Homework 1

Group 2
02/27/2019

Part 1: Overview

The purpose of this assignment is to explore, analyze and model professional baseball team performance from the years 1871 to 2006. Our objective is to build a multiple linear regression model on the provided data to predict the number of wins for the team.**

Dependencies

Replication of our work requires the following dependencies:

```
library(dplyr)
library(tidyr)
library(ggplot2)
library(car)
library(corrplot)
library(Hmisc)
library(psych)
library (MASS)
library(lmtest)
library(faraway)
library(knitr)
```

Data Preparation

We first read the training and test data from the csv files located in our repository.

```
train_data <- "moneyball-training-data.csv"
test_data <- "moneyball-evaluation-data.csv"
moneyball_data <- read.csv(train_data, header=TRUE, stringsAsFactors=FALSE, fileEncoding="latin1")
test_data <- read.csv(test_data, header = TRUE, stringsAsFactors = FALSE)</pre>
```

Part 2: Data Exploration

Upon review of the dataset, we found large amounts of missing variables. We choose to replace the empty data points with the mean of that data column. The method was preferable to removing the data with omitted values, because that would have removed 90% of the provided data.

We calculated the appropriate means to compensate for the incomplete data below:

```
sapply(moneyball_data, function(y) sum(length(which(is.na(y)))))/nrow(moneyball_data)*100
```

```
##
              INDEX
                         TARGET WINS
                                        TEAM BATTING H TEAM BATTING 2B
##
           0.000000
                            0.000000
                                              0.000000
                                                               0.000000
                     TEAM BATTING HR
##
   TEAM BATTING 3B
                                      TEAM BATTING BB
                                                        TEAM BATTING SO
##
           0.000000
                            0.00000
                                              0.000000
                                                               4.481547
##
   TEAM BASERUN SB
                     TEAM_BASERUN_CS TEAM_BATTING_HBP
                                                        TEAM PITCHING H
                                             91.608084
##
           5.755712
                           33.919156
                                                               0.000000
## TEAM PITCHING HR TEAM PITCHING BB TEAM PITCHING SO
                                                        TEAM FIELDING E
                            0.000000
##
           0.000000
                                              4.481547
                                                               0.000000
## TEAM_FIELDING_DP
          12.565905
##
```

sapply(test_data, function(y) sum(length(which(is.na(y)))))/nrow(moneyball_data)*100

```
##
              INDEX
                      TEAM_BATTING_H
                                      TEAM_BATTING_2B
                                                        TEAM BATTING 3B
##
          0.0000000
                           0.0000000
                                             0.0000000
                                                              0.0000000
##
   TEAM BATTING HR
                     TEAM BATTING BB
                                      TEAM_BATTING_SO TEAM_BASERUN_SB
##
          0.0000000
                           0.0000000
                                             0.7908612
                                                              0.5711775
   TEAM BASERUN CS TEAM BATTING HBP
                                      TEAM PITCHING H TEAM PITCHING HR
##
##
          3.8224956
                          10.5448155
                                             0.0000000
                                                              0.0000000
## TEAM PITCHING BB TEAM PITCHING SO
                                      TEAM FIELDING E TEAM FIELDING DP
          0.0000000
##
                           0.7908612
                                             0.0000000
                                                              1.3620387
```

We also choose to removed "index" and "TEAM_BATTING_HBP" columns as "TEAM_BATTING_HBP" has 92% of missing values" and "index" was just a counter.

```
moneyball_data<-subset(moneyball_data, select = -c(INDEX))
moneyball<-subset(moneyball_data, select = -c(TEAM_BATTING_HBP))

test_data <- subset(test_data, select = -c(INDEX))
test_data <- subset(test_data, select = -c(TEAM_BATTING_HBP))</pre>
```

Summary Statistics

Through these steps, we replaced the missing data with the appropriate mean data.

```
replace_mean <- function(x){
    x <- as.numeric(as.character(x))
    x[is.na(x)] = mean(x, na.rm=TRUE)
    return(x)
}
moneyball_filled <- apply(moneyball, 2, replace_mean)
moneyball_filled <- as.data.frame(moneyball_filled)

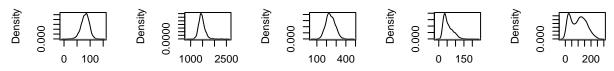
test_filled <- apply(test_data, 2, replace_mean)
test_filled <- as.data.frame(test_data)</pre>
```

TEAM_BATTING_H	1469.3900
TEAM_BATTING_2B	241.3205
TEAM_BATTING_3B	55.9112
TEAM_BATTING_HR	95.6332
TEAM_BATTING_BB	498.9575
TEAM_BATTING_SO	NA
TEAM_BASERUN_SB	NA
TEAM_BASERUN_CS	NA
TEAM_PITCHING_H	1813.4633
TEAM_PITCHING_HR	102.1467
TEAM_PITCHING_BB	552.4170
TEAM_PITCHING_SO	NA
TEAM_FIELDING_E	249.7490
TEAM_FIELDING_DP	NA

