

L12: Spectral analysis of analog signals

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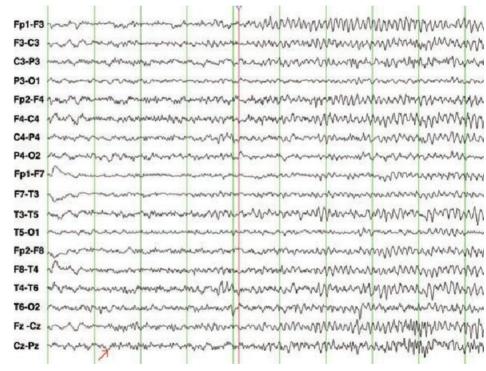
Common analog signals in neuroscience

- membrane potential, transmembrane current recordings
- electroencephalogram EEG
- magnetoencephalogram MEG
- local field potential LFP

Electroencephalogram - EEG

Electroencephalography (**EEG**) is an electrophysiological monitoring method to record electrical activity of the brain.





- typically noninvasive through electrodes on the scalp
- measures voltage fluctuations resulting from ionic current within the neurons in the brain
- focus on event-related potentials, or spectral content: exhibits prominent oscillations
- used for example in epilepsy, sleep disorder, anesthesia, coma research

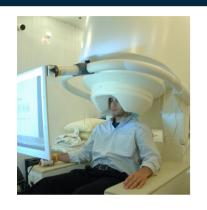
Magnetoencephalogram - MEG

Magnetoencephalography (MEG) is a functional neuroimaging technique for mapping brain activity by recording magnetic fields produced by electrical currents occurring naturally in the brain, using very sensitive magnetometers.

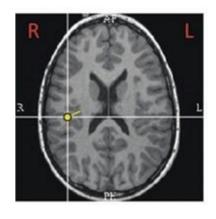




Magnetoencephalogram - MEG



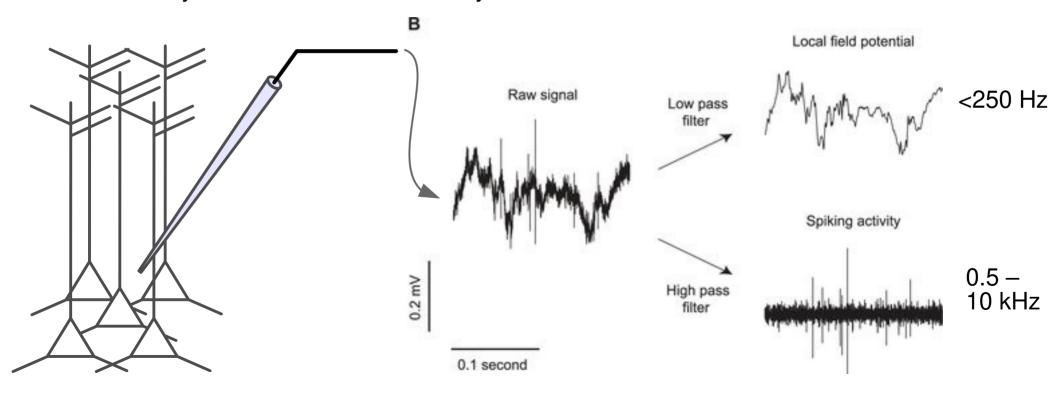




- noninvasive through devices capable of measuring small magnetic fields
- magnetic fields are generated by ionic current flow: the effect of multiple neurons (50,000 100,000) excited together in a specific area generates a measurable magnetic field
- MEG provides timing as well as spatial information about brain activity
- used to study perceptual and cognitive brain processes: localizing regions affected by pathology; determining functions of parts of the brain

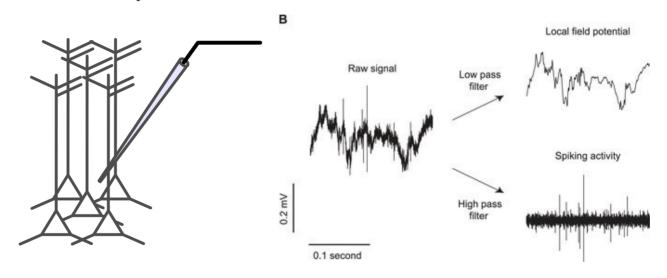
Local Field Potential - LFP

Local field potentials (LFP) are transient electrical signals generated in nervous tissue by the summed and synchronous electrical activity of the individual neurons in that tissue.



