

Logistics Engineering Design Constants

1. Circuitry Factor: **1.2** (g)
 - $1.2 \times \text{GC distance} \approx \text{actual road distance}$
2. Local vs. Intercity Transport:
 - Local: $< 50 \text{ mi}$ \Rightarrow use actual road distances
 - Intercity: $> 50 \text{ mi}$ \Rightarrow can estimate road distances
 - $50\text{-}250 \text{ mi}$ \Rightarrow return possible (11 HOS)
 - $> 250 \text{ mi}$ \Rightarrow always one-way transport
 - $> 500\text{-}750 \text{ mi}$ \Rightarrow intermodal rail possible
3. Inventory Carrying Cost (h) = funds + storage + obsolescence
 - **16%** average (no product information, per U.S. Total Logistics Costs)
 - $(16\% \approx 5\% \text{ funds} + 6\% \text{ storage} + 5\% \text{ obsolescence})$
 - 5-10% low-value product (construction)
 - 25-30% general durable manufactured goods
 - 50% computer equipment
 - $>> 100\%$ perishable goods (produce)

Logistics Engineering Design Constants

4. $\frac{\text{Value}}{\text{Transport Cost}} \gg 1: \text{\$1 ft}^3 \approx \frac{\$2,620 \text{ Shanghai-LA/LB shipping cost}}{2,400 \text{ ft}^3 \text{ 40' ISO container capacity}}$

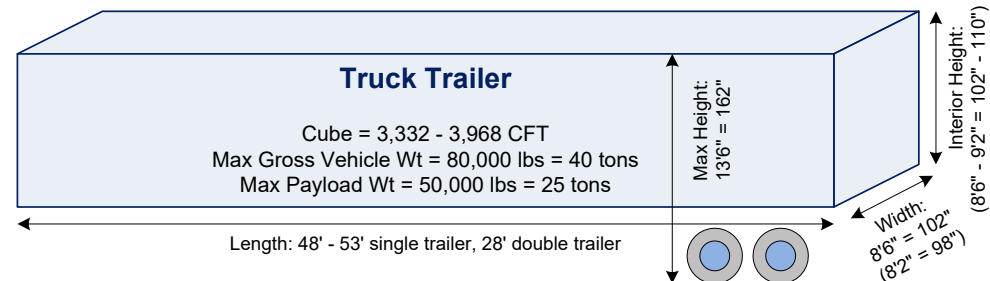
5. TL Weight Capacity: **25 tons** (K_{wt})

- (40 ton max per regulation) –
(15 ton tare for tractor-trailer)
= 25 ton max payload
- Weight capacity = 100% of physical capacity



6. TL Cube Capacity: **2,750 ft³** (K_{cu})

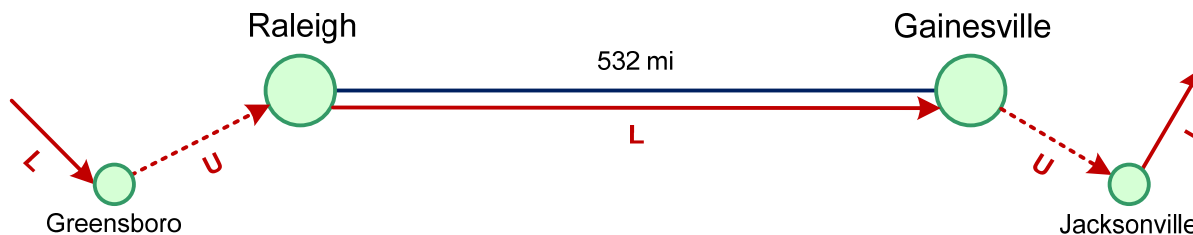
- Trailer physical capacity = 3,332 ft³
- Effective capacity =
 $3,332 \times 0.80 \approx 2,750 \text{ ft}^3$
- Cube capacity = 80% of
physical capacity



