

1. Introduction

The global COVID-19 pandemic has sent shockwaves throughout the entire world and will likely have long-reaching effects on human behavior and culture. There are an incredible number of unknowns and so any investigations into data-driven models are useful. Two of the more difficult aspects of this problem are the number of unknown factors and the time delayed effects. The time delay is due to both incubation time as well as the existence of asymptomatic carriers. Additionally, human behavior also contributes to the time delayed effect because people do not instantaneously change their routines. To help governments as well as citizens, I prepare a collection of models which forecast the future number of new cases. As this is mainly an educational project, I only focus on forecasting a single day into the future due to the rate at which these models degrade. To arrive at a quality model, I first examine, clean and wrangle the datasets, explore them, and then test the different model types before creating the final deliverable model.

2. Data

In order to create a good predictive model I utilize a number of different datasets, choosing and creating numerical features that are believed to contain the most useful subset of information. The original datasets contain information on case numbers, test numbers, government responses, and many other relevant quantities. While there is considerable overlap between these datasets, there are inconsistencies in reporting and quality between the datasets. This is examined in more detail in the data exploration notebook; the discussion is too specific to serve any purpose here as it does not directly affect the modeling phase of this project. The datasets used here are dynamic; changing everyday to include the most recent information. More specifically I use four different datasets which contain global data, that is, data on a large number of countries around the world.

The datasets I use are: the John's Hopkins CSSE (JHU) dataset on cases, recovered, deaths, etc. The "Our World in Data" (OWID) dataset contains case information as well as time independent quantities such as population, rate of smokers, percentage of population above 65 years of age, and many more features. The Oxford COVID-19 Government Response Tracker (OxCGRT) dataset contains the responses of various governments in regards to quarantine measures as well as governmental aid for its citizens. The most important feature is their "government response index" which quantifies each government's response with a score ranging from 0-100. The fourth and final data set comes from the FIND test tracker dataset which tracks

testing around the world (also contains case information but this is copied from JHU, per their description).

Because I am aggregating multiple datasets, it is important that they are consistent with each other, therefore, I apply a number of different wrangling and cleaning steps to the data. This produces separate datasets for exploration and model training purposes. I find it the most convenient to use the python package Pandas to perform these tasks. The specific operations are best described in the notebooks, and so their discussion is withheld from this report. The links to the datasets (or repositories) are included at the end of this report.

3. Data Cleaning and Wrangling

The first of the cleaning steps is to rename the columns and location names such that they are consistent between DataFrames. This is done via a combination of Pandas operations, regular expressions, and custom functions. In addition, each dataset has a unique set of locations and dates for which it is defined. For this reason, the data used for modeling contains only the countries and dates which are present in all of the data sets, i.e. the intersection. The main motivating factor behind this idea is to contain as few missing values as possible.

I also modify the data when it seems sensible; such as imputing missing values, fixing reporting errors, ensuring that cumulative variables are indeed non-decreasing. These modifications are mainly to reduce any confusions that may otherwise arise in the data exploration process. Perhaps the most important wrangling step I perform is to engineer a number of moving averages of the time dependent features. These features are useful in conveying time dependence to the regression models. I elect to use moving averages of widths 3, 7, 14 days. The motivations for these widths are to capture multiple time scales, to account and capture seasonality effects, and to capture the time delayed nature of the spread of the infection.

4. Exploration

The COVID-19 pandemic has overshadowed the world since mid to late March 2020, when most countries had at least one recorded case. While the age of the pandemic is approaching four months old for most countries, globally the COVID-19 pandemic seems to be worsening. This is partly due to what I refer to as “quarantine fatigue”. This is a name I give to social unrest which prompts government officials to relax social distancing restriction. To get an idea for how badly the

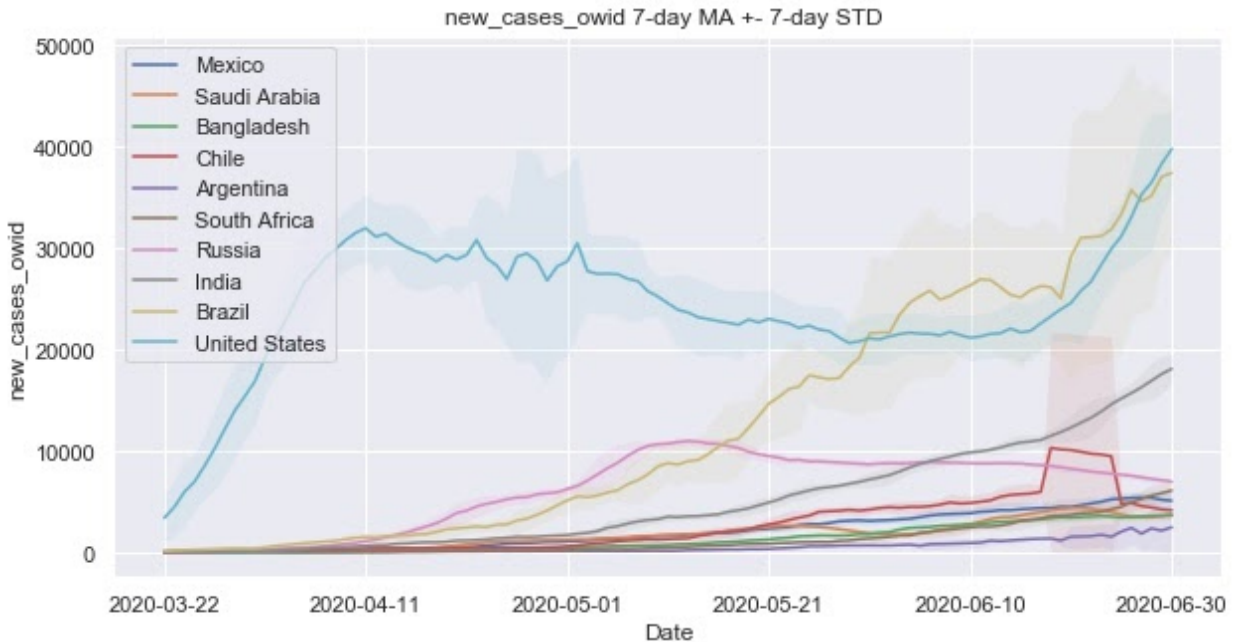


Figure 1: The 7-day moving averages of the 10 countries with highest number of new cases,

