

nopo

Implementation of a matching-based decomposition technique with postestimation commands

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DECOMPOSITIONS IN THE SOCIAL SCIENCES

- Decomposition techniques are a common way to examine gaps in socio-economic outcomes between two groups (e.g., sex, race, nativity)
 - To what extent contribute observed differences in group characteristics to gaps?
 - ⇒ Explained component
 - Gaps not accounted for by observed differences in group characteristic might indicate differential returns or unobservables
 - **⇒** Unexplained component



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 Explained component
 - Gaps not accounted for by observed differences in group characteristic might indicate differential returns or unobservables
 - **⇒** Unexplained component
- Methods invoke different assumptions, can lead to different results, and provide different insights (Strittmatter and Wunsch 2021; Hamjediers and Sprengholz 2023)
 - Many applications rely on regression-based techniques (Blinder 1973; Oaxaca 1973), Nopo
 (2008) proposed a matching-based approach

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Decomposition à la Ñopo

- 1. Each member of group B can be matched to all potential matches of group A along a set of characteristics X (one-to-many-matching), providing two pieces of information:
 - ullet Who can be matched (subscript m) and who cannot be matched (subscript u)
 - ullet Weights to calculate counterfactual outcome $\overline{Y}_{A^B,m}$ that reflects
 - ullet outcome of group A if it had the same characteristics as group B
 - ullet outcome of group B if it had the same returns to characteristics as group A



Decomposition à la Ñopo

2. If $D = \overline{Y}_B - \overline{Y}_A$, gap can be decomposed into four components after matching:

$$D = D_0 + D_X + D_A + D_B$$

$$= \overline{Y}_{B,m} - \overline{Y}_{A^B,m} + \overline{Y}_{A^B,m} - \overline{Y}_{A,m} + D_A + D_B$$

$$= \underbrace{\overline{Y}_{B,m} - \overline{Y}_{A^B,m}}_{\text{splitting difference among matched by reweighted group A}}_{\text{explained component}} + D_A + D_B$$

pertains only to matched units

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DECOMPOSITION À LA ÑOPO

2. If $D = \overline{Y}_B - \overline{Y}_A$, gap can be decomposed into four components after matching:

$$D = D_0 + D_X + \underbrace{D_A + D_B}_{\text{out of support}}$$

$$D_A = \underbrace{(\overline{Y}_{A,m} - \overline{Y}_{A,u})}_{\text{gap between unmatched } A} \underbrace{(N_{A,u}/N_A)}_{\text{share of unmatched } A}$$

$$D_B = \underbrace{(\overline{Y}_{B,u} - \overline{Y}_{B,m})}_{\text{gap between unmatched and matched } B} \underbrace{(N_{B,u}/N_B)}_{\text{share of unmatched } B}$$

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LINKS TO OTHER APPROACHES

- Generally, similar to two-fold (Kitagawa-)Blinder-Oaxaca-Decomposition
 (Hamjediers and Sprengholz 2023)
 - Advantages of matching-based decomposition:
 - + Non-parametric estimation \rightarrow no assumptions about functional form
 - + D_0 & D_X apply only to matched units o no model-based extrapolation
 - Disdvantages of matching-based decomposition:
 - Suffers from curse of dimensionality \rightarrow risk of attributing too much to D_A & D_B
 - Does not allow to disentangle explained component across predictors
- ⇒ Similar arguments as for regression- vs. matching-based adjustment for confounders in estimating (local) treatment effects

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LINKS TO OTHER APPROACHES

• Component D_0 is equal to the average treatment effect on the treated ATT after matching

$$ATT = Po_{t=1}^{T=1} - Po_{t=0}^{T=1}$$
$$= \overline{Y}_{B,m} - \overline{Y}_{A^B,m} = D_0$$

⇒ All other components of Nopo's approach are seldom assessed in estimations of treatment effects via matching

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IT'S ALL ABOUT THE MATCHING

Originally, exact matching on (coarsened) predictors

(cf. ado-file nopomatch of Atal et al. (2013))

- We extend it to Propensity Score Matching (Rosenbaum and Rubin 1983) and Multivariate Distance Matching
- ullet Trade-off between reaching balance on predictors between B,m and A^B,m vs. curse of dimensionality and lack of common support (lacus et al. 2012)

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NEW COMMAND: NOPO

- More flexible, inference for all components
- Allows matching by different measures
 - nopo calls kmatch (Jann 2017) inherently or can be used as postestimation-command after matching via kmatch (Jann 2017)
- Provides postestimation commands for descriptives after matching, contribution of groups to D_A and D_B , and components across distribution of Y
- Illustration based on example from Hamjediers and Sprengholz (2023):
 - Data: GSOEP, 2014-2019, one observation per individual
 - Groups: Native men (A) and immgriant women (B)
 - Outcome: hourly gross wages
 - Predictors: age, married, educational attainment, labor market experience,
 2-digit ISCO-08 occupations, part-time indicator (all coarsened)

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nopo decomp depvar varlist [if] [in] [weights], by(varname)

Outlook

STANDALONE USAGE

. nopo decomp wage age_c married edu lmexp parttime isco2d, by(grp)

