



# Introduction to Data Mining

## Chapter 3 Data Exploration

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Based in Slides by by Tan,  
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# R Code Examples

- Available R Code examples are indicated on slides by the R logo



- The Examples are available at [https://mhahsler.github.io/Introduction to Data Mining R Examples/](https://mhahsler.github.io/Introduction%20to%20Data%20Mining%20R%20Examples/)



# Topics

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- **Exploratory Data Analysis**
- Summary Statistics
- Visualization



# What is Data Exploration?

**“A preliminary exploration of the data to better understand its characteristics.”**

- Key motivations of data exploration include
  - Helping to select the right tool for preprocessing or analysis
  - Making use of humans’ abilities to recognize patterns.
    - People can recognize patterns not captured by data analysis tools
- Related to the area of Exploratory Data Analysis (EDA)
  - Created by statistician John Tukey
  - Seminal book is "Exploratory Data Analysis" by Tukey
  - A nice online introduction can be found in Chapter 1 of the NIST Engineering Statistics Handbook
  - <http://www.itl.nist.gov/div898/handbook/index.htm>

# Topics

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- Exploratory Data Analysis
- **Summary Statistics**
- Visualization



# Summary Statistics

Summary statistics are numbers that summarize properties of the data

- Summarized properties include location and spread for continuous data

Examples:      location - mean  
                    spread - standard deviation

- Most summary statistics can be calculated in a single pass through the data

# Frequency and Mode

- The frequency of an attribute value is the percentage of time the value occurs in the data set
  - For example, given the attribute 'gender' and a representative population of people, the gender 'female' occurs about 50% of the time.
- The mode of an attribute is the most frequent attribute value
- The notions of frequency and mode are typically used with **categorical data**.

# Measures of Location: Mean and Median

- For quantitative features.
- The mean is the most common measure of the location of a set of points.
- However, the mean is very sensitive to outliers.
- Thus, the median or a trimmed mean is also commonly used.

$$\text{mean}(x) = \bar{x} = \frac{1}{m} \sum_{i=1}^m x_i$$

$$\text{median}(x) = \begin{cases} x_{(r+1)} & \text{if } m \text{ is odd, i.e., } m = 2r + 1 \\ \frac{1}{2}(x_{(r)} + x_{(r+1)}) & \text{if } m \text{ is even, i.e., } m = 2r \end{cases}$$



# Measures of Spread: Range and Variance

- Range is the difference between the max and min
- The variance or standard deviation is the most common measure of the spread of a set of points.

$$\text{variance}(x) = s_x^2 = \frac{1}{m-1} \sum_{i=1}^m (x_i - \bar{x})^2$$

- However, this is also sensitive to outliers, so that other measures are often used.

$$\text{AAD}(x) = \frac{1}{m} \sum_{i=1}^m |x_i - \bar{x}|$$

$$\text{MAD}(x) = \text{median}\left(\{|x_1 - \bar{x}|, \dots, |x_m - \bar{x}|\}\right)$$