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- invasive through extracellular electrode placed nearby neurons generating signal
- LFP is the extracellular current flow the reflects the linearly summed postsynaptic potentials from local cell groups

Analog signals recorded from the brain



Oscillations in the brain

Delta oscillations (0.5-4 Hz)

associated with deep sleep – also known as slow-wave sleep

Theta oscillations (4-8 Hz)

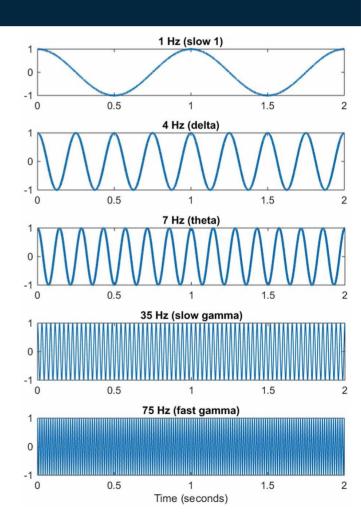
- observed during active motor behavior and REM sleep (rapid-eye movement sleep)
- prominently observed in the hippocampus

Beta oscillations (15-30 Hz)

associated with normal waking consciousness and movement

Gamma oscillations (30-150 Hz)

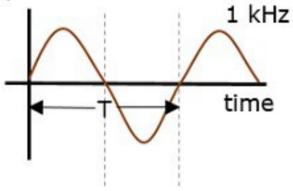
occurring during conscious perception

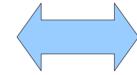


Starting point in analog signal processing

Time Domain Representation

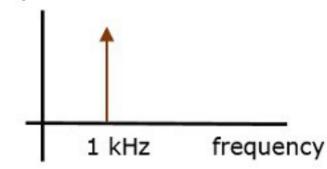
Amplitude





Frequency Domain Representation

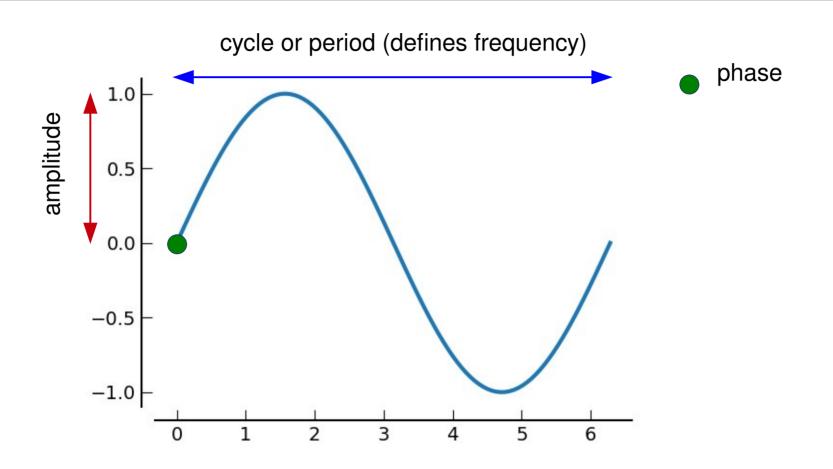
Amplitude



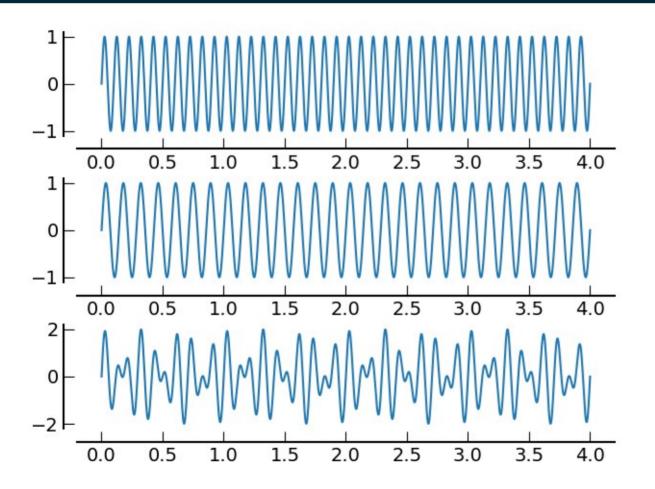
- show how a signal changes over time
- signals are recorded and often represented in time domain