current state of the world pandemic is, Figure 1 displays the ten countries which had the highest number of new cases and new deaths (3-day moving average) as of June 30th, 2020. I investigate the first of these qualities by comparing the average reaction time with the current (June 30th) death rate. For the strength of the government's reaction, I investigate whether or not the number of new cases is related to the OxCGRT's "stringency index". Lastly, the different types of responses (school closings, public transport closings, etc.) are investigated by using two dimensional ANOVA analysis to look for statistical relationships between different countries and the types of reactions, using the change in new cases per million people before and after each mandate. A criticism of this usage of Anova is that the different factors in this case are not truly independent, but it is only supposed to serve as a crude measure of the effectiveness of different measures.

I define the "average reaction time" as the average date of the implementation of all government mandates. This can (and is) only computed for countries which indeed enacted all different quarantine measures. The death rate is computed by the number of deaths per capita divided by the number of new cases per capita. Note that positive average reaction time indicates that the country reacted after its first case.

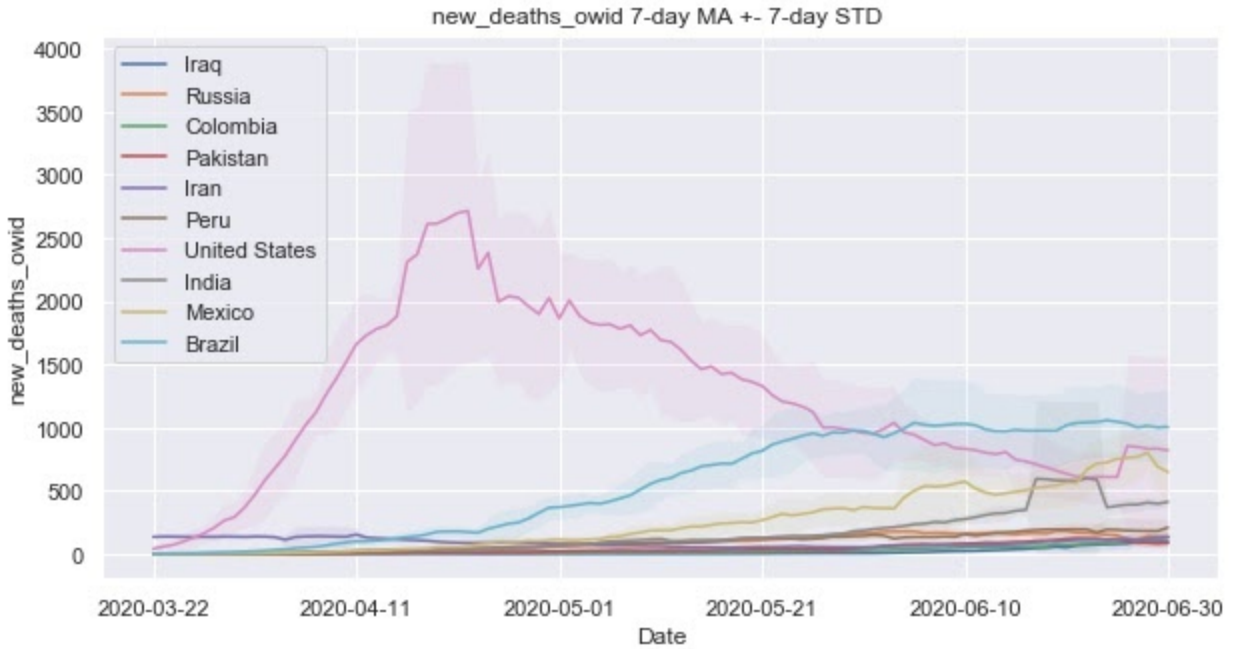


Figure 2 : The 7-day moving average of the number of new deaths, for the countries from figure 1.

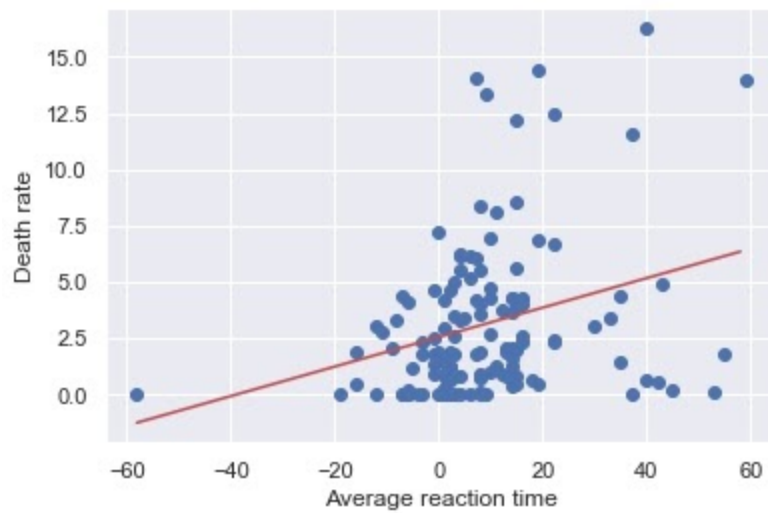


Figure 3 : The current death rate plotted against the “average reaction time” of each government. Average reaction time is calculated by taking the average of the dates of each government mandate.

This provides an intuitive result which can be summarized by the following statement: countries that are slow to respond to the pandemic suffer more as a consequence. This leads us to my next analysis, given that government intervention is necessary, how strong does said intervention need to be? To explore this, I will first compare two countries which have drastically different outcomes, before looking at the set of all countries.

