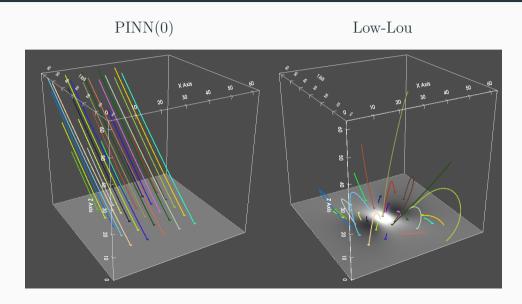
# Reconstruction of Coronal Magnetic Fields using Physics-Informed Neural Networks

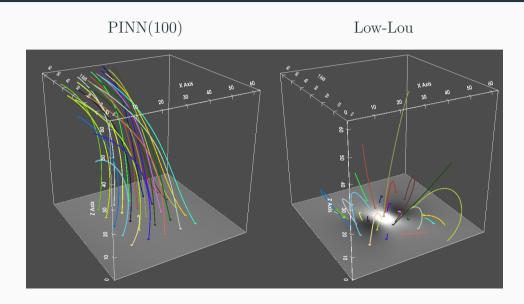
전민규

학사졸업논문

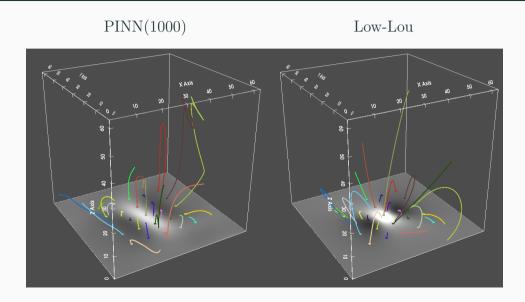
The 3D magnetic fields



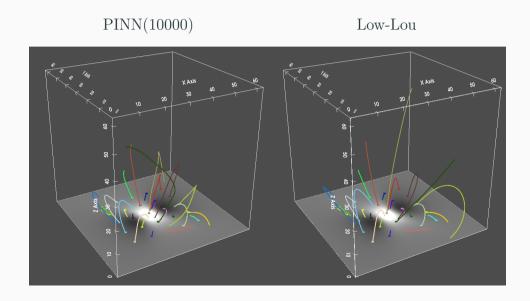
The 3D magnetic fields



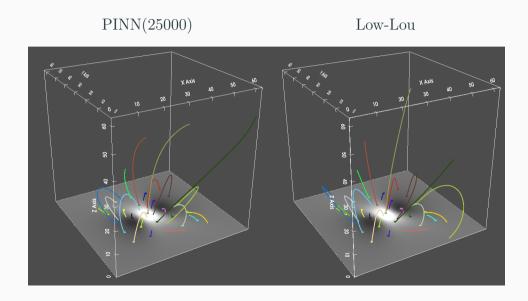
The 3D magnetic fields



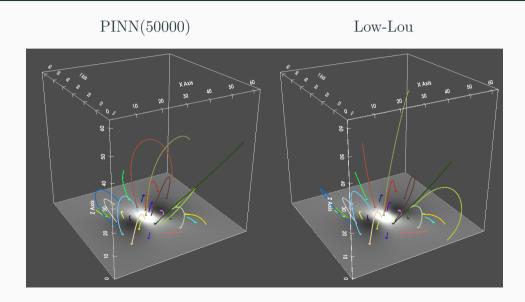
The 3D magnetic fields



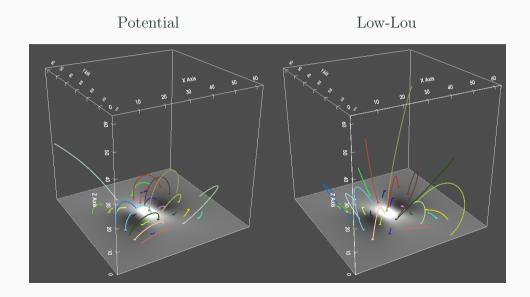
The 3D magnetic fields



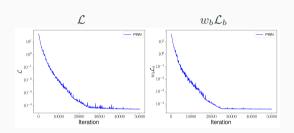
The 3D magnetic fields



The 3D magnetic fields



#### Loss



$$w_{\rm ff} \mathcal{L}_{\rm ff} \qquad w_{\rm div} \mathcal{L}_{\rm div}$$

$$\hat{\mathbf{B}} = \mathcal{N}(\boldsymbol{x}; \boldsymbol{\theta})$$

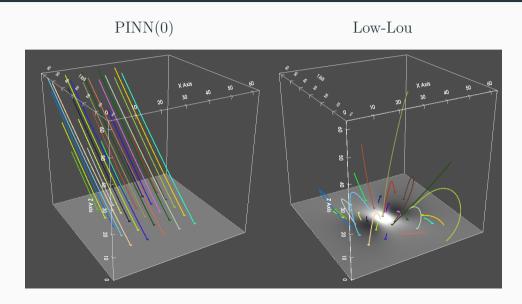
$$\mathcal{L}_{\mathrm{ff}}(\boldsymbol{\theta}; \mathcal{T}_f) = \frac{1}{|\mathcal{T}_f|} \sum_{\boldsymbol{x} \in \mathcal{T}_f} \frac{|(\nabla \times \hat{\mathbf{B}}) \times \hat{\mathbf{B}}|^2}{|\hat{\mathbf{B}}|^2}$$

