

1 **Synergistic retrievals of ice in high clouds from lidar, Ku-band radar and**
2 **submillimeter wave radiometer observations**

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⁷ ABSTRACT: In this study, we investigate the synergy of lidar, Ku-band radar, and sub-millimeter-
⁸ wave radiometer measurements in the retrieval of the ice from satellite observations. The synergy
⁹ is analyzed through the generation of a large dataset of IWC profile and simulated lidar, radar and
¹⁰ radiometer observations. The characteristics of the instruments e. g. frequencies, sensitivities, etc.
¹¹ are set based on the expected characteristics of instruments of the AOS mission. A cross-validation
¹² methodology is used to assess the accuracy of the retrieved IWC profiles from various combinations
¹³ of observations from the three instruments. Specifically, the IWC and associated observations is
¹⁴ randomly divided into two datasets, one for the training and the other for the evaluation. The
¹⁵ training dataset is used to train the retrieval algorithm, while the evaluation dataset is used to
¹⁶ assess the retrieval performance. The dataset of IWC profiles is derived from CloudSat reflectivity
¹⁷ observations.

¹⁸ The retrieval of the ice water content IWC profiles from the computed observations is achieved in
¹⁹ two steps. In the first step, a class, out of 18 potential classes characterized by different vertical
²⁰ distribution of IWC, is estimated from the observations. The 18 classes are predetermined based on
²¹ k-Means clustering algorithm. In the second step, the IWC profile is estimated using a Ensemble
²² Kalman Smoother (EKS) algorithm that uses the estimated class as a priori information.
²³ The results of the study show that the synergy of lidar, radar, and radiometer observations is
²⁴ significant in the retrieval of the IWC profiles. The inclusion of the lidar observations in the
²⁵ retrieval process has a larger impact on the retrieval performance than the inclusion of the radar
²⁶ observations.

27 **1. Introduction**

28 The future NASA Atmospheric Observing System (AOS) mission (Braun 2022) is expected
29 to feature new combinations of observations that may be used to quantify the amounts of ice
30 in high clouds and characterize the microphysical properties of ice particles. These observations
31 include lidar backscatter, Ku-band radar reflectivity, and submillimeter wave radiometer brightness
32 temperature measurements. While not optimal for cloud ice estimation, but for the characterization
33 of a broader spectrum of cloud and precipitation processes, these observations are nevertheless
34 synergistic from the characterization of ice clouds perspective. That is, despite the fact that lidar
35 observations attenuate quickly in thick ice clouds and the Ku-band radar will not be able to detect
36 clouds characterized by an echo weaker than 8.0 dBZ, the active observations are expected to
37 provide context that may be incorporated into the radiometer retrievals. Herein, term retrieval
38 is defined as the process of estimating geophysical variables from remote sensing observations.
39 In this study, we investigate the impact of incorporating lidar and radar observations into the
40 radiometer retrieval of ice clouds. Because the existent amount of coincident backscatter lidar,
41 Ku-band radar, and submillimeter-wave radiometer observations is rather insufficient to derive
42 conclusive results, we employ accurate physical models to simulate lidar, radar and radiometer
43 observations and use a cross-validation methodology to characterize the retrieval accuracy. As
44 estimates from passive instrument observations strongly depend on "a priori" information (Rodgers
45 2000), for results to be relevant in real applications, it is necessary to base them on realistic vertical
46 distributions of ice properties. Such distributions may be derived from cloud-resolving-model
47 (CRM) simulations (Pfreundschuh et al. 2020; Liu and Mace 2022) or directly from observations.
48 In this study, we employ the latter approach, as CRMs may still be deficient in properly reproducing
49 the vertical distribution of ice clouds and their associated microphysical properties. Specifically,
50 we use observations and products from the CloudSat (CS) mission (Stephens et al. 2002) to derive
51 a database of ice microphysical properties and associated simulated lidar, radar, and radiometer
52 observations. This database is used to investigate the accuracy of estimated ice cloud properties
53 from the simulated observations. Another major difference relative to previous studies is the
54 unique combination of instruments investigated herein. The article is organized as follows. In
55 Section 2, we describe the approach used to derive the ice properties and the associated simulated

56 observations, the retrieval and the evaluation methodology. In Section 3, we present the results of
57 the evaluation methodology. We conclude in Section 4.

58 **2. Methodology**

59 As previously mentioned, we use CloudSat (CS) observations (Stephens et al. 2002) to derive
60 the vertical distributions of ice properties needed in the investigation. Although research quality
61 CS cloud ice products exist, to maximize the physical consistency of the approach, we do not use
62 them but derive ice amounts and associated properties directly from CS reflectivity observations.
63 This ensures the consistency between the particle distribution assumptions and the electromagnetic
64 scattering properties used in the CS reflectivity processing and those used the simulation of the
65 lidar, Ku-band radar and radiometer observations. Lidar, Ku-band radar, and submillimeter-
66 wave radiometer observations are simulated from CS observations using accurate physical models
67 and realistic assumptions consistent with the most recent knowledge in the field of ice cloud
68 microphysics, and a non-parametric estimation methodology based on the k-Means clustering
69 algorithm MacKay (2003) is used to investigate the instrument synergy. Details of the methodology
70 are presented below.