Logistics Engineering Design Constants

7. TL Revenue per Loaded Truck-Mile: **\$2/mi** in 2004 (r)

- TL revenue for the carrier is your TL cost as a shipper



15%, average deadhead travel

\$1.60, cost per mile in 2004

$$\frac{\$1.60}{1 - 0.15} = \$1.88, \text{ cost per loaded-mile}$$

6.35%, average operating margin for trucking

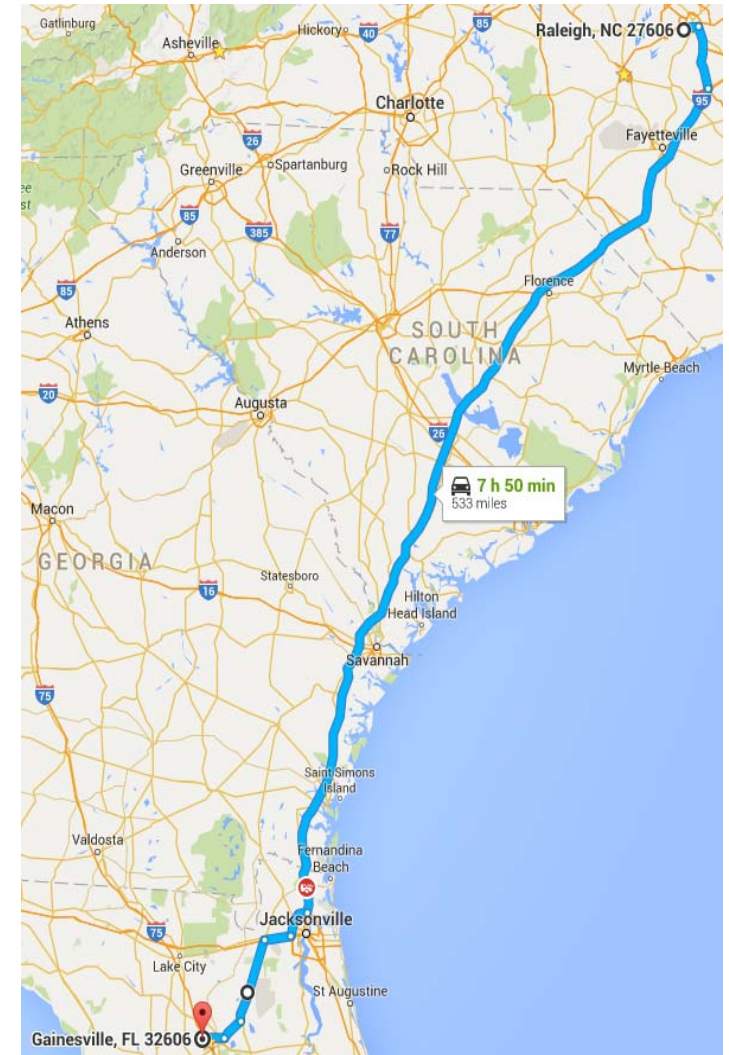
$$\frac{\$1.88}{1 - 0.0635} \approx \$2.00, \text{ revenue per loaded-mile}$$

One-Time vs Periodic Shipments

- **One-Time Shipments** (*operational* decision): know shipment size q
 - Know when and how much to ship, need to determine if TL and/or LTL to be used
 - Must contact carrier or have agreement to know charge
 - Can/should estimate charge before contacting carrier
- **Periodic Shipments** (*tactical* decision): know demand rate f , must determine size q
 - Need to determine how often and how much to ship
 - Analytical transport charge formula allow “optimal” size (and shipment frequency) to be estimated
 - U.S. Bureau of Labor Statistic's *Producer Price Index* (PPI) for TL and LTL used to estimate transport charges

