



# Neural Data Science with **Python**

## L4 : Wrangling Spike Trains

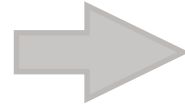
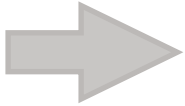
*Michael Graupner*

*SPPIN – Saint-Pères Institute for the Neurosciences*

*Université Paris Cité, CNRS*

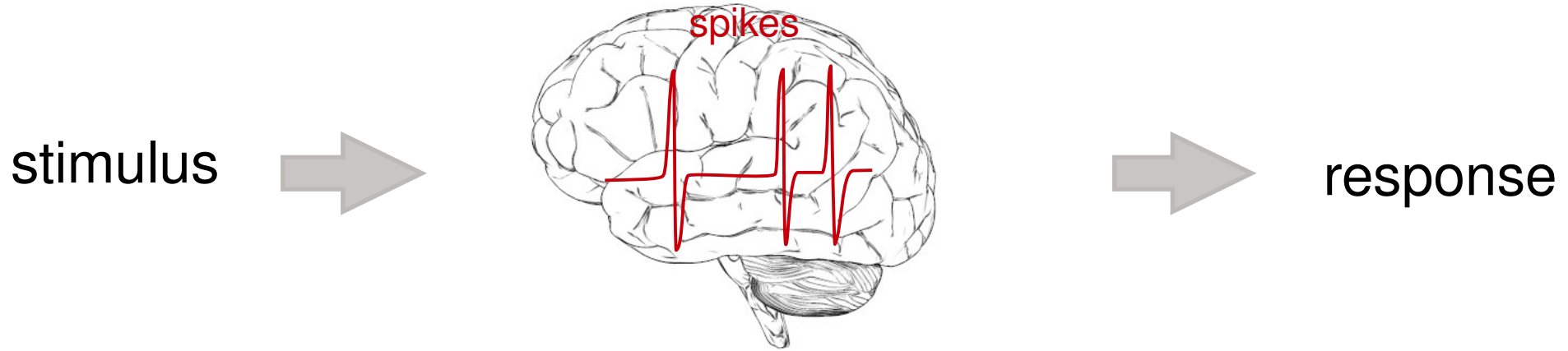
# Cognitive processing

stimulus



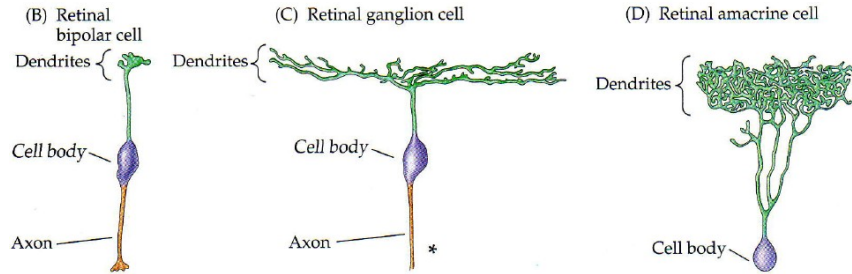
response

# The quest for the Neural Code



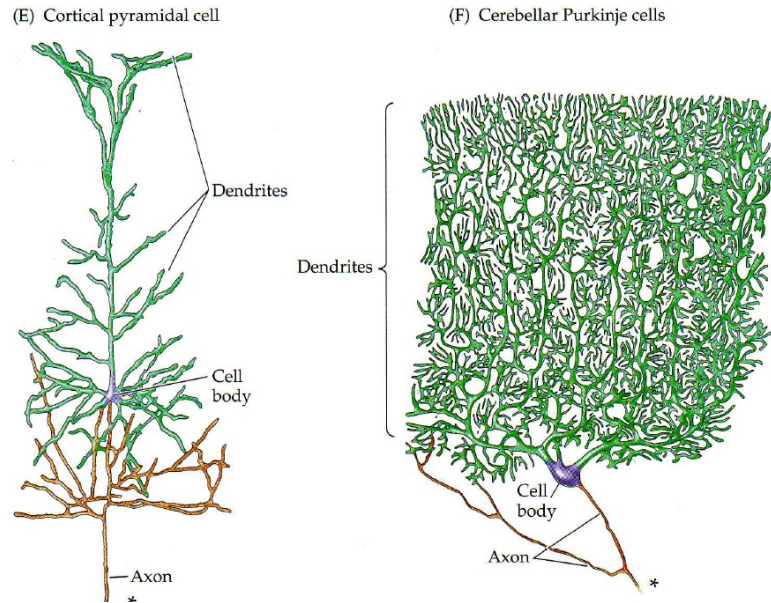
- How is information represented in the brain ?  
Is the information carried by the timing of spikes, or in the firing rate
- How much information is carried by neural populations ?  
Population codes are complicated, neurons might carry redundant information
- On what time scales is information represented ?  
Over which time scale is information integrated ?