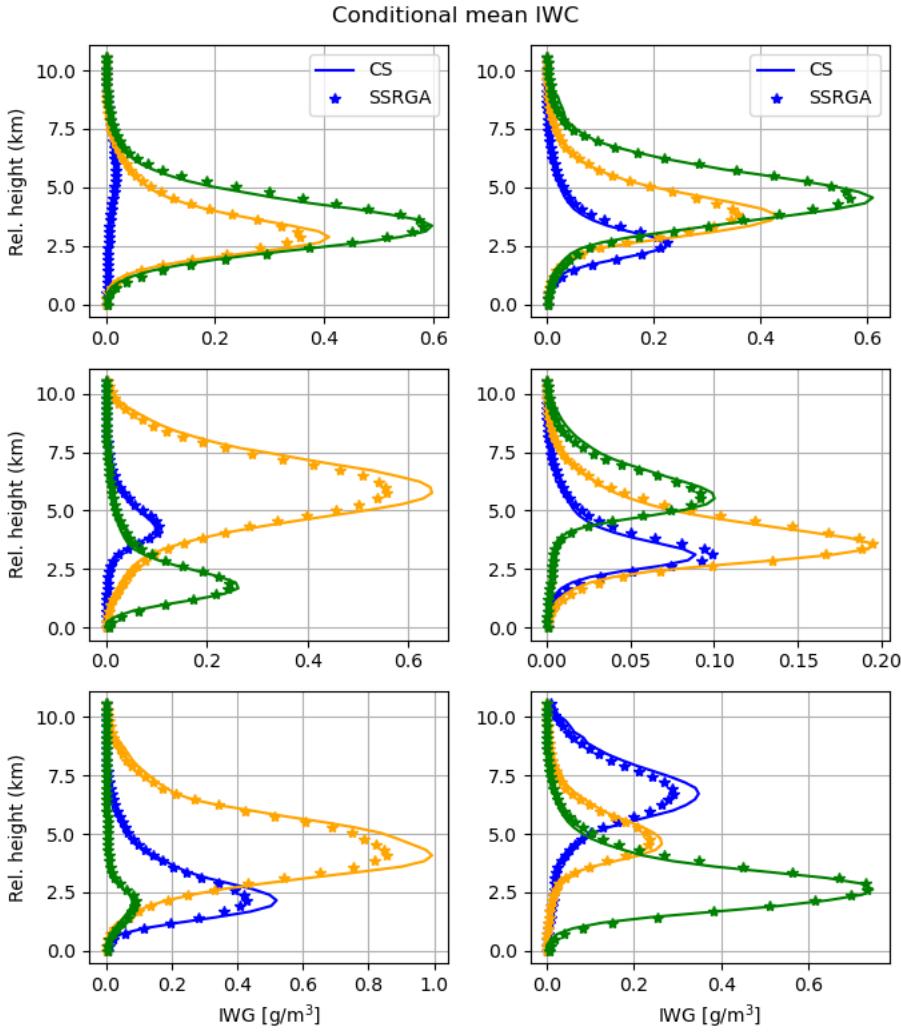
71 *a. Assumptions and forward models*

72 To quantify the number of ice particles in an elementary atmospheric volume as a function of
73 their size, we use normalized gamma functions (Bringi et al. 2003). The benefit of normalized
74 gamma functions is that they encapsulate the variability of Ice Water Content (IWC) - reflectivity
75 relationship into a single parameter, i.e. the normalized Particle Size Distribution (PSD) intercept
76 (Testud et al. 2001; Bringi et al. 2003). The normalized PSD intercept is defined as $N_w = \frac{4^4}{\pi \rho_w} \frac{IWC}{D_m^4}$,
77 where IWC is the ice water content associated with the PSD, and D_m is the mass weighted mean
78 diameter. Testud et al. (2001) showed that the variability in IWC reflectivity (Z) relationships may
79 be fully explained by variability in N_w , and that a formula of the type

$$IWC = N_w^{1-b} a Z^b \quad (1)$$

84 perfectly explains the relationships between IWC and Z calculated from observed PSDs. Equation
85 (1) is not sufficient to derive accurate, unbiased estimates of ice water contents, because N_w

varies considerably in time and space. Nevertheless, multiple studies showed that it is beneficial to parameterize N_w as a function of various variables, such as temperature (Hogan et al. 2006; Delanoë and Hogan 2008; Deng et al. 2010), rather than using N_w independent relations. In this study, we parameterize N_w as a function of temperature based on the CloudSat 2C-ICE product (Deng et al. 2010, 2013). Specifically, we cluster, based on similarity, a large set 2C-ICE profiles into 18 classes using a k-Means procedure. The mean IWC profiles associated with the 18 classes are shown in continuous lines in Figure 1. Alternative estimates, derived using PSD assumptions and electromagnetic scattering calculations that enable accurate and physically consistent simulations of radar observations at Ku-band and radiometer observations of submillimeter-wave frequencies are also shown in Figure 1. These estimates are based on the self-similarity Rayleigh-Gans approximation (SSRGA) of Hogan et al. (2017). Details regarding the estimation process are provided in the following paragraphs. As apparent in Figure 1, the CS and SSRGA estimates are in good agreement. Some discrepancies due to differences between the SSRGA N_w parameterization and the CS 2C-ICE "a priori assumptions" are also apparent, but they are not deemed critical in this study, whose objective is the investigation of synergistic lidar, Ku-band radar and submillimeter-wave radiometer retrievals, because the outcome is not likely to be sensitive to such details. One may notice that the average IWC profiles in Figure 1 are characterized by different peak values and heights. This facilitates a simple way to reverse-engineer to (some extent) the "a priori" assumptions used in the CS 2C-ICE product and use them in formulation of the type described in Equation (1). Specifically, the derivation of relationships of the type $IWC = a_i Z^{b_i}$ for every class i may be used to study a_i as a function of height. Shown in Figure 2 is a representation of the class multiplicative coefficient a_i as a function of relative height scatter plot. As apparent in the figure, and as expected, a_i exhibits a strong variation with the relative height. Coefficient b_i exhibits a height dependency as well (not shown), but the range of variation is significantly smaller, almost zero relative to the mean value of b . Given that any deviation of the multiplicative coefficient in an IWC-Z relation from an average is equivalent to a deviation of the associated N_w from its mean value (Testud et al. 2001), the variation of a as a function of relative-height may be converted into a N_w as a function of relative-height relationship. We, therefore, use the data in Fig. 2 to parameterize N_w as a function of the relative height.



