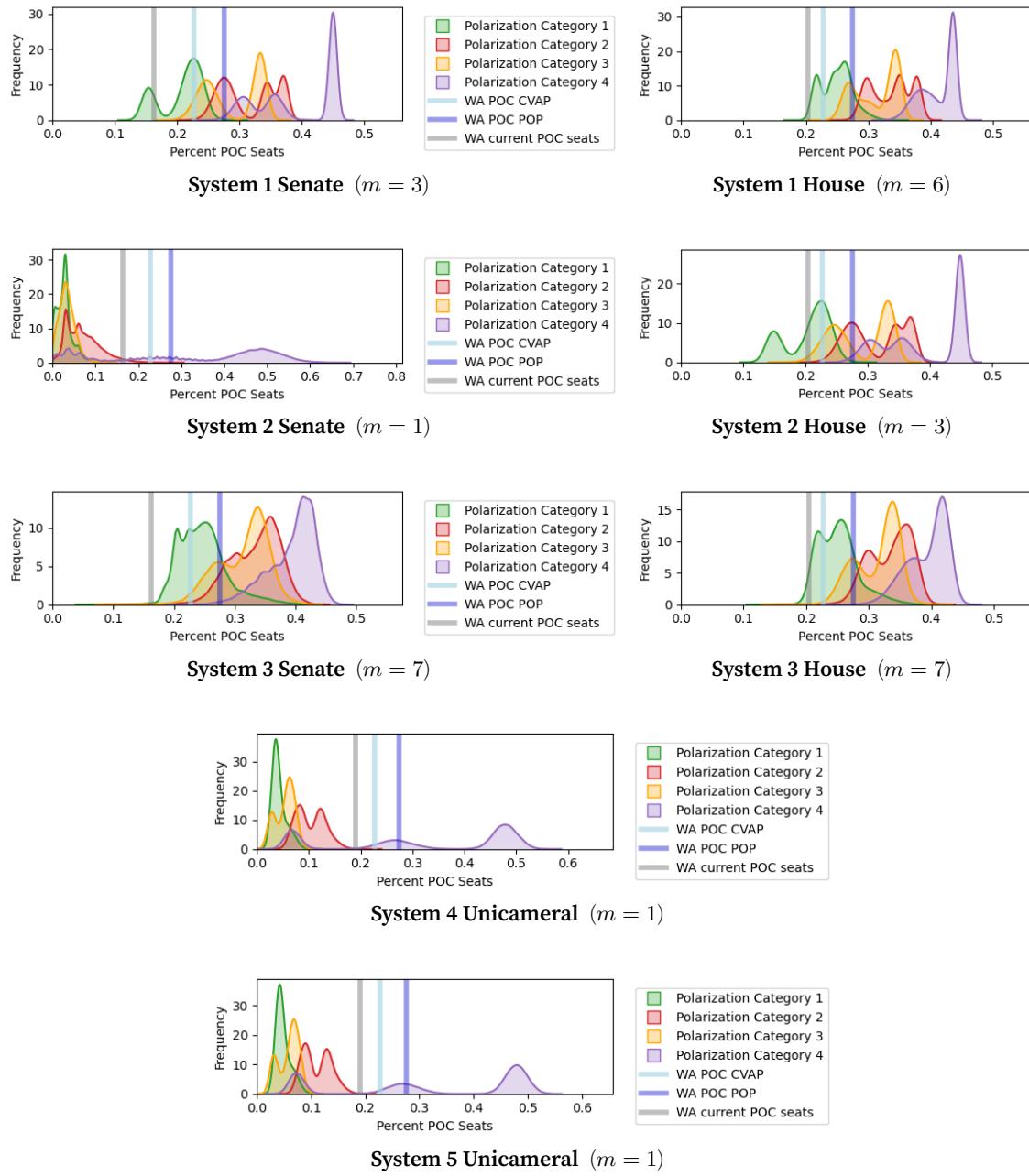
Though there is variability across models and parameters, the top-line findings are striking. Systems employing multi-member districts ( $m \geq 3$ ) are consistently projected to outperform the status quo; in fact, except at the highest level of polarization considered here (Level 1), they are projected to match or exceed proportional representation for people of color in Washington.

Results are presented in Figures 3-4 and Table 3. Figure 3 breaks down the results by racial polarization level, while Figure 4 breaks them down by the model of voter ranking behavior.