Nopo decomposition 8954 Exact matching: N strata 1783 N matched strata 488 (unique combinations of matching set)

		N / %		Mean
Group	Matched	Unmatched	Total	wage
A: Native Men grp == 1	3110 51.4	2939 48.6	6049	20.5
B: Immigrant Women grp == 4 (ref)	1 1387 1 47.7	1518 52.3	2905	12.1

wage	Coefficient	Std. err.	z	P> z	[95% conf.	interval]
D	, 0.00102.	.2067519	-40.55	0.000	-8.789253	-7.978801
DO		.5407104	-4.45	0.000	-3.466067	-1.346521
DX		.6061777	-8.35	0.000	-6.246837	-3.870664
DA		.1257708	6.15	0.000	.5266609	1.019674
DB		.1285267	-13.17	0.000	-1.944057	-1.440242

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. nopo decomp wage age_c married edu lmexp parttime isco2d, by(grp)

Nopo decomposition Exact matching:

N = 8954
N strata = 1783
N matched strata = 488
(unique combinations of matching set)

	ļ		N / %		Mean
Group	-	Matched	Unmatched	Total	wage
A: Native Men grp == 1	 	3110 51.4	2939 48.6	6049	20.5
B: Immigrant Women grp == 4 (ref)	İ	1387 47.7	1518 52.3	2905	12.1

wage	Coefficient			P> z	[95% conf.	interval]
D DO DX DA DB	-8.384027 -2.406294 -5.05875 .7731673	.2067519 .5407104 .6061777 .1257708 .1285267	-40.55 -4.45 -8.35 6.15 -13.17	0.000 0.000 0.000 0.000 0.000	-8.789253 -3.466067 -6.246837 .5266609	-7.978801 -1.346521 -3.870664 1.019674 -1.440242

Interpretations:

- D0 Among the matched, 2.41 Euro lower wages for group B are unexplained
- DX Compositional differences account for 5.06 Euro of the gap among matched units
- DA Unmatched units of group A earn lower wages than matched units, which accounts for 0.77 Euro of the gap
- DB Unmatched units of group B earn lower wages than matched units, which accounts for 1.69 Euro of the gap



- General Options:
 - Swap groups: swap
 - Defining matching direction: bref(varname == #)
 - Normalize outcome to the reference group of the matching: normalize



. nopo decomp wage \${pred}, by(grp) bref(grp == 1) swap normalize Normalized outcome generated: _wage_norm

Nopo decomposition Exact matching:

8954 N strata 1783 N matched strata 488 (unique combinations of matching set)

	!	N / %		Mean
Group	 Matched	Unmatched	Total	_wage_norm
A: Immigrant Women grp == 4	1387 47.7	1518 52.3	2905	.591
B: Native Men grp == 1 (ref)	3110 51.4	2939 48.6	6049	1

•	Coefficient		z	P> z	[95% conf	interval]
D DO DX DA DB	. 4090725 . 1813969 . 1828367 . 0825632 0377243	.0100878 .0299544 .0328027 .0062711 .0061366	40.55 6.06 5.57 13.17 -6.15	0.000 0.000 0.000 0.000 0.000	.3893008 .1226873 .1185446 .0702721 0497518	.4288443 .2401065 .2471288 .0948542 0256968

- General Options:
 - Swap groups: swap
 - Defining matching direction: bref(varname == #)
 - Normalize outcome to the reference group of the matching: normalize
- Options to adjust matching procedure correspondingly to kmatch:
 - kmatch() allows for exact matching (em) (the default), propensity score matching (ps), and multivariate distance matching (md)
 - Matching-specific options from kmatch can be implemented via kmatchopt()

```
. qui: nopo decomp wage ${pred}, by(grp)
. qui: est store em
. qui: nopo decomp wage ${pred}, by(grp) kmatch(ps)
. qui: est store ps
. qui: nopo decomp wage ${pred}, by(grp) kmatch(md)
. qui: est store md
. qui: nopo decomp wage ${pred}, by(grp) kmatch(ps) kmopt(pscmd(probit) bw(0.0001))
. qui: est store ps_probbw
```