80 FIG. 1. Mean CS IWC profiles for 18 classes derived using the k-Means clustering algorithm. Associated
 81 mean profiles derived from CS reflectivity observations derived using SSRGA scattering calculations and N_w
 82 parameterization developed in this study are shown using symbol *. The vertical coordinate is defined relative
 83 to the freezing level

115 For the determination of reference a and b values to be used with Equation (1), we assume that
 116 PSDs are normalized gamma distributions with $N_w = 0.08 \text{ cm}^{-4}$ and $\mu = 2$ and calculate

$$Z = \frac{\lambda^4}{\pi^5 |K_w|^2} \int_0^\infty N(D, D_m) \sigma_b(D) dD \quad (2)$$

Multiplicative factor in CloudSat 2ICE IWC-Z relation

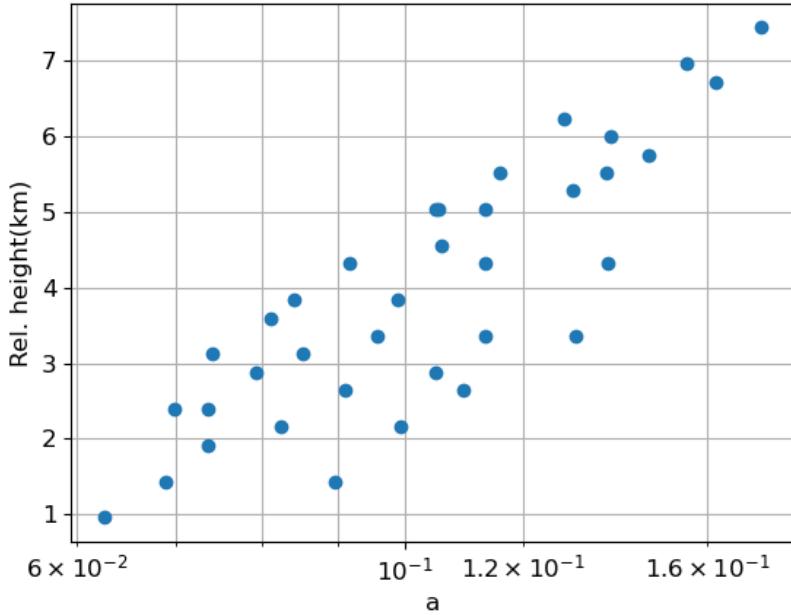
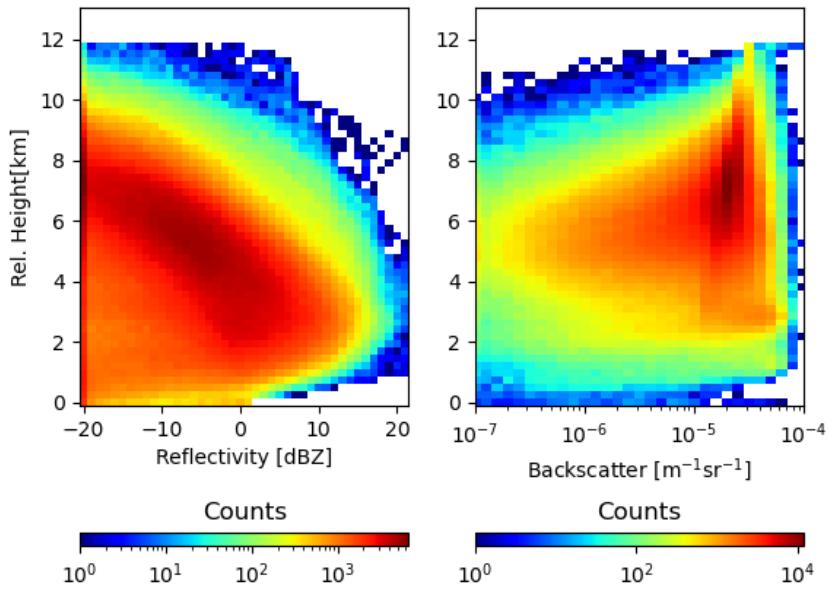


FIG. 2.

where λ is the radar frequency, $|K_w|$ is the dielectric factor of water, $N(D, D_m)dD$ is the number of ice particles of diameter with D and $D+dD$ per unit volume, D_m is the mass weighted mean diameter of the distribution, and $\sigma_b(D)$ is the backscattering cross-section of ice particle of diameter D . The mass weighted mean diameter is equidistantly sampled to span the entire range of IWC values in the CS 2C-ICE dataset. The assumed mass-size relation is that of Brown and Francis (1995) because it works well with the SSRGA scattering calculations (Heymsfield et al. 2022). The open source software scatter-1.1 of (Hogan 2019) is used to provide the actual scattering properties. The SSRGA theory was developed for millimeter and submillimeter-wave calculations and may not be applicable at lidar's wavelength. Therefore, for lidar calculations, we use the Mie solution included in the scatter-1.1 package. Although more accurate calculations based on more realistic ice particle shapes exist, they are rather incomplete and not readily available. Moreover, Wagner and Delene (2022) compared lidar backscatter observations with backscatter calculations based on coincident PSD observations and the Mie solution and found good agreement, which suggests that electromagnetic properties derived from Mie calculations are adequate for practical applications. The lidar molecular backscatter and extinction are calculated using the lidar module of the CFMIP Observation Simulator Package (COSP; Bodas-Salcedo et al. (2011)). To account for multiple-



136 FIG. 3. Simulated distributions of Ku-band radar reflectivity (left) and lidar backscatter (right) as function of
 137 height above the freezing level

133 scattering in the lidar observations, we are using the multiscatter-1.2.11 model (Hogan 2015) of
 134 Hogan and Battaglia (2008). Shown in Figure 3 are the distributions of simulated Ku-band radar
 135 reflectivity and lidar backscatter as function of height above the freezing level.