Histogram

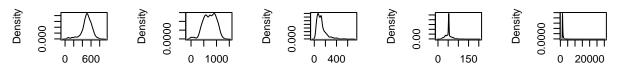
Now that we have a 'good' dataset, we can look at some histograms for each data vector. Our output suggests that most variables are fairly normally distributed and span many orders of magnitude. This tells us that our model will have some kind scaling factor between our data vectors.

t(x = moneyball_fillα = moneyball_filled{= moneyball_filled\$ = moneyball_filled\$ = moneyball_filled\$



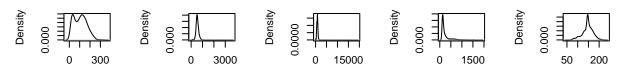
N = 2276 Bandwidth = 3 N = 2276 Bandwidth = 2 N = 2276 Bandwidth = 8 N = 2276 Bandwidth = 5 N = 2276 Bandwidth = 1

= moneyball_filled\$= moneyball_filled\$= moneyball_filled\$= moneyball_filled\$\text{} = moneyball_filled



N = 2276 Bandwidth = 1 N = 2276 Bandwidth = 4 N = 2276 Bandwidth = 1 N = 2276 Bandwidth = 1 N = 2276 Bandwidth = 3

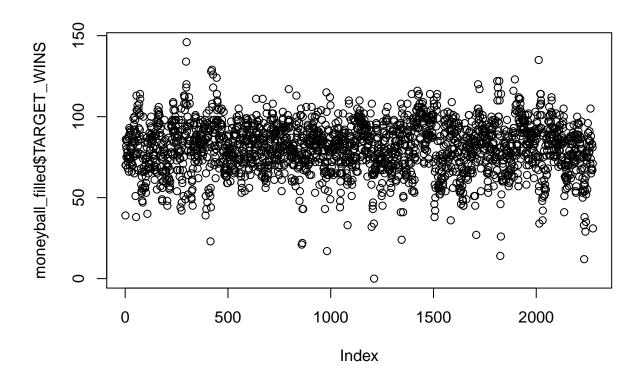
= moneyball_filled\$\text{\text{\text{=}}} moneyball_filled\$\text{\text{\text{=}}} moneyball_filled\$\text{\text{\text{=}}} moneyball_filled\$\text{\text{\text{\text{-}}}}



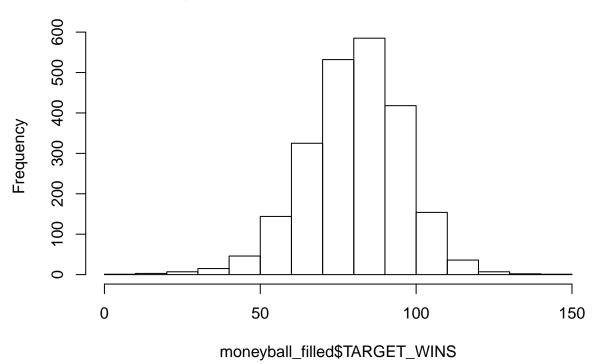
N = 2276 Bandwidth = 1 N = 2276 Bandwidth = 1 N = 2276 Bandwidth = 4 N = 2276 Bandwidth = 1 N = 2276 Bandwidth

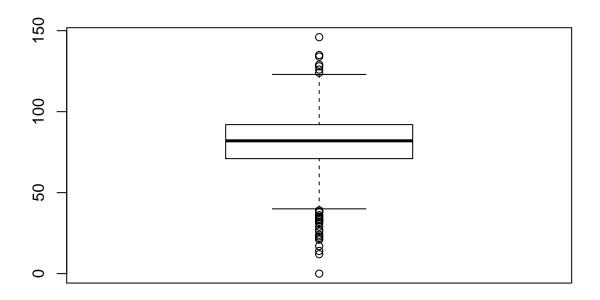
Target Wins Variable

To better understand the goal of our model, we examined the targeted wins variable. Below are the plots that show this variable follows a normal, unimodal distribution that is slightly skewed to the left.



Histogram of moneyball_filled\$TARGET_WINS

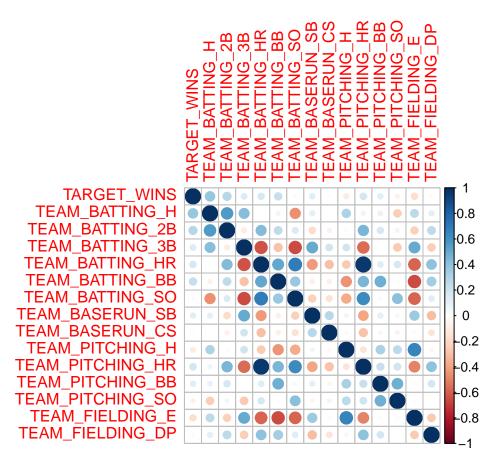




```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.00 71.00 82.00 80.79 92.00 146.00
```

Correlation

We then checked for correlation among our dependent variables, as all variables are numeric we will rely on correlation. Below is a correlation plot that highlights the correlation between various data vectors. Dark blue is a high, positive correlation and dark red is a large negative correlation.