- emphasizes periodic or repeating components of the signal
- decomposes a function of time (a signal) into its constituent frequencies

Sine wave: cyclically repeating signal

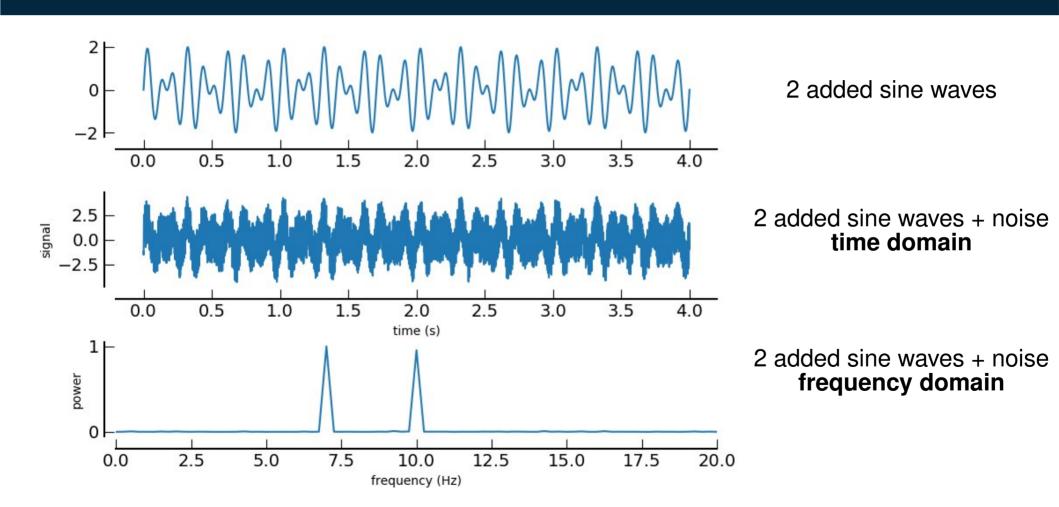


Example: Adding two sine waves

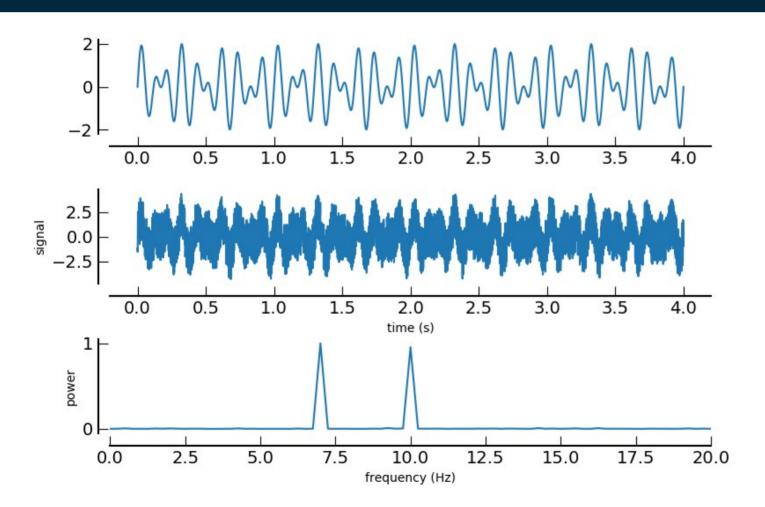


What is the frequency in each of the signals?

