

Spiking neural network simulation with Brian

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Why study networks of neurons?

- Studying neurons in isolation has its limits
 - the brain is **highly recurrent**, the output of a neuron affects the network and therefore its input
- Everything we perceive, think, or do results from the **activity of many neurons**
- **Memories** (short and long-term) are stored on the network level, not in individual neurons
- **Dynamics of the network** (and not just of individual neurons) are important for healthy brains ("brain rhythms") as well as in disease (e.g. epilepsy)

Modelling networks of neurons

Three main components:

1) Individual neurons

How is a single neuron modeled?

2) Synaptic connectivity

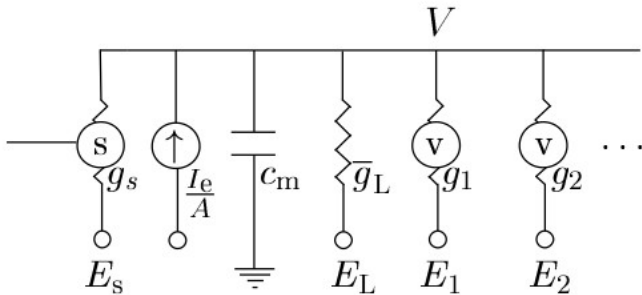
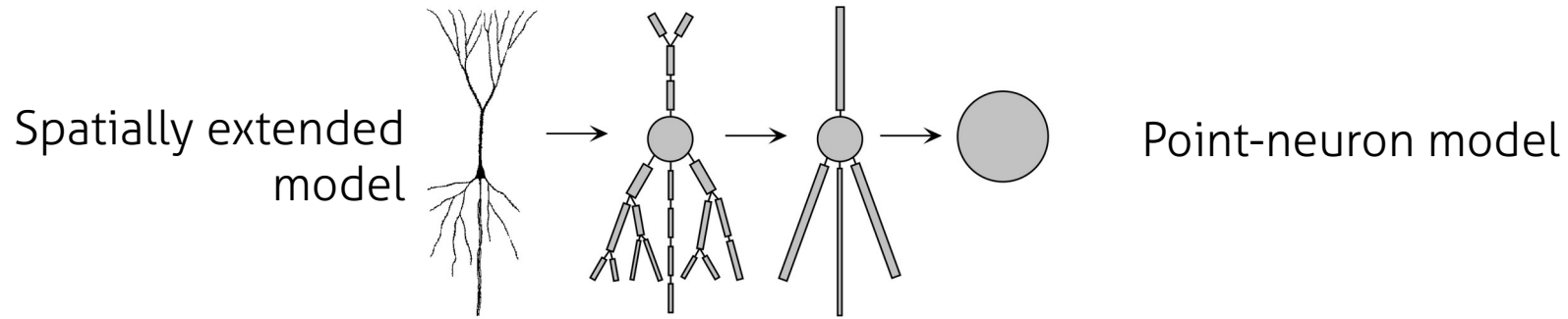
Which neurons connect to each other?

3) Synaptic models

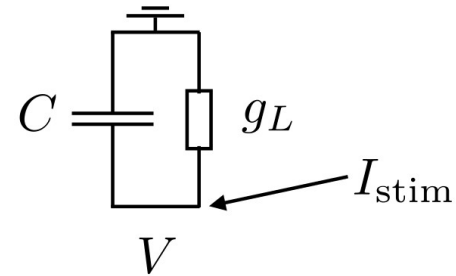
What is the effect of a spike arriving at the synapse?