Truck Shipment Example

- Product shipped in cartons from Raleigh, NC (27606) to Gainesville, FL (32606)
- Each identical unit weighs 40 lb and occupies 9 ft³ (its *cube*)
 - Don't know linear dimensions of each unit
- Units can be stacked on top of each other in a trailer
- Additional info/data is presented only when it is needed to determine answer



Truck Shipment Example: One-Time

1. Assuming that the product is to be shipped P2P TL, what is the maximum payload for each trailer used for the shipment?

$$q_{\max}^{wt} = K_{wt} = 25 \text{ ton}$$

$$K_{cu} = 2750 \text{ ft}^3$$

$$s = \frac{40 \text{ lb/unit}}{9 \text{ ft}^3/\text{unit}} = 4.4444 \text{ lb/ft}^3$$

$$K_{cu} = \frac{q_{\max}^{cu}}{\left(\frac{s}{2000}\right)} \Rightarrow q_{\max}^{cu} = \frac{s K_{cu}}{2000}$$

$$\begin{aligned} q_{\max} &= \min \left\{ q_{\max}^{wt}, q_{\max}^{cu} \right\} = \min \left\{ K_{wt}, \frac{s K_{cu}}{2000} \right\} \\ &= \min \left\{ 25, \frac{4.4444(2750)}{2000} \right\} = 6.1111 \text{ ton} \end{aligned}$$

Truck Shipment Example: One-Time

2. On Jan 10, 2018, 350 units of the product were shipped.
How many truckloads were required for this shipment?

$$q = 350 \frac{40}{2000} = 7 \text{ ton}, \quad \left\lceil \frac{q}{q_{\max}} \right\rceil = \left\lceil \frac{7}{6.1111} \right\rceil = 2 \text{ truckloads}$$

3. Before contacting the carrier (and using Jan 2018 PPI), what is the estimated TL transport charge for this shipment?



$$d = 532 \text{ mi}$$

$$r = \frac{PPI_{TL}^{\text{Jan 2018}}}{PPI_{TL}^{2004}} \times r_{2004} = \frac{PPI_{TL}}{102.7} \times \$2.00 / \text{mi}$$

$$= \frac{131.0}{102.7} \times \$2.00 / \text{mi} = \$2.5511 / \text{mi}$$

$$c_{TL} = \left\lceil \frac{q}{q_{\max}} \right\rceil r d = \left\lceil \frac{7}{6.1111} \right\rceil (2.5511)(532) = \$2,714.39$$

Truck Shipment Example: One-Time

 UNITED STATES DEPARTMENT OF LABOR
 BUREAU OF LABOR STATISTICS

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Databases, Tables & Calculators by Subject

Change Output Options: From: 2008 ▾ To: 2018 ▾
☐ include graphs ☐ include annual averages

Data extracted on: September 5, 2018 (4:22:19 PM)

PPI Industry Data

Series Id: PCU484121484121
Series Title: PPI industry data for General freight trucking, long-distance TL, not seasonally adjusted
Industry: General freight trucking, long-distance TL
Product: General freight trucking, long-distance TL
Base Date: 200312

Download:  [xlsx](#)

Year	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
2008	116.0	115.9	116.5	117.8	120.5	123.0	124.0	124.0	121.8	121.3	117.8	115.1
2009	113.2	112.1	110.4	109.7	109.8	110.1	111.4	111.0	111.7	110.8	111.5	110.9
2010	110.8	111.0	111.9	112.2	113.2	113.5	113.4	113.7	113.8	114.4	115.8	116.1
2011	116.5	117.4	119.3	121.0	121.7	121.4	121.3	121.2	122.0	122.0	123.2	123.3
2012	124.0	124.6	126.2	126.7	127.0	125.8	125.6	126.8	127.4	127.2	126.9	127.0
2013	126.7	127.2	128.0	127.5	127.8	127.6	127.6	127.6	127.1	127.2	127.6	127.4
2014	127.9	128.2	128.7	129.5	130.6	130.8	130.3	130.4	130.4	129.7	129.8	128.9
2015	126.7	126.0	126.0	126.2	126.3	127.1	126.9	126.2	125.9	125.5	125.8	124.8
2016	124.6	123.4	123.2	123.6	122.8	122.7	123.0	123.0	123.3	124.1	124.1	124.2
2017	124.4	124.7	124.2	124.3	124.0	124.2	124.2	125.9	126.6	126.6	128.5	130.3
2018	131.0	132.0	132.0	132.6(P)	133.6(P)	135.9(P)	138.6(P)					