# Neurons = principal computation units



dendrites

soma

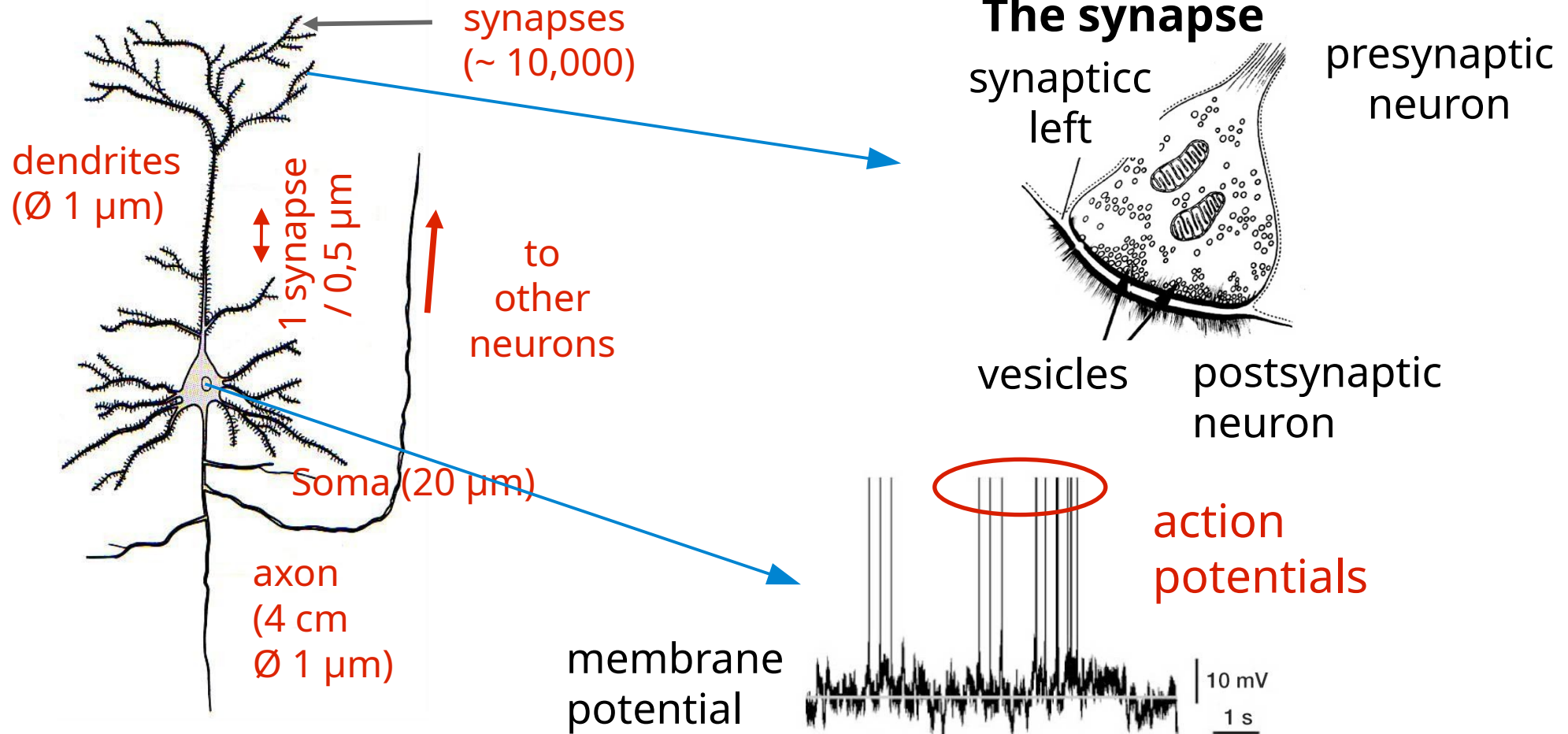


axon

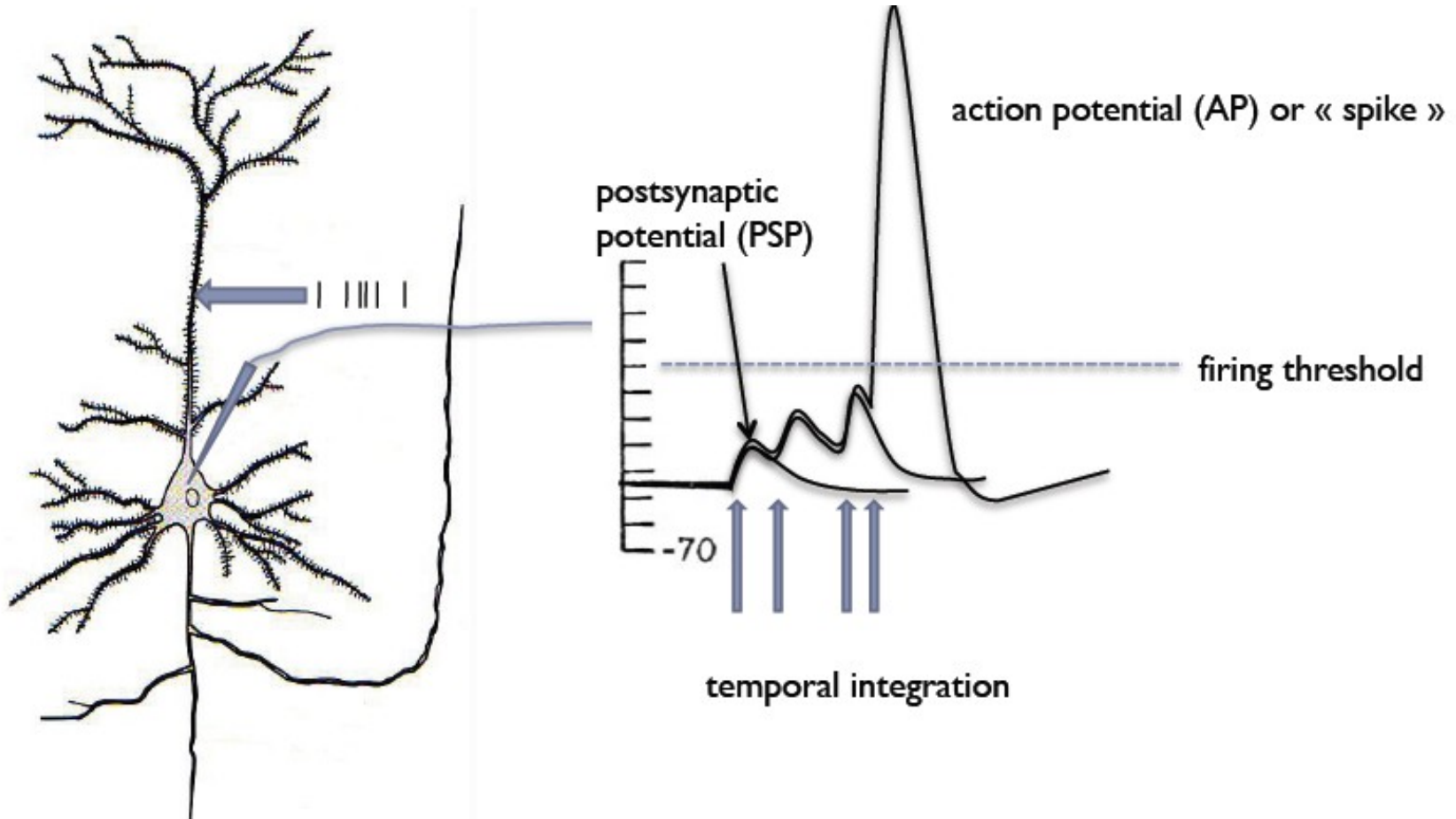
flow of information



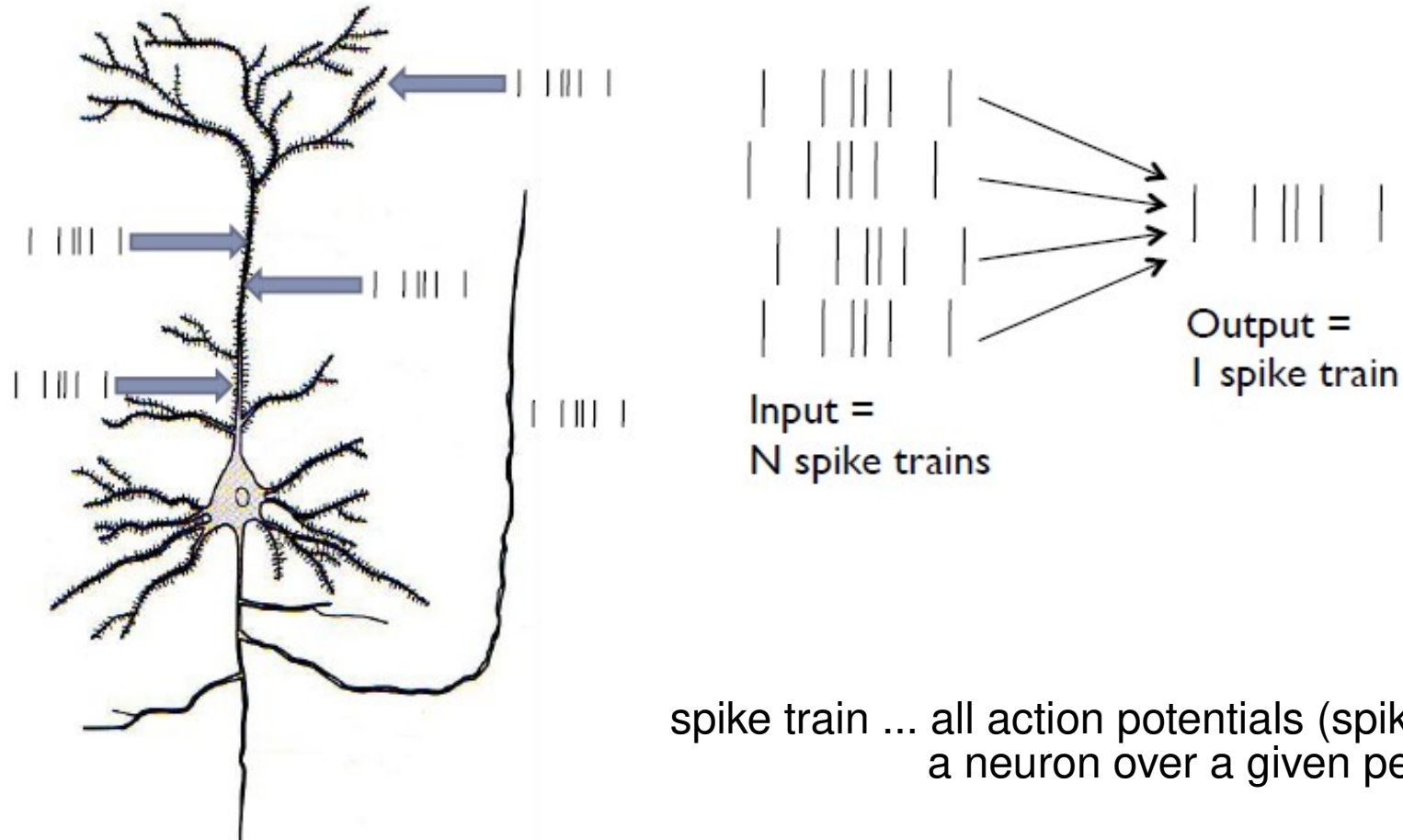
# Typical cortical neuron



# Neural