Worksheet2

STAT414

2024-09-15

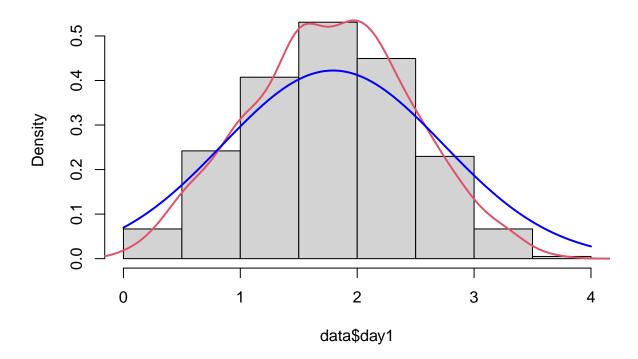
```
# #1 - Use the DownloadFestival data set for this part. The dataset and its analysis is available
# in DSUR book.
#install.packages("EnvStats")
#read in the data using read.table, delimited by whitespace, filling blank values
data <- read.table("C:/Users/criss/Desktop/STAT414/Assignments/9-21/DownloadFestival.dat",
                   header = TRUE, sep = "", stringsAsFactors = FALSE, fill=TRUE)
head(data, 10)
##
      ticknumb gender day1 day2 day3
## 1
          2111
                Male 2.64 1.35 1.61
## 2
          2229 Female 0.97 1.41 0.29
         2338 Male 0.84
## 3
                           NA
                                 NA
## 4
         2384 Female 3.03
                                 NA
                           NA
## 5
         2401 Female 0.88 0.08
                                 NA
## 6
         2405 Male 0.85 NA
                                 NA
## 7
         2467 Female 1.56 NA
                                 NA
## 8
         2478 Female 3.02 NA
                                 NA
## 9
         2490 Male 2.29 NA
                                 NA
## 10
         2504 Female 1.11 0.44 0.55
max(data$day1)
## [1] 20.02
max(data$day2,na.rm = TRUE)
## [1] 3.44
max(data$day3,na.rm = TRUE)
## [1] 3.41
sd(data$day1,na.rm = TRUE)
```

[1] 0.9444949

```
day2_sd <- sd(data$day2,na.rm = TRUE)
day3_sd <- sd(data$day3,na.rm = TRUE)

#Generate histogram, histogram line, and superimpose normal line for day 1 data
hist(data$day1,probability=TRUE,xlim = c(0, 4),breaks= c(0,0.5,1,1.5,2,2.5,3,3.5,4,4.5,22))
lines(density(data$day1), col = 2, lwd = 2)
curve(dnorm(x, mean=mean(data$day1), sd=sd(data$day1)), lwd=2, col="blue", add=TRUE)</pre>
```

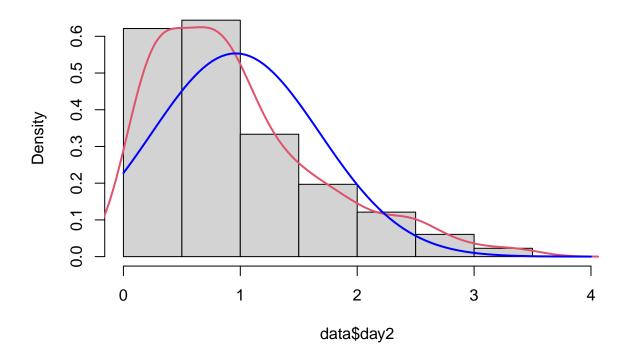
Histogram of data\$day1



cat("The normal line is symmetric and matches the actual line representation of 'day 1' well,
therefore we can say that a Normal Distribution is appropriate for this dataset.")

The normal line is symmetric and matches the actual line representation of 'day 1' well, ## therefore we can say that a Normal Distribution is appropriate for this dataset.