Here, we notice several variables have poor correlation with the target variable (p<0.1):

- TEAM_FIELDING_E
- TEAM_BASERUN_CS
- TEAM_BATTING_SO
- TEAM_BATTING_3B

However, others have strong correlation between each others (>0.6):

- TEAM_PITCHING_HR vs TEAM_BATTING_HR (0.969)
- TEAM_BATTING_HR vs TEAM_BATTING_SO (0.693)
- TEAM_BATTING_3B vs TEAM_BATTING_SO (-0.656)

Due to co-linearity or statistical irrelevance, we can remove: TEAM_FIELDING_E, TEAM_BASERUN_CS, TEAM_BATTING_SO, TEAM_BATTING_3B, and TEAM_BATTING_HR.

Part 3: Modeling

Model 1

We started with a naive model that uses all of the data vectors. We got an adjusted R^2 value of 31.4%.

```
##
## Call:
## Im(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
##
## TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BATTING_SO +
##
## TEAM_BASERUN_SB + TEAM_BASERUN_CS + TEAM_PITCHING_H + TEAM_PITCHING_HR +
```

```
TEAM_PITCHING_BB + TEAM_PITCHING_SO + TEAM_FIELDING_E + TEAM_FIELDING_DP,
##
##
       data = moneyball_filled)
##
## Residuals:
##
               1Q Median
                               3Q
                                      Max
  -49.994
           -8.576
                    0.136
                            8.345
                                   58.628
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    2.502e+01 5.397e+00
                                           4.636 3.75e-06 ***
## TEAM_BATTING_H
                    4.824e-02 3.687e-03
                                         13.085 < 2e-16 ***
                   -2.006e-02
## TEAM_BATTING_2B
                               9.152e-03
                                          -2.192 0.028486 *
## TEAM_BATTING_3B
                    6.047e-02 1.676e-02
                                           3.608 0.000315 ***
## TEAM_BATTING_HR
                    5.299e-02 2.743e-02
                                           1.932 0.053488 .
## TEAM_BATTING_BB
                    1.042e-02 5.818e-03
                                           1.790 0.073544
## TEAM_BATTING_SO
                   -9.349e-03
                               2.551e-03
                                          -3.665 0.000253 ***
## TEAM_BASERUN_SB
                    2.949e-02 4.462e-03
                                           6.610 4.78e-11 ***
## TEAM BASERUN CS
                   -1.188e-02 1.614e-02
                                          -0.736 0.461905
## TEAM_PITCHING_H -7.342e-04
                               3.676e-04
                                          -1.997 0.045946 *
## TEAM PITCHING HR 1.480e-02
                               2.432e-02
                                           0.609 0.542877
## TEAM_PITCHING_BB 8.891e-05
                               4.145e-03
                                           0.021 0.982891
## TEAM PITCHING SO 2.843e-03
                               9.187e-04
                                           3.095 0.001994 **
## TEAM_FIELDING_E -2.112e-02
                               2.480e-03
                                          -8.516
                                                  < 2e-16 ***
## TEAM FIELDING DP -1.210e-01 1.302e-02 -9.297 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.04 on 2261 degrees of freedom
## Multiple R-squared: 0.3189, Adjusted R-squared: 0.3147
## F-statistic: 75.63 on 14 and 2261 DF, p-value: < 2.2e-16
```