Also: how does this effect change over time (plasticity)

Individual neurons



Hodgkin-Huxley formalism



integrate-and-fire model

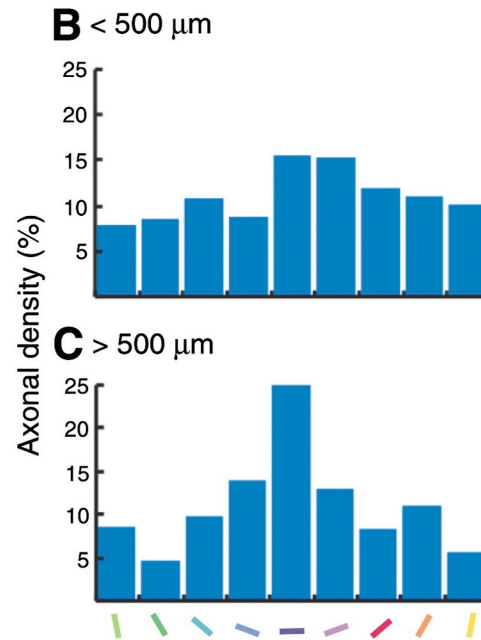
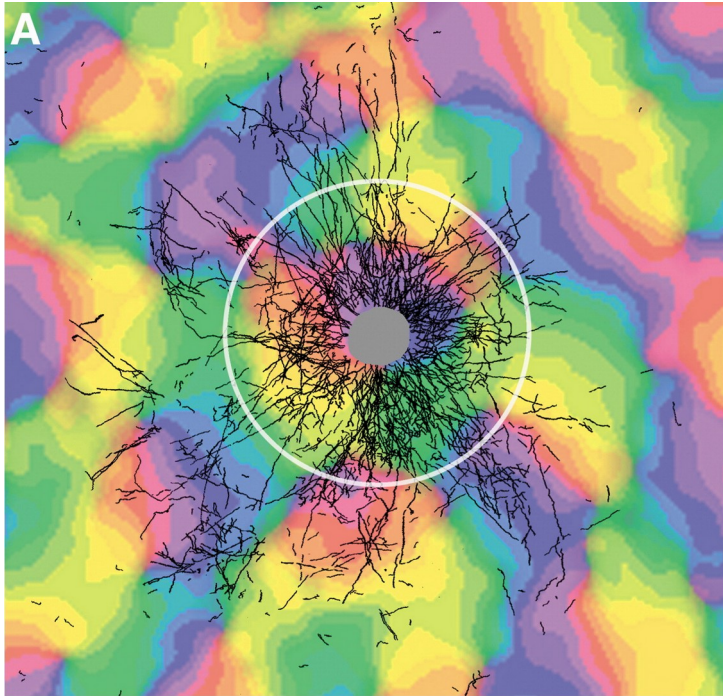
→ see lecture/tutorial 7

- Structured connectivity



Synaptic connectivity

- Structured connectivity



Superficial layers of V1
in Macaque monkeys

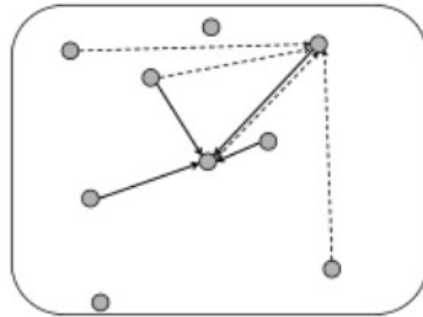
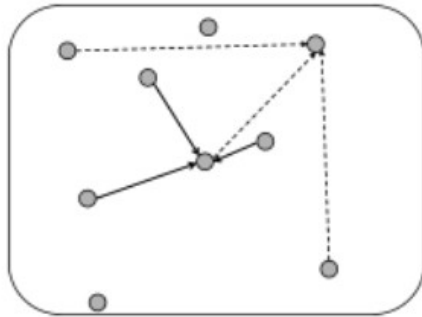
Synaptic connectivity