136 The radiometer observations are calculated using a one-dimensional efficient, but accurate,
 139 radiative transfer solver based on Eddington's approximation (Kummerow 1993). The Eddington's
 140 approximation has been found to work well in cloud and precipitation retrieval application despite
 141 its simplicity relative to more general (but also computationally intensive) approaches such as the
 142 Monte Carlo radiative transfer solvers (Liu et al. 1996) It should be noted tough that the phase
 143 functions of ice particles tend to be highly asymmetric at sub-millimeter wave frequencies. For
 144 radiative transfer solutions based on the Eddington's approximation to be accurate it is necessary that
 145 the delta-scaling approach (Joseph et al. 1976) be employed. The delta-scaling approach transforms
 146 the initial radiative transfer equation into an equivalent one characterized by a less asymmetric
 147 scattering function and more extinction, which makes the solution Eddington approximation more
 148 stable and accurate. The absorption due to water vapor and other gases is quantified using the

Rosenkranz model (Rosenkranz 1998). The water vapor, temperature, and pressure distributions are derived based on a WRF simulation of summer convection over the United States. Specifically, the water vapor, temperature, and pressure profiles associated with times and areas where the model produces anvils are selected and clustered into 40 classes using the k-Means approach. The mean extinction profiles at the radiometer frequencies are calculated for every class and used in process of calculating the brightness temperatures from the estimated ice profiles using a simple Monte Carlo procedure. That is, given a retrieved ice profile and its scattering property, an anvil class and its associated absorption, temperature, and pressure profiles are randomly selected and attached to the ice scattering properties. To make the procedure physically meaningful, temperature rather than height is used in the ice scattering-gas absorption collocation process. The emissivities are randomly chosen between 0.8 and 1.0 and assumed constant for all radiometer frequencies. Brightness temperatures are calculated at 89-, 183.31 ± 1.1 , and 325.15 ± 1.5 GHz, which correspond to three of the 10 channels of the SAPHIR-NG radiometer envisioned to be deployed in the AOS mission (Brogniez et al. 2022). The other channels are centered on the same water vapor absorption lines and are not likely to offer additional information in this rather controlled experiment. Nevertheless, the other channels are expected to be useful in reducing the uncertainties caused by variability in the vertical distribution of water vapor, which may be greater in real life than in the simulated environment.

The processing steps used to process the CS reflectivity observations and calculate the lidar, Ku-band and submillimeter-wave radiometer observations may be summarized as follows:

1. Derivation of physically consistent radar and radiometer lookup tables to relate basic radar and radiometer properties (e.g. reflectivity, attenuation, extinction, scattering-albedo, etc.) to PSD parameters such as IWC and D_m . The tables are derived for a single of N_w , but are usable with any value of N_w using the "normalization" operations described in (Grecu et al. 2011).
2. Derivation of Nw-relative height parameterization using the 2C-ICE product.
3. Estimation of IWC and related PSD parameters from CS W-band radar observations, using the tables constructed in Step 1 and parameterization derived in Step 2.

177 4. Calculation of lidar, Ku-band radar and radiometer observations from the estimates derived
178 in Step 3 and the tables obtained in Step 1.

179 The application of these steps produces a large dataset of approximately 200,000 cloud ice
180 profiles and associated lidar, radar and radiometer observations that may be used to investigate the
181 synergy of the three sensors. Details are provided in the next section.

182 *b. Estimation and evaluation*

183 Given that the lidar observations may attenuate quickly in thick clouds, while the Ku-band radar
184 will not detect clouds with an echo weaker than 8.0 dBZ, the radiometer is the instrument likely
185 to provide by itself the most complete information about the total amount of ice in its observing
186 volume. However, the vertical distribution of ice is difficult to quantify from radiometer-only
187 observations, because significantly different ice vertical distributions may lead to very similar
188 radiometer observations. This makes radiometer-only retrievals highly dependent on the "a priori"
189 information on the distribution of ice clouds in the atmosphere. As previously mentioned, this
190 is the reason why CS-based IWC retrievals were preferred to CRM simulations, as retrievals are
191 expected to result in more natural and less biased distributions.

192 We employ a two-step estimation methodology similar to that of Grecu et al. (2018). In the
193 first step, we estimate the IWC class, out of the 18 classes shown in Figure 1, to which the
194 estimated IWC profile is most likely to belong. The class is estimated directly from the synthetic
195 observations. In the second step, we estimate the IWC profile, using a class specific ensemble
196 Kalman Smoother (EKS) methodology similar to that of Grecu et al. (2018). The EKS algorithm
197 updates the estimated IWC relative to the mean IWC of the class to which the profile belongs. The
198 differences between the actual active and passive observations and their mean class values are used
199 in the update. The second step of this procedure is formally identical to the one used in Grecu
200 et al. (2018), but the first step is different. In Grecu et al. (2018), the first step was based on a
201 simple distance-based evaluation. That strategy is likely to be suboptimal in this study, because the
202 joint distribution of IWC profiles and associated observations are significantly more complex. We
203 therefore use a more complex classification methodology based on the TensorFlow library (Abadi
204 et al. 2016). The class estimation model is defined as a TensorFlow Model with two dense layers
205 of 30 neurons each, followed by a softmax layer (Goodfellow et al. 2016). The class estimation

206 model is trained using the 70% of the simulated observations and the corresponding IWC profiles,
207 the remaining 30% of the data being used for evaluation.

$$\mathbf{X} = \bar{\mathbf{X}}_i + \mathbf{Cov}(\mathbf{X}_i, \mathbf{Y}_i) \mathbf{Cov}(\mathbf{Y}_i, \mathbf{Y}_i)^{-1} (\mathbf{Y} - \bar{\mathbf{Y}}_i) \quad (3)$$

208 where \mathbf{X} is the state variable describing the IWC profile, \mathbf{Y} is the vector containing the variation, \mathbf{X}_i is
209 the set of state variables for profiles in class i , and \mathbf{Y}_i is the set of associated observations. Variables
210 $\bar{\mathbf{X}}_i$ and $\bar{\mathbf{Y}}_i$ are the mean values of the state variables and observations in class i , respectively. The
211 covariance matrices between \mathbf{X}_i and \mathbf{Y}_i are denoted by $\mathbf{Cov}(\mathbf{X}_i, \mathbf{Y}_i)$. In step 1, the class is estimated
212 using the TensorFlow model, while in step 2, the IWC profile is estimated using the EKS algorithm
213 summarized in Equation 3.