Signal with noise



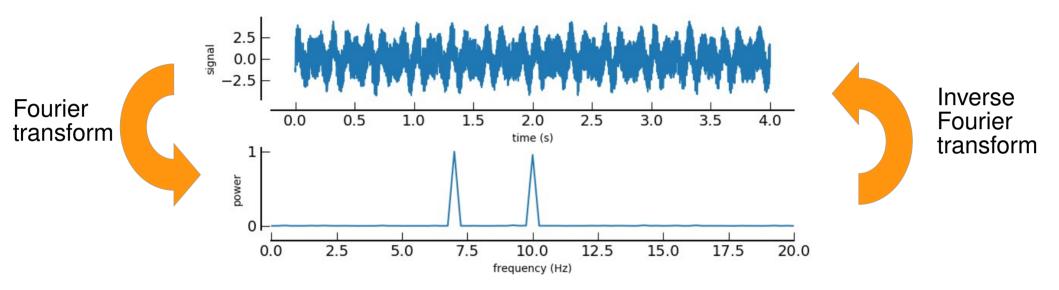
Signal with noise



Noisy and compound signals:

hard to discern signal frequency in the time domain but not in the frequency domain.

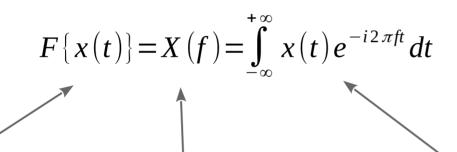
Fourier transform



- Fourier transform: transports the signal from the time domain into frequency space
- Inverse Fourier transform: transports any signal in the frequency domain back in the time domain

Fourier transform

the Fourier transform of a time series usually involves complex numbers representing **magnitude** and **phase** (we are only interested in magnitude here)



Fourier transform of the signal x(t)

Fourier transform itself, which is a function of frequencies f

inner-product of the signal with the exponential term: looking for the presence of sine waves with certain frequencies and outputs the degree (power)

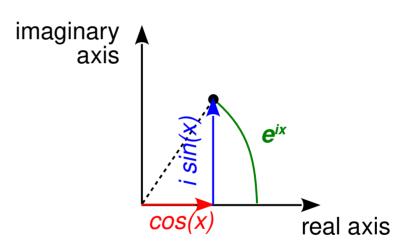


Jean-Baptiste Joseph Fourier (1768-1830)

Euler's formula

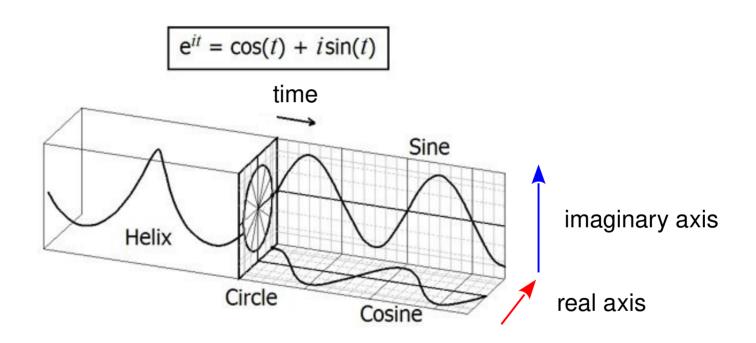
Euler's formula establishes relationship between trigonometric functions and complex exponential function.

$$e^{ix} = \cos x + i \sin x$$



- circular motion can be described by :
 - 1. decomposing Cartesian coordinates into an x- (cosine) and y-coordinate (sine)
 - 2. moving on the radius by the phase angle (angular distance)

Euler's formula describes circular motion

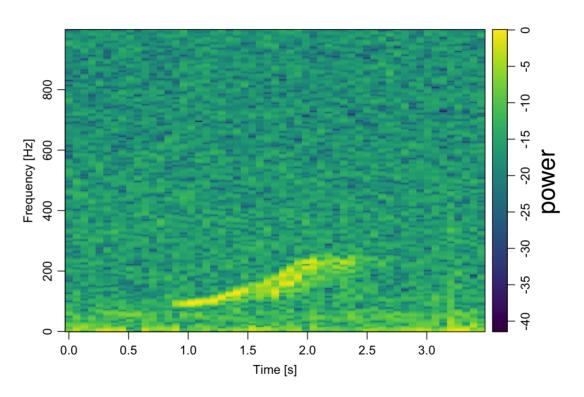


- adding time, creates a helix in the 3D space of complex numbers and time
- Euler's formula describes rotations