integration

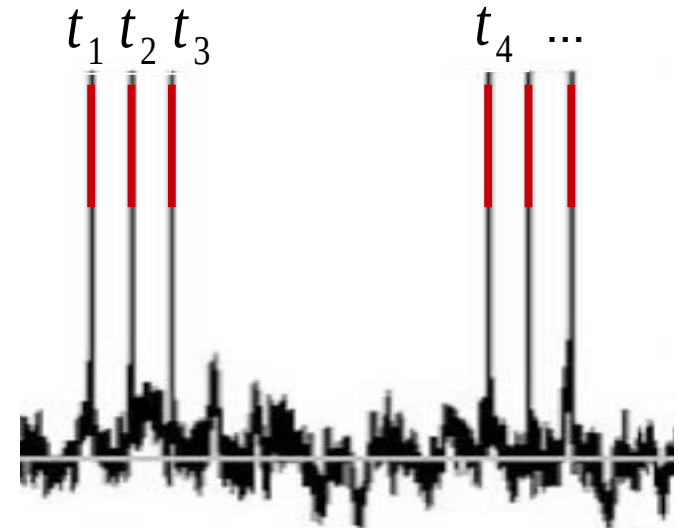


# Neural integration



# Statistics of trains of action potentials

- Spike train (also: discharges, action potentials):
  - a sequence of spike times  $t^k$
  - only the action potential is considered