214 As already mentioned, a cross-validation methodology is used for evaluation, with 70% of the
215 data used for training and the remaining 30% of the data used for validation. The partition of
216 the data into training and evaluation subsets is done randomly. Usually, the partition, training
217 and evaluation steps are repeated several times. However, given the fact that differences in the
218 relationships between the ice property and their associated simulated observations are functions of
219 the meteorological context, and that all regimes are well-sampled in both the training and testing
220 subsets (e.g. out of every 10 pixels in a scene, about 7 end-up in the training dataset, while the others
221 in the testing dataset), the repetition of the partition, training, and evaluation steps multiple times
222 is not necessary. Therefore, in our evaluation, we partition the data into training and evaluation
223 only once and perform all the evaluation for a single partition. The evaluation criteria include the
224 correlation coefficient, the bias, and visual inspections of graphical representations of the estimated
225 properties relative to their references.

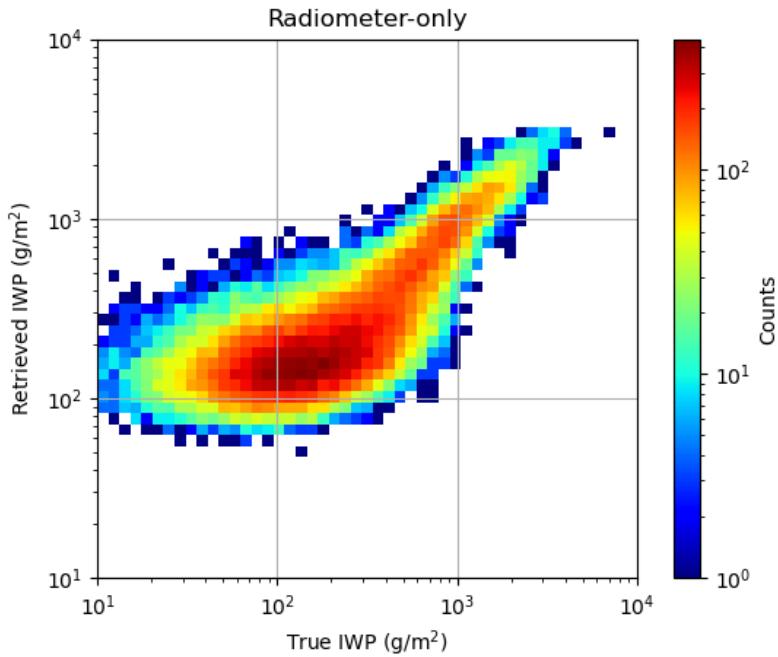
226 3. Results

227 a. Radiometer-only retrievals

228 As previously mentioned, submillimeter-wave radiometers are likely to provide by themselves
229 more complete information about the total amount of ice in their observing volumes than lidars
230 or Ku-band radars with limited sensitivity. However, radiometers observations are an integrated
231 measure of radiative process in clouds that provide little information about the vertical distribution

234 of ice. From this perspective, an evaluation in terms of the ice water path (*IWP*) defined as the
 235 vertical integral of the *IWC*, i.e. $IWP = \int_0^{Z_{top}} IWC(z)dz$ is insightful. Shown in Figure 4 is the
 236 frequency of *IWP* estimated from radiometer-only observations as a function of its true value. As
 237 apparent in the figure, there is good correlation between the retrieved and the true *IWP* values.
 238 The numerical value of the correlation coefficient is 0.92, and there is no-overall bias. That is, the
 239 mean values of retrieved *IWP* and true *IWP* values are equal. However, conditional biases are
 240 apparent, with overestimation of *IWP* for values smaller than 100 g/m^2 and some underestimation
 241 for values larger than 1000 g/m^2 . The biases at the low end of the *IWP* range are not surprising,
 242 given that the impact caused by ice scattering on the total radiometric signal is small for low
 243 values of *IWP* and hard to distinguish from other sources of variability in radiometer observations.
 244 Saturation effects are most likely responsible for underestimation at the high end. It should be
 245 noted that in this evaluation, only atmospheric profiles that exhibit ice detectable by the CS radar
 246 are used. Therefore, a radiometer-only estimation procedure derived from this training dataset
 247 is likely to result in significant overestimation if not used in conjunction with a discrimination
 248 procedure. However, such procedure is not critical in this study, as the lidar observations may be
 249 used to discriminate between clear skies and ice clouds. Although the radiometer-only estimation
 250 procedure is able to estimate the integrated amount of ice in clouds fairly well, its ability to
 251 characterize the vertical distribution of ice in clouds is limited. Figure 5 shows the conditional
 252 vertical distributions of the estimated and true *IWC* for the 18 classes described in Section 2a and
 253 shown in Figure 1. As apparent in the figure, there are significant differences between the estimated
 254 and true *IWC* profiles.

255 Further insight into the radiometer-only estimation performance may be derived by defining the
 256 ice profile gravity center (GC) as $z_{GC} = \frac{\int_0^{Z_{top}} zIWC(z)dz}{\int_0^{Z_{top}} IWC(z)dz}$, where z is the distance relative to the
 257 freezing level, the Z_{top} is the distance from the top of the atmosphere to the freezing level. Shown
 258 in Figure 6 is the frequency of *IWC* gravity center estimated from radiometer-only observations
 259 as a function of its true value. It may be observed in the figure that while the true *IWC* gravity
 260 center exhibits quite a broad distribution, the one retrieved from the radiometer-only observations
 261 exhibits a multimodal narrow distribution. Moreover, there is almost no correlation between the
 262 retrieved and the true *IWC* gravity center. This is another indication that, while the total amount



228 FIG. 4. Frequency plot of estimated IWP derived radiometer-observations as a function of the true IWP used
 229 in observations synthesis

263 of ice may be reasonably estimated from radiometer-only observations, its vertical distribution can
 264 not be determined from radiometer-only observations.