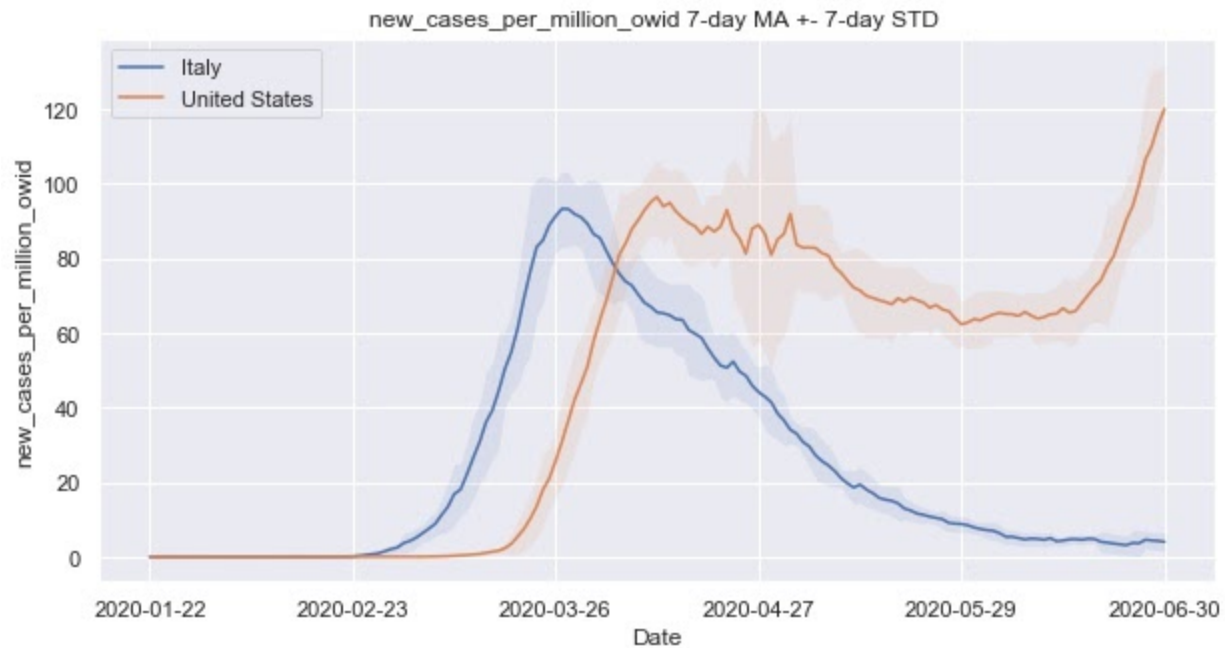


Figure 4: The comparison of the time series for the new cases per million people

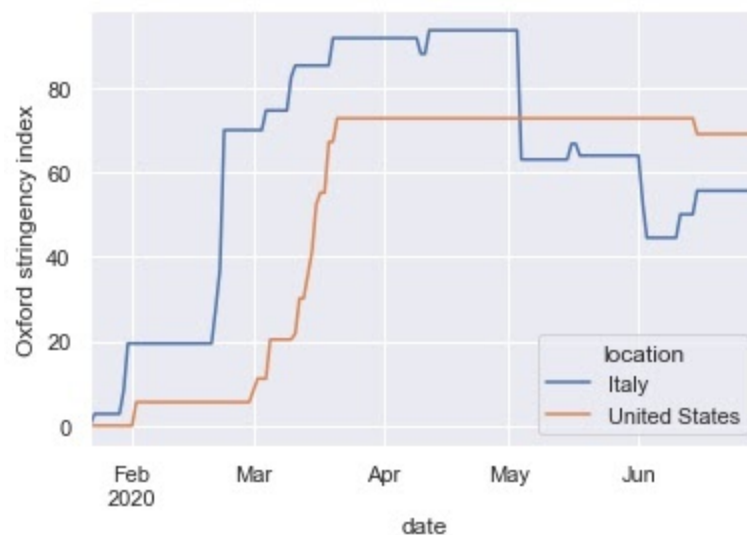


Figure 5: The time series of the OxCGRT “stringency index” for Italy and the United States.

Although Italy had a similar number of cases per million as the United States (and earlier on, when less information on the disease was out), their reaction and subsequent actions seem to have (at least temporarily) quelled the pandemic. As can be seen in Figure 4, the United States likely did not control the pandemic enough, leading to a much smaller decrease followed by a dramatic increase in the number of cases per million. To analyze the differences between each country's reaction, I utilize the OxCGRT dataset's "stringency index", which is a quantification for how each government responded to the pandemic, in terms of quarantine measures.

Using Figure 5 to compare the United States and Italy, we see that the Italian government was much more strict when their cases per million were peaking in late March. Once the pandemic was under control, however, this allowed for them to loosen restrictions sooner. This of course is a biased sample of two countries, taken to be a representation of the best and worst case scenarios. I will now attempt to extend this analysis to all countries.

4.1 The effect of government actions

The differences between the behavior of the pandemic begs the question, how do government actions affect the spread of COVID19? To investigate this effect, I look to the relationship between the stringency index and the number of new cases (per million). I'm going to utilize 30-day averages in an attempt to only capture the longest time scale and not the seasonality of the pandemic. Specifically I'm going to look at the relationship between the average (and max) stringency index and percentage increase (or decrease) between the average number of new cases two months ago and the previous month.

Before jumping right into the problem, I first wanted to get a general idea as to whether this is a plausible hypothesis or not. The easiest way of doing so is to simply plot the global stringency average versus the average number of new cases per million people. As can be seen in Figure 6, they seem to have some inverse proportionality, at least from May forward. Assuming this serves as evidence that my main hypothesis is at least plausible, I begin the full analysis. I engineer three quantities to investigate the effect of stringency. The average number of new cases per million people in the past 30 days, the same quantity between 60 and 30 days ago, and the average stringency between 60 and 30 days ago (used the maximum as well, see COVID19_eda.ipynb).