Then, we removed the least significant variable, TEAM_PITCHING_BB. This yielded a slight increase in our R^2 score at 31.5%.

```
##
## Call:
  lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
       TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BATTING_SO +
       TEAM_BASERUN_SB + TEAM_BASERUN_CS + TEAM_PITCHING_H + TEAM_PITCHING_HR +
##
       TEAM_PITCHING_SO + TEAM_FIELDING_E + TEAM_FIELDING_DP, data = moneyball_filled)
##
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -49.994 -8.576
                    0.136
                             8.345
                                   58.626
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                            4.640 3.67e-06 ***
## (Intercept)
                    25.0145796
                                5.3904993
## TEAM_BATTING_H
                     0.0482393
                                0.0036807
                                           13.106 < 2e-16 ***
## TEAM_BATTING_2B
                    -0.0200575
                                0.0091490
                                           -2.192 0.028457 *
## TEAM_BATTING_3B
                     0.0604730 0.0167556
                                            3.609 0.000314 ***
```

```
## TEAM BATTING HR
                    0.0527106 0.0240710
                                            2.190 0.028641 *
## TEAM_BATTING_BB
                               0.0033664
                    0.0105175
                                           3.124 0.001805 **
## TEAM BATTING SO
                   -0.0093631
                               0.0024585
                                          -3.809 0.000144 ***
## TEAM_BASERUN_SB
                    0.0295055
                               0.0044087
                                            6.693 2.76e-11 ***
## TEAM BASERUN CS
                   -0.0118872
                               0.0161276
                                          -0.737 0.461155
## TEAM PITCHING H
                   -0.0007306
                               0.0003283
                                          -2.225 0.026147 *
## TEAM PITCHING HR 0.0150659
                               0.0209923
                                            0.718 0.473025
## TEAM_PITCHING_SO 0.0028567
                               0.0006717
                                            4.253 2.20e-05 ***
## TEAM_FIELDING_E -0.0211192
                               0.0024784
                                          -8.521
                                                  < 2e-16 ***
## TEAM_FIELDING_DP -0.1210298
                               0.0130139
                                          -9.300 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.04 on 2262 degrees of freedom
## Multiple R-squared: 0.3189, Adjusted R-squared: 0.315
## F-statistic: 81.49 on 13 and 2262 DF, p-value: < 2.2e-16
```

We repeated the above procedure for TEAM_BASERUN_CS, netting us a score of 31.52%. By removing two variables we were able to oh-so-slightly increase our R^2 value while reducing the amount of data we have to track and the processing time for tracking it.

```
##
## Call:
## lm(formula = TARGET WINS ~ TEAM BATTING H + TEAM BATTING 2B +
##
       TEAM BATTING 3B + TEAM BATTING HR + TEAM BATTING BB + TEAM BATTING SO +
       TEAM_BASERUN_SB + TEAM_PITCHING_H + TEAM_PITCHING_HR + TEAM_PITCHING_SO +
##
##
       TEAM_FIELDING_E + TEAM_FIELDING_DP, data = moneyball_filled)
##
## Residuals:
##
       Min
                1Q
                    Median
                                3Q
                                       Max
  -49.905
           -8.584
                     0.124
                             8.406
                                    58.593
##
##
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    24.2348098
                                5.2851330
                                            4.585 4.78e-06 ***
## TEAM BATTING H
                     0.0482055
                                                   < 2e-16 ***
                                0.0036800
                                           13.099
                                           -2.224 0.026235 *
## TEAM_BATTING_2B
                    -0.0203302
                                0.0091405
## TEAM BATTING 3B
                     0.0608466
                                0.0167463
                                            3.633 0.000286 ***
## TEAM_BATTING_HR
                     0.0543985
                                0.0239594
                                            2.270 0.023274 *
## TEAM_BATTING_BB
                     0.0107643
                                0.0033494
                                            3.214 0.001328 **
## TEAM BATTING SO
                                           -3.800 0.000148 ***
                    -0.0093418
                                0.0024580
## TEAM BASERUN SB
                     0.0287600
                                0.0042906
                                            6.703 2.57e-11 ***
## TEAM PITCHING H
                    -0.0007390
                                0.0003281
                                           -2.253 0.024372 *
## TEAM_PITCHING_HR 0.0147103
                                            0.701 0.483372
                                0.0209846
## TEAM_PITCHING_SO 0.0028640
                                0.0006716
                                            4.265 2.08e-05 ***
## TEAM_FIELDING_E -0.0207217
                                0.0024188
                                           -8.567
                                                   < 2e-16 ***
## TEAM_FIELDING_DP -0.1211603
                                0.0130114
                                           -9.312
                                                   < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.04 on 2263 degrees of freedom
```

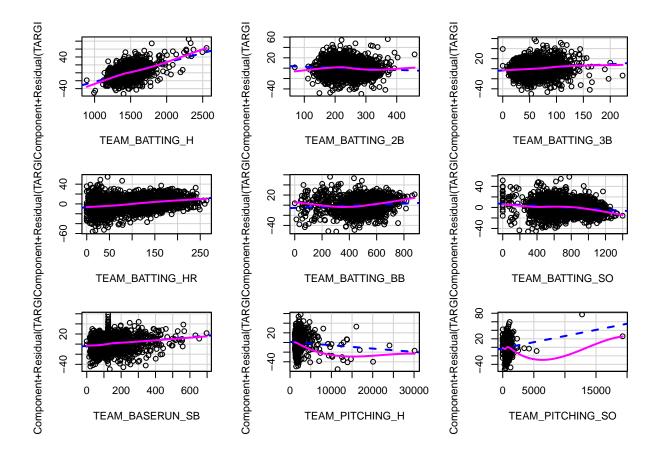
```
## Multiple R-squared: 0.3188, Adjusted R-squared: 0.3152
## F-statistic: 88.25 on 12 and 2263 DF, p-value: < 2.2e-16</pre>
```