265 *b. Synergistic retrievals*

266 The synergy of the instrument on the estimates may be investigating by simply incorporating lidar
 267 and radar observations into the retrieval process and comparing the results with the radiometer-
 268 only estimates. Although the lidar observations are subject to attenuation, they are able to provide
 269 information about the vertical distribution of ice in clouds, especially at the top of the clouds. The
 270 radar observations, on the other hand, are able to provide information in the bottom part of the
 271 clouds, where the lidar signal is below the noise level due to attenuation. Therefore, the combined
 272 used of lidar and radar observations is expected to provide a more complete characterization of
 273 the vertical distribution of ice in clouds and enable the derivation of more specific estimates than
 274 those derived from radiometer-only observations.

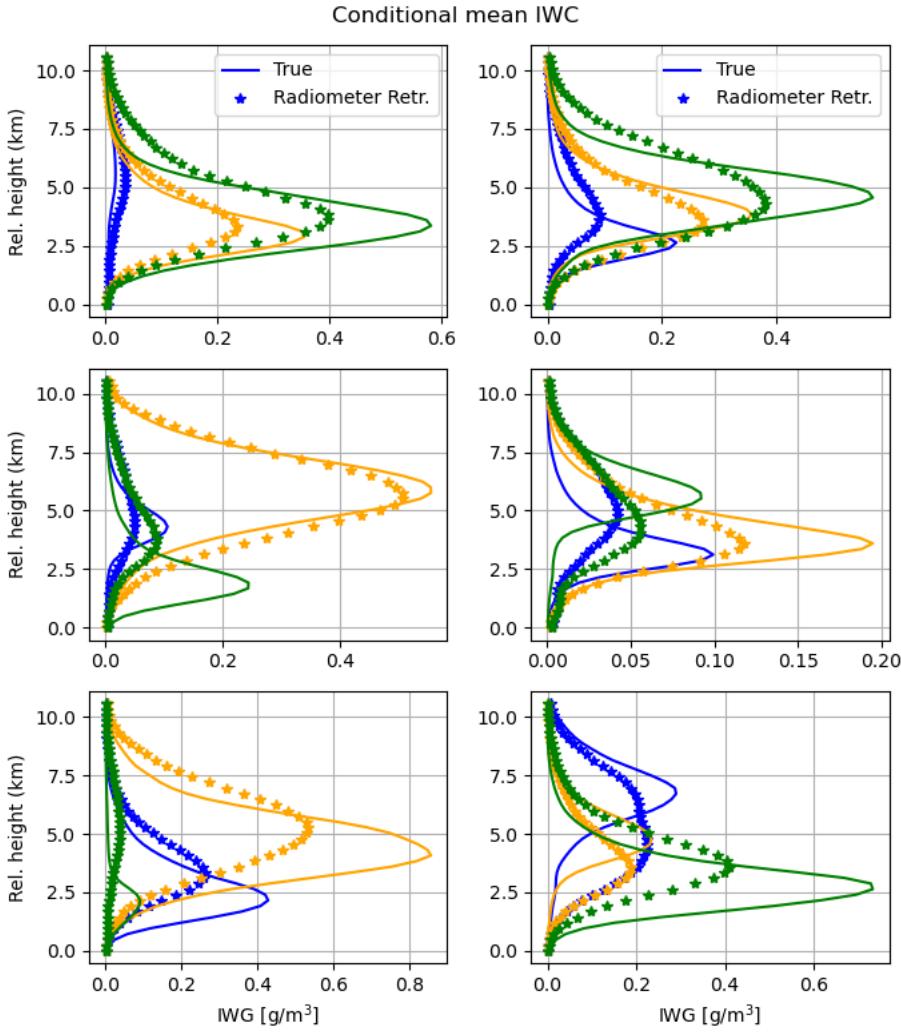


FIG. 5. True and radiometer-only retrieved conditional mean IWC for the 18 classes described in Figure 1.

275 Shown in Figure 7 is the distribution of the synergistic IWP estimates as a function of their
 276 true values. As apparent in the figure, the synergistic IWP estimates are more accurate than the
 277 radiometer-only estimates. At the same time, as apparent in Figure 8, the retrieved conditional
 278 mean IWC for the 18 classes described section 2a and shown in Figure 1 are in significantly better
 279 (almost perfect) agreement with the true IWC profiles than those derived from radiometer-only
 280 observations. Furthermore, as seen in Figure 8 the synergistic IWC gravity center estimates are in
 281 very good agreement with the true IWC gravity center.

282 While the estimates based on all instruments are significantly more accurate than those based on
 283 radiometer-only observations, it is useful to investigate how the two active instruments (lidar and

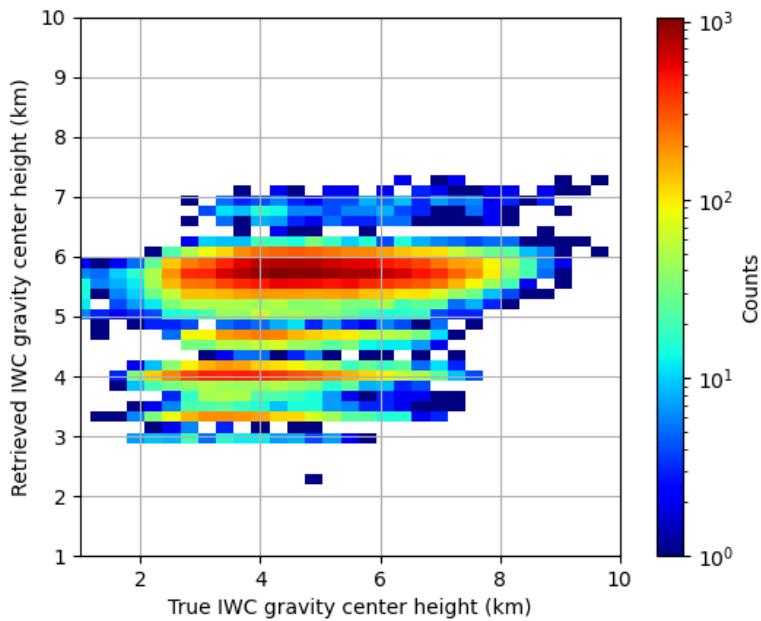


FIG. 6. Same as in Figure 4, but for the *IWC* gravity center.