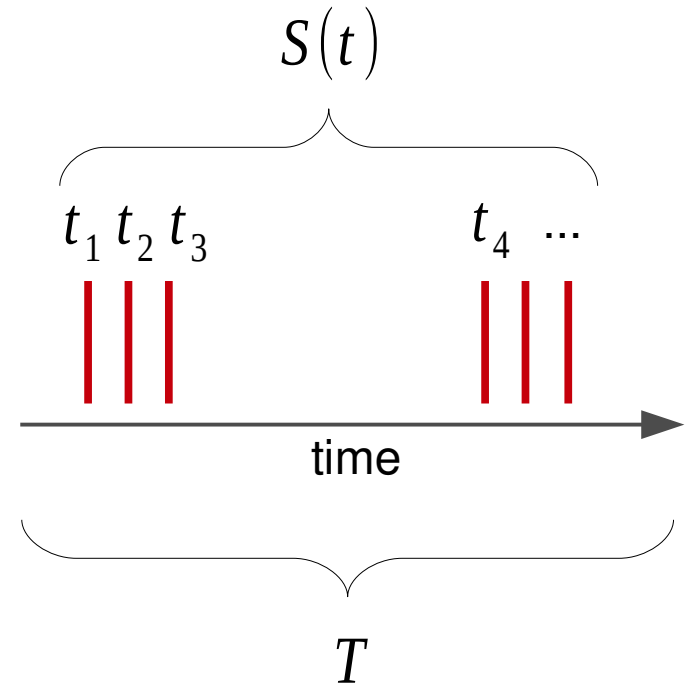




# Statistics of spike-trains: firing rate

- Spike train (also: discharges, action potentials):
  - a sequence of spike times  $t^k$
  - only the action potential is considered
  - a signal  $S(t)$
- Firing rate  $r$  or  $\nu$ :
  - number of spikes/time

$$r = \frac{N_{\text{spikes}}}{T}$$



# Statistics of spike trains: inter-spike interval

- Spike train (also: discharges, action potentials):
  - a sequence of spike times  $t^k$
  - only the action potential is considered
  - a signal  $S(t)$

- Firing rate  $r$  or  $\nu$ :
  - number of spikes/time

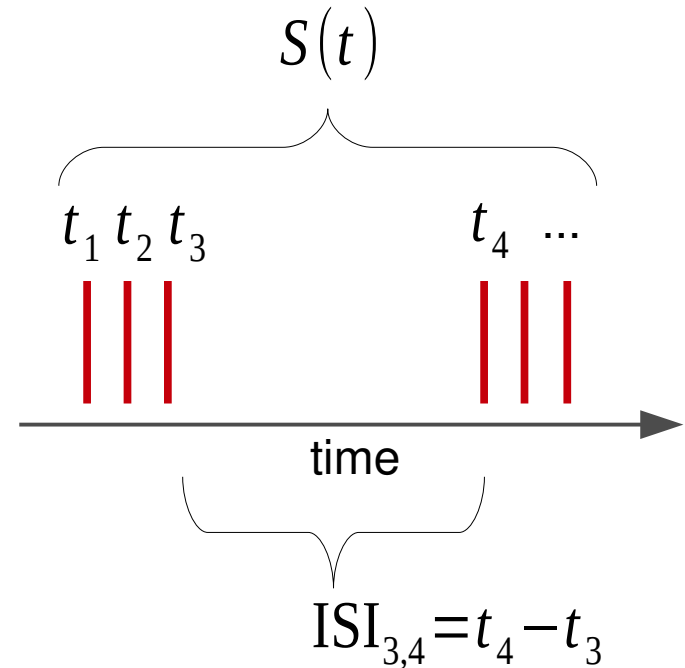
$$r = \frac{N_{spikes}}{T}$$

- Inter-spike interval (ISI) :

$$ISI = t^{n+1} - t^n$$

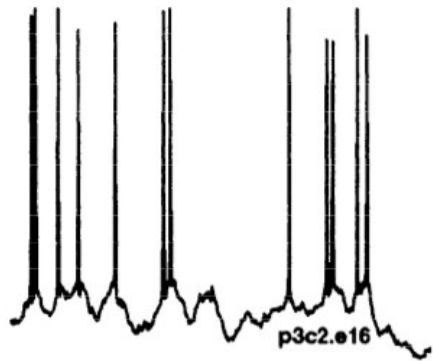
- Firing rate from ISI :

$$r = \frac{1}{ISI_{mean}}$$



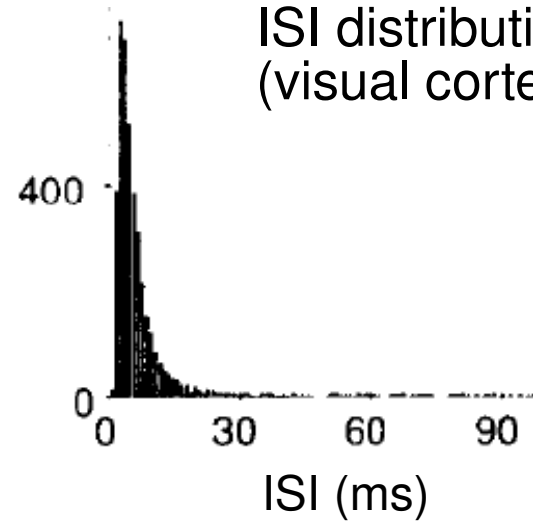
# Statistics of spike-trains : inter-spike interval