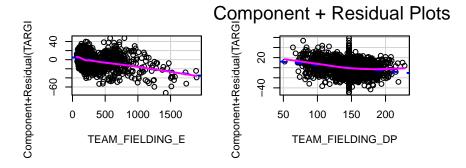
By removing TEAM_PITCHING_HR, we increase our R^2 value one last time to 31.53%.

```
##
## Call:
## lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
##
      TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BATTING_SO +
##
       TEAM_BASERUN_SB + TEAM_PITCHING_H + TEAM_PITCHING_SO + TEAM_FIELDING_E +
       TEAM_FIELDING_DP, data = moneyball_filled)
##
##
## Residuals:
##
      Min
                10 Median
                               3Q
                                      Max
##
  -49.899
           -8.568
                    0.091
                            8.397
                                   58.651
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   23.6666983 5.2220414
                                           4.532 6.14e-06 ***
## TEAM_BATTING_H
                    0.0484570 0.0036621
                                         13.232 < 2e-16 ***
## TEAM BATTING 2B
                   -0.0205123 0.0091358
                                          -2.245 0.024847 *
## TEAM_BATTING_3B
                                           3.767 0.000170 ***
                    0.0624661 0.0165843
## TEAM_BATTING_HR
                    0.0697785 0.0096266
                                           7.249 5.75e-13 ***
## TEAM BATTING BB
                    0.0107446 0.0033489
                                           3.208 0.001354 **
## TEAM BATTING SO
                   -0.0093019 0.0024571
                                          -3.786 0.000157 ***
## TEAM_BASERUN_SB
                    0.0287708 0.0042901
                                           6.706 2.51e-11 ***
## TEAM_PITCHING_H -0.0006920
                               0.0003211
                                          -2.155 0.031253 *
## TEAM_PITCHING_SO 0.0028867
                                           4.304 1.75e-05 ***
                               0.0006707
## TEAM_FIELDING_E -0.0205973
                               0.0024120
                                         -8.540 < 2e-16 ***
## TEAM_FIELDING_DP -0.1210083  0.0130082  -9.302  < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.03 on 2264 degrees of freedom
## Multiple R-squared: 0.3186, Adjusted R-squared: 0.3153
## F-statistic: 96.25 on 11 and 2264 DF, p-value: < 2.2e-16
```

Evaluate Non-linearity

Below we use the crPlots() function to check for non-linearity.





TEAM_PITCHING_H, TEAM_PITCHING_SO did not pass the check for non-linearity. So, we will transform them and refit the model. We are using a log10 transform because these numbers span many orders of magnitude.

```
##
##
  Call:
##
   lm(formula = TARGET WINS ~ TEAM BATTING H + TEAM BATTING 2B +
##
       TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BATTING_SO +
##
       TEAM_BASERUN_SB + TEAM_PITCHING_H + TEAM_PITCHING_SO + TEAM_FIELDING_E +
##
       TEAM_FIELDING_DP, data = moneyball_filled)
##
   Residuals:
##
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
   -53.500
            -8.353
                     0.050
                              8.276
                                     63.152
##
##
##
   Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    -18.385299
                                 13.648651
                                            -1.347 0.178102
## TEAM_BATTING_H
                       0.041874
                                  0.003784
                                            11.065
                                                     < 2e-16 ***
## TEAM_BATTING_2B
                      -0.020476
                                            -2.249 0.024630 *
                                  0.009106
## TEAM_BATTING_3B
                      0.087638
                                  0.016862
                                              5.197 2.20e-07 ***
  TEAM_BATTING_HR
                      0.058540
                                  0.009697
                                              6.037 1.83e-09 ***
## TEAM_BATTING_BB
                      0.012944
                                  0.003388
                                              3.821 0.000137 ***
## TEAM BATTING SO
                      -0.001186
                                  0.002534
                                            -0.468 0.639742
## TEAM_BASERUN_SB
                                              7.311 3.65e-13 ***
                      0.031437
                                  0.004300
## TEAM PITCHING H
                      17.140905
                                  4.594173
                                              3.731 0.000195 ***
                                            -2.904 0.003717 **
## TEAM_PITCHING_SO
                     -2.656620
                                  0.914734
```

```
## TEAM_FIELDING_E -0.030455 0.002954 -10.309 < 2e-16 ***

## TEAM_FIELDING_DP -0.120505 0.013004 -9.267 < 2e-16 ***

## ---

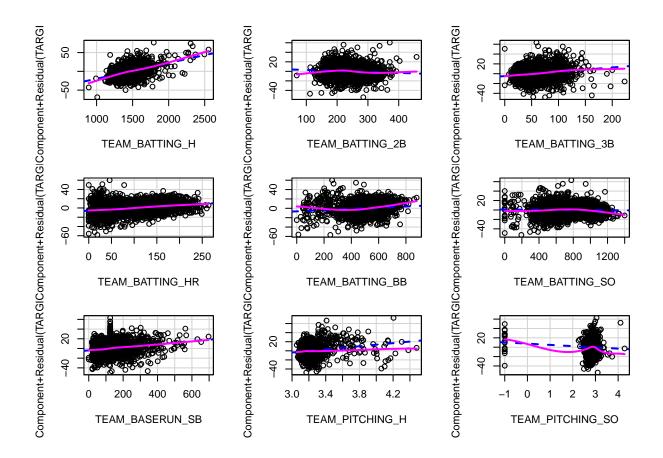
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

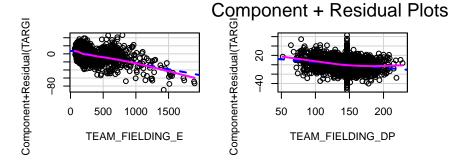
##

## Residual standard error: 13.03 on 2264 degrees of freedom

## Multiple R-squared: 0.319, Adjusted R-squared: 0.3157

## F-statistic: 96.42 on 11 and 2264 DF, p-value: < 2.2e-16
```