$$\mathcal{L}_{\text{div}}(\boldsymbol{\theta}; \mathcal{T}_f) = \frac{1}{|\mathcal{T}_f|} \sum_{\boldsymbol{x} \in \mathcal{T}_f} |\nabla \cdot \hat{\mathbf{B}}|^2$$

$$\mathcal{L}_b(oldsymbol{ heta}; \mathcal{T}_b) = rac{1}{|\mathcal{T}_b|} \sum_{oldsymbol{x} \in \mathcal{T}_b} |\hat{\mathbf{B}} - \mathbf{B}|^2$$

$$\mathcal{L}_f = w_{\rm ff} \mathcal{L}_{\rm ff} + w_{\rm div} \mathcal{L}_{\rm div} + w_b \mathcal{L}_b$$

The 3D magnetic fields



## Figures of merit (Schrijver et al. 2006)

$$C_{\text{vec}} = \frac{\sum_{i} \mathbf{B}_{i} \cdot \mathbf{b}_{i}}{(\sum_{i} |\mathbf{B}_{i}|^{2} \sum_{i} |\mathbf{b}_{i}|^{2})^{1/2}}$$

$$C_{\text{CS}} = \frac{1}{M} \sum_{i} \frac{\mathbf{B}_{i} \cdot \mathbf{b}_{i}}{|\mathbf{B}_{i}||\mathbf{b}_{i}|}$$

$$\epsilon = \frac{\sum_{i} |\mathbf{B}_{i}|^{2}}{\sum_{i} |\mathbf{b}_{i}|^{2}}$$

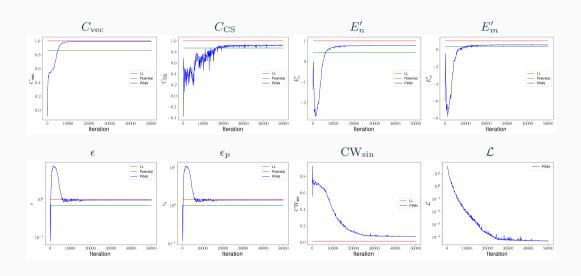
$$\epsilon_{p} = \frac{\sum_{i} |\mathbf{B}_{i}|^{2}}{\sum_{i} |\mathbf{B}_{i}|^{2}}$$

$$E'_{m} = 1 - \frac{1}{M} \frac{\sum_{i} |\mathbf{B}_{i} - \mathbf{b}_{i}|}{\sum_{i} |\mathbf{b}_{i}|}$$

$$CW_{\text{sin}} = \frac{\sum_{i} \frac{|\mathbf{J}_{i} \times \mathbf{B}_{i}|}{|\mathbf{B}_{i}|}}{\sum_{i} |\mathbf{J}_{i}|}$$

Here, *i* refers to each grid point, M is the total number of grid points,  $\mathbf{B}$  is the numerical magnetic field,  $\mathbf{b}$  is the reference magnetic field,  $\mathbf{B}_{\mathrm{p}}$  is the potential magnetic field whose lower boundary condition is the same as that of  $\mathbf{B}$ , and  $\mathbf{J} = \nabla \times \mathbf{B}$  is the current density in an appropriate unit system.

## Figures of merit + Loss



## Figures of merit + Loss

Field	$C_{\mathrm{vec}}$	$C_{\mathrm{CS}}$	$E'_n$	$E'_m$	$\epsilon$	$\epsilon_p$	$\mathrm{CW}_{\mathrm{sin}}$	$\mathcal{L}^{\mathrm{a}}$
Low-Lou <sup>b</sup>	1.00000	1.00000	1.00000	1.00000	1.00000	1.44490	$0.01308^{c}$	_
Potential	0.86465	0.86925	0.43003	0.36242	0.69209	1.00000	_d	_
PINN(0)	0.07115	0.33540	-1.37088	-6.07067	0.71824	1.03779	0.55813	40.23570
PINN(100)	0.25771	0.46100	-0.00643	-0.46701	0.08056	0.11640	0.76066	31.32017
PINN(1000)	0.54244	0.32404	-2.31914	-6.41640	5.59377	8.08246	0.71701	6.46577
PINN(10000)	0.98630	0.63065	0.68766	0.28275	0.96939	1.40068	0.38403	0.00848
PINN(25000)	0.99402	0.92134	0.78452	0.55897	0.96481	1.39406	0.07853	0.00006
PINN(50000)	0.99359	0.92271	0.77129	0.50928	0.96247	1.39068	0.06848	0.00005

<sup>&</sup>lt;sup>a</sup>The total loss of PINN.

<sup>&</sup>lt;sup>b</sup>The parameters of the Low-Lou model are  $(n=1, m=1, l=0.3, \Phi=\pi/2)$ .

<sup>&</sup>lt;sup>c</sup>This is not zero due to numerical grids.

<sup>&</sup>lt;sup>d</sup>The metric CW<sub>sin</sub> is undefined for the potential field.