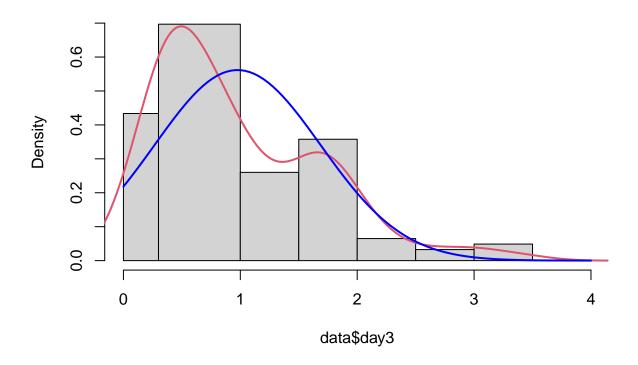
Histogram of data\$day2



cat("The normal line is heavily skewed with a right-skew and a long tail, the line is definitely
not symmetric, therefore we can say that a Normal Distribution is not appropriate for 'day 2'")

The normal line is heavily skewed with a right-skew and a long tail, the line is definitely ## not symmetric, therefore we can say that a Normal Distribution is not appropriate for 'day 2'

Histogram of data\$day3

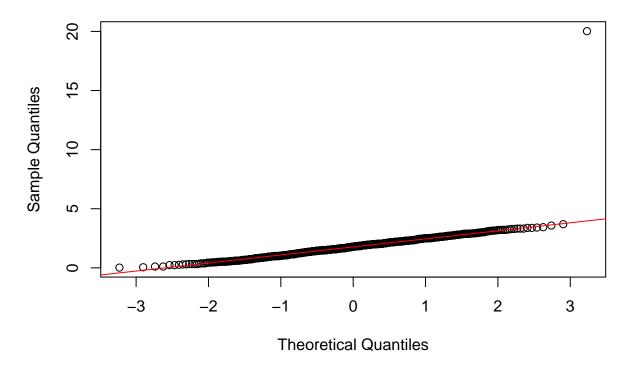


cat("The normal line is heavily skewed with a right-skew and a long tail, the line is definitely
not symmetric, therefore we can say that a Normal Distribution is not appropriate for 'day 3'")

The normal line is heavily skewed with a right-skew and a long tail, the line is definitely ## not symmetric, therefore we can say that a Normal Distribution is not appropriate for 'day 3'

```
#Create qqplots of the 3 days, as well as a reference line that shows normal fit
qqnorm(data$day1, main="day1 qq plot")
qqline(data$day1, col="red")
```

day1 qq plot

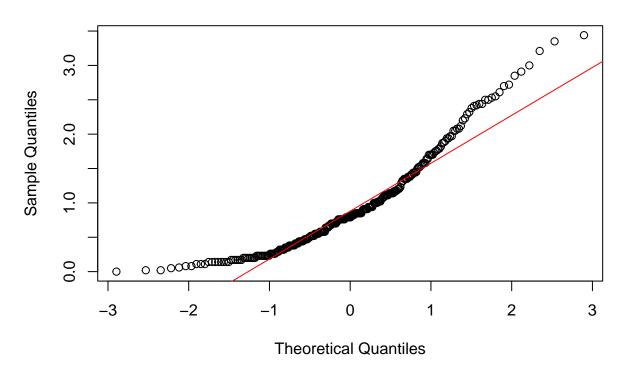


cat("The datapoints of day 1 fall along the reference line, therefore we can say
 Normal distribution is appropriate to model this dataset")

The datapoints of day 1 fall along the reference line, therefore we can say
Normal distribution is appropriate to model this dataset

```
qqnorm(data$day2, main="day2 qq plot")
qqline(data$day2, col="red")
```

day2 qq plot

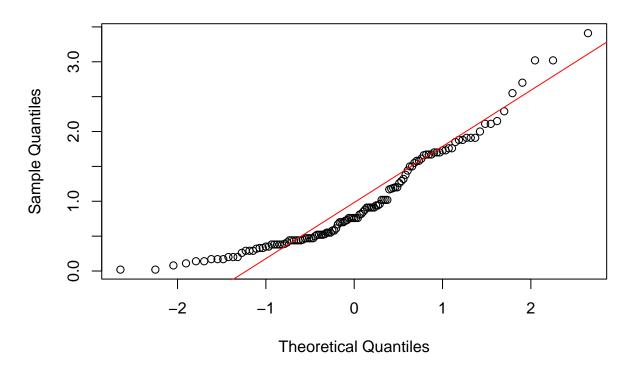


cat("The datapoints of day 2 do not fall along the reference line, therefore
we can say Normal distribution is not appropriate to model this dataset")