$$\text{interquartile range}(x) = x_{75\%} - x_{25\%}$$

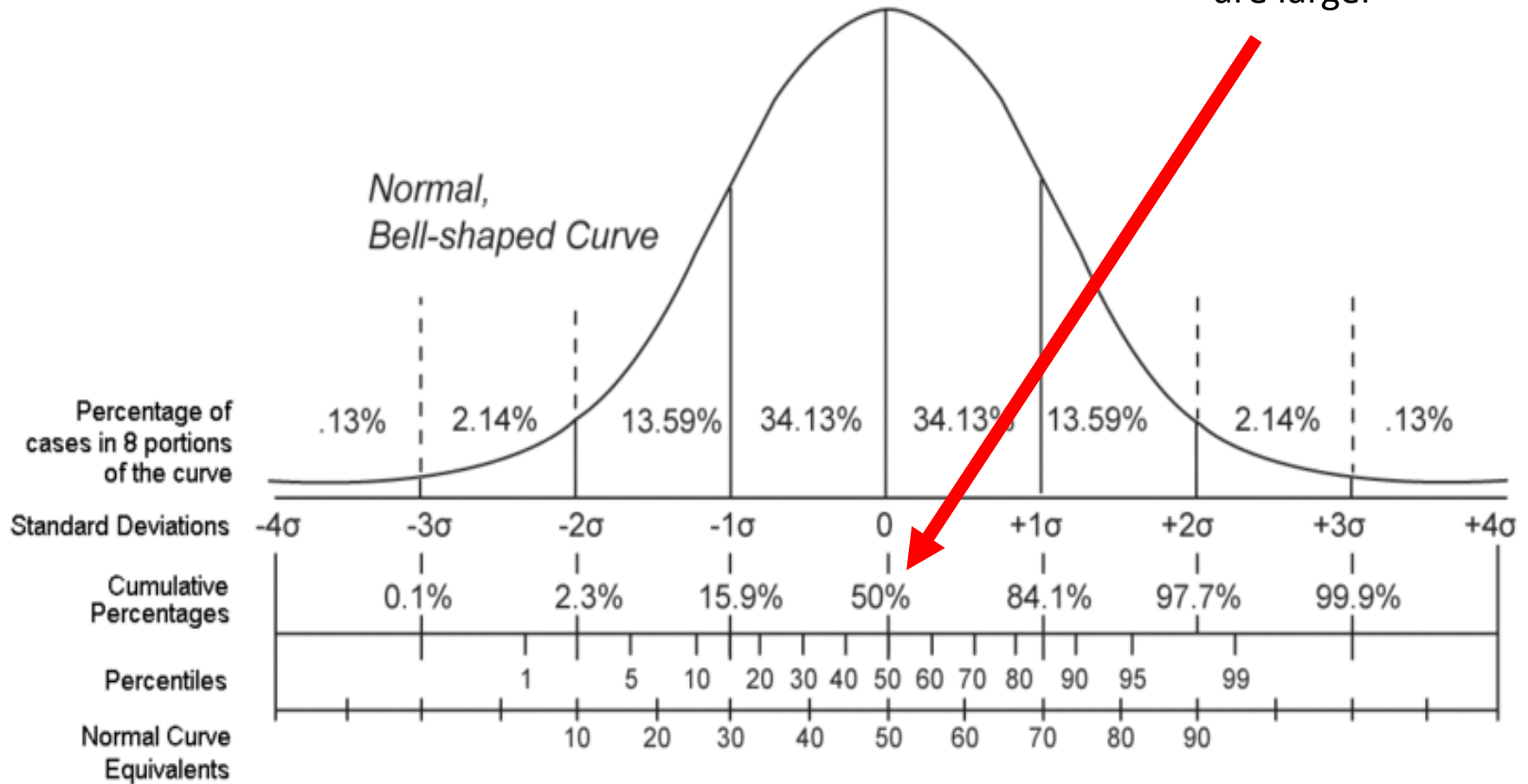


# Percentiles

- Given an ordinal or continuous attribute  $x$  and a number  $p$  between 0 and 100, the  $p^{th}$  percentile is a value  $x_{p\%}$  of  $x$  such that  $p\%$  of the observed values of  $x$  are less than  $x_{p\%}$ .
- Example: the 50th percentile is the value  $x_{50\%}$  such that 50% of all values of  $x$  are less than  $x_{50\%}$ .

# Percentiles

Median – 50% of the cases has a smaller value & 50% are larger



# Multivariate Summary Statistics

Object	$x_1$	$x_2$
1	12	15
2	2	4
...	...	...
m	18	4

- Covariance between features i and j

$$s_{ij} = \frac{1}{m-1} \sum_{k=1}^m (x_{ki} - \bar{x}_i)(x_{kj} - \bar{x}_j)$$

- Correlation

$$r_{ij} = \frac{s_{ij}}{s_i s_j}$$

- $s_i$  is the variance of feature i

# Topics

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- Exploratory Data Analysis
- Summary Statistics
- **Visualization**

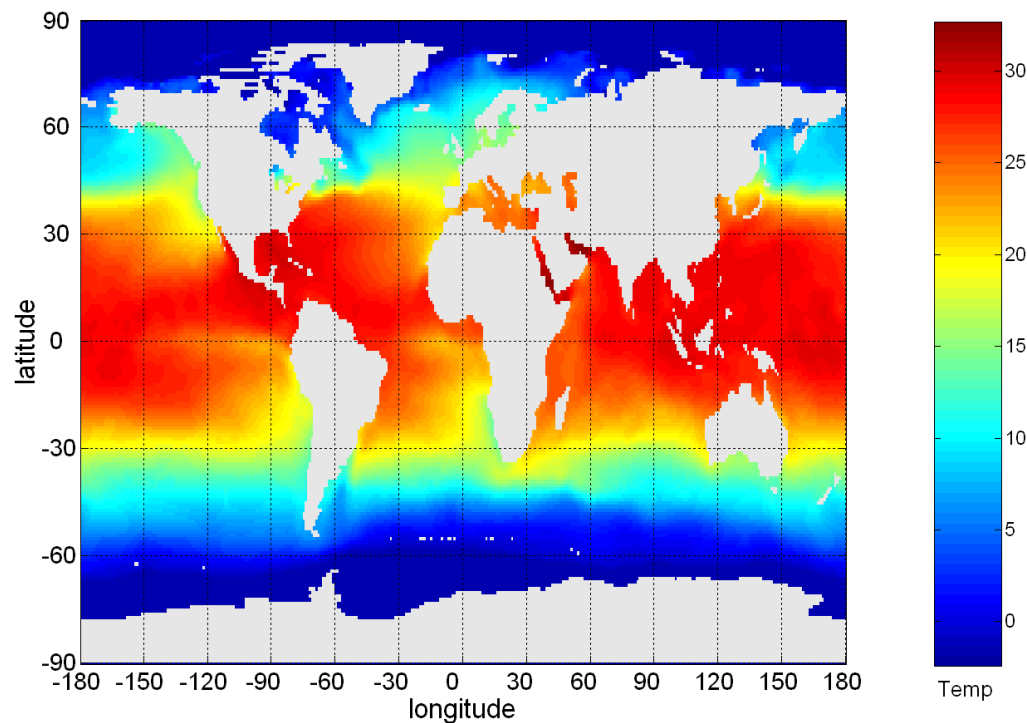


# Visualization

- Visualization is the conversion of data into a visual or tabular format so that the characteristics of the data and the **relationships among data items or attributes** can be analyzed or reported.
- Visualization of data is one of the most powerful and appealing techniques for data exploration.
  - Humans have a well-developed ability to analyze large amounts of information that is presented visually
  - Can detect general patterns and trends
  - Can detect outliers and unusual patterns

# Example: Sea Surface Temperature

- The following shows the Sea Surface Temperature (SST) for July 1982
- Tens of thousands of data points are summarized in a single figure



# Representation

- Is the mapping of information to a visual format
- Data objects, their attributes, and the relationships among data objects are translated into graphical elements such as points, lines, shapes, and colors.
- Example:
  - Objects are often represented as points
  - Their attribute values can be represented as the position of the points or the characteristics of the points, e.g., color, size, and shape
  - If position is used, then the relationships of points, i.e., whether they form groups or a point is an outlier, is easily perceived.



# Arrangement

- Is the placement of visual elements within a display
- Can make a large difference in how easy it is to understand the data
- Example:

	1	2	3	4	5	6
1	0	1	0	1	1	0
2	1	0	1	0	0	1
3	0	1	0	1	1	0
4	1	0	1	0	0	1
5	0	1	0	1	1	0
6	1	0	1	0	0	1
7	0	1	0	1	1	0
8	1	0	1	0	0	1
9	0	1	0	1	1	0

	6	1	3	2	5	4
4	1	1	1	0	0	0
2	1	1	1	0	0	0
6	1	1	1	0	0	0
8	1	1	1	0	0	0
5	0	0	0	1	1	1
3	0	0	0	1	1	1
9	0	0	0	1	1	1
1	0	0	0	1	1	1
7	0	0	0	1	1	1

# The Iris Dataset

Many of the exploratory data techniques are illustrated with the Iris Plant data set.

