

Kernel: SageMath 9.7

In [1]:

```
#Definir variables
n = var('n')
x = var('x')
```

In [4]:

```
#Ejercicio 1
f(n)=(n^3 + 2*n -1)/(5*n^3 + n**2 -2*n +1)
limit(f(n), n = infinity)
```

Out[4]: $1/5$

In [5]:

```
#Ejercicio 2
reset("f")
f(n)=(sqrt(n**2 - n)- sqrt(n**2 + 4*n))
limit(f(n), n= infinity)
```

Out[5]: $-5/2$

In [7]:

```
#Ejercicio 3
reset("f")
f(n)=(ln(1+n+sqrt(n)) - ln(n))
limit(f(n), n = oo)
```

Out[7]: 0

In [21]:

```
#Ejercicio 4
reset("f")
f(n)=n**3
sum(f(n), n, 0, 1000000)
limit(f(n)/n**4, n = infinity)
```

Out[21]: 0

In [10]:

```
#Ejercicio 5
reset("f")
f(n)=((n**3 - 2*n)/(n**3 + 3*n^2 - 2*n -1))**n
limit(f(n), n = oo)
```

Out[10]: $e^{(-3)}$

In [11]:

```
#Ejercicio 6
reset("f")
f(n)= (n+2)/(n**3 - n)
sum(f(n), n, 2, infinity)
```

Out[11]: $5/4$

In [19]:

```
#Ejercicio 7
reset("f")
f(n)=1/(n**3 - n)
sum(f(n),n, 2, infinity)
```

Out[19]: $1/4$

In [22]:

```
#Ejercicio 8
reset("f")
f(n)= (-1)**n * x^n
sum(f(n), x, 0, oo)
```

Out[22]: $(-1)^n \cdot \text{sum}(x^n, x, 0, +\text{Infinity})$

In [23]:

```
#Ejercicio 9
reset("f")
f(n)= (-1)^n * 4^n * x^(2*n)
sum(f(n), x, 0, infinity)
```

Out[23]: $4^n \cdot (-1)^n \cdot \text{sum}(x^{(2*n)}, x, 0, +\text{Infinity})$

In [2]:

```
#Ejercicio 10 (taylor(f(x), x, pt, orden max))
reset("f")
f(x)= 1/(1 + x^2)
taylor(f(x), x, 0, 3)
```

Out[2]: $-8x^3 + 4x^2 - 2x + 1$

In [3]:

```
#Ejercicio 11
g(x)= x*cos(x)
taylor(g(x), x, 0, 3)
```

Out[3]: $-1/2x^3 + x$