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```
. esttab em ps md ps_probbw, se nonumbers nonotes ///
> mtitles("exact" "prop. score" "multi. dist." "probit ps") ///
> stats(nA mshareuwA nB mshareuwB bwidth, label("N(A)" "% matched A" "N(B)" "% matched B" "Bandwidth"))
```

	exact	prop. score	multi. dist.	probit ps
D	-8.384*** (0.207)	-8.384*** (0.207)	-8.384*** (0.207)	-8.384*** (0.207)
DO	-2.406*** (0.541)	-2.652*** (0.504)	-3.957*** (0.402)	-3.680*** (0.788)
DX	-5.059*** (0.606)	-5.650*** (0.546)	-4.427*** (0.452)	-3.673*** (0.829)
DA	0.773*** (0.126)	0(.)	0 (.)	0.260* (0.101)
DB	-1.692*** (0.129)	-0.0827*** (0.0232)	0 (.)	-1.291*** (0.111)
N(A) % matched A N(B) % matched B Bandwidth	6049 51.41 2905 47.75	6049 100 2905 96.73 0.00265	6049 100 2905 100 2.325	6049 62.08 2905 55.42 0.000100

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AS POSTESTIMATION AFTER KMATCH

- Can be used after kmatch by just prompting nopo decomp
- Needs that following options of kmatch are specified:
 - tval(#) to define reference group (if different from tval(1))
 - att and/or atc; should be coherent to matching direction



AS POSTESTIMATION AFTER KMATCH

. nopo decomp

Nopo decomposition Propensity-score matching:

Kernel bandwidth:

8954 1.0e-03

	! _		N / %		Mean
Group	<u> </u>	Matched	Unmatched	Total	wage
A: Native Men grp == 1	İ	5900 97.5	149 2.5	6049	20.5
B: Immigrant Women grp == 4 (ref)	İ	2516 86.6	389 13.4	2905	12.1

	Coefficient		z	P> z	[95% conf.	interval]
D DO DX DA DB	-8.384027 -3.02594 -5.066576 0101861	.2067519 .6471339 .6814688 .0206239 .049454	-40.55 -4.68 -7.43 -0.49 -5.69	0.000 0.000 0.000 0.621 0.000	-8.789253 -4.294299 -6.40223 0506082 3782534	-7.978801 -1.757581 -3.730921 .0302361 1843973

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AS POSTESTIMATION AFTER KMATCH

- Invoked kmatch-command in standalone usage is returned and can be copied for case-specific adjustments
- . qui: nopo decomp wage \${pred}, by(grp) kmatch(ps)
- . display "`e(kmatch_cmdline)'" kmatch ps grp age_c married edu lmexp parttime isco2d (wage) , tval(4) att generate wgenerate replace

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DESCRIPTION BY MATCHING STATUS

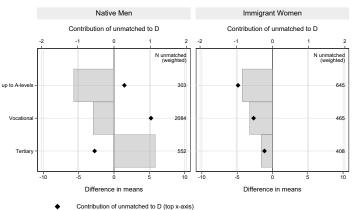
. qui: nopo decomp wage \${pred}, by(grp)

. nopo summari	. nopo summarize wage age married edu_1 edu_2 edu_3, label						
		Native Men		Immigran	t Women		
I	unmatched	matched	matched ~d	matched	unmatched		
			+	++			
Hourly wag~)			l				
Mean	19.7	21.3	16.2	13.8	10.6		
SD	9.71	10.4	9.74	7.65	5.52		
Age I				1			
Mean	44.8	43.9	38.9	38.9	41.6		
SD I	9.94	11	10.2	10	8.79		
Married			İ	i i			
Mean	.612	.669	I .607	i .607 i	.759		
SD I	.487	.471	.488	i .489 i	.428		
edu==up to~s	i i	i	i	i i			
Mean	.103	.055	l .199	i .199 i	.425		
SD I	.304	.228	l .399	1 .399	.494		
edu==Vocat~1	.504	. 220	l .333	1 .555	.434		
	700	I F04	1 40	1 10 1	200		
Mean	.709	.504	.49	.49	.306		
SD	.454	.5	.5	.5	.461		
edu==Terti~y							
Mean	.188	.441	.311	.311	. 269		
SD	.391	. 497	.463	.463	.443		



Variable-specific contribution to D_A and D_B

nopo dadb edu



Category-specific mean of unmatched - overall mean of matched (bottom x-axis)

See application in Sprengholz and Hamjediers (2022), Figure 2

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Components along outcome-distribution

. nopo gapoverdist Component distribution across 100 quantiles of wage requested

	Estimate	Sum over q	Minimum among compared g Unique q values	roups
D	-8.38	-8.39	100	2905
DO	-2.41	-2.36	98	1387
DX	-5.06	-5.1	98	3110
DA	.773	.773	100	2939
DB	-1.69	-1.69	100	1387

Note:

- The component sum across quantiles should correspond to the estimates with well populated quantiles.
- There are less unique quantile values than quantiles requested which means that across some quantiles, the value of wage does not change for (one of) the groups compared to estimate the component.
- Use the nquantiles(#) option to set the number of quantiles.

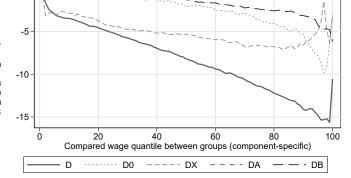
Components along outcome-distribution

nopo gapoverdist Component distribution across 100 quant

	 Estimate	Sum over q
	· 	
D	-8.38	-8.39
DO	-2.41	-2.36
DX	-5.06	-5.1
DA	.773	.773
DB	-1.69	-1.69

Note:

- The component sum across quantiles sh well populated quantiles.
- There are less unique quantile values that across some quantiles, the value (one of) the groups compared to estim
- Use the nquantiles(#) option to set t



See application in Nopo (2008), Figure 2

OUTLOOK

- On our to-do-list:
 - Options for component-size relative to gap
 - Standard errors are still too large and need to be adjusted
 - bootstrap-prefix can be applied
 - Write a help-file
- Current version is available on git: github.com/mhamjediers/nopo_decomposition
- Any feedback is of course very welcome



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