- Included as a demo dataset in many tools (R, scikit-learn, Rapidminer, ...).
- Can be obtained from the UCI Machine Learning Repository <http://www.ics.uci.edu/~mlearn/MLRepository.html>
- From the statistician R.A. Fisher
- 150 flowers, three types (classes).
- Four (non-class) attributes

	▲ Sepal.Length ▾	Sepal.Width ▾	Petal.Length ▾	Petal.Width ▾	Species ▾
1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa

...

Iris Versicolor



Iris Virginica

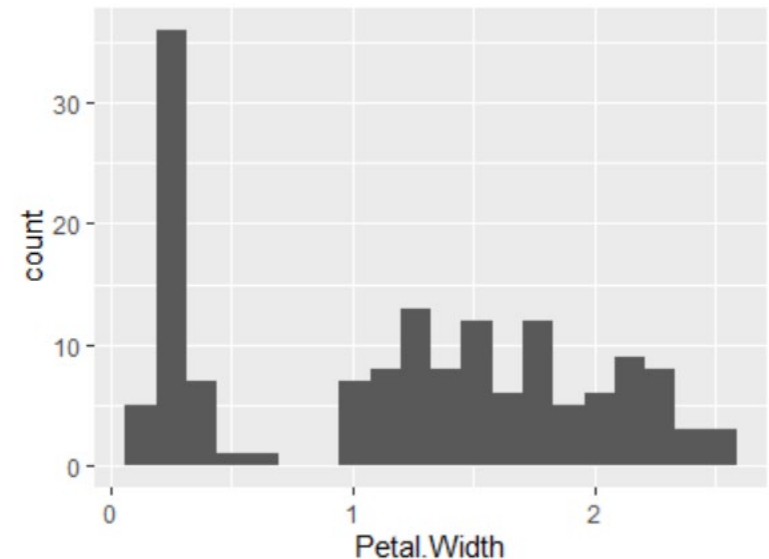
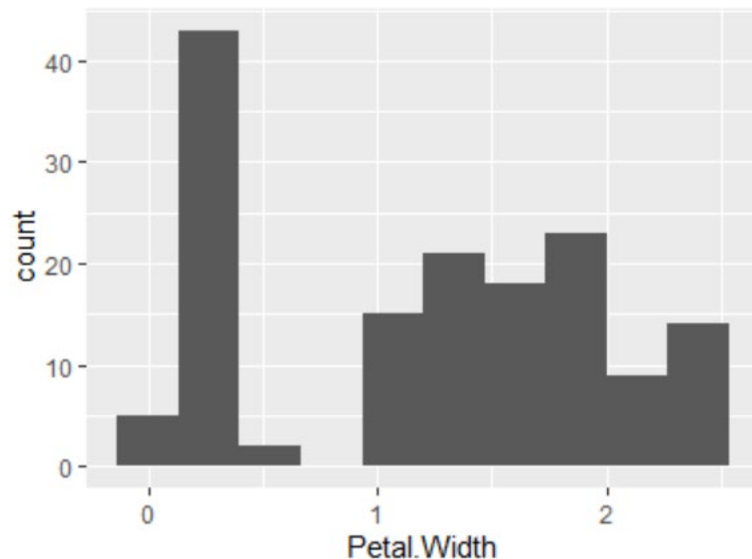


Iris Setosa



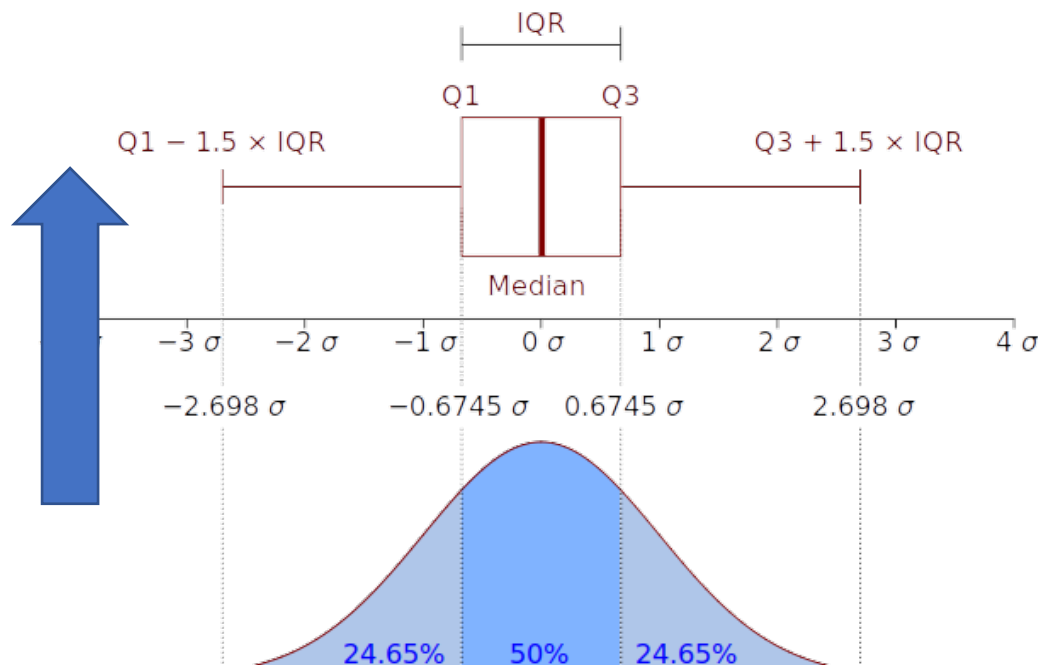
# Distribution: Histograms

- Usually shows the distribution of values of a single variable
- Divide the values into bins and show a bar plot of the number of objects in each bin.
- The height of each bar indicates the number of objects
- Shape of histogram depends on the number of bins
- Example: Petal Width (10 and 20 bins, respectively)