P : Preliminary. All indexes are subject to revision four months after original publication.

Truck Shipment Example: One-Time

4. Using the Jan 2018 PPI LTL rate estimate, what was the transport charge to ship the fractional portion of the shipment LTL (i.e., the last partially full truckload portion)?

$$q_{\text{frac}} = q - q_{\text{max}} = 7 - 6.1111 = 0.8889 \text{ ton}$$

$$r_{LTL} = PPI_{LTL} \left[\frac{\frac{s^2}{8} + 14}{\left(q_{\text{frac}}^{\frac{1}{7}} d^{\frac{15}{29}} - \frac{7}{2} \right) (s^2 + 2s + 14)} \right]$$

$$= 177.4 \left[\frac{\frac{4.49^2}{8} + 14}{\left(0.8889^{\frac{1}{7}} 532^{\frac{15}{29}} - \frac{7}{2} \right) (4.49^2 + 2(4.49) + 14)} \right] = \$3.1469 / \text{ton-mi}$$

$$c_{LTL} = r_{LTL} q_{\text{frac}} d = 3.1469(0.8889)(532) = \$1,488.13$$

Truck Shipment Example: One-Time

5. What is the change in total charge associated with the combining TL and LTL as compared to just using TL?

$$\begin{aligned}\Delta C &= c_{TL} - (c_{TL-1} + c_{LTL}) \\ &= \left\lceil \frac{q}{q_{\max}} \right\rceil r d - \left(\left\lfloor \frac{q}{q_{\max}} \right\rfloor r d + r_{LTL} q_{\text{frac}} d \right) \\ &= -\$130.93\end{aligned}$$

Truck Shipment Example: One-Time

6. What would the fractional portion have to be so that the TL and LTL charges are equal?

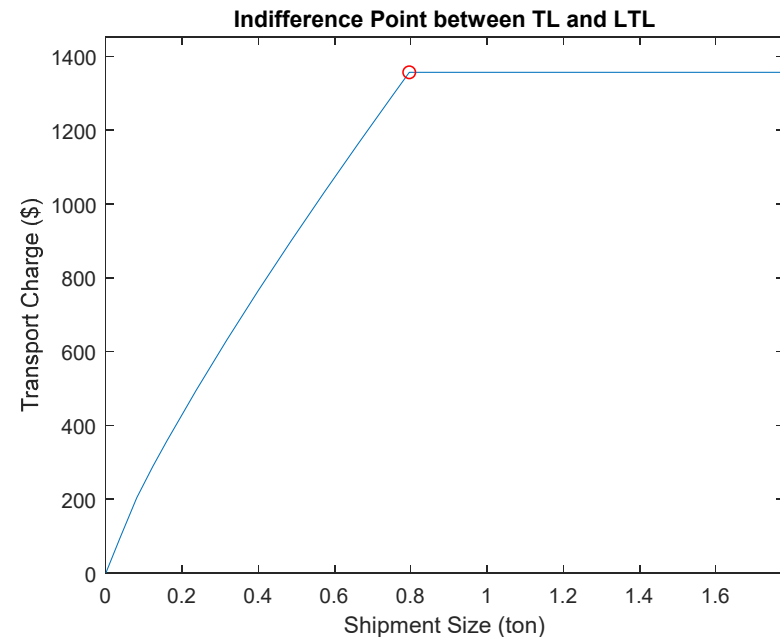
$$c_{TL}(q) = \left\lceil \frac{q}{q_{\max}} \right\rceil r d$$