The main quantity I engineer is the difference of case number averages in the previous 30-days and between 30 and 60 days ago. These case number differentials are compared to the average stringency from 60 to 30 days ago using univariate regression. By using this time period for the average stringency, I am assuming that there is a very significant delay with respect to changes in stringency.

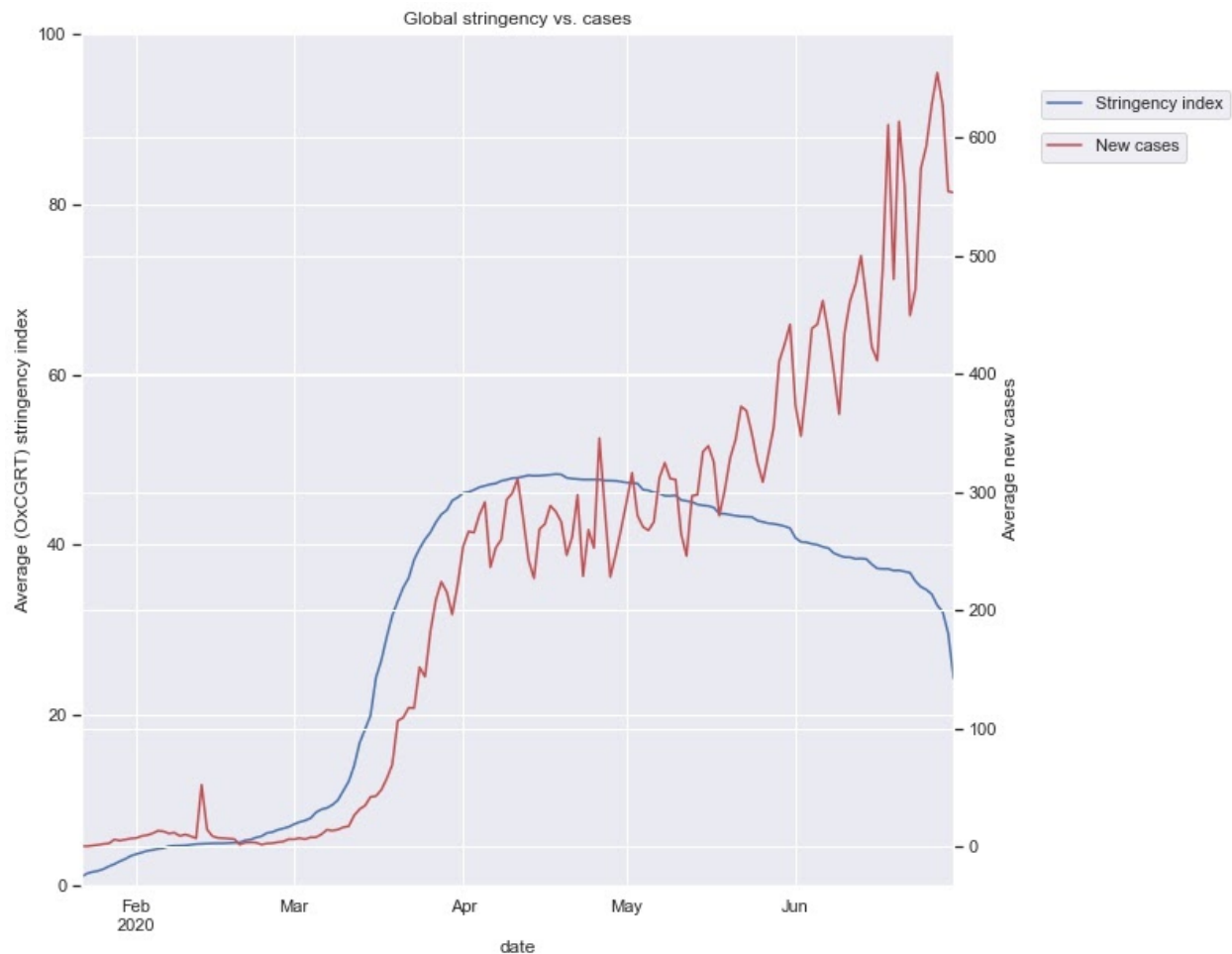


Figure 6 : The OxCGRT government response index vs. the number of new cases per million people, global averages.

The result of my analysis shows that the average case differential does in fact share a relationship with the average stringency index, using a 95% confidence interval. However, the result is not one I expected, but it makes sense in hindsight. It does not show that more stringent countries have a better reduction in case numbers; rather, more stringent countries have worsening positions. My interpretation of this is that countries with worsening epidemics are forced to become more stringent, but they are reacting too late and so it doesn't affect the new case numbers immediately, hence the reason for the increase. Reminder that negative case differential here means that the average case number increases.

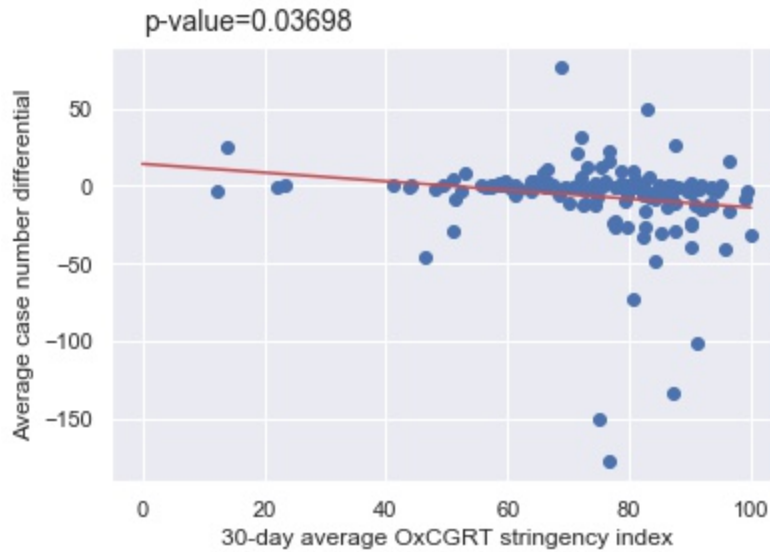


Figure 7 : The regression analysis of average stringency vs. average case differential.