Fourier transform

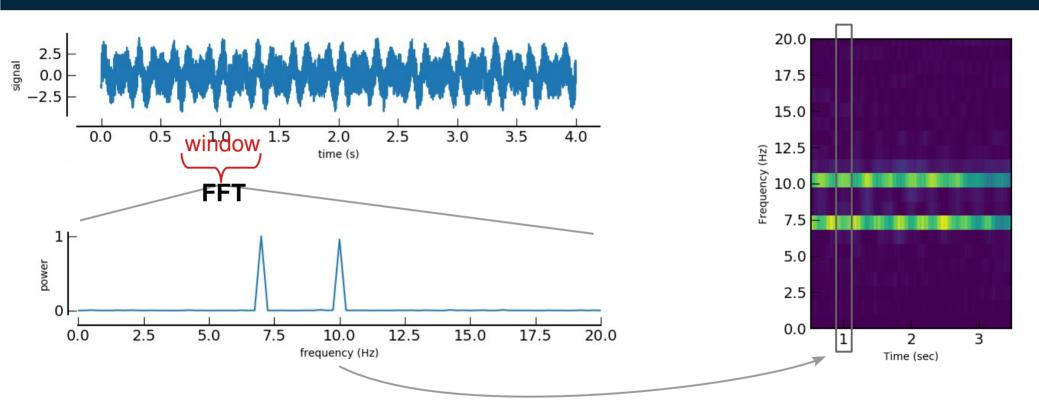
- power lies in it's generality : can be applied to analyze a wide variety of signals
- in neuroscience : signals include EEG, MEG, LFP, fMRI, visual signals, sound signals, etc.
- original formula defined over all time (-infinity → +infinity): the fast Fourier transform (FFT) introduces a discrete Fourier transform on short time windows of a signal sampled at discrete time points

Visualization: spectrogram



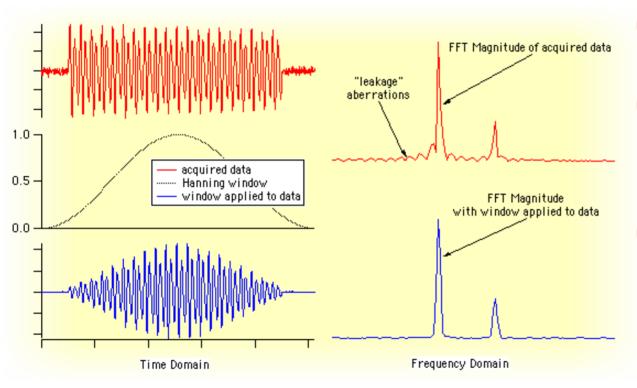
visual representation of power at different frequencies over time (stack of FFT outputs)

Visualization: construction of a spectrogram



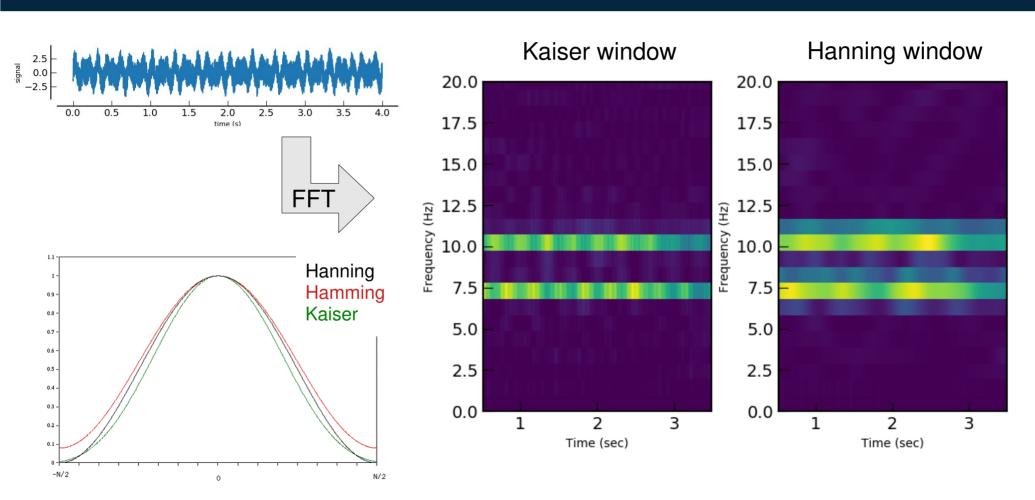
 the spectrogram results from doing the FFT on the part of the signal which falls into the window and plotting the frequency content in that window

