Assignment2

CMSC462

2024-09-19

```
#install.packages("tidyverse")
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.4
                     v readr
                                 2.1.5
## v forcats 1.0.0
                      v stringr
                                  1.5.1
                   v tibble
## v ggplot2 3.5.1
                                 3.2.1
## v lubridate 1.9.3
                      v tidyr
                                1.3.1
## v purrr
            1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
#Read data, and display sample of dataset
Data = read_csv(file = "C:/Users/criss/Desktop/CMSC462/Assignments/[9-22]Assignment 2/myData.csv")
## New names:
## Rows: 100000 Columns: 3
## -- Column specification
## ------ Delimiter: "," dbl
## (3): ...1, x, y
## i Use 'spec()' to retrieve the full column specification for this data. i
## Specify the column types or set 'show_col_types = FALSE' to quiet this message.
## * '' -> '...1'
Data
## # A tibble: 100,000 x 3
##
      . . . 1
             x
     <dbl> <dbl> <dbl>
##
        1 87.4
## 1
        2 41.9
## 2
                  10
                  13
## 3
        3 45.5
## 4
        4 30.7
## 5
       5 20.8
                  10
## 6
       6 17.1
## 7
        7 5.95
## 8
        8 19.5
## 9
       9 66.1
                   8
## 10
      10 92.0
```

i 99,990 more rows

```
#create an empty vector to store the point estimates of the samples to be taken for x&y,
#first 5 elements will be of sample 25, later 5 elements will be of sample 100.
meanx <- c()</pre>
meany <- c()</pre>
sdx \leftarrow c()
sdy <- c()
for(i in 1:10){ #iterate 10 times
  if(i<6){
    meanx[i] = mean(sample(Data$x,25)) #populate first 5 elements with PE of random sample of 25
    meany[i] = mean(sample(Data$y,25))
    sdx[i] = sd(sample(Data$x,25))
    sdy[i] = sd(sample(Data$y,25))
  }else{
    meanx[i] = mean(sample(Data$x,100)) #populate last 5 element with PE of random sample of 100
    meany[i] = mean(sample(Data$y,100))
    sdx[i] = sd(sample(Data$x,100))
    sdy[i] = sd(sample(Data$y,100))
  }
}
meanx
## [1] 55.22881 46.63432 51.89651 47.99033 38.98472 54.69677 54.34758 48.08768
## [9] 51.00309 51.26608
meany
## [1] 10.20 10.80 10.52 9.68 10.36 9.74 10.26 9.37 10.44 10.38
#Calculate 95% CI for x and y, by applying 95% CI = Xbar +- 1.96*(s/sqrt(n))
#Upper and lower limit for 25 samples:
UL_X_25 \leftarrow c()
UL_Y_25 <- c()
LL_X_25 \leftarrow c()
LL_Y_25 \leftarrow c()
#Apply the confidence interval formula for 95% confidence: Xbar +- 1.96(sd/sqrt(n))
for(i in 1:5){
  UL_X_{25}[i] = meanx[i] + (1.96)*(sdx[i] / sqrt(25))
  UL_Y_{25}[i] = meany[i] + (1.96)*(sdy[i] / sqrt(25))
  LL_X_{25}[i] = meanx[i] - (1.96)*(sdx[i] / sqrt(25))
 LL_Y_{25}[i] = meany[i] - (1.96)*(sdy[i] / sqrt(25))
#Upper and lower limit for 100 samples:
UL_X_{100} \leftarrow c()
UL_Y_{100} \leftarrow c()
LL_X_100 <- c()
LL_Y_100 \leftarrow c()
```

```
for(i in 6:10){
  UL_X_{100}[i-5] = meanx[i] + (1.96)*(sdx[i] / sqrt(100))
  UL_Y_{100}[i-5] = meany[i] + (1.96)*(sdy[i] / sqrt(100))
  LL_X_{100}[i-5] = meanx[i] - (1.96)*(sdx[i] / sqrt(100))
 LL_Y_{100}[i-5] = meany[i] - (1.96)*(sdy[i] / sqrt(100))
UL_X_25
## [1] 66.28655 58.73508 64.57241 59.84808 51.32745
UL_Y_25
## [1] 11.49380 12.04723 11.67335 10.88886 11.22418
LL_X_25
## [1] 44.17106 34.53357 39.22061 36.13257 26.64200
LL_Y_25
## [1] 8.906202 9.552766 9.366649 8.471139 9.495820
UL_X_100
## [1] 60.25964 60.25128 53.61980 56.63454 56.77940
UL_Y_100
## [1] 10.32726 10.82547 10.00603 10.99550 11.07148
LL_X_100
## [1] 49.13390 48.44387 42.55557 45.37164 45.75276
LL_Y_100
## [1] 9.152740 9.694526 8.733969 9.884495 9.688524
# Create a 2x4 matrix to display the intervals
table <- matrix(nrow = 4, ncol = 2)
\# Name the columns and rows appropriately
colnames(table) <- c('Lower limit', 'Upper limit')</pre>
rownames(table) <- c('X 25 sample', 'Y 25 sample', 'X 100 sample', 'Y 100 sample')</pre>
# Calculate the means of each upper limit and lower limit for the CI's
limits <- c(mean(LL_X_25), mean(UL_X_25),</pre>
```

```
mean(LL_Y_25), mean(UL_Y_25),
            mean(LL_X_100), mean(UL_X_100),
            mean(LL_Y_100), mean(UL_Y_100))
# Fill the table with the calculated means
table[,] <- matrix(limits, nrow = 4, byrow = TRUE)</pre>
# Convert to table
limits_table <- as.table(table)</pre>
limits table
##
                Lower limit Upper limit
## X 25 sample
                               60.153916
                  36.139960
                               11.465485
## Y 25 sample
                   9.158515
## X 100 sample
                  46.251548
                               57.508932
## Y 100 sample
                   9.430851
                               10.645149
#Calculate actual population means
mean(Data$x)
## [1] 50.01188
mean(Data$y)
```

[1] 10.00173

cat("As we can see, the actual mean for x is ~50.01, and the actual mean for y
 is ~10, for the population. Both of these values fall into their sampled
 95% confidence intervals, for both 25 samples and 100 samples. 50.01 falls
 into the 25 x sample: (40.82,64.43) CI and into the 100 x sample:
 (42.79, 54.29) CI. And 10 falls into the 25 y sample: (9.06,11.42) CI and
 into the 100 y sample: (9.22, 10.41) CI. We can observe that for both X
 and Y, the 100 sample confidence intervals are more accurate in regards to
 the population mean, because both upper and lower limits are closer to the
 true mean compared to the 25 sample intervals.")

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