The datapoints of day 2 do not fall along the reference line, therefore ## we can say Normal distribution is not appropriate to model this dataset

```
qqnorm(data$day3, main="day3 qq plot")
qqline(data$day3, col="red")
```

day3 qq plot



cat("The datapoints of day 3 do not fall along the reference line, therefore
we can say Normal distribution is not appropriate to model this dataset")

The datapoints of day 3 do not fall along the reference line, therefore ## we can say Normal distribution is not appropriate to model this dataset

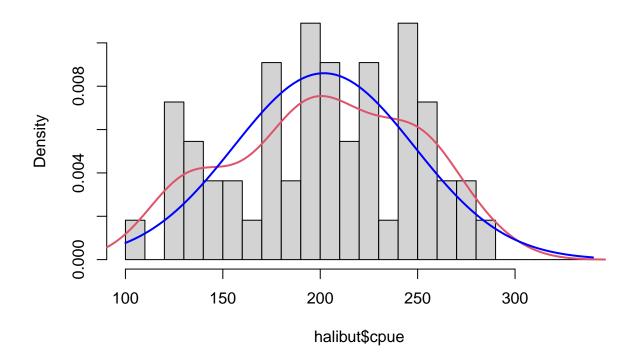
```
# #2 - The dataset halibut (available in the R package EnvStats) has two variables: Annual Catch
# Per Unit Effort (CPUE), and biomass and exploitable biomass of Pacific halibut for the years
# 1935 through 1989. Dataset is analyzed in the Millard and Neerchal book. (Warning: It uses
# SPLUS, a precursor to the R package. Syntax is very similar, but not identical.)
library(readxl)
library(ggplot2)

data <- read_excel("halibut_df.xls") #import excel data
halibut <- data.frame(data) #convert excel sheet to dataframe
head(halibut,10)</pre>
```

```
##
      cpue biomass
      132
           171.19
## 2
      143 179.71
## 3
       160
           182.77
## 4
       171 190.01
## 5
      145
           199.12
## 6
      155 208.18
```

```
## 7 178 214.28
## 8 179 222.83
## 9 177 239.13
## 10 221 258.25
#Compute summary statistics of cpue and biomass
summary(halibut$cpue)
##
     Min. 1st Qu. Median
                           Mean 3rd Qu.
                                             Max.
##
     108.0 174.0 202.0
                            201.9 242.0
                                            290.0
summary(halibut$biomass)
     Min. 1st Qu. Median Mean 3rd Qu.
##
                                             Max.
##
    124.0 181.2 241.3 236.5 300.5 314.9
#loop to generate breaks for the histogram of cpue
cpue_breaks <- c()</pre>
i <- 100
count <- 1
while(i <= max(halibut$cpue)+50){</pre>
  cpue_breaks[count] = i
 i <- i + 10
 count <- count + 1</pre>
}
cpue_breaks
## [1] 100 110 120 130 140 150 160 170 180 190 200 210 220 230 240 250 260 270 280
## [20] 290 300 310 320 330 340
#Histogram of cpue, with normal curve
hist(halibut$cpue,probability=TRUE,breaks=cpue_breaks)
lines(density(halibut$cpue), col = 2, lwd = 2)
curve(dnorm(x, mean=mean(halibut$cpue), sd=sd(halibut$cpue)), lwd=2,
col="blue", add=TRUE)
```