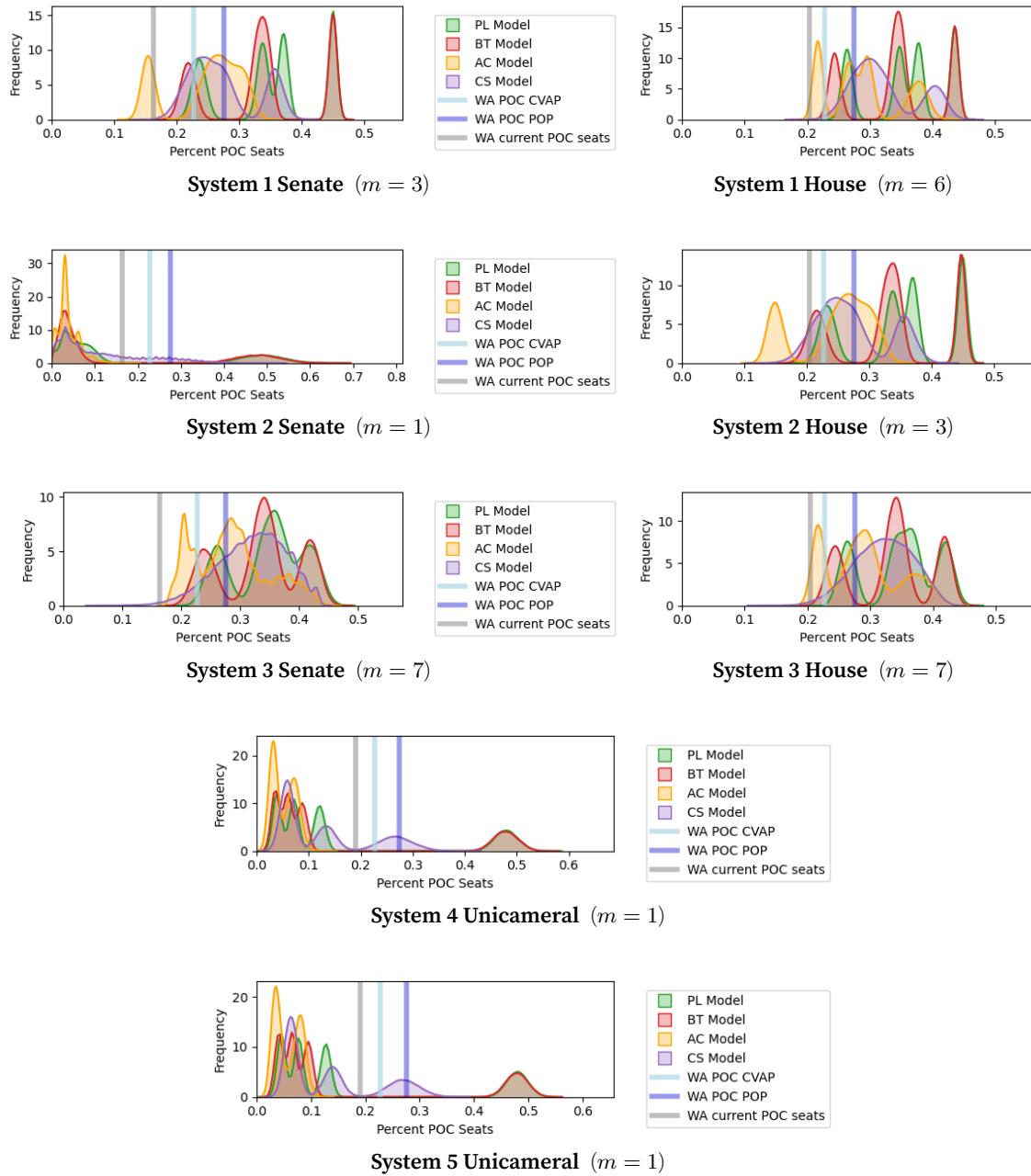
	Polarization Category	System 1 ( $m = 3, 6$ )	System 2 ( $m = 1, 3$ )	System 3 ( $m = 7, 7$ )	System 4 ( $m = 1$ )	System 5 ( $m = 1$ )
Est. POC-Preferred Senators	1	23-35 (of 147)	0-1 (of 33)	10-14 (of 49)		
	2	40-54 (of 147)	1-4 (of 33)	14-18 (of 49)		
	3	36-50 (of 147)	0-1 (of 33)	13-17 (of 49)		
	4	45-66 (of 147)	2-16 (of 33)	18-21 (of 49)		
Est. POC-Preferred Representatives	1	64-80 (of 294)	15-23 (of 99)	21-27 (of 98)		
	2	87-111 (of 294)	27-37 (of 99)	29-36 (of 98)		
	3	79-102 (of 294)	24-33 (of 99)	27-33 (of 98)		
	4	111-128 (of 294)	30-45 (of 99)	36-41 (of 98)		
Combined Legislators	1	86-112 (of 441) 20-25%	15-23 (of 132) 11-18%	31-41 (of 147) 21-28%	5-9 (of 150) 3-6%	8-13 (of 200) 4-7%
	2	127-166 (of 441) <b>29-38%</b>	28-39 (of 132) 21-30%	44-54 (of 147) <b>30-37%</b>	11-20 (of 150) 7-13%	16-28 (of 200) 8-14%
	3	115-152 (of 441) <b>26-34%</b>	24-35 (of 132) 19-26%	40-50 (of 147) <b>27-34%</b>	4-11 (of 150) 3-7%	6-15 (of 200) 3-8%
	4	156-194 (of 441) <b>25-44%</b>	23-61 (of 132) <b>24-46%</b>	54-62 (of 147) <b>37-42%</b>	10-72 (of 150) 7-48%	15-96 (of 200) 7-48%