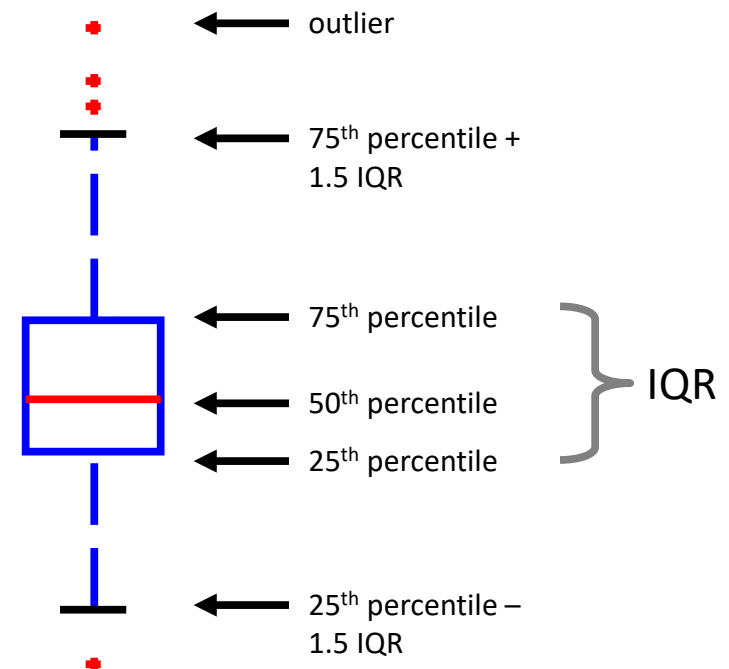


# Distribution Box Plots

- Invented by J. Tukey
- Simplified version of a PDF/histogram.

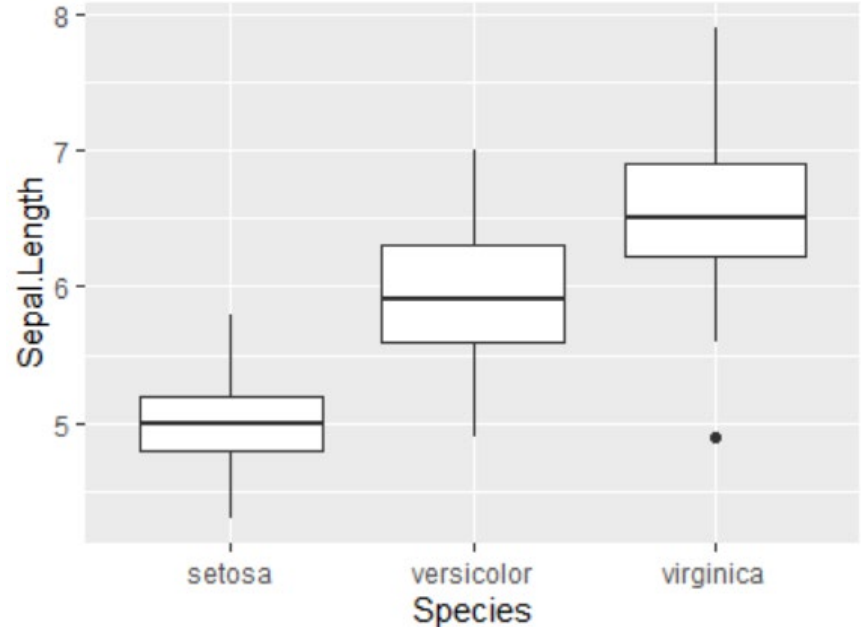
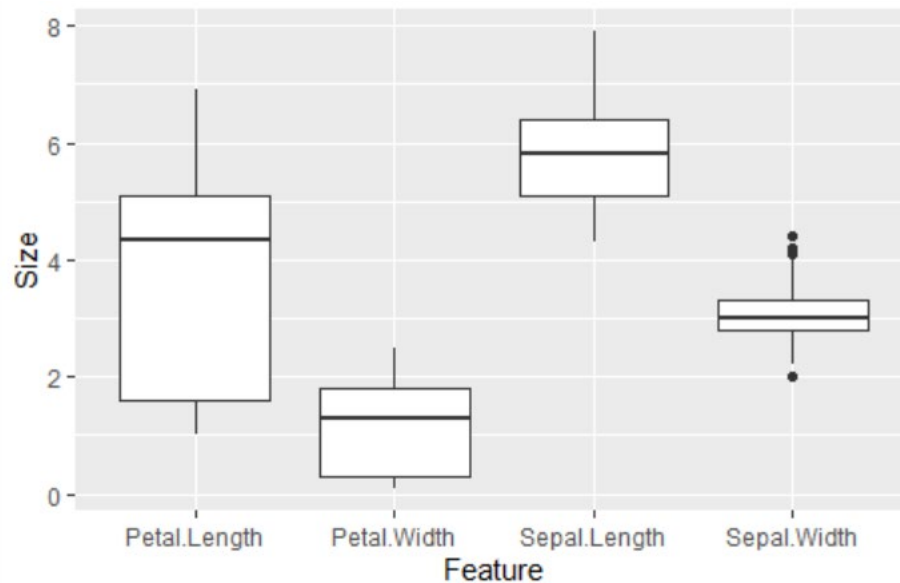