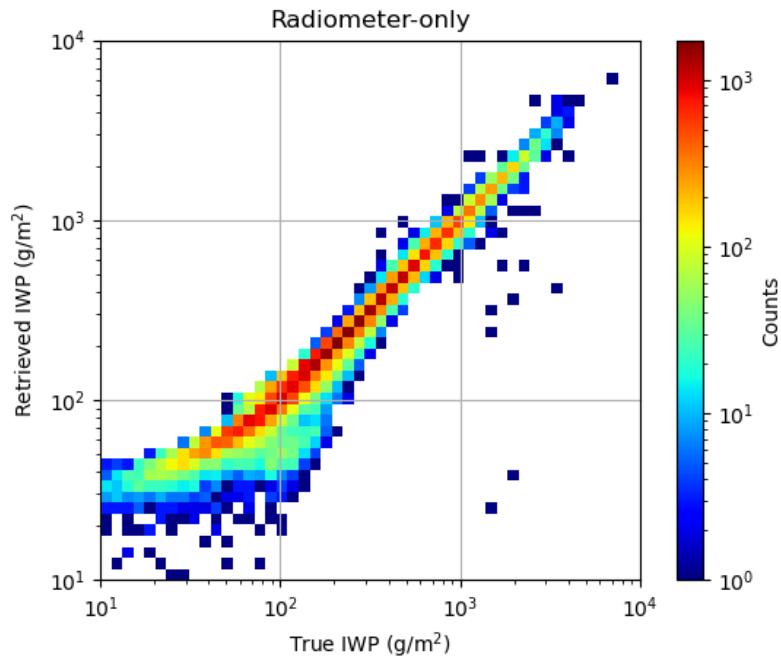


FIG. 7. Same as in Figure 4, but with the lidar and radar observations incorporated in the retrievals.

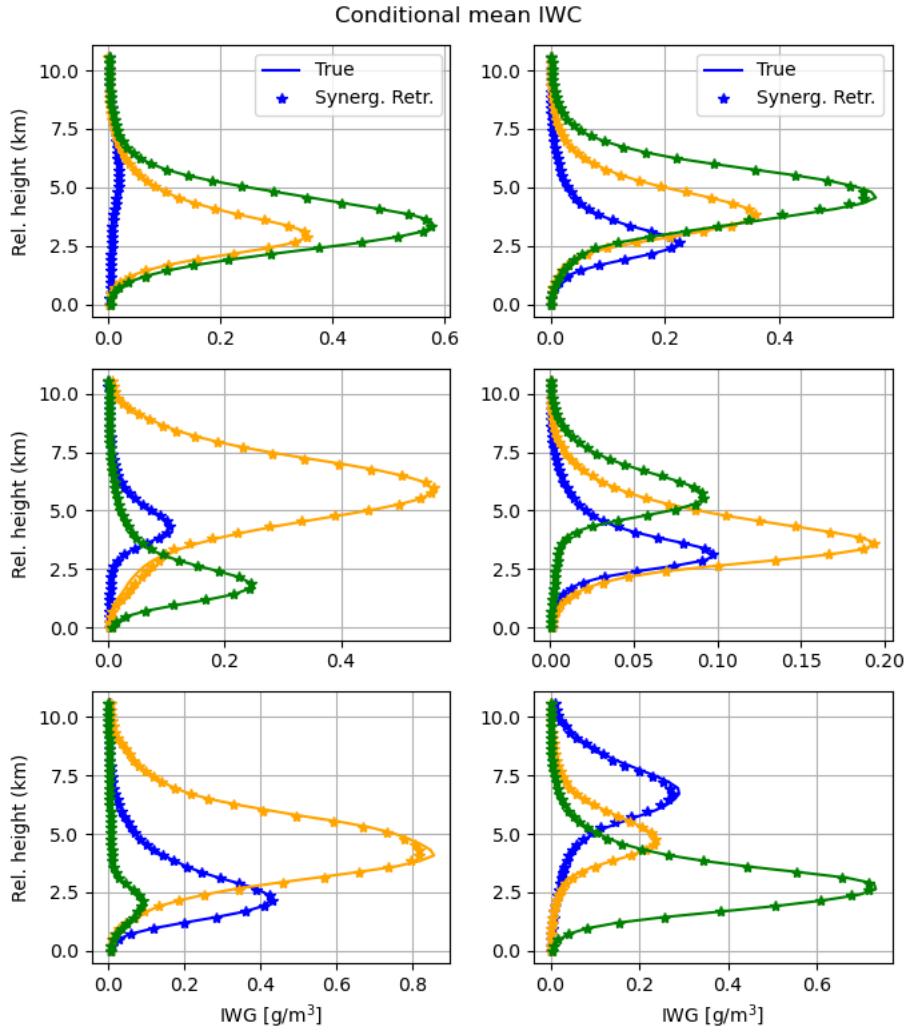


FIG. 8. Same as in Figure 5, but with the lidar and radar observations incorporated in the retrievals.

radar) impact the estimates. For conciseness, we used two statistical scores, namely, the normalized root mean square (NRMS) and the classification accuracy, to summarize the performance of the estimates. The NRMS is defined as

$$NRMS = \frac{\sqrt{\frac{\sum_{i=1}^N (IWC_i - IWC_{true,i})^2}{N}}}{\sqrt{\frac{\sum_{i=1}^N (IWC_{true,i} - \bar{IWC})^2}{N}}} \quad (4)$$

where IWC_i is the estimated IWP for the i -th sample, $IWC_{true,i}$ is the true IWC for the i -th sample, \bar{IWC} is the IWC mean, and N is the size of the estimation dataset. The classification accuracy is