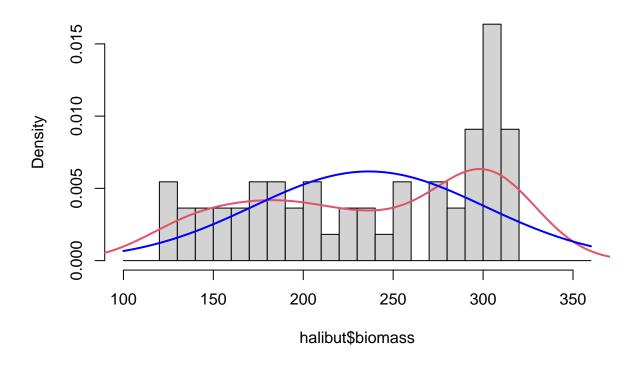
Histogram of halibut\$cpue



```
#loop to generate breaks for the histogram of biomass
bio_breaks <- c()
j <- 100
count2 <- 1
while(j <= max(halibut$biomass)+50){
  bio_breaks[count2] = j
  j <- j + 10
  count2 <- count2 + 1
}
bio_breaks</pre>
```

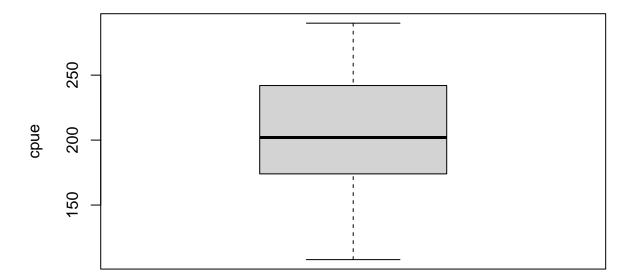
[1] 100 110 120 130 140 150 160 170 180 190 200 210 220 230 240 250 260 270 280 ## [20] 290 300 310 320 330 340 350 360

Histogram of halibut\$biomass



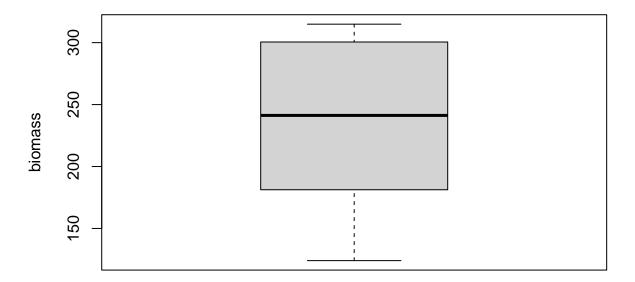
#Boxplot of cpue
boxplot(data\$cpue,main="Boxplot of cpue", ylab="cpue")

Boxplot of cpue



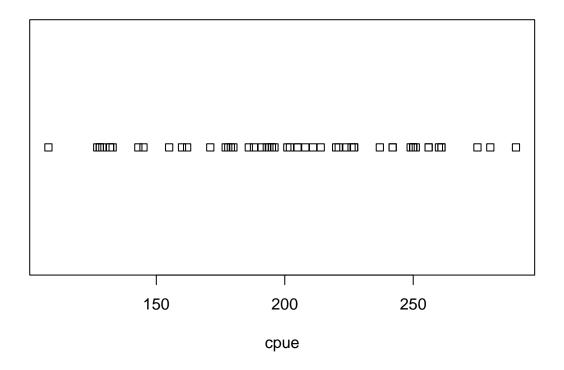
```
#Boxplot of biomass
boxplot(data$biomass,main="Boxplot of biomass", ylab="biomass")
```

Boxplot of biomass



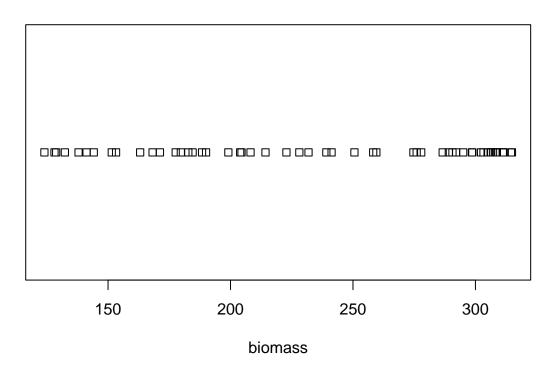
```
#Strip plot of cpue
stripchart(data$cpue,main="Strip plot of cpue", xlab="cpue")
```