PDF or histogram



# Examples of Box Plots

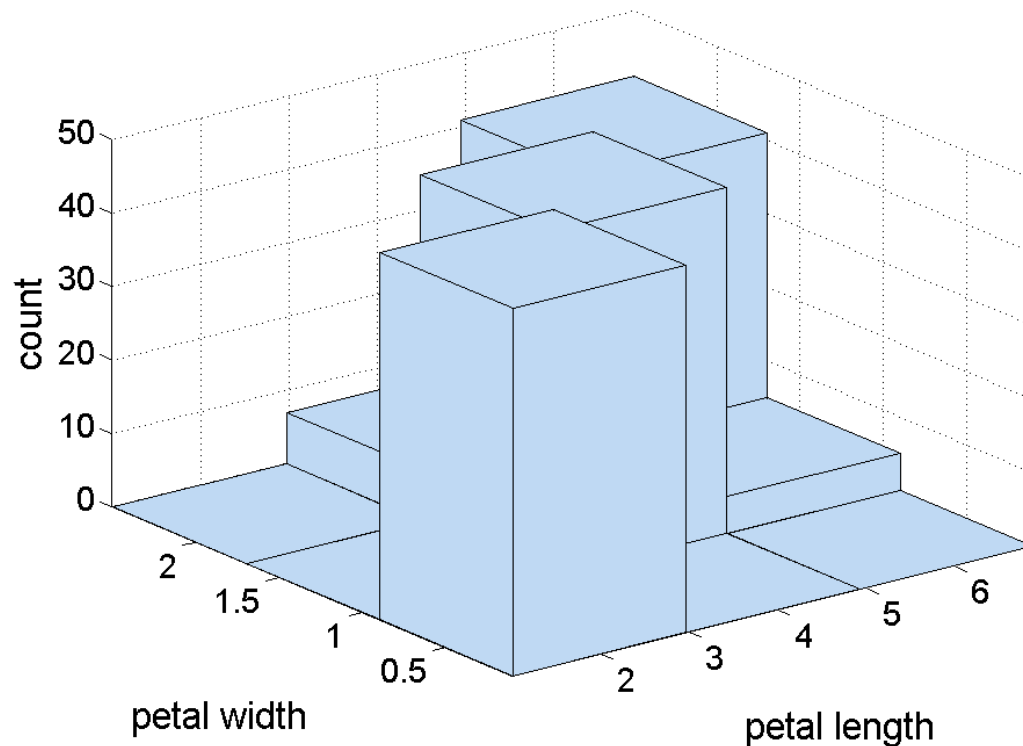
- Box plots can be used to compare attributes or subgroups.



	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa

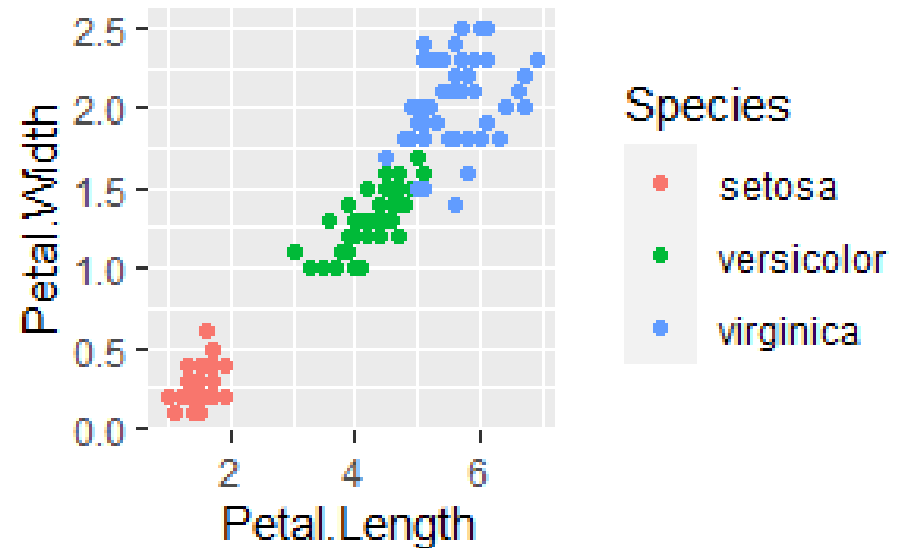
# Two-Dimensional Histograms

- Show the joint distribution of the values of two attributes
- Example: petal width and petal length
  - What does this tell us?