$$r_{LTL}(q) = PPI_{LTL} \left[\frac{\frac{s^2}{8} + 14}{\left(q^{\frac{1}{7}} d^{\frac{15}{29}} - \frac{7}{2} \right) (s^2 + 2s + 14)} \right]$$

$$c_{LTL}(q) = r_{LTL}(q) q d$$

$$q_I = \arg \min_q (\|c_{TL}(q) - c_{LTL}(q)\|)$$

$$= 0.7960 \text{ ton}$$

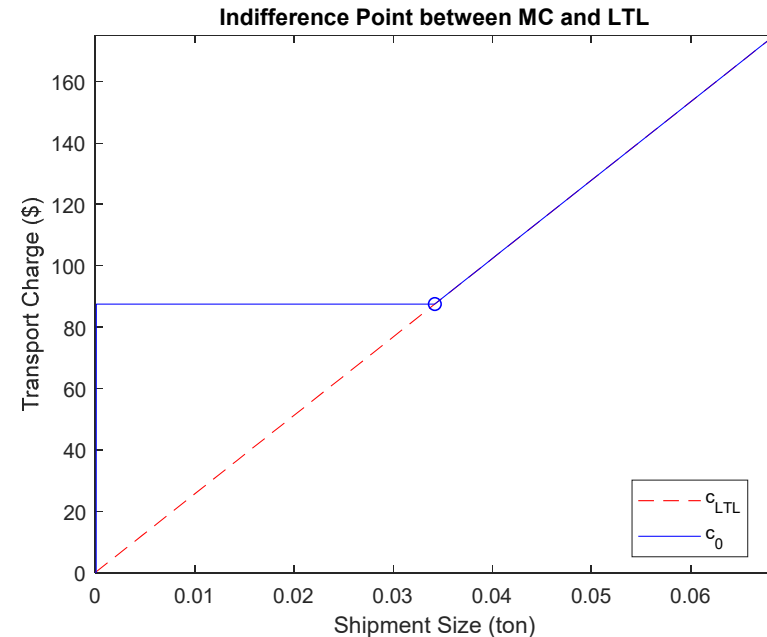


Truck Shipment Example: One-Time

7. What are the TL and LTL minimum charges?

$$MC_{TL} = \left(\frac{r}{2} \right) 45 = \$57.40$$

$$\begin{aligned} MC_{LTL} &= \left(\frac{PPI_{LTL}}{104.2} \right) \left(45 + \frac{d^{\frac{28}{19}}}{1625} \right) \\ &= \left(\frac{177.4}{104.2} \right) \left(45 + \frac{532^{\frac{28}{19}}}{1625} \right) = \$87.51 \end{aligned}$$



- Why do these charges not depend on the size of the shipment?
- Why does only the LTL minimum charge depend of the distance of the shipment?

Truck Shipment Example: One-Time

- Independent Transport Charge (\$):

$$c_0(q) = \min \left\{ \max \{ c_{TL}(q), MC_{TL} \}, \max \{ c_{LTL}(q), MC_{LTL} \} \right\}$$



Truck Shipment Example: One-Time

8. Using the same LTL shipment, find online one-time (spot) LTL rate quotes using the FedEx LTL website

$$q_{\text{frac}} = 0.8889 \text{ ton}$$

$$= 0.8889(2000) = 1778 \text{ lb}$$

- Most likely freight class:

$$s = \frac{40 \text{ lb/unit}}{9 \text{ ft}^3/\text{unit}}$$

$$= 4.4444 \text{ lb/ft}^3$$

$$\Rightarrow \text{Class 200}$$

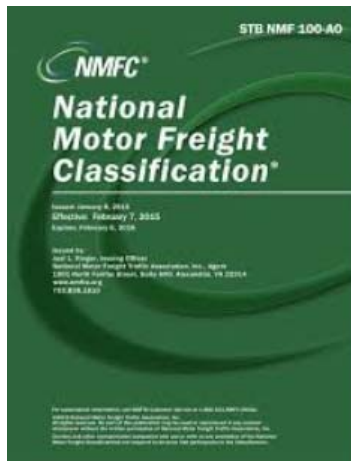
- What is the rate quote for the reverse trip from Gainesville (32606) to Raleigh (27606)?