In Vivo Visual Stimulation



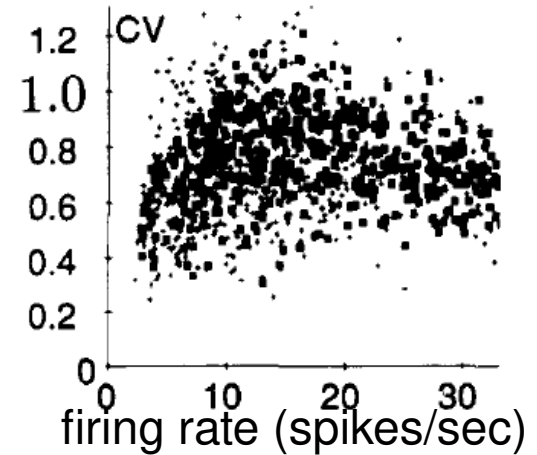
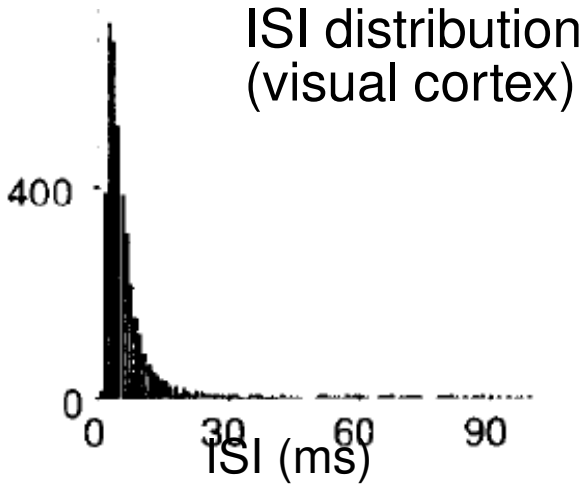
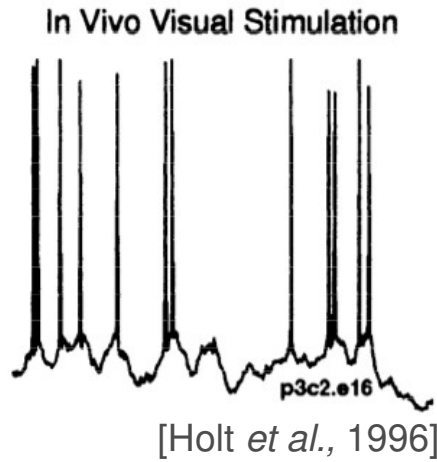
[Holt *et al.*, 1996]

ISI distribution  
(visual cortex)



- ISIs of cortical neurons are highly variable
- ISI distribution is highly skewed with a few outliers

# Statistics of spike-trains : coefficient of variation



- Coefficient of Variation (CV) :

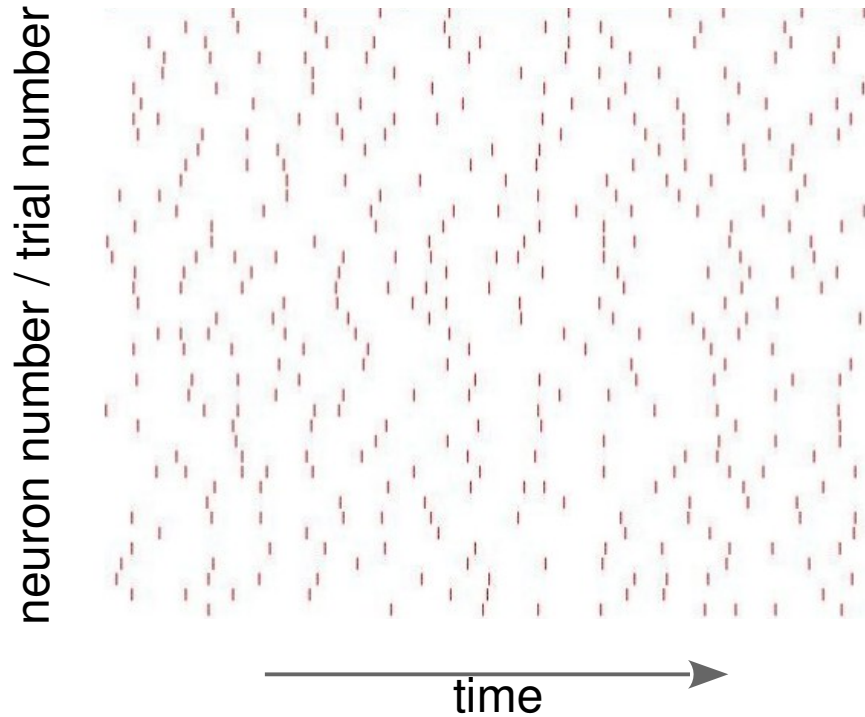
- ratio between standard-deviation and mean of the inter-spike interval