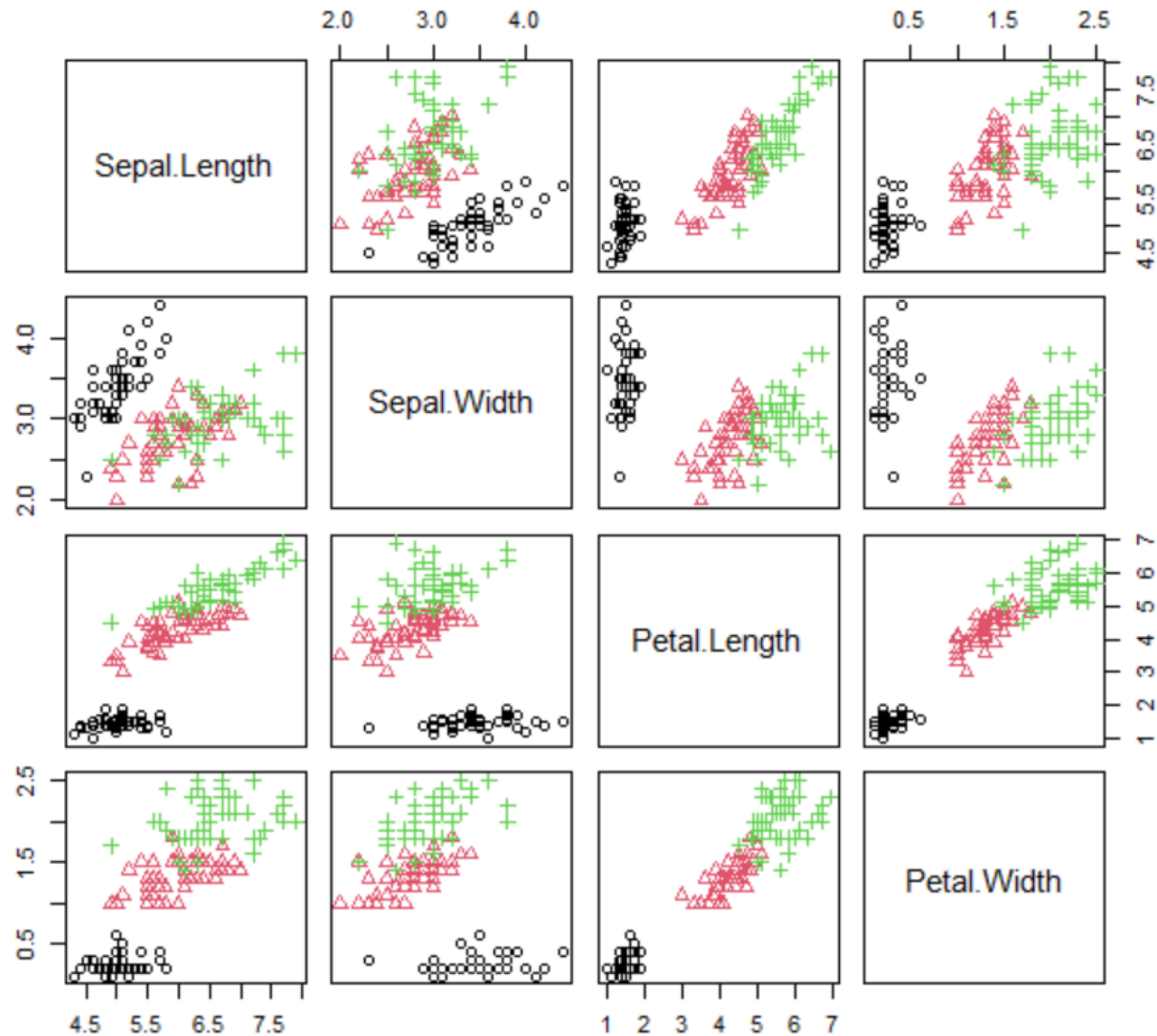


# Scatter Plots

- Attributes values determine the position
- Two-dimensional scatter plots most common, but can have three-dimensional scatter plots
- Often additional attributes can be displayed by using the size, shape, and color of the markers that represent the objects



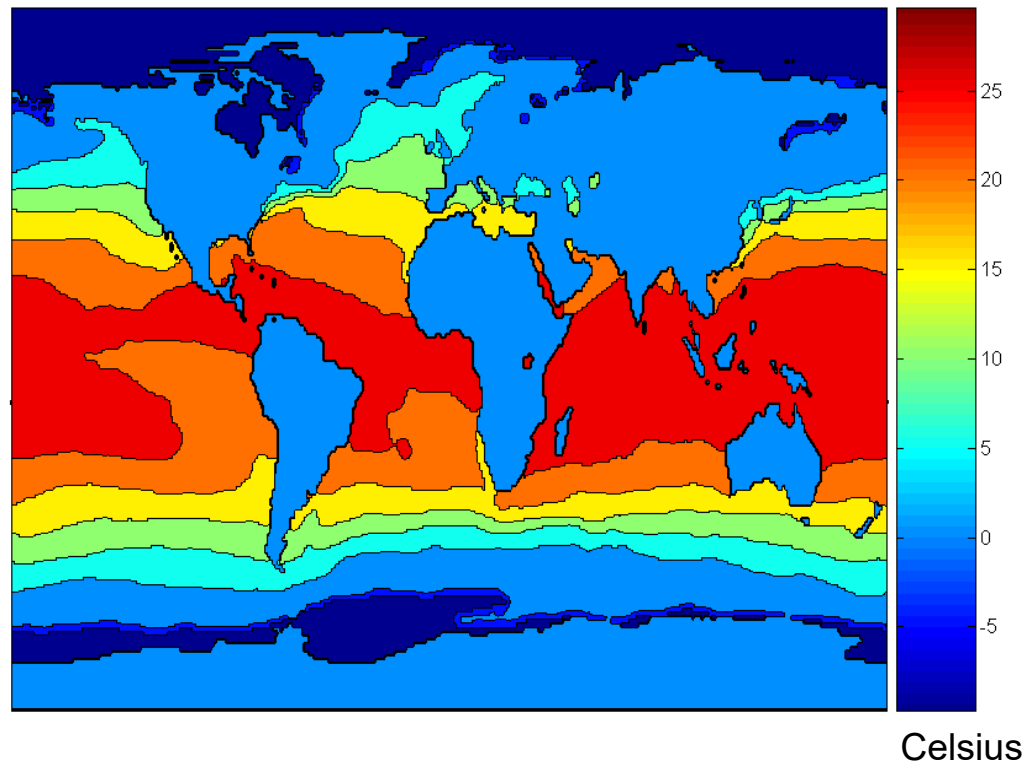
# Scatter Plot Array of Iris Attributes





# Contour Plots

- Useful when a continuous attribute is measured on a **spatial grid**
- They partition the plane into regions of similar values
- The contour lines that form the boundaries of these regions connect points with equal values
- The most common example is contour maps of elevation
- Can also display temperature, rainfall, air pressure, etc.