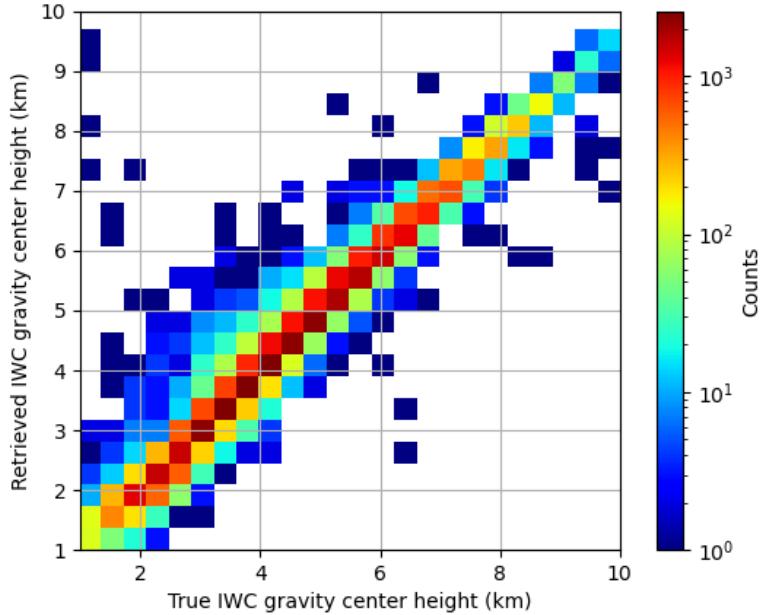


FIG. 9. Same as in Figure 6, but with the lidar and radar observations incorporated in the retrievals.

289 defined as

$$CA = \frac{\sum_{i=1}^N \delta_i}{N} \quad (5)$$

290 where δ_i is a binary variable that is equal to 1 if the estimated IWC class for the i -th sample is
291 equal to the true IWC class for the i -th sample, and 0 otherwise. The performance summary is
292 shown in Table 1 for several combinations of instruments. It may be observed in the table that the
293 performance of the estimates based on all instruments is significantly better than those based on
294 radiometer-only observations. Furthermore, the inclusion of the lidar observations in the retrieval
295 process has a larger impact on the retrieval performance than the inclusion of the radar observations.
296 This is expected since the lidar observations are able to provide information about the top of the
297 clouds, where the radar observations are above the noise level only occasionally. Nevertheless, the
298 inclusion of the radar observations in the retrieval process has a notable impact on the accuracy of
299 the IWC estimates relative to radiometer-only retrievals.

TABLE 1. Performance summary.

Score \ Instruments	Radiometer	Radar-Radiometer	Lidar-Radiometer	Radar-Lidar-Radiometer
NRMS	0.73	0.59	0.32	0.22
Class. Accuracy	0.39	0.48	0.92	0.94

300 4. Conclusions

301 In this study, we investigate the synergy of lidar, Ku-band radar, and sub-millimeter-wave
 302 radiometer measurements in the retrieval of the ice from satellite observations. The synergy is
 303 analyzed through the generation of a large dataset of IWC profile and the calculation of lidar, radar
 304 and radiometer observations using realistic models. The characteristics of the instruments (e.g.
 305 frequencies, sensitivities, etc.) are set based on the expected characteristics of instruments of the
 306 AOS mission. A cross-validation methodology is used to assess the accuracy of the retrieved IWC
 307 profiles from various combinations of observations from the three instruments. Specifically, the
 308 IWC and associated observations is randomly divided into two datasets, one for the training and
 309 the other for the evaluation. The training dataset is used to train the retrieval algorithm, while the
 310 evaluation dataset is used to assess the retrieval performance.

311 To ensure the self-consistency of results and their relevance to practical applications, the dataset
 312 of IWC profiles is derived from CloudSat reflectivity observations. Although subject to potential
 313 biases and uncertainties due to deficiencies in the retrieval models, these profiles are deemed to
 314 be more realistic than those derived from cloud resolving model simulations. Moreover, they
 315 are roughly consistent with the 2C-ICE CloudSat product (Deng et al. 2015), while relying on
 316 assumptions and parameterizations that enable the accurate computation of backscatter lidar, Ku-
 317 band radar, and sub-millimeter-wave radiometer observations.

318 The retrieval of the ice water content (IWC) profiles from the computed observations is achieved
 319 in two steps. In the first step, a class, out of 18 potential classes characterized by different vertical
 320 distribution of IWC, is estimated from the observations. The 18 classes are predetermined based on
 321 k-Means clustering algorithm. In the second step, the IWC profile is estimated using an Ensemble
 322 Kalman Smoother (EKS) algorithm that uses the estimated class as a priori information.

323 The results of the study show that the synergy of lidar, radar, and radiometer observations is
 324 significant in the retrieval of the IWC profiles. The inclusion of the lidar observations in the retrieval

325 process has a larger impact on the retrieval performance than the inclusion of the radar observations.
326 Although results are not directly comparable to those from other studies (Pfreundschuh et al.
327 2020; Liu and Mace 2022), given the differences between the instruments in this study relative
328 to those from other studies, it may be concluded that they are not inconsistent with previous
329 studies. Specifically, previous studies show some skills in radiometer-only retrievals and significant
330 improvements in the retrieval performance when the active observations are incorporated. From
331 this perspective, our findings are consistent with previous studies.

332 Further work is necessary out to assess the impact of sources of uncertainties such as variability
333 in the PSD intercept not captured by the current parameterization, differences in the instruments'
334 footprint sizes, and non-uniform beam filling on the retrievals of the IWC profiles. Other sources of
335 uncertainties that need be considered include the potential existence of supercooled liquid water in
336 the clouds and uncertainties in the electromagnetic scattering properties used in the in instruments'
337 forward models.

338 *Acknowledgments.* This work was supported by the NASA Remote Sensing Theory project
339 through Grant 80NSSC20K1729. The authors thank Dr. Lucia Tsaoussi (NASA Headquarters) for
340 her support of this effort.

341 *Data availability statement.* The CloudSat data can be accessed at:
342 <https://www.cloudsat.cira.colostate.edu/>.

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