Spectrogram: window function



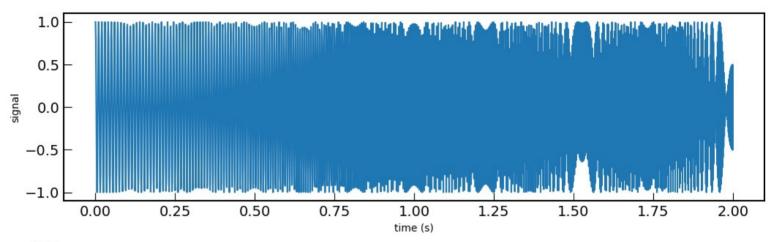
- Fourier transform is defined for infinite time, splitting the data into pieces introduces edge artifacts
- window functions try to avoid these edge artifacts as much as possible: done by amplifying the center and smooth out the edge of the window
- different window function emphasize different properties

Spectrogram: window functions

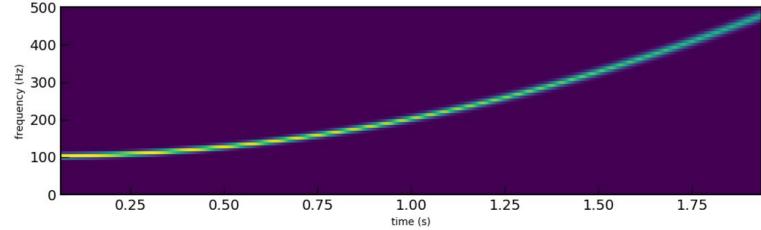


Spectrogram: useful insights

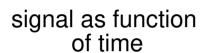
signal as function of time

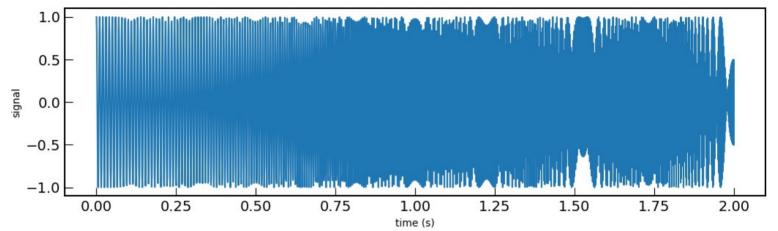


signal in frequency domain



Spectrogram: useful insights

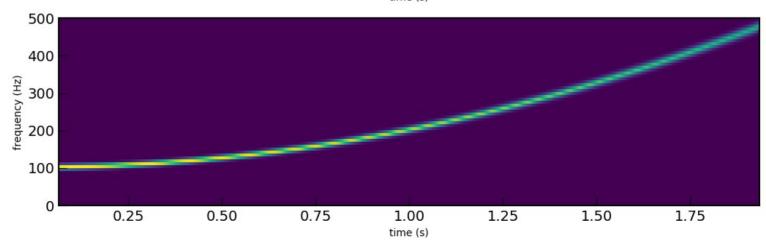




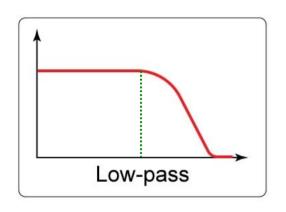
signal in frequency domain

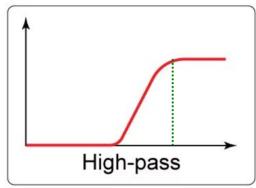


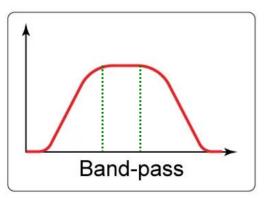
(exponential chirp)

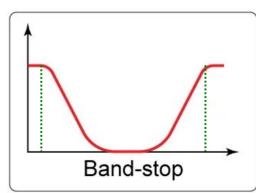


Signal filtering









- Filtering is a process that removes frequencies or frequency bands from a signal.
- frequency below/above a cutoff frequency are attenuated (for lowpass/high-pass filters)
- band-pass and band-stop filters are determined by a frequency band

frequency

...... cut-off frequency(ies)

Signal filtering