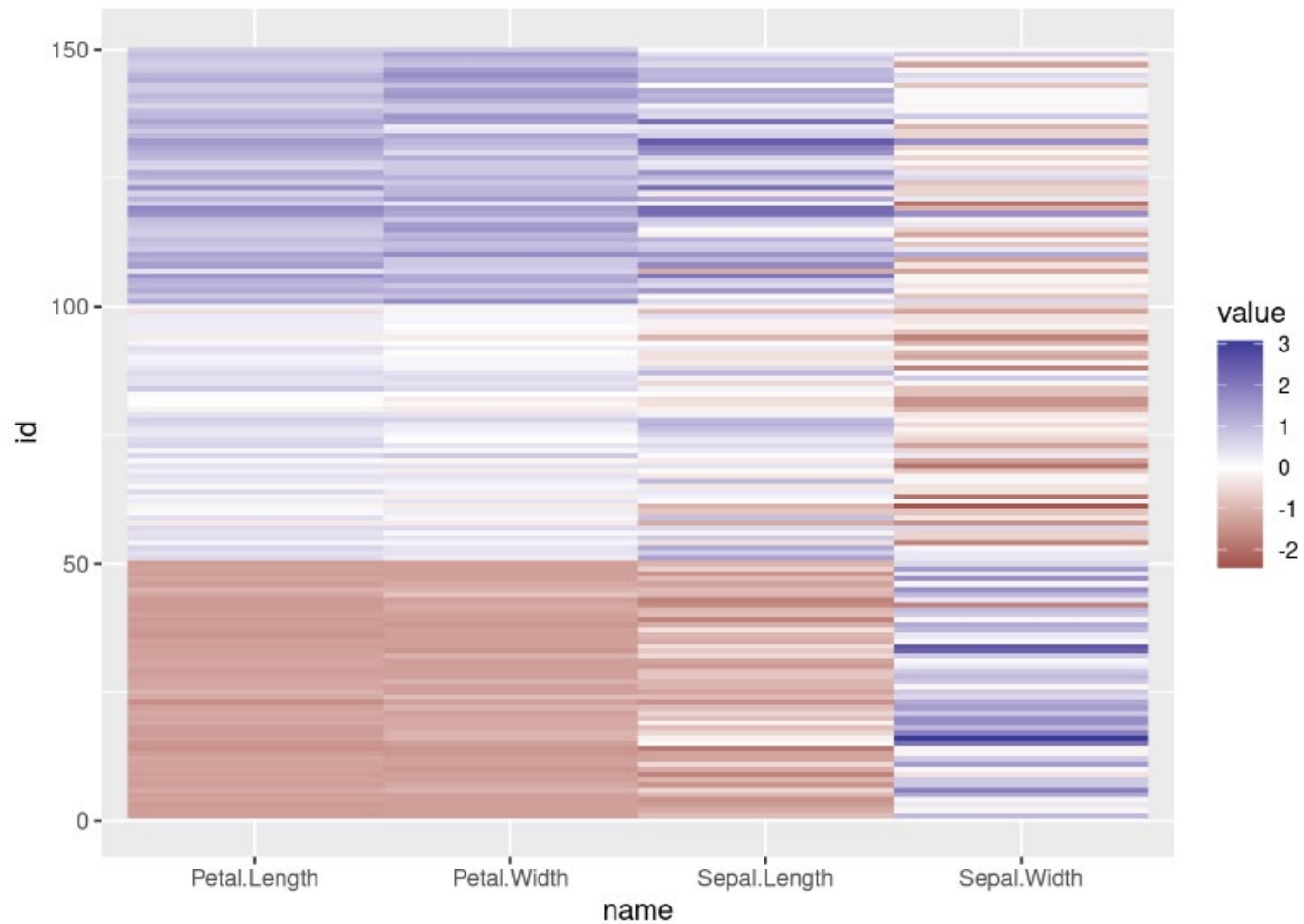


# Matrix Plots

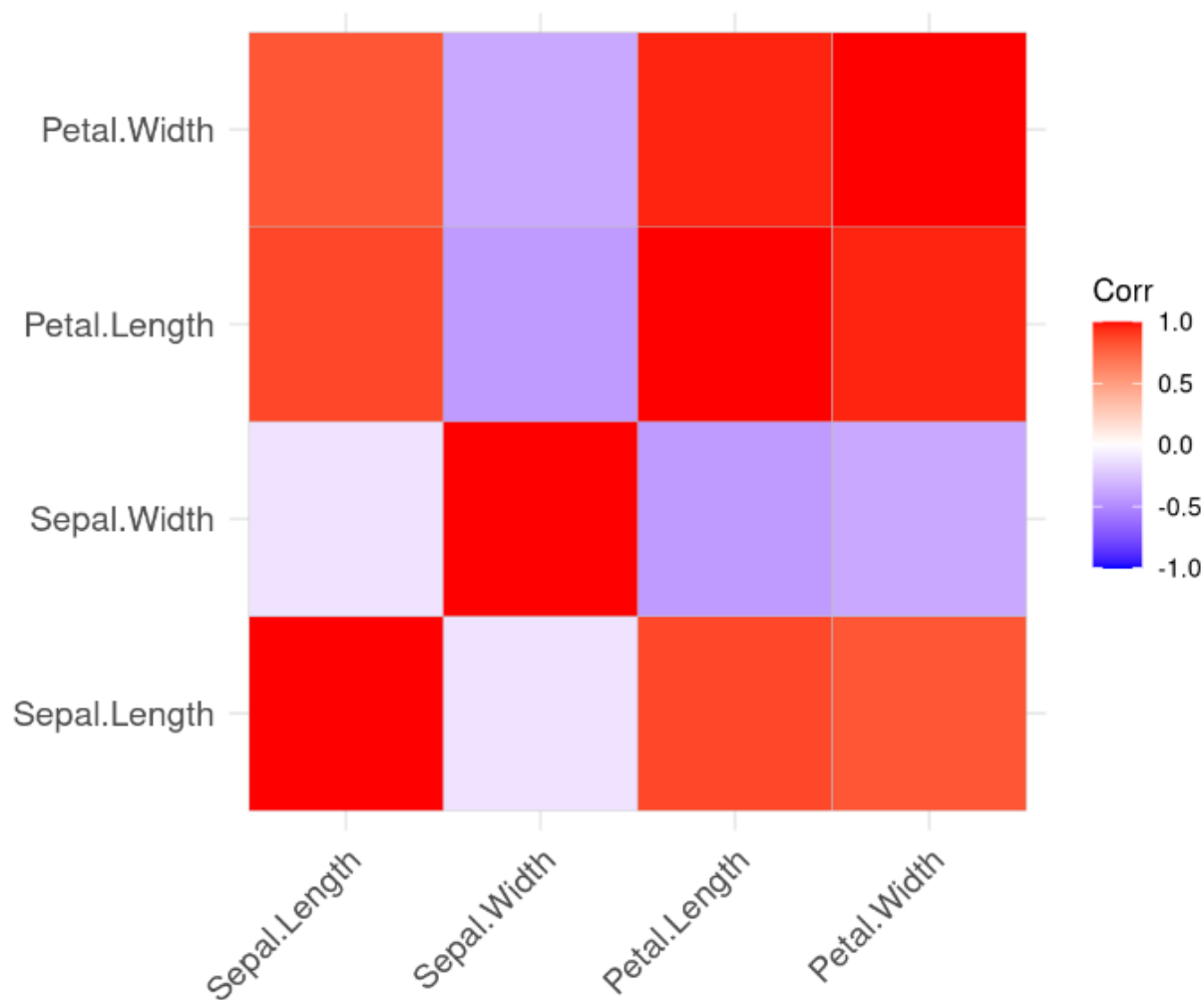
- Can plot a data matrix
- Can be useful when objects are sorted according to class
- Typically, the attributes are normalized to prevent one attribute from dominating the plot
- Plots of similarity or distance matrices can also be useful for visualizing the relationships between objects