Class-Density Relationship

Class	Load Density (lb/ft ³)		Max Physical Weight (tons)	Max Effective Cube (ft ³)
	Minimum	Average		
500	—	0.52	0.72	2,750
400	1	1.49	2.06	2,750
300	2	2.49	3.43	2,750
250	3	3.49	4.80	2,750
200	4	4.49	6.17	2,750
175	5	5.49	7.55	2,750
150	6	6.49	8.92	2,750
125	7	7.49	10.30	2,750
110	8	8.49	11.67	2,750
100	9	9.72	13.37	2,750
92.5	10.5	11.22	15.43	2,750
85	12	12.72	17.49	2,750
77.5	13.5	14.22	19.55	2,750
70	15	18.01	24.76	2,750
65	22.5	25.50	25	1,961
60	30	32.16	25	1,555
55	35	39.68	25	1,260
50	50	56.18	25	890

Truck Shipment Example: One-Time

- The *National Motor Freight Classification* (NMFC) can be used to determine the product class
- Based on:
 1. Load density
 2. Special handling
 3. Stowability
 4. Liability



Item	Description	Class	NMFC	Sub
Abietic Acid	Abietic Acid, in drums	55	42605	-
Accordions	Accordions, in boxes	125	138820	-
Acetonitrile	Acetonitrile, in boxes or drums. See item 60000 for class dependent upon released value	85	42645	-
Acetylene	in steel cylinders	70	85520	-
Acid Fish Scrap	Fish Scrap, NOI, dry, not ground, pulverized nor screened, or Acid Fish Scrap, in bags	77.5	69980	-
Aircraft Parts	metal, struts, skins, panels	200	11790	01
Aluminum Channel	U channel	60	13340	-
Aluminum Table Set	aluminum table SU	200	82105	01
Ambulance Stretcher	stretcher	200	56920	06
Arches Support	Iron Steel	60	52460	-
Architectural Details	6 - 8 lbs per cubic foot	125	56290	05
Architectural Details	2 - 4 lbs per cubic ft	250	56290	03
Assembled Furniture	Bathroom cabinet set up	300	39220	01
Assembled Furniture	Highboys, dressers, wooden set up	125	80120	01
Assembled Furniture	Wood furniture 4-6 Lbs per cu ft	150	82270	04
Assembled Furniture	Chairs wooden setup w/out upholstery	300	80770	01
Assembled Furniture	Chairs wooden setup w/out upholstery KD	125	80770	03
Assembled Furniture	Couch w/ back & arms put together	175	80865	03
Assembled Furniture	Chairs put together w/ upholstery	200	79255	01
Assembled Furniture	Metal cabinets in boxes	110	39270	06
Assembled Furniture	18 gauge steel cabinet	70	39340	-
Assembled Furniture	Benches, cabinets, tables for workstations	125	23410	-
Assembled Furniture	Buffets, china cabinets put together	125	80080	-
Assembled Furniture	Cabinets of metal or plastic for storage	92.5	39235	-
Assembled Furniture	Tanning bed	150	109050	-
Assembled Furniture	Mattresses, in packages or boxes	200	79550	-
Athletic / Sporting Goods	Gym equipment, playground, sports items. Density Item			
Attachments: Backhoe	NOI: Attachments, backhoe (Backhoes), tractor or truck, on lift truck skids or pallets:	175	114217	01
Attachments: Backhoe	Attachments, backhoe (Backhoes), tractor or truck, on lift truck skids or pallets: Each shipped with all components secured to a single pallet, platform or skid, weighing 1100 pounds or more and having a density of 8 pounds or greater per cubic foot	100	114217	02