Strip plot of cpue



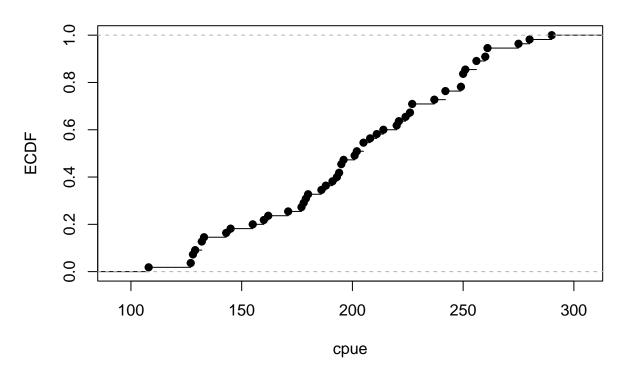
```
#Strip plot of biomass
stripchart(data$biomass,main="Strip plot of biomass", xlab="biomass")
```

Strip plot of biomass



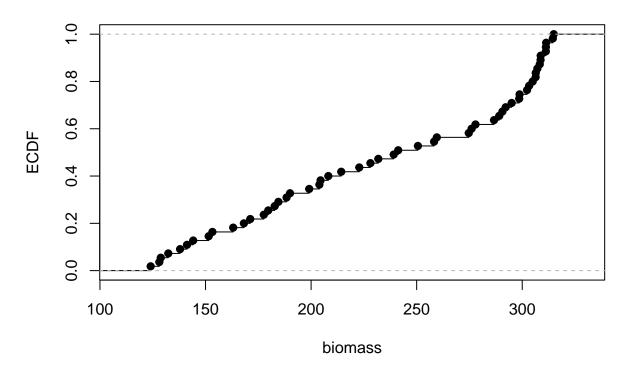
```
#Quantile (Empirical CDF / ECDF) plot of cpue
ecdf_cpue <- ecdf(halibut$cpue) #use ecdf function
plot(ecdf_cpue, main = "Quantile plot of cpue", xlab = "cpue", ylab = "ECDF")</pre>
```

Quantile plot of cpue



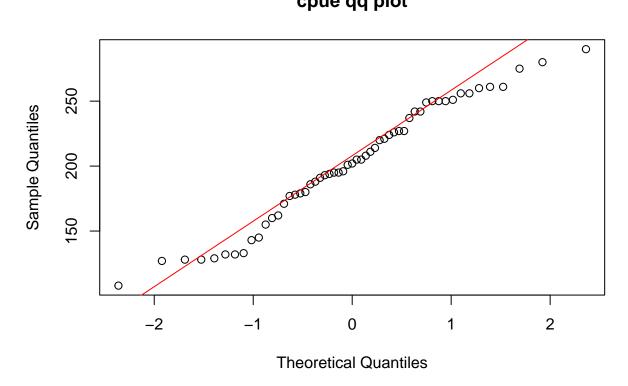
```
#Quantile (Empirical CDF / ECDF) plot of cpue
ecdf_biomass <- ecdf(halibut$biomass) #use ecdf function
plot(ecdf_biomass, main = "Quantile plot of biomass", xlab = "biomass", ylab = "ECDF")</pre>
```