**Table 3.** Summary of simulation outcomes across election systems. For each polarization level, each trial fixes a ranking model and averages over scenarios, candidate pools, and districting plans. The reported range shows how those averages range across the models. The blue shading marks the instances in which all four models project representation at least proportional to CVAP share. (Recall that POC population share is 27.5%, POC CVAP share is 22.7%, and the current POC share of legislators is 19%).

Results suggest that the systems where districts elect a single member—System 2 Senate, System 4 Unicameral, and System 5 Unicameral—would likely underperform for POC voters in most cases, and could only approach proportionality in the case of minimal racial polarization (Level 4). By contrast, systems with multi-member districts are consistently predicted to perform significantly better for POC voters, with outcomes approaching and even exceeding proportionality regardless of polarization category.



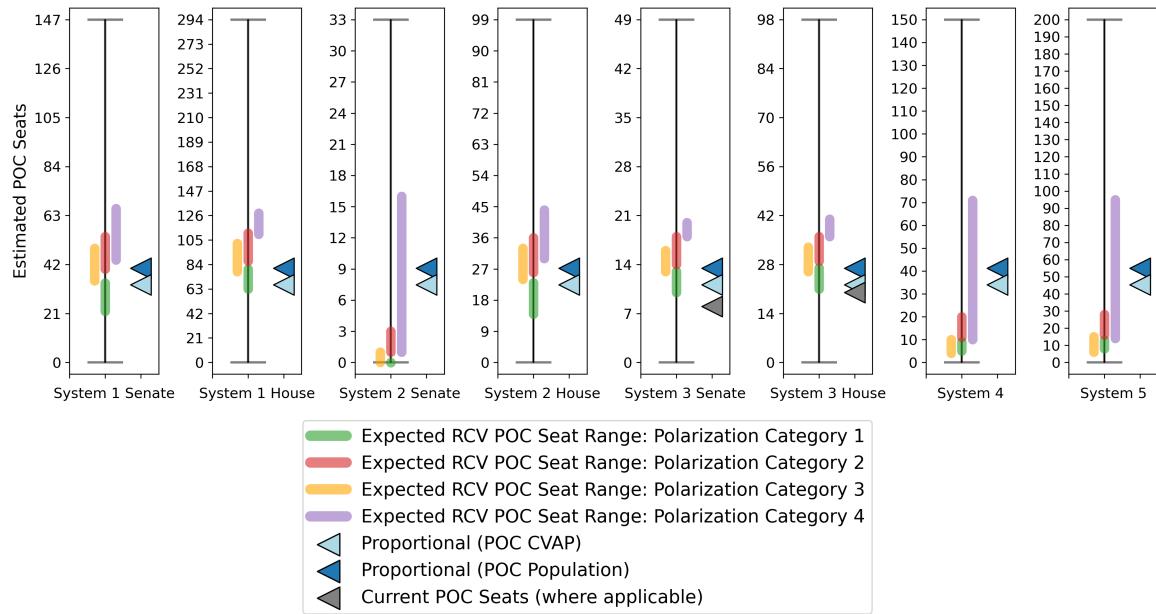
**Figure 3.** RCV simulation outcomes across polarization levels for each election system.



**Figure 4.** RCV simulation outcomes across voter ranking models for each election system.

## 4 Conclusion

In this study, we have estimated the opportunity for POC voters to elect candidates of choice under five different election systems using forms of ranked choice voting. Our results are summarized in Figure 5.



**Figure 5.** Overall election system performance summary. The multi-member instances (System 1 Senate and House, System 2 House, System 3 Senate and House) tend to outperform the status quo, and are usually projected to secure proportional representation for people of color. The single-member instances (System 2 Senate, System 4 and 5 Unicameral) are projected to be much less successful for POC representation.

Our analysis shows that the systems that employ single member districts—System 2 Senate (33 single-member districts), System 4 Unicameral (150 single-member districts), and System 5 Unicameral (200-single-member districts)—are not predicted to provide reliable electoral opportunity for POC voters. Only in the presence of extremely low levels of racially polarization could these reasonably perform near-proportionally, and even then the outcome is uncertain.

Across the board, RCV with multi-member districts projects to provide more reliable opportunity for POC voters in Washington to elect candidates of choice. In particular, System 1 (both chambers), System 2 (House), and System 3 (both chambers), under most models and scenarios considered, would secure an expectation that approaches or even exceeds proportionality.