# Visualization of the Iris Data Matrix

Deviation from feature mean



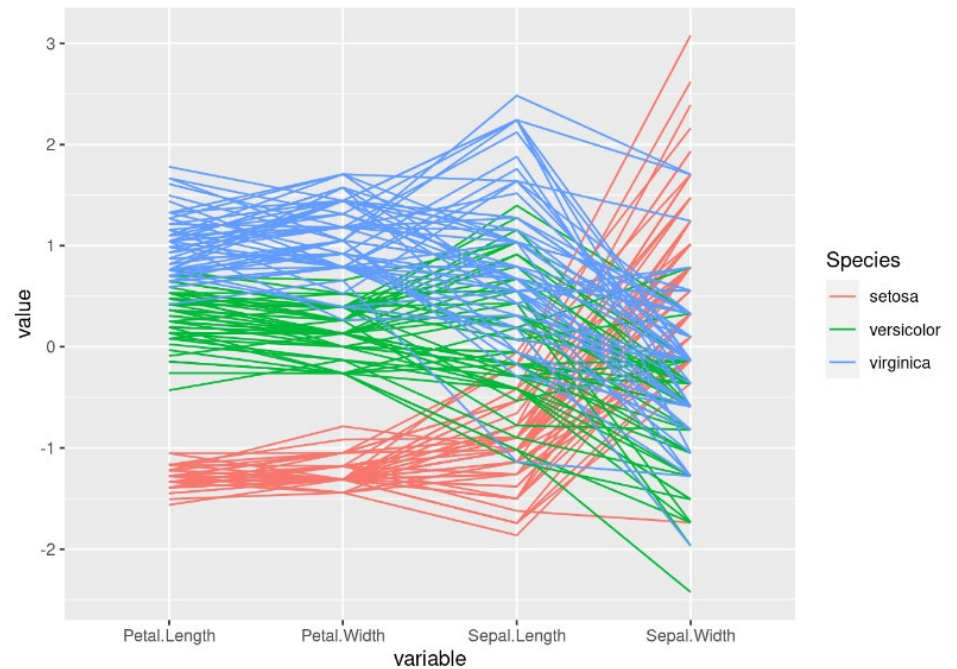
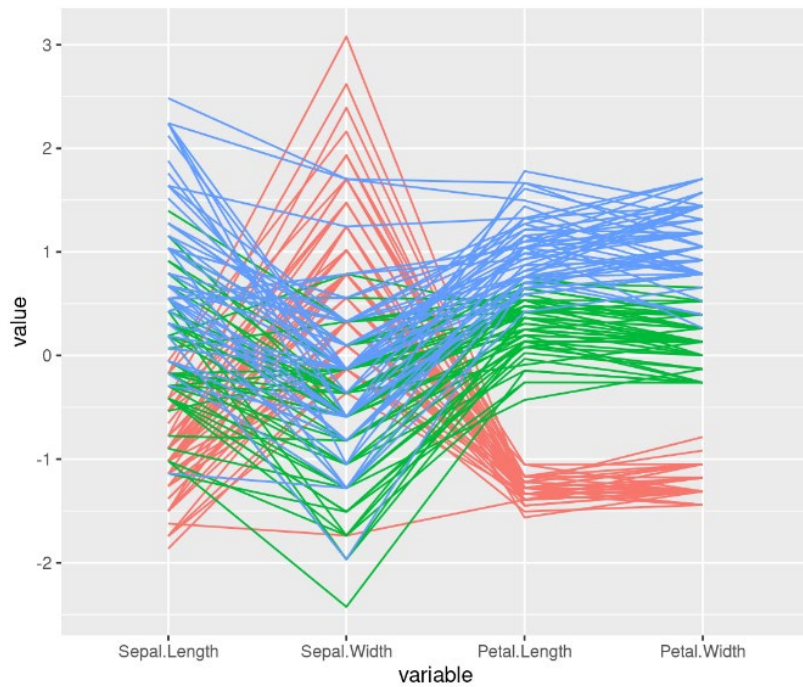
# Visualization of the Iris Correlation Matrix



# Parallel Coordinates

- Used to plot the attribute values of high-dimensional data
- Instead of using perpendicular axes, use a set of parallel axes
- The attribute values of each object are plotted as a point on each corresponding coordinate axis and the points are connected by a line
- Thus, each object is represented as a line
- Often, the lines representing a distinct class of objects group together, at least for some attributes
- Ordering of attributes is important in seeing such groupings

# Parallel Coordinates Plots for Iris Data



Reordered features

# Other Visualization Techniques

- Star Plots

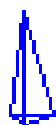
- Similar approach to parallel coordinates, but axes radiate from a central point
- The line connecting the values of an object is a polygon

- Chernoff Faces

- Approach created by Herman Chernoff
- This approach associates each attribute with a characteristic of a face
- The values of each attribute determine the appearance of the corresponding facial characteristic
- Each object becomes a separate face
- Relies on human's ability to distinguish faces

# Star Plots for Iris Data

- Setosa



1



2



3

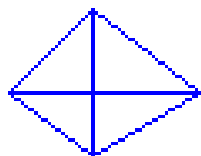


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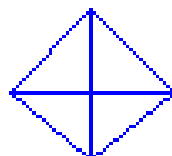


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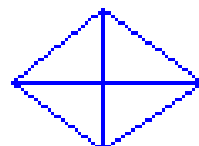
- Versicolor



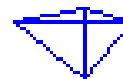
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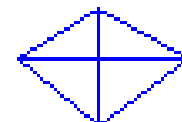
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53

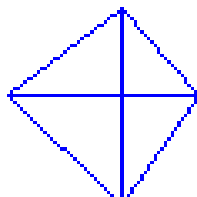


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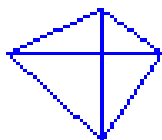


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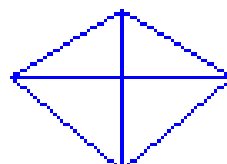
- Virginica



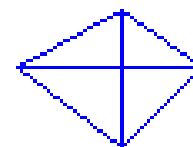
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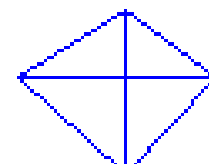
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103



104



105



# Chernoff Faces for Iris Data

- Setosa



1



2



3



4



5

- Versicolor



51



52



53



54



55

- Virginica



101



102



103



104



105