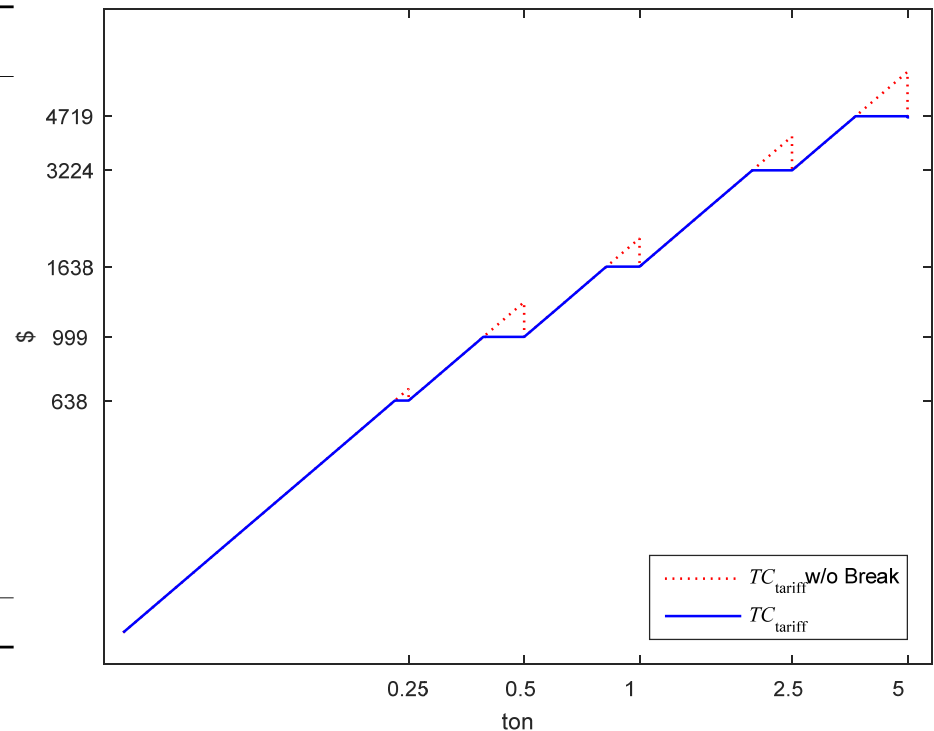
Truck Shipment Example: One-Time

- CzarLite tariff table for O-D pair 27606-32606

$$cwt = \text{hundredweight} = 100 \text{ lb} = \frac{100}{2000} = \frac{1}{20} \text{ ton}$$

**Tariff (in \$/cwt) from Raleigh, NC (27606) to Gainesville, FL (32606)
(532 mi, CzarLite DEMOCZ02 04-01-2000, minimum charge = \$95.23)**