- Unstructured (random) connectivity

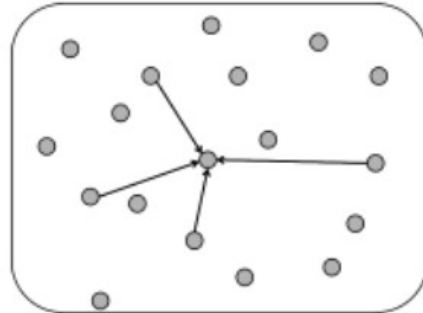
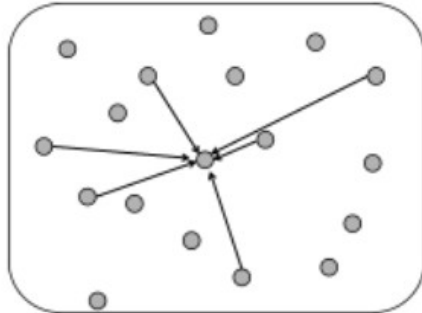
Fixed probability

Fixed number of inputs

$N = 9$



$N = 18$



Synaptic models

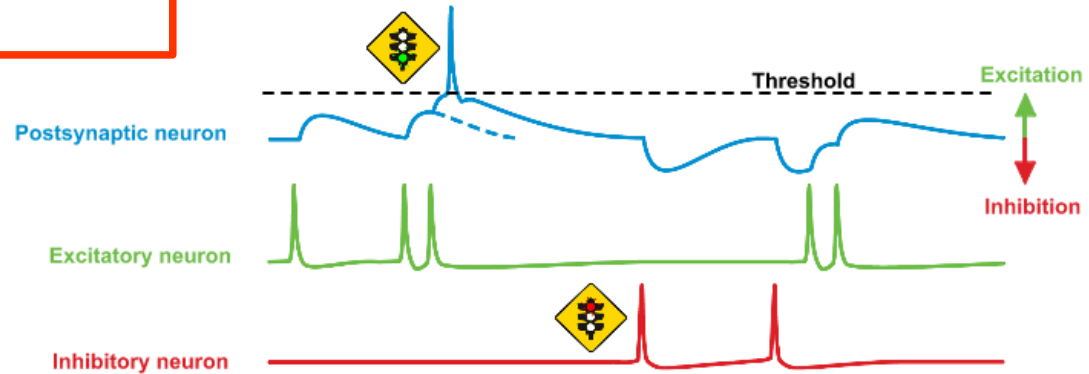
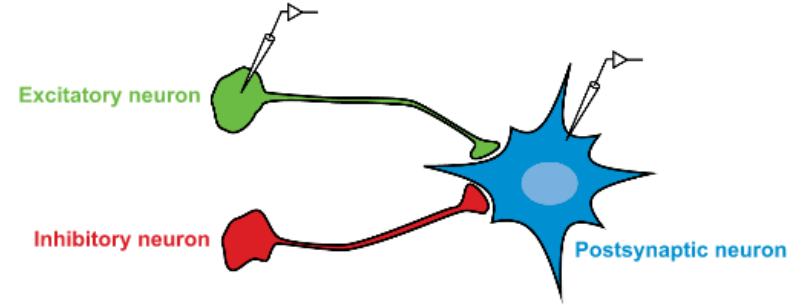
Synapses

?

Why can we talk about excitatory/inhibitory *neurons* and not just synapses?

!