The stringency index is an aggregation of different quarantine and social distancing measures. The previous result then makes it obvious to investigate which measures are the most effective. Towards this goal, I use two-way ANOVA analysis, wherein the two different dimensions are the mandate types (closing schools, restricting gatherings, etc.) and the countries.

The numerical quantity that serves as the “observation” variable will again be the average case differential described previously. In this case, the differentials are not with respect to the time periods previously used (i.e. 60 to 30 days ago and 30 days ago until the present) but rather they will be computed before and after the implementation of each government mandate. There are a number of countries whose ratios are not finite or defined, therefore these countries are dropped from the ANOVA analysis. Using the statsmodels python package API, I perform type 2 ANOVA analysis on these factors using the ratio values. The result of the analysis is that both the type of quarantine measure as well as the country have an effect on whether the number of new cases drops or not. The ANOVA results are described in the following table, which displays the degrees of freedom, F statistic, p-values and residual values.

	sum_squares	df	F	PR(>F)
Mandate type	3826.913544	7	9.772289	~ 0
Country	612201.09	123	88.968175	~ 0

Table 1: 2-way ANOVA analysis, government mandates and countries are being related to the average case differential before and after the enactment of each mandate.

To see whether or not the requirements for the analysis are sensible, I check the distributions of the residuals as well as the variances for the mandate types.

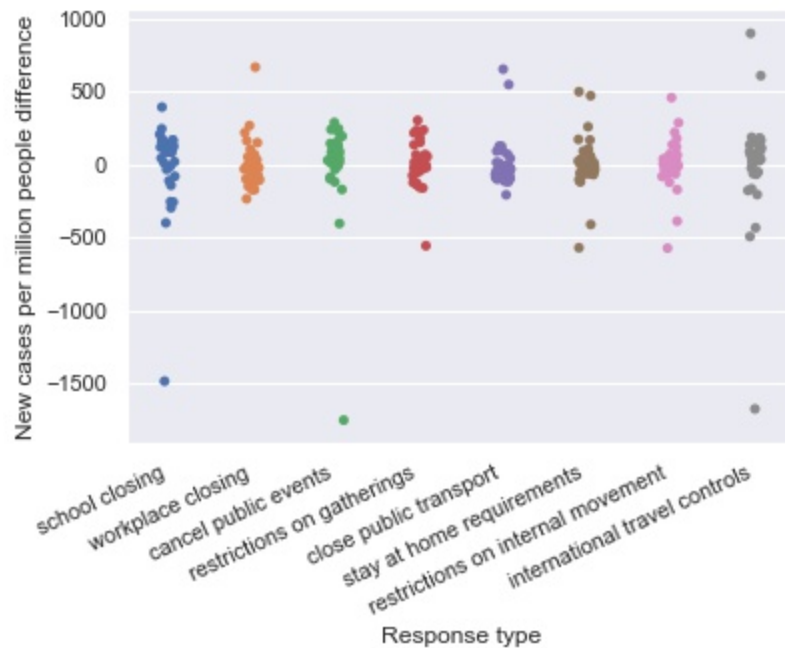


Figure 8: Residual distribution with respect to different factors.

This ANOVA analysis leads me to believe that one of the OxCGRT dataset's index variables (i.e. the government response index or stringency index) should be included in the

modeling process. This is important because as it turns out, there are many features which seem to only worsen the performance of the predictive models. I only have hypotheses for why this occurs, but going forward the only features which shall be used (including moving averages for the ridge regression model) are the number of new cases per million people, its logarithm, and the government response index. The reason why I reduce the number of features so drastically is because there will be at maximum a number of samples on the order of 20000.

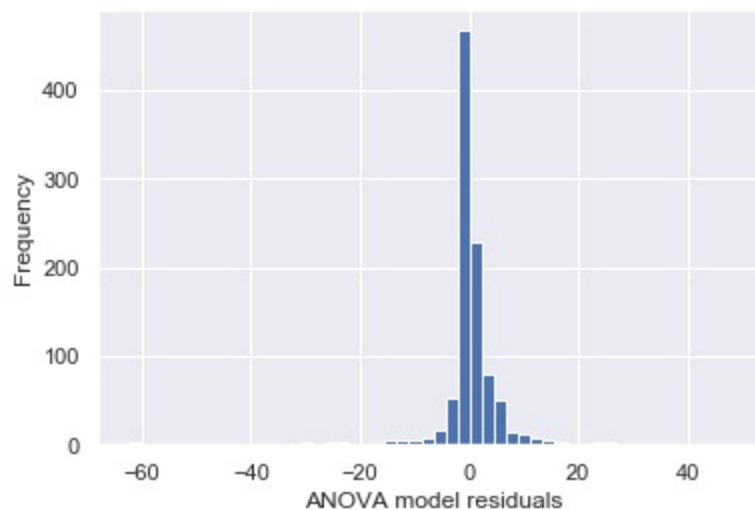


Figure 9: Overall residual distribution

5. Predictive models for COVID-19 case numbers

The primary goal of this project is to compare the performance of several predictive models for the number of new cases per million people, not find the best model possible. Naturally, in the context of future prediction, a forecast interval needs to be decided upon. I will focus on predicting a single day into the future. I will utilize three types of models: a neural network with two fully connected layers, a neural network with two convolutional layers and two fully connected layers and a simple ridge regression model. Before attacking the full problem, I was able to develop my intuition with a prototyping stage for the model implementation. This prototyping focused on implementing the three different models but only for a very small subset of the data. This allowed me to debug as well as determine the correct format for the data in order to be used with the keras API. The prototyping was completed in the notebook,

COVID19_model_prototypes.ipynb. The numerical experiments in this prototyping stage explored the effectiveness of scaling the variables, different data formats. Notably missing from this notebook was the tuning of model hyper parameters. This tuning was reserved for the notebooks dedicated to the full version of each model.