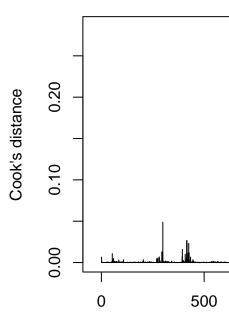


Now we remove TEAM_BATTING_SO because it has a p-value > 0.05.

```
##
## Call:
  lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
##
##
       TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BASERUN_SB +
##
       TEAM_PITCHING_H + TEAM_PITCHING_SO + TEAM_FIELDING_E + TEAM_FIELDING_DP,
##
       data = moneyball_filled)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
   -53.382
           -8.328
                     0.025
                              8.211
                                     62.933
##
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                           -1.595 0.110905
## (Intercept)
                    -20.516367
                                12.864856
## TEAM_BATTING_H
                      0.042628
                                  0.003424
                                            12.448 < 2e-16 ***
## TEAM_BATTING_2B
                     -0.021583
                                  0.008792
                                            -2.455 0.014167 *
## TEAM_BATTING_3B
                      0.089227
                                             5.403 7.23e-08 ***
                                  0.016513
## TEAM_BATTING_HR
                      0.055774
                                  0.007688
                                             7.255 5.50e-13 ***
## TEAM_BATTING_BB
                      0.013293
                                  0.003304
                                             4.023 5.93e-05 ***
## TEAM BASERUN SB
                      0.030879
                                  0.004130
                                             7.476 1.09e-13 ***
## TEAM_PITCHING_H
                     17.440250
                                  4.548668
                                             3.834 0.000129 ***
## TEAM_PITCHING_SO
                     -2.847123
                                  0.819083
                                            -3.476 0.000519 ***
## TEAM_FIELDING_E
                     -0.030494
                                  0.002953 -10.328 < 2e-16 ***
## TEAM FIELDING DP
                     -0.119878
                                  0.012932
                                            -9.270 < 2e-16 ***
## ---
```

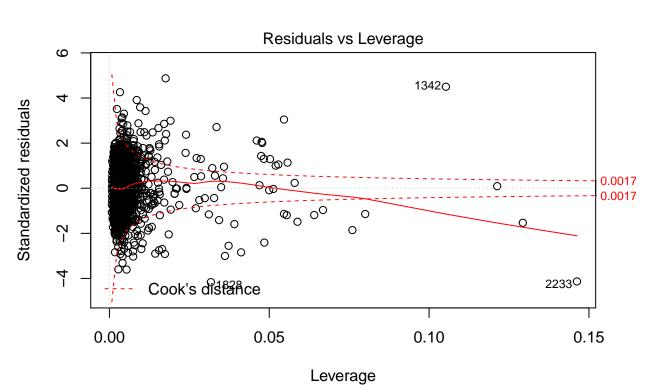
```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.03 on 2265 degrees of freedom
## Multiple R-squared: 0.319, Adjusted R-squared: 0.316
## F-statistic: 106.1 on 10 and 2265 DF, p-value: < 2.2e-16</pre>
```

Eliminating Outliers



ARGET_WINS ~ TEAM_BATTI

Then, we used Cook's distance to identify extreme values, removing them as necessary.