- measures the irregularity of spike trains

- spike are often irregular ( $CV \sim 1$ ) and vary from one trial to another

$$CV = \frac{ISI_{\text{standard deviation}}}{ISI_{\text{mean}}}$$

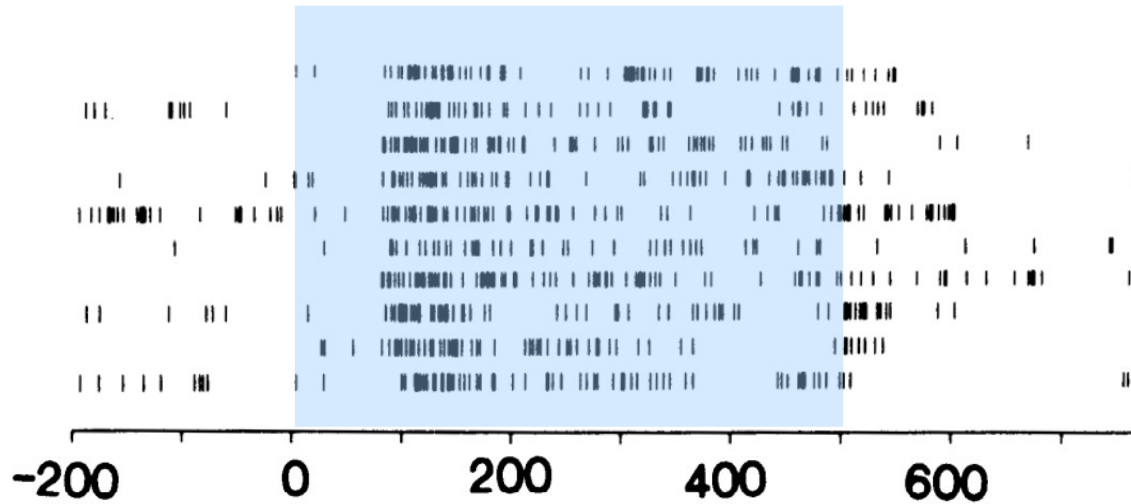
# Visualization of spike-trains : raster plot



- provides raw view of spike-times
- each individual vertical line represents an action potential at a specific time of a given neuron, or at a given repetition
- also called **rastergram**

# Visualization of spike-trains : PSTH

visual stimuli, duration = 500 ms

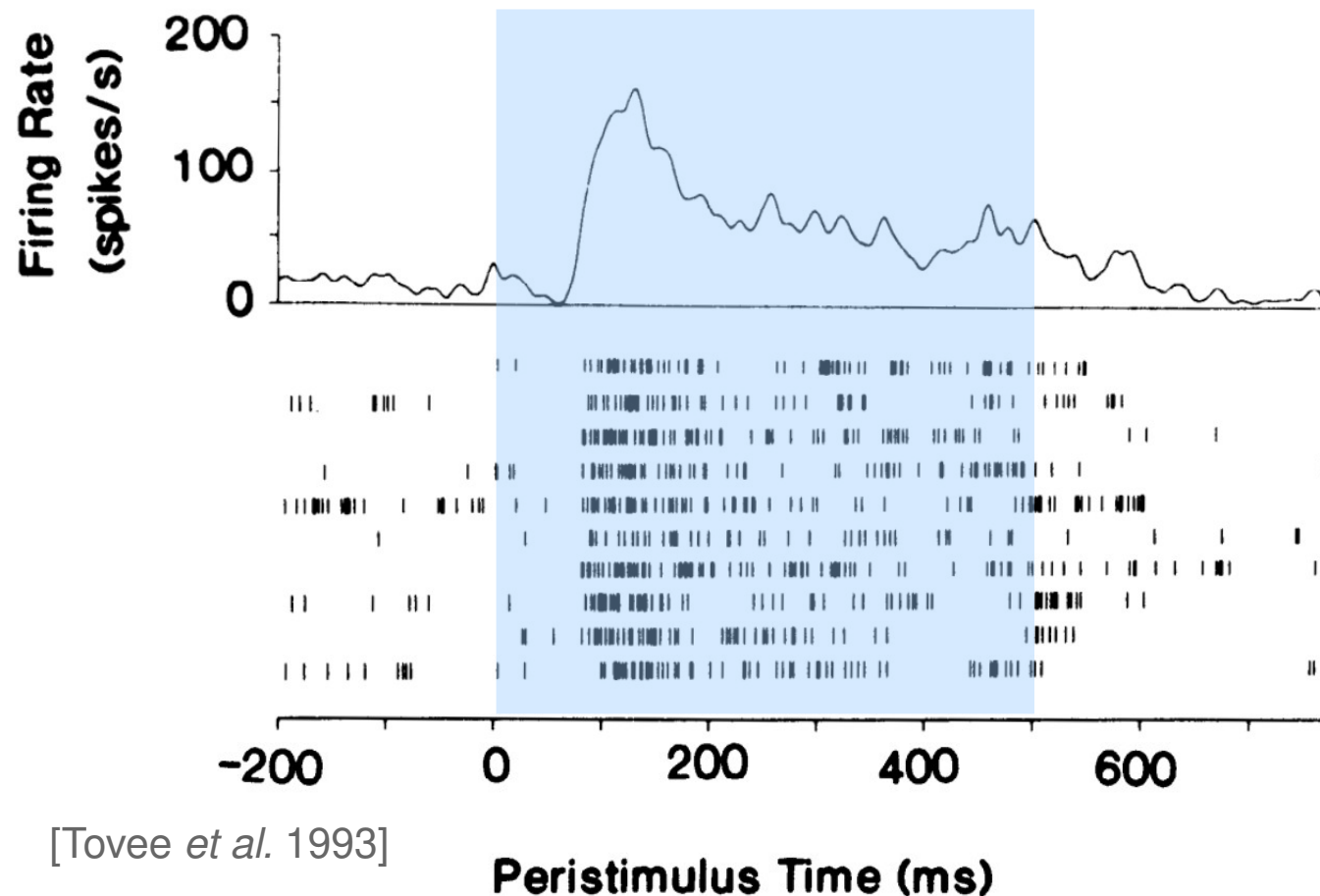


- recording in primate visual cortex
- each line represents a repetition of the same recording

[Tovee *et al.* 1993]

