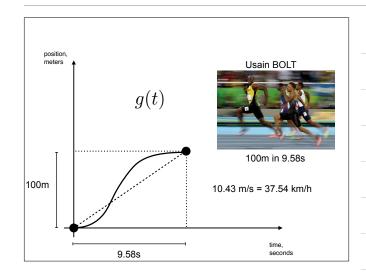
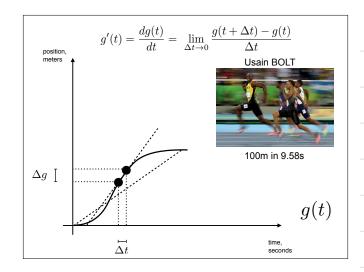
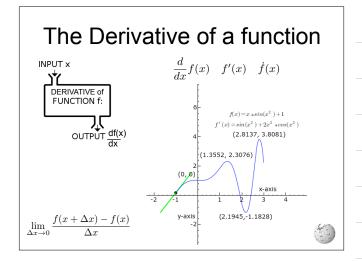
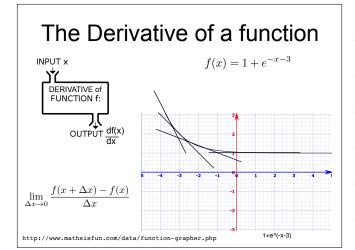
elementary math <u>refresher</u>

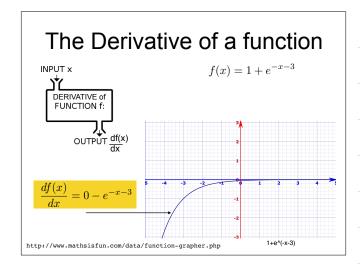
- (Mathematical) functions of one variable
- The graph of a function
- Adding or multiplying by a constant: how does the graph change?
- Straight lines, exponentials, logarithms,...
- First derivative of a function of one variable
- Definite and indefinite integrals (of a function of one variable)













$$\frac{d}{dx}a = 0$$

$$\frac{d}{dx}x = 1 \qquad \qquad \frac{d}{dx}x^n = n \ x^{n-1}$$

$$\frac{d}{dx}\ln(x) = \frac{1}{x}$$

$$\frac{d}{dx}e^x = e^x$$

$$\frac{d}{dx}sin(x) = cos(x) \qquad \frac{d}{dx}cos(x) = -sin(x)$$

$$\frac{d}{dx} \left[a f(x) \right] = a \frac{d}{dx} f(x) \qquad \qquad \text{multiplication by a constant}$$

$$\frac{d}{dx}\left[af(x)+bg(x)\right]=a\frac{d}{dx}f(x)+b\frac{d}{dx}g(x) \qquad \text{ linear combination }$$

$$\frac{d}{dx}\left[f(x)g(x)\right] = g(x)\frac{d}{dx}f(x) + f(x)\frac{d}{dx}g(x) \hspace{1cm} \text{product}$$

$$\frac{d}{dx}\left[\frac{f(x)}{g(x)}\right] = \frac{g(x)\frac{d}{dx}f(x) - f(x)\frac{d}{dx}g(x)}{g(x)^2} \qquad \qquad \text{ratio}$$

$$\frac{d}{dx}\left[f(g(x))\right] = \frac{d}{du}f(u)\frac{d}{dx}g(x)$$
 composition (chain-rule $u=g(x)$

$$\frac{d}{dx}\left[3sin(x)\right] = 3cos(x) \qquad \qquad \text{multiplication by a constant}$$

$$\frac{d}{dx}\left[sin(x) - e^x\right] = cos(x) - e^x \qquad \qquad \text{linear combination}$$

$$\frac{d}{dx}\left[x^4ln(x)\right] = 4x^3ln(x) + \frac{x^4}{x} \qquad \qquad \text{product}$$

$$\frac{d}{dx}\left[\frac{1}{x}\right] = -\frac{1}{x^2} \qquad \qquad \text{ratio}$$

$$\frac{d}{dx}\left[e^{-x/a}\right] = -\frac{e^{-x/a}}{a} \qquad \qquad \text{composition (chain-rule)}$$

Indefinite Integrals (inverse operation of the derivatives)

$$g(t) \to \frac{d}{dt}g(t)$$

$$\int f(x)dx = F(x) + constant$$

$$\frac{d}{dx}(F(x) + constant) = f(x)$$

Integrals of elementary functions

$$\int a \, dx = a \, x + constant$$

$$\int x \, dx = \frac{1}{2} x^2 + constant \qquad \int x^n \, dx = \frac{1}{n+1} x^{n+1} + constant$$

$$\int \frac{1}{x} \, dx = \ln(x) + constant$$

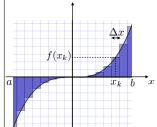
$$\int e^{a \, x} \, dx = \frac{1}{a} e^{a \, x} + constant$$

$$\int cos(x) \, dx = sin(x) + constant$$

$$\int sin(x) \, dx = -cos(x) + constant$$

Definite Integrals

(fundamental theorem of integral calculus)



$$A = f(a)\Delta x + \dots$$

$$+f(x_k)\Delta x + f(x_{k+1})\Delta x +$$

$$+f(x_{k+2})\Delta x + f(x_{k+3})\Delta x + \dots$$

$$\dots + f(b)\Delta x$$

$$A = \sum_{k=1}^{N} f(x_k) \Delta x$$

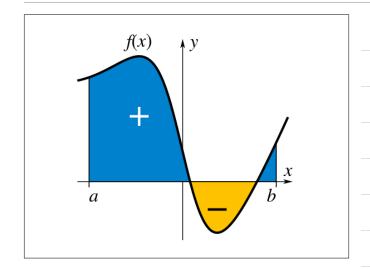
$$A = \sum_{k=0}^{N} f(x_k) \Delta x \to \int_a^b f(x) dx$$

$$\int_a^b f(x) dx = F(b) - F(a)$$

$$\int_a^b \frac{d}{dx} F(x) dx = F(b) - F(a)$$

$$\int_a^b f(x) dx = F(x) + constant$$

$$\frac{d}{dx} (F(x) + constant) = f(x)$$











- https://www.khanacademy.org/math/algebra-home/alg-functions
- https://www.mathsisfun.com/calculus/introduction.html
- http://www-math.mit.edu/~djk/calculus_beginners/
- https://www.khanacademy.org/math/calculus-home