The data is formatted into different time windows, hereafter referred to as “frames”. These frames are simply the name given to collections of multiple days worth of feature data, arranged into rows such that they each represent a sample of the training data. The idea behind the creation of these frames is to leverage multiple days worth of data when making predictions. For example, if I have three features and a frame consisting of 10 days, then the dimension of each sample is $3 * 10 = 30$. This is a strategy for trying to impart knowledge of forward time evolution onto the models.

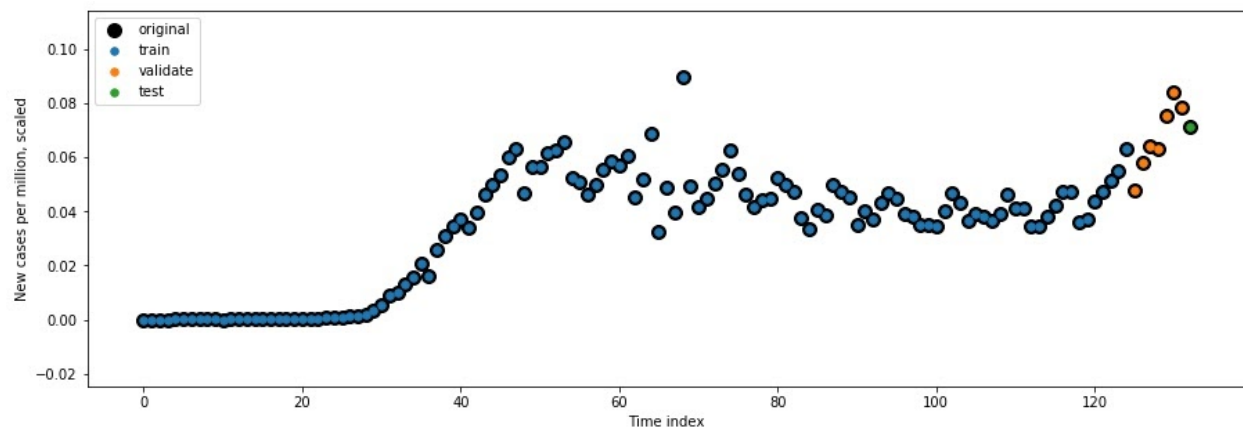


Figure 10 : The split of the different frames into training, validation and testing sets. Each point plotted represents the most recent date within each frame (i.e. the right endpoint of each frame).

After these frames are created, they are split into three subsets for the purpose of model training and testing; the splitting visualized by the color coding in Figure 10. Each point in the plot identifies the right edge of each time frame. In other words, while it appears that there is a single day contained in the testing set, represented by the single green point, there is in fact a single *frame* contained in the testing set (whose leading edge is the green colored point). The

discussion of the specifics of which features are used and the specifics of the time frames is kept to the separate model notebooks.

The final measure of performance is visualized by plotting the true versus predicted values of each of the three models: ridge regression, fully connected neural network, and convolutional neural network. The predictions for each country's new cases are compared with a naive baseline, which is to say a baseline prediction which simply consists of using the most recent values.

Figures 11, 12, and 13 contain the following: the two plots in the first row are scatter plots of the predicted values versus the actual values. The two plots in the second row are a plot of the residuals (predicted values - actual values) vs. the actual value. The first column always corresponds to the naive baseline (it's repeated three times, once for each model, for ease of comparison). The second (right) column corresponds to either one of the three models previously mentioned. the fully connected neural network ("NN"), the convolutional neural network ("CNN") or the ridge regression model. I used the mean squared error as the loss function for all three models, but also include the explained variance correlation score as well.

These scores are included in the top left of each scatter plot of predicted vs. actual values (first row). Due to their size, the figures (figures 11, 12, 13) are placed after the conclusion of this report. The summary of the results are that all three models' predictions worsen as the true value increases in magnitude.. At the very least, all three models performed better than the surprisingly accurate naive baseline, which indicates to me that all three models are viable for predictions.

In conclusion, this problem is obviously very dynamic and difficult. Due to the tremendous scale of the problem, capturing all relevant information is impossible; especially when it is a quantity which is hard to quantify such as human behavior. I believe that this project and the many others like it will in fact remain relevant for years to come, because COVID-19 is most likely not going away anytime soon. I suspect that it will be much like the weather and other travel advisories where forecasts and recommendations are provided as guidelines for daily behavior. Before I get to recommendations for and descriptions of future work, it is important to take a step back from my notebooks and recommend actions other than more model tuning.

I believe the most important recommendation that I can make is to collect data which quantifies the usage of facial masks per country. The second recommendation is to perform a broader and deeper investigation into which government mandated quarantine measures are the most effective. In third place, I believe that a better quantification of human behavior is needed, because people do not necessarily follow the government's guidelines, and so the effective stringency may not be reflected by the OxCGR index.

In terms of the model selection my recommendation would be as follows. For the quickest deployment use Ridge regression, for maximum accuracy, use a CNN. I think that over time, as the number of samples increases, this should benefit the neural networks more than the regression.

6. Future Work

The quantitative or coding recommendations fall into three categories, data selection, model choices, and model tuning.

Acquiring more data is beneficial but I could also use the current data in a different manner. So far, I have included all possible historical data but this need not be the case. For example, we could truncate the time series to only use more recent values, to better capture the current behavior. Additionally, I only explored time frames of constant length. It is possible to change the length of the time frames or have a heterogeneous set of time frame lengths. My choice of features was mostly qualitative; it may be wise to use a more quantitative feature selection. For feature engineering and processing, it would be wise to investigate other means of rescaling the data and perhaps transforming it using various nonlinear functions.