→ "Dale's law"
Neurons release the same neurotransmitter(s) on every synapse



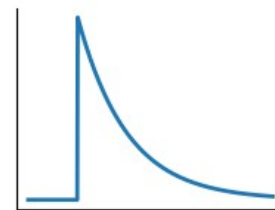
Synaptic models

Synapses

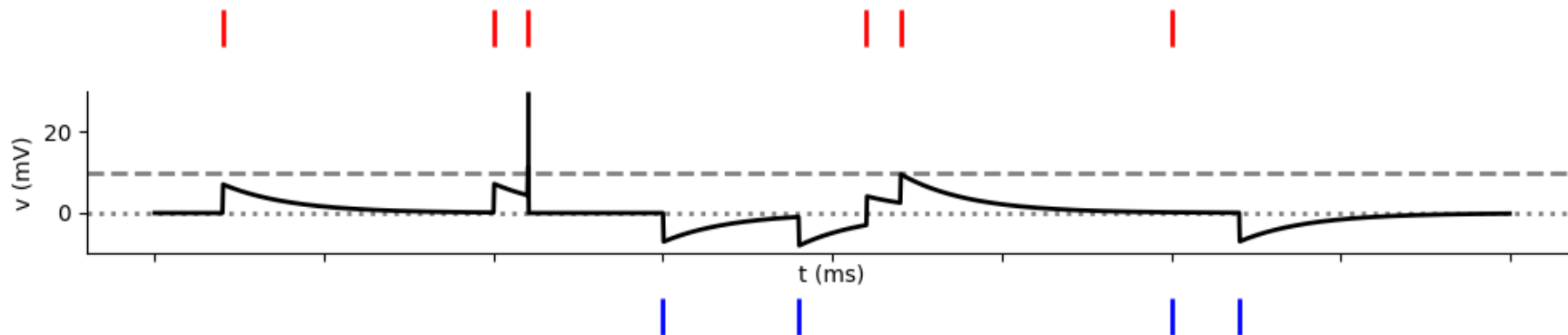
For each spike: increase V_m by J_{ij}

weight from j to i

membrane potential



“delta synapse”

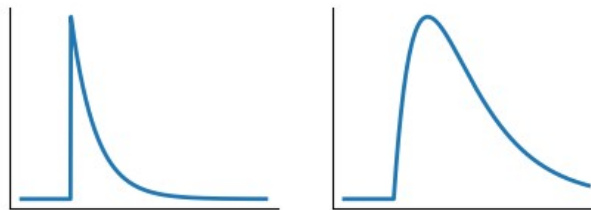


Synaptic models

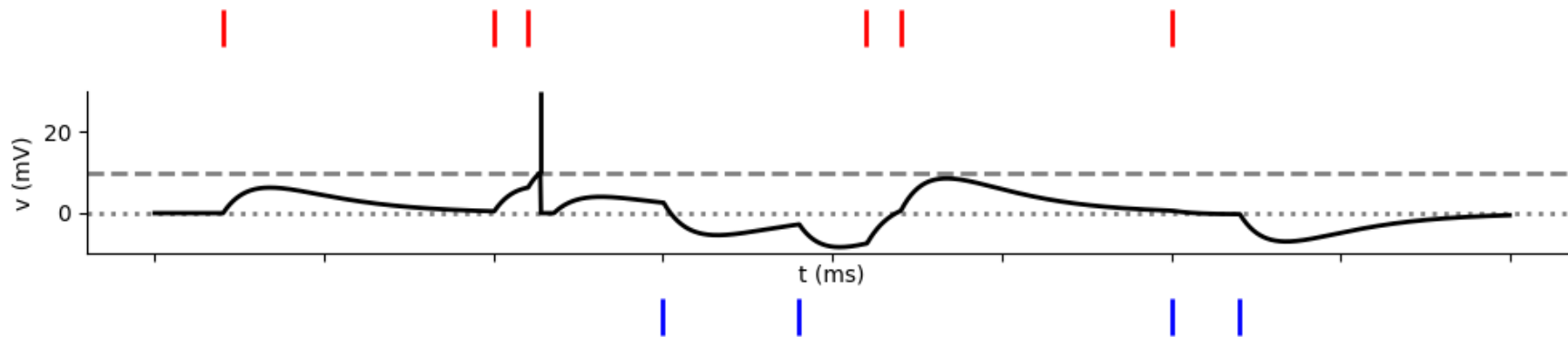
Synapses

For each spike: increase I_{syn} by J_{ij}
Between spikes: I_{syn} exponentially decays to 0

synaptic current membrane potential



Current-based
synapse



Synaptic models

Synapses

$$I_{syn} = g_{syn} (E_{syn} - V_m)$$

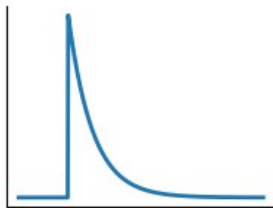
For each spike:

increase g_{syn} by J_{ij}

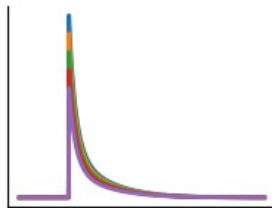
Between spikes:

g_{syn} exponentially decays to 0

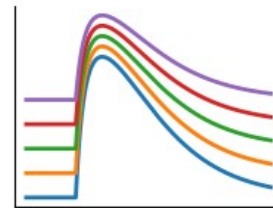
synaptic
conductance



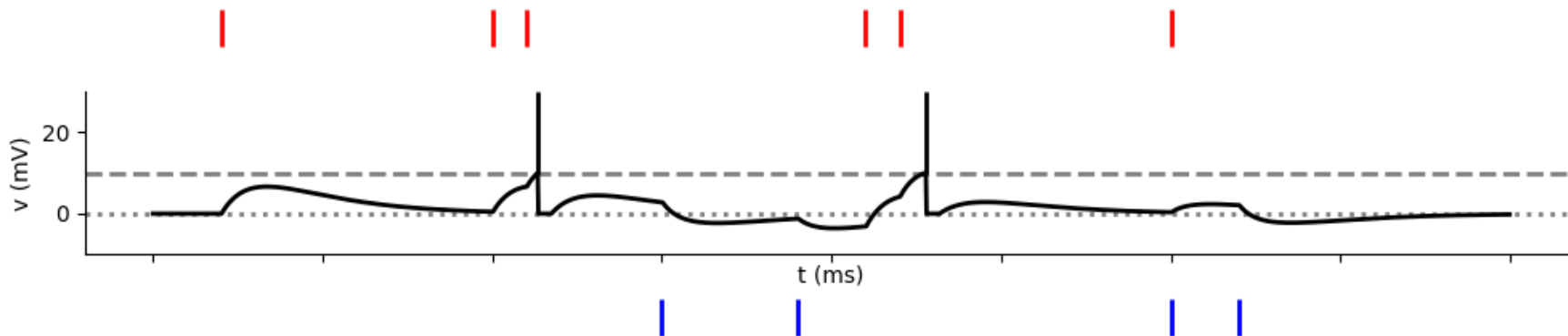
synaptic current



membrane potential



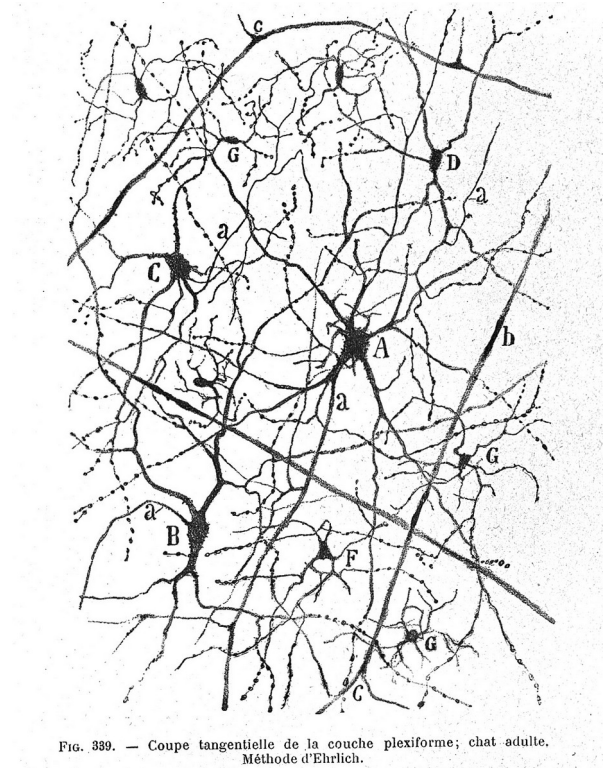
exponential
conductance-based



Neurons in a network

In the mouse cortex

- **Neurons:** $\sim 90\,000/\text{mm}^3$
Synapses: ~ 8000 per neuron
 $\sim 270\,000\,000$ synapses/ mm^3
- **Fewer inhibitory neurons**
($\sim 20\%$ of all neurons)