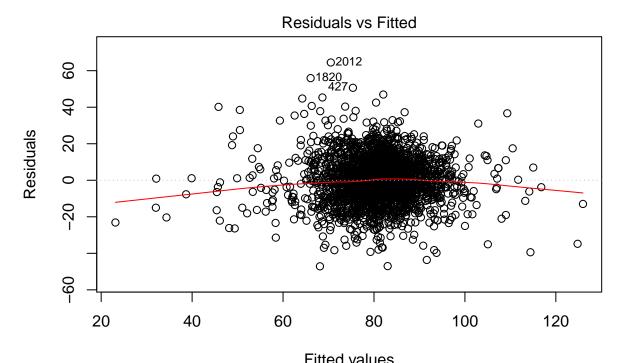
ARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B + TEAM_BATTING_3B + 1

Then, we re-fit the model to the new data, yielding our highest R^2 value of 31.57%.

```
##
## Call:
## lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
       TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BATTING_SO +
##
       TEAM_BASERUN_SB + TEAM_PITCHING_H + TEAM_PITCHING_SO + TEAM_FIELDING_E +
##
##
       TEAM FIELDING DP, data = moneyball filled)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                      Max
## -47.117 -8.396
                     0.026
                             8.238 64.496
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -18.936246 14.300248 -1.324 0.185574
## TEAM_BATTING_H
                     0.039743
                                0.003901
                                          10.187 < 2e-16 ***
                    -0.021808
## TEAM_BATTING_2B
                                0.009043
                                          -2.412 0.015957 *
## TEAM_BATTING_3B
                     0.101540
                                0.016844
                                          6.028 1.93e-09 ***
## TEAM_BATTING_HR
                     0.065471
                                0.009640
                                           6.791 1.41e-11 ***
## TEAM_BATTING_BB
                     0.012322
                                0.003354
                                           3.674 0.000245 ***
                                          -0.584 0.559106
## TEAM_BATTING_SO
                    -0.001465
                                0.002507
## TEAM BASERUN SB
                     0.032302
                                           7.556 5.99e-14 ***
                                0.004275
## TEAM_PITCHING_H
                                           3.814 0.000140 ***
                     18.926032
                                 4.961698
## TEAM_PITCHING_SO
                     -3.560746
                                0.932952
                                          -3.817 0.000139 ***
## TEAM FIELDING E
                     -0.031367
                                0.003048 -10.291 < 2e-16 ***
## TEAM FIELDING DP
                   -0.120207
                                0.012872 -9.339 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.89 on 2261 degrees of freedom
## Multiple R-squared: 0.3245, Adjusted R-squared: 0.3212
## F-statistic: 98.72 on 11 and 2261 DF, p-value: < 2.2e-16
```

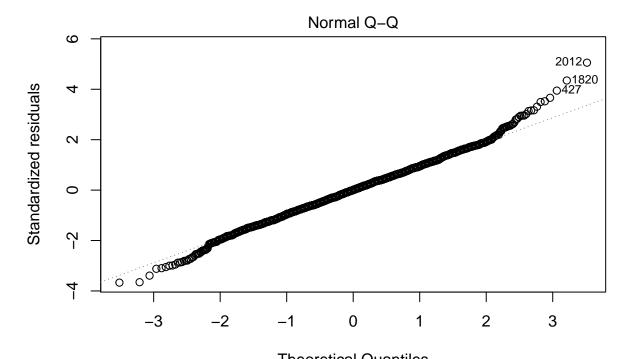
Checking for Colinearity

```
TEAM_BATTING_H TEAM_BATTING_2B
##
                                       TEAM_BATTING_3B
                                                         TEAM_BATTING_HR
##
           4.322088
                             2.438948
                                               3.007291
                                                                4.650721
    TEAM_BATTING_BB
                     TEAM_BATTING_SO
##
                                       TEAM_BASERUN_SB
                                                         TEAM_PITCHING_H
           2.294133
                             5.045176
                                               1.812464
                                                                5.617980
##
## TEAM_PITCHING_SO
                     TEAM_FIELDING_E TEAM_FIELDING_DP
           1.722976
                             6.490171
                                               1.364366
##
```