In regards to the choice for models, the most obvious avenue for new investigations is to implement different models such as SVM and neural networks with different architectures. I believe that another important investigation for the future is to investigate how each of the models generalizes to other forecast intervals, i.e. longer than a single day. Likewise, a single model for all countries may not be a wise endeavor, it may be better to create a more targeted model via grouping countries into categories by some metric (proximity for example).

For model tuning, of course more exploration with regards to hyperparameters can be performed, but also different loss functions and optimization methods. For example, to perhaps

better capture and predict the large case number values, a loss function such as root mean square logarithmic error could be used; which penalizes underestimation more than overestimation. Underestimation has the potential for terrible consequences if it allows the pandemic to spread out of control.

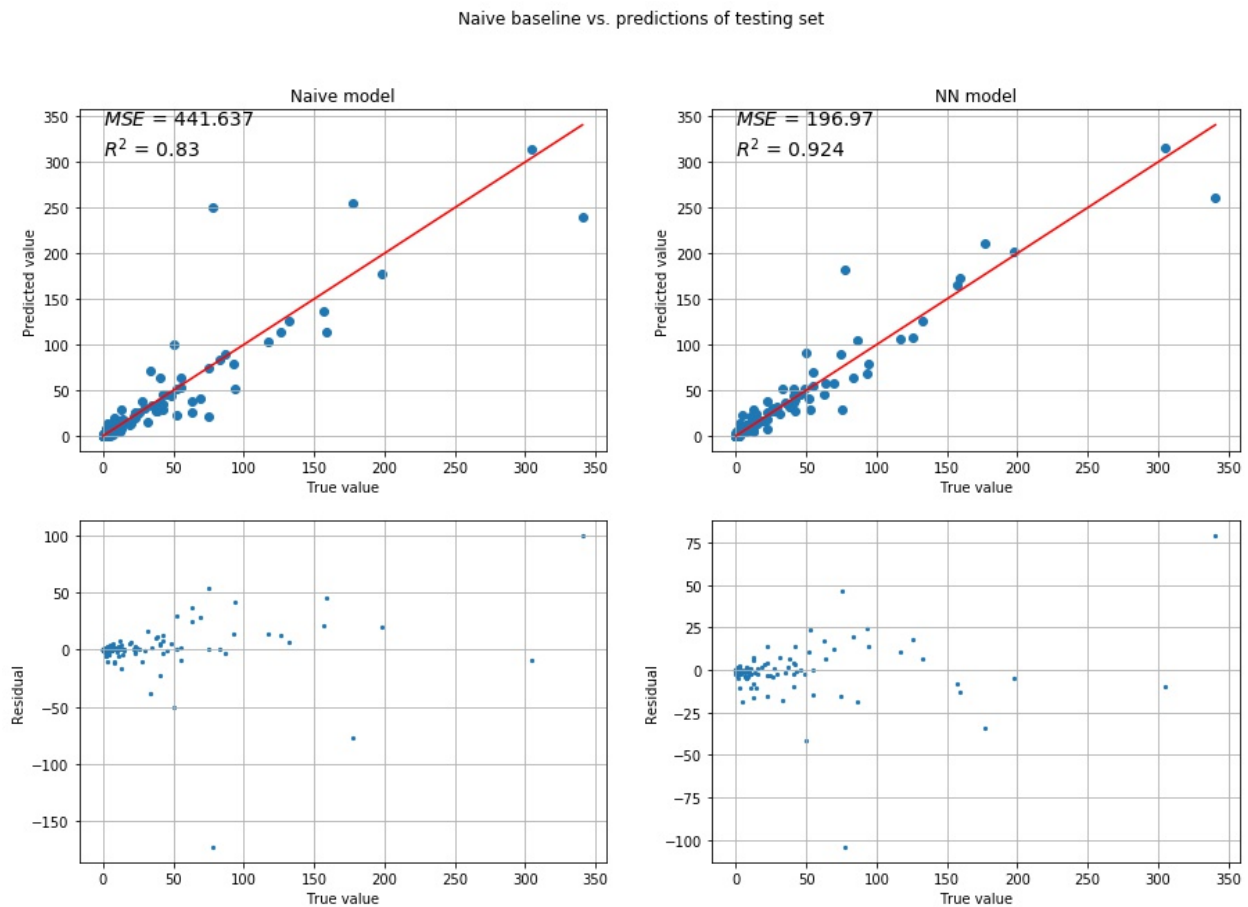


Figure 11: The performance analysis visualized for the fully connected neural network model.