Quantile plot of biomass

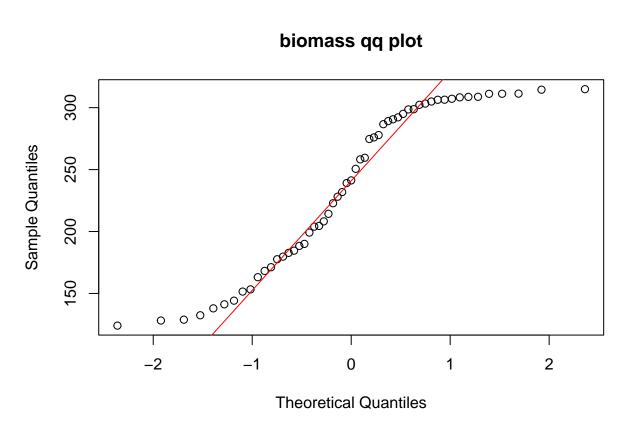


```
#qqplot and reference line of cpue
qqnorm(halibut$cpue, main="cpue qq plot")
qqline(halibut$cpue, col="red")
```

cpue qq plot



```
#qqplot and reference line of biomass
qqnorm(halibut$biomass, main="biomass qq plot")
qqline(halibut$biomass, col="red")
```



```
#For the tukey mean difference plot, there are no 2 groups to compare cpue and biomass
#therefore simply divide the dataset in half and compare the two halves.
\#nrow(halibut) = 55
cpue1 <- halibut$cpue[1:(55/2)]</pre>
cpue2 <- halibut$cpue[ceiling((55/2)):55]</pre>
length(cpue1)
```

[1] 27

```
length(cpue2)
```

[1] 28

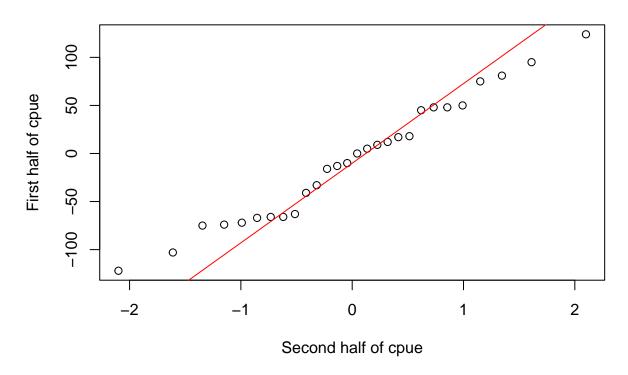
```
bio1 <- halibut$biomass[1:(55/2)]</pre>
bio2 <- halibut$biomass[ceiling((55/2)):55]
#Tukey mean difference plot of cpue
qqnorm(cpue2 - cpue1, main="Tukey Mean-Difference Q-Q Plot for cpue",
       xlab="Second half of cpue", ylab="First half of cpue")
```

Warning in cpue2 - cpue1: longer object length is not a multiple of shorter ## object length

```
qqline(cpue2 - cpue1, col = "red")
```

Warning in cpue2 - cpue1: longer object length is not a multiple of shorter
object length

Tukey Mean-Difference Q-Q Plot for cpue

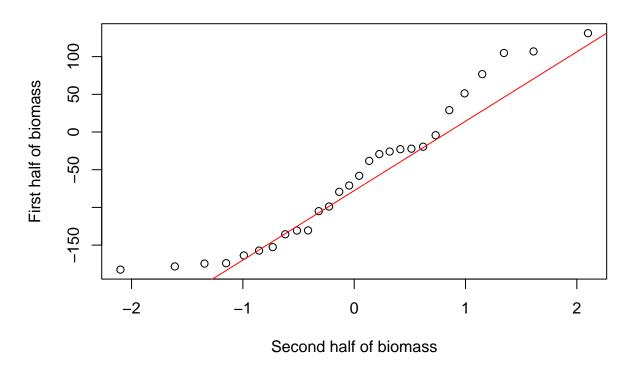


Warning in bio2 - bio1: longer object length is not a multiple of shorter
object length

```
qqline(bio2 - bio1, col = "red")
```

Warning in bio2 - bio1: longer object length is not a multiple of shorter
object length

Tukey Mean-Difference Q-Q Plot for biomass



cat("Cpue appears to be normally distributed if we analyze the features of all the visual plots we have generated for cpue.

- * The histogram has a clear symmetrical curve that the super-imposed normal curve is very similar to. The peak is centered.
- * The boxplot is mostly symmetrical about the median, and the wiskