

Discussion 14

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Problem

Key Idea 8.8.1 gives the n^{th} term of the Taylor series of common functions. In Exercises 3, verify the formula given in the Key Idea by finding the first few terms of the Taylor series of the given function and identifying a pattern.

$$f(x) = e^x; c = 0$$

```
library(pracma)

x <- function(x) exp(x)

result <- taylor(x,0,2)

result
```

```
## [1] 0.5 1.0 1.0
```

```
sum(result)
```

```
## [1] 2.5
```

Ex. 3

$$f(x) = e^x ; c = 0 \text{ (centered at 0) } \text{Maclaurin polynomial}$$

$$P_n = \left(\frac{f^n(a)(x-a)^n}{n!} \right)$$

$f^n(x)$	$f^n(a) = f^n(0)$
$f^0(x) = e^x$	$f^0(0) = e^0 = 1$
$f^1(x) = e^x$	$f^1(0) = e^0 = 1$
$f^2(x) = e^x$	$f^2(0) = e^0 = 1$

$$P_2 = \frac{f^0(0)(x-0)^0}{0!} + \frac{f^1(0)(x-0)^1}{1!} + \frac{f^2(0)(x-0)^2}{2!}$$

$$P_2 = \frac{1(x-0)^0}{0!} + \frac{1(x-0)^1}{1!} + \frac{1(x-0)^2}{2!}$$

$$P_2 = 1 + x + \frac{x^2}{2}$$

when $x=1$ — approx value e

$$1 + (1) + \frac{(1)^2}{2} \rightarrow 1 + 1 + 0.5 \rightarrow \boxed{2.5}$$

Save result
using pragma