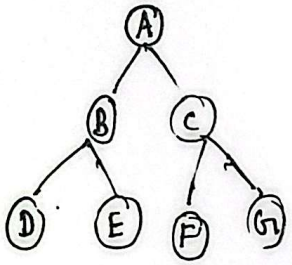
Heap

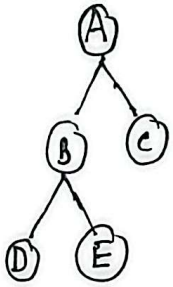
Binary tree :- A binary tree is a tree data structure where each node have at most two children.

(i) Left child (ii) Right child.



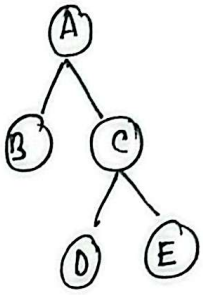
T→

1	2	3	4	5	6	7
A,	B,	C,	D,	E,	F	G



T→

1	2	3	4	5
A	B	C	D	E



T→

1	2	3	4	5	6	7
A	B	C	-	-	D	E

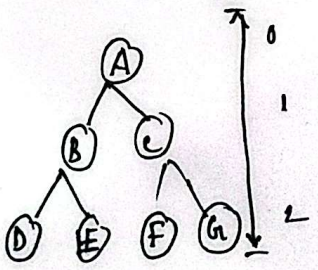
if a node is at index → i

its left child is at → $2 * i$

its right child is at → $2 * i + 1$

its parent is at → $\left[\frac{i}{2}\right]$ → floor

Full Binary Tree



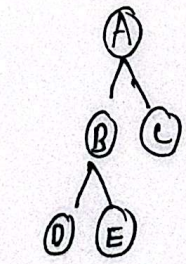
if $h = n$

$\therefore$ number of nodes $= 2^{h+1} - 1$

Binary tree with maximum number of node is called full binary tree.

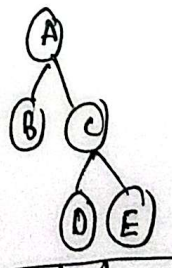
Complete binary tree.

There in no empty elements or gap in between two nodes.



A	B	C	D	E

Complete



A	B	C	-	-	D	E

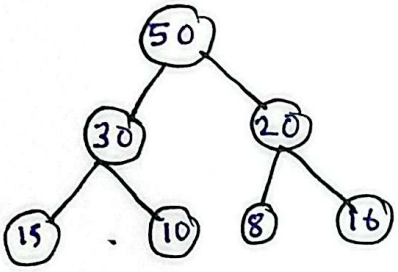
Not complete

Heap

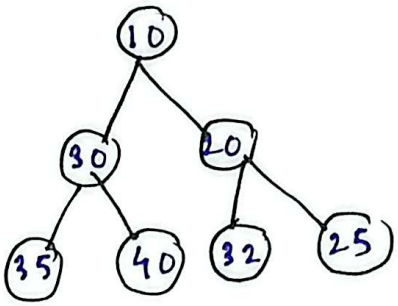
For heap it has to be complete binary tree.

Max Heap

Max Heap



Min Heap



Incertinon (T.C. → $O(\log n) \Rightarrow O(1) \rightarrow O(\log n)$ → Direction is leaf to root

Because Height of a complete binary tree is $O(\log n)$

Deletion → Direction is root to leaf

T.C → $O(\log n)$

* When we delet from max heap we delete the largest element.