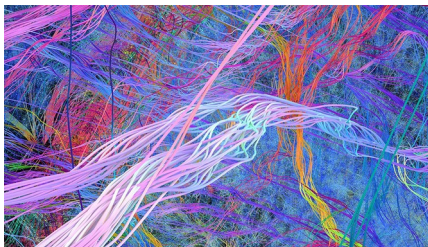


Network models: approaches

With thousands of neurons and millions of synapses (even in a very small part of the brain), how can we decide on the parameters? How can we get closer to an understanding of the system?

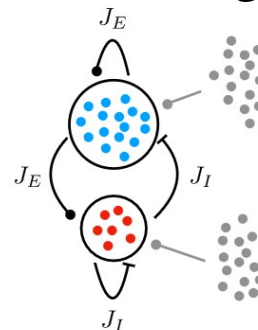
Roughly, two opposing approaches:

Try to gather as much data as possible
Use complex models and supercomputers



© Blue Brain Project/EPFL

Simplify everything as much as possible
Use mathematics to gain insights



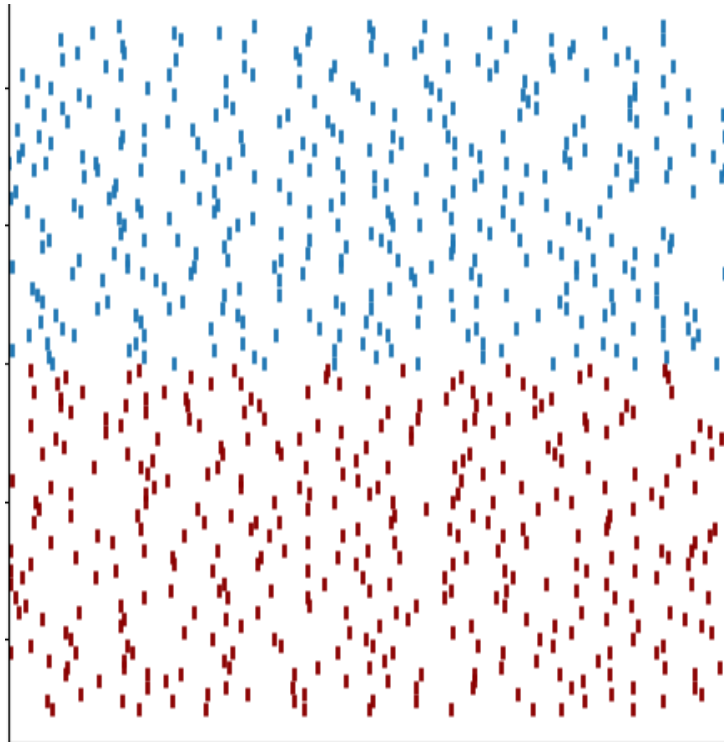
Network models: approaches

Today, we'll simplify things a lot

- **Leaky integrate-and-fire** point neuron model
(no Hodgkin-Huxley dynamics, no neuronal morphology, ...)
- **Homogeneous population**, all neurons are “the same”
(no neuron types, no heterogeneity, ...)
- **Simple synapse** model (“delta synapses”)
(no synaptic dynamics, no adaptation, no plasticity...)
- **Random connectivity** between neurons
(no structure, no position in space, ...)

Network dynamics

How can we characterize network activity?



Individual neurons:

Weakly or strongly active?

Firing regularly or irregularly?

Firing rate,
ISI distribution → CV

Network:

Synchronized or unsynchronized?

Oscillating?

e.g. spectral analysis
(auto)correlation