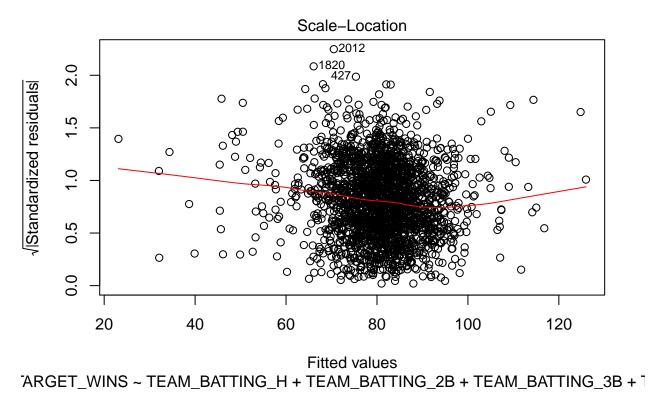
Fitted values

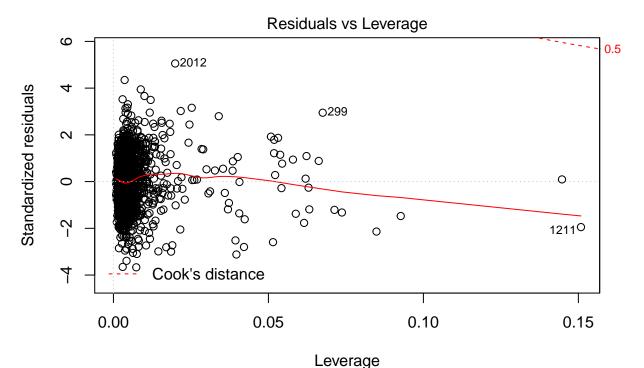
ARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B + TEAM_BATTING_3B + 7



Theoretical Quantiles

ARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B + TEAM_BATTING_3B + 7





ARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B + TEAM_BATTING_3B + 1

TEAM_FIELDING_E is withing the range 5-10 (suggesting co linearity with other variables), but eliminating TEAM_FIELDING_E does not improve the model. This yields our highest R^2 value with 40% of the variance explained by our model.

```
##
## Call:
  lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
       TEAM_BATTING_3B + TEAM_BATTING_HR + TEAM_BATTING_BB + TEAM_BATTING_SO +
##
       TEAM_BASERUN_SB + TEAM_PITCHING_H + TEAM_PITCHING_SO + TEAM_FIELDING_E +
##
##
       TEAM_FIELDING_DP, data = moneyball_data)
##
##
  Residuals:
##
       Min
                                 3Q
                1Q
                    Median
                                        Max
                                     29.766
   -32.317
            -7.199
                     0.121
                              7.045
##
##
   Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                    58.312951
                                 6.019406
                                            9.687
                                                   < 2e-16 ***
                                           -0.943 0.34594
## TEAM_BATTING_H
                                 0.010615
                     -0.010007
## TEAM_BATTING_2B
                    -0.049989
                                 0.008875
                                            -5.633 2.05e-08 ***
## TEAM_BATTING_3B
                      0.181788
                                 0.018982
                                            9.577
                                                    < 2e-16 ***
## TEAM_BATTING_HR
                      0.100845
                                 0.009158
                                           11.012
                                                    < 2e-16 ***
## TEAM_BATTING_BB
                                           10.870 < 2e-16 ***
                      0.034055
                                 0.003133
```

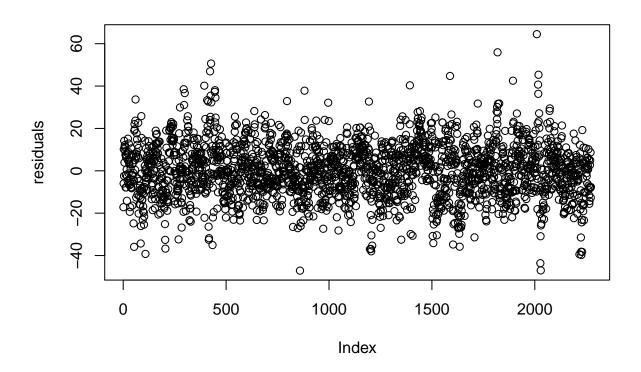
```
## TEAM BATTING SO
                     0.045928
                                 0.016420
                                                   0.00521 **
                                            2.797
                                                   < 2e-16 ***
##
  TEAM_BASERUN_SB
                     0.069889
                                           12.626
                                 0.005535
                     0.037438
  TEAM PITCHING H
                                 0.009239
                                            4.052 5.29e-05
  TEAM_PITCHING_SO
                                           -4.217 2.59e-05 ***
                    -0.065427
                                 0.015514
  TEAM FIELDING E
                    -0.116444
                                 0.007029
                                          -16.566
                                                   <
                                                     2e-16
  TEAM FIELDING DP -0.112850
                                           -9.190
                                                   <
##
                                 0.012279
                                                     2e-16 ***
##
  Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
##
  Residual standard error: 10.19 on 1823 degrees of freedom
     (441 observations deleted due to missingness)
## Multiple R-squared: 0.4045, Adjusted R-squared:
  F-statistic: 112.6 on 11 and 1823 DF, p-value: < 2.2e-16
```

Part 4: Model Evaluation

Using our finished model above, we can predict the number of wins for each team. We rounded to a whole number so that the finished values have some real world analogue. The F-statistics has a p value of basically 0, so we can determine that our model is statistically significant.

```
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                        NA
                             74
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##
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                            82
                                 78
```

Additionally, we can use a residual plot to verify our model. We can see that our model's residuals are fairly normal and randomly distributed. They also are centered and zero.



Min. 1st Qu. Median Mean 3rd Qu. Max. ## -47.11665 -8.39565 0.02552 0.00000 8.23798 64.49592