Naive baseline vs. predictions of testing set

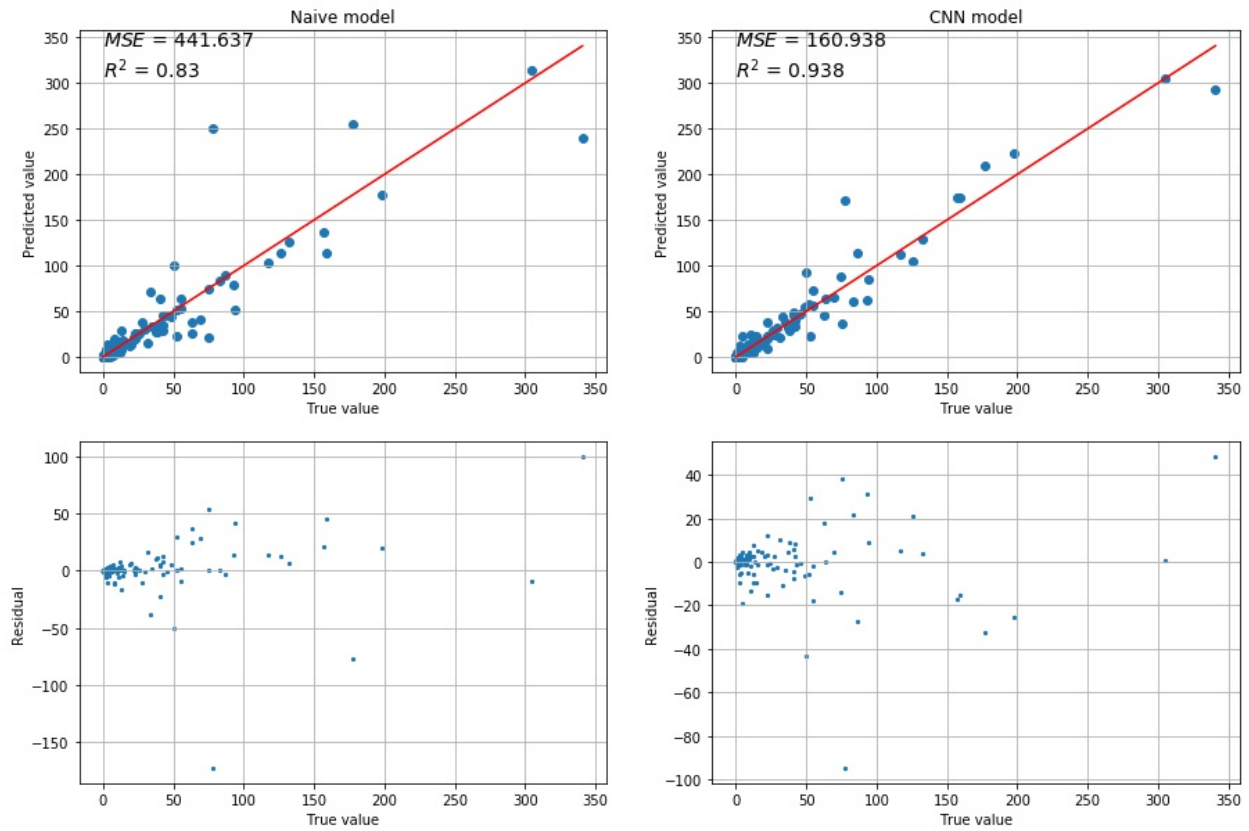


Figure 12: The performance analysis visualized for the convolutional neural network model.

Naive baseline vs. predictions of testing set

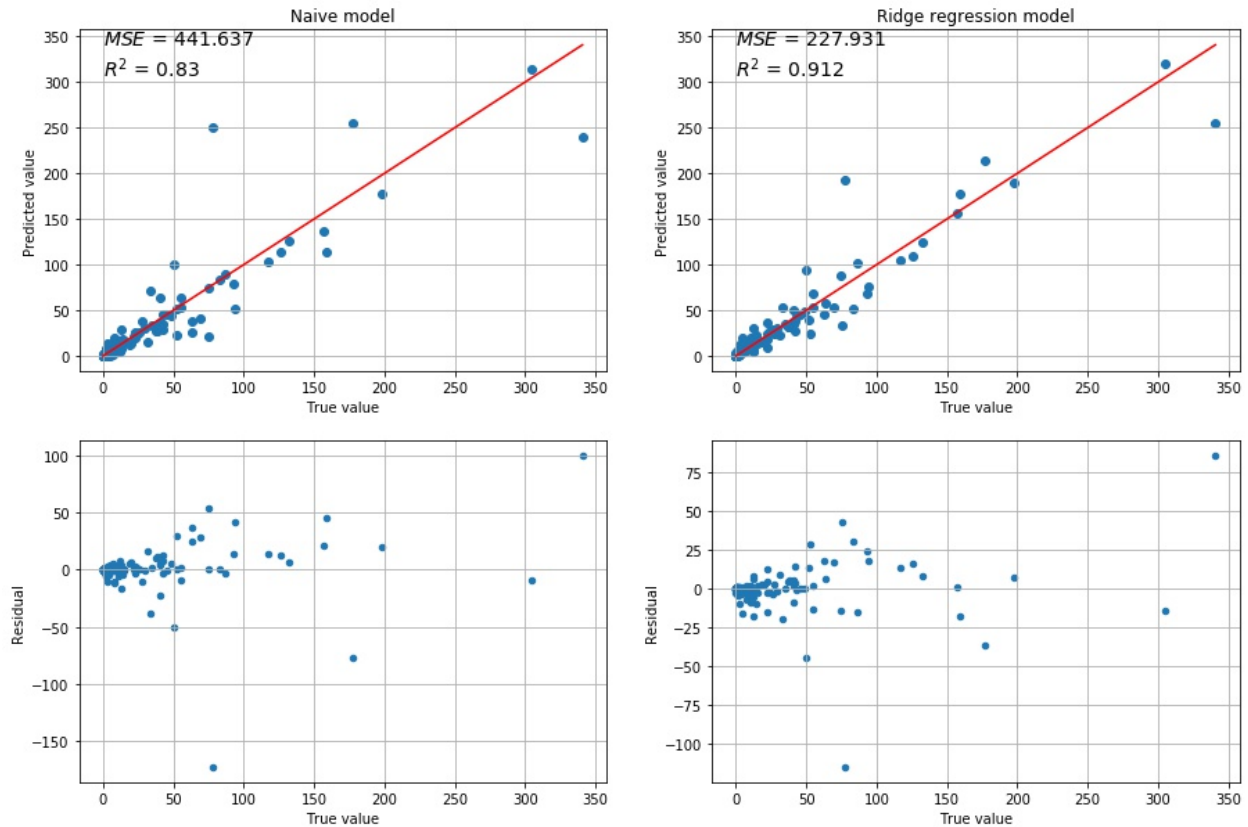


Figure 13: The performance analysis visualized for the ridge regression model.

Appendix:

Datasets

1. JHU CSSE data URL : <https://www.github.com/CSSEGISandData/COVID-19>
2. OWID data URL : <https://www.github.com/owid/covid-19-data/>
3. OxCGRT government response data URL:
<https://github.com/OxCGRT/covid-policy-tracker/>
4. FIND Test Tracker data URL : https://finddx.shinyapps.io/FIND_Cov_19_Tracker/
Choose "Tests and cases" dataset, select "All" as the entry number, save as test_tracker_cases_and_tests.csv for use in data cleaning notebook.