Freight Class	Rate Breaks (<i>i</i>)								
	1	2	3	4	5	6	7	8	9&10
500	341.42	314.14	245.80	201.48	158.60	112.37	55.66	55.66	55.66
400	273.88	251.99	197.19	161.61	127.22	91.12	45.10	45.10	45.10
300	206.34	189.85	148.56	121.76	95.85	69.47	34.43	34.43	34.43
250	172.56	158.77	124.23	101.83	80.15	58.03	28.79	28.79	28.79
200	138.78	127.69	99.92	81.89	64.47	47.19	23.40	23.40	23.40
175	121.37	111.68	87.39	71.62	56.38	41.27	20.39	20.39	20.39
150	104.49	96.13	75.22	61.66	48.53	35.96	17.75	17.75	17.75
125	87.59	80.60	63.07	51.69	40.69	30.24	15.00	15.00	15.00
110	77.57	71.37	55.85	45.77	36.04	28.61	14.40	14.40	14.40
100	71.23	65.55	51.29	42.04	33.09	27.58	14.03	10.80	9.90
92	66.48	61.18	47.88	39.24	30.89	25.75	13.68	10.52	9.66
85	61.74	56.80	44.45	36.43	28.68	23.91	13.20	10.15	9.32
77	56.99	52.44	41.04	33.63	26.48	22.07	12.60	9.68	8.89
70	52.77	48.55	37.99	31.14	24.51	20.43	12.00	9.23	8.47
65	50.07	46.08	36.05	29.56	23.04	19.39	11.87	9.14	8.39
60	47.44	43.64	34.15	28.00	21.82	18.37	11.76	9.04	8.30
55	44.75	41.17	32.22	26.40	20.59	17.32	11.64	8.96	8.22
50	41.57	38.26	29.94	24.54	19.12	16.10	11.52	8.85	8.14
Tons (q_i^B)	0.25	0.5	1	2.5	5	10	15	20	∞



Truck Shipment Example: One-Time

9. Using the same LTL shipment, what is the transport cost found using the undiscounted CzarLite tariff?

$$q = 0.8889, \quad \text{class} = 200$$

$$\text{disc} = 0, \quad MC = 95.23$$

$$i = \arg \left\{ q_i^B \mid q_{i-1}^B \leq q < q_i^B \right\}$$

$$= \arg \left\{ q_3^B \mid q_2^B \leq q < q_3^B \right\}$$

$$= \arg \left\{ q_3^B \mid 0.5 \leq 0.8889 < 1 \right\} = 3$$

$$c_{\text{tariff}} = (1 - \text{disc}) \max \left\{ MC, \min \left\{ OD(\text{class}, i) 20q, OD(\text{class}, i + 1) 20q_i^B \right\} \right\}$$

$$= (1 - 0) \max \left\{ 95.23, \min \left\{ OD(200, 3) 20(0.8889), OD(200, 4) 20(1) \right\} \right\}$$

$$= \max \left\{ 95.23, \min \left\{ (99.92) 20(0.8889), (81.89) 20(1) \right\} \right\}$$

$$= \max \left\{ 95.23, \min \left\{ 1, 776.23, 1, 637.80 \right\} \right\} = \$1,637.80$$

Freight Class	Rate Breaks (<i>i</i>)								
	1	2	3	4	5	6	7	8	9&10
500	341.42	314.14	245.80	201.48	158.60	112.37	55.66	55.66	55.66
400	273.88	251.99	197.19	161.61	127.22	91.12	45.10	45.10	45.10
300	206.34	189.85	148.56	121.76	95.85	69.47	34.43	34.43	34.43
250	172.56	158.77	124.23	101.83	80.15	58.03	28.79	28.79	28.79
200	138.78	127.69	99.92	81.89	64.47	47.19	23.40	23.40	23.40
175	121.37	111.68	87.39	71.62	56.38	41.27	20.39	20.39	20.39
50	41.57	38.26	29.94	24.54	19.12	16.10	11.52	8.85	8.14
Tons (q_i^B)	0.25	0.5	1	2.5	5	10	15	20	∞

Truck Shipment Example: One-Time

10. What is the implied discount of the estimated charge from the CzarLite tariff cost?

$$\begin{aligned} disc &= \frac{C_{\text{tariff}} - C_{LTL}}{C_{\text{tariff}}} \\ &= \frac{1,637.80 - 1,488.13}{1,637.80} \\ &= 9.14\% \end{aligned}$$

- What is the weight break between the rate breaks?

$$\begin{aligned} q_i^W &= \frac{OD(class, i+1)}{OD(class, i)} q_i^B \\ &= \frac{81.89}{99.92} (1) = 0.8196 \text{ ton} \end{aligned}$$