**Peristimulus Time (ms)**

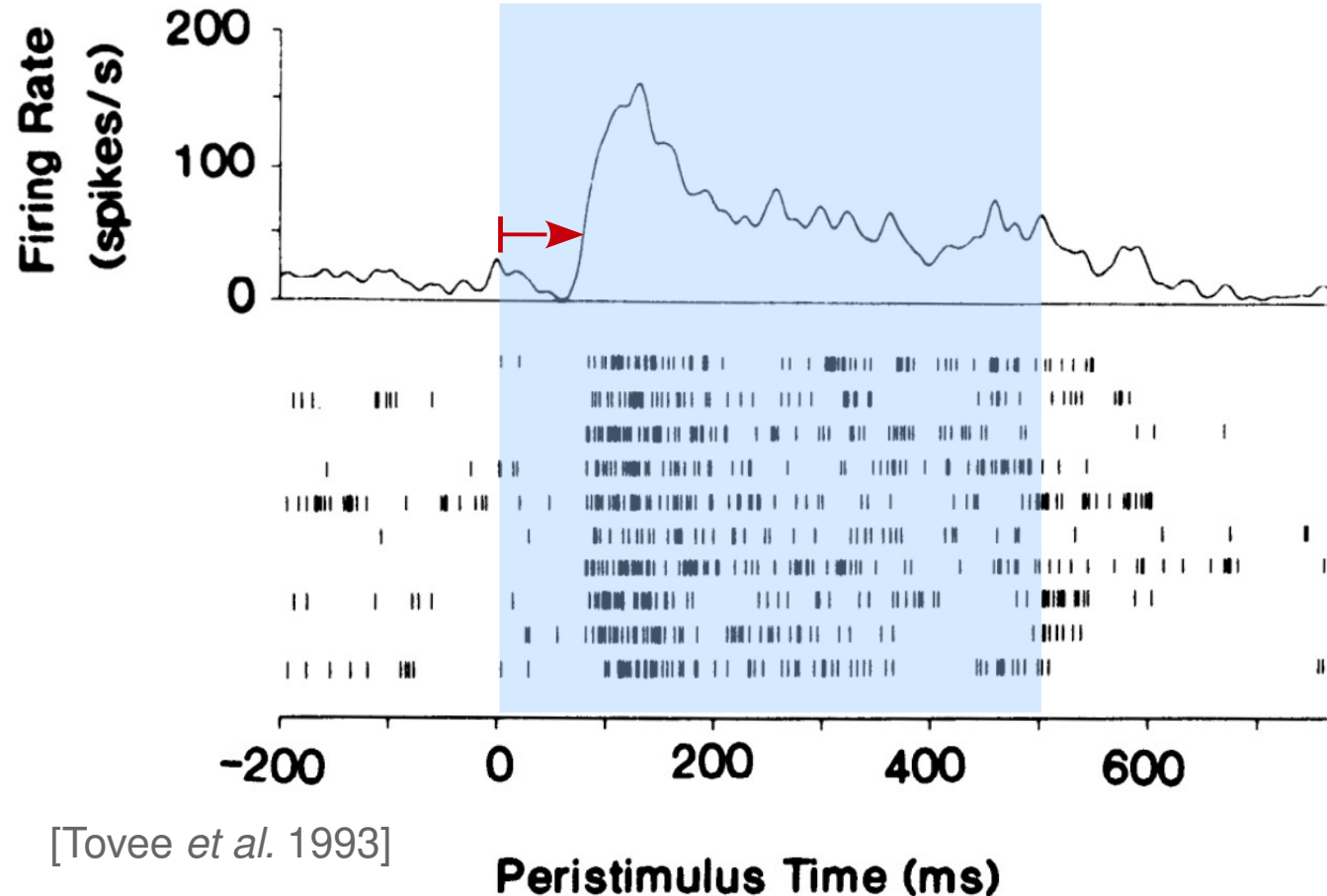
# Visualization of spike-trains : PSTH



- the **peri-stimulus time histogram** averages all repetitions of an experiment, showing spike number/firing rate before, during and after a stimulus
- construction : time is binned and responses falling in the same bin are combined

[Tovee *et al.* 1993]

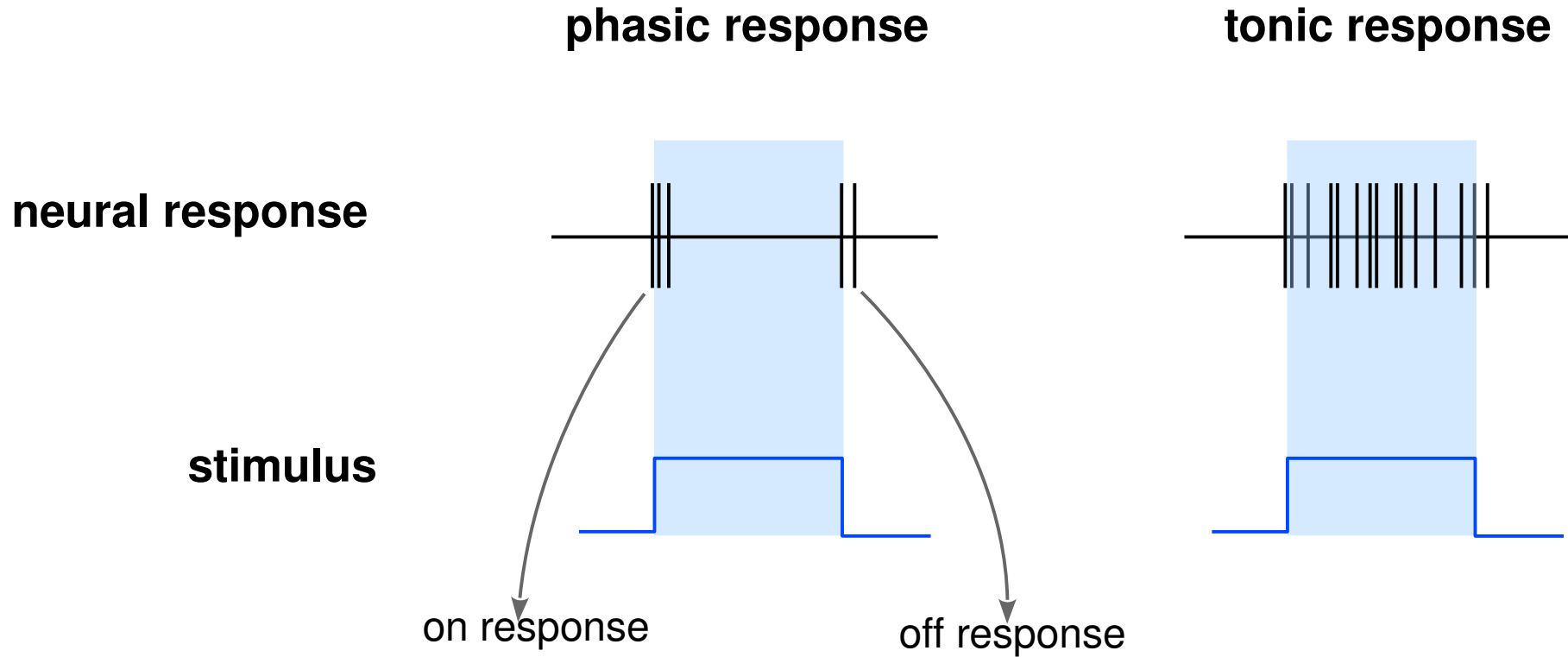
# Response latency



- **response latency** : the time it takes a neuron to respond to a stimulus



# Neural response behaviors

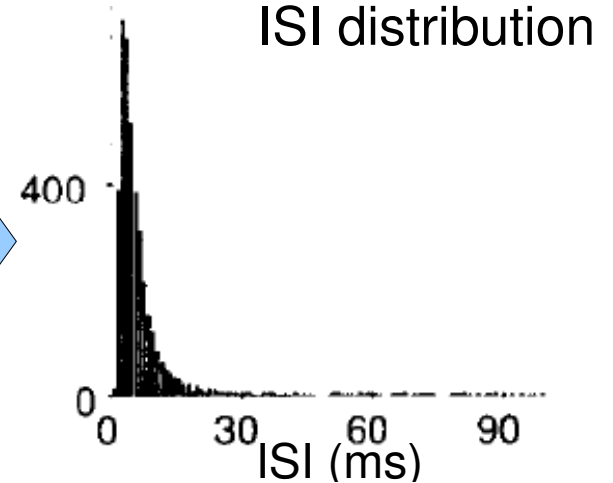
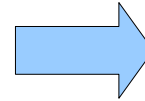
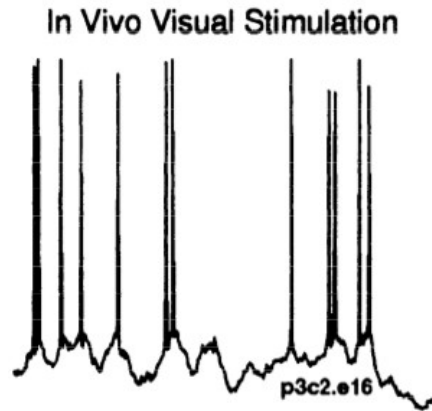


# The Poisson process

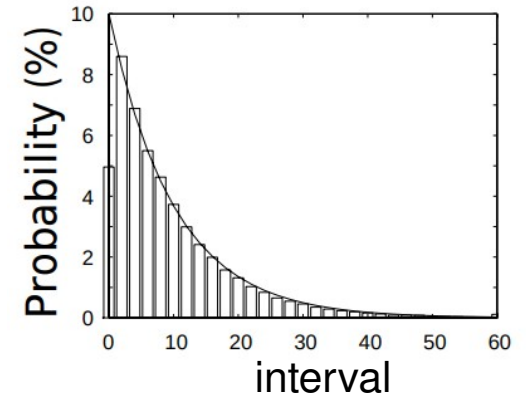
## real neurons

→ highly variable,  
maybe spikes don't  
matter, only the rate

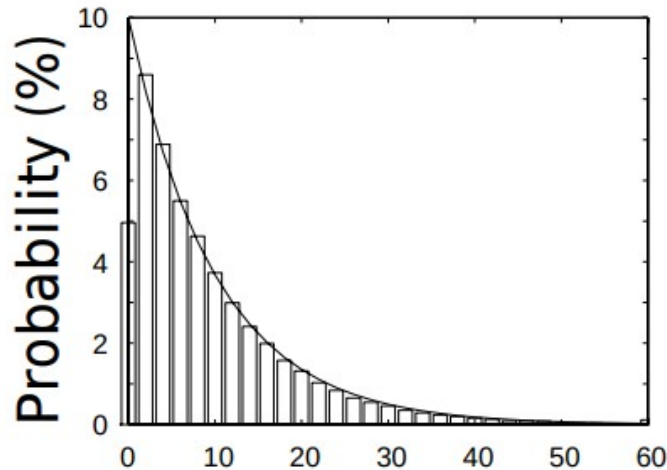
→ **Poisson process**



Poisson processes are used to describe cases with rare, random events in time or space, e.g., radioactive emissions, traffic accidents, earthquakes and action potentials.



# The Poisson process



- **Poisson process** : used in scenarios where we are counting the occurrences of certain events that appear to happen at a certain rate  $r$ , but completely at random (without a certain structure).
- The **interspike interval (ISI) density (histogram)** for a homogeneous Poisson process (constant rate) is an exponential function. The most likely interspike intervals are short ones and long intervals have a probability that falls exponentially as a function of their duration.

$$p(\tau) = r \exp^{-r\tau}$$

$\tau$  ... waiting time for the next spike to occur

$r$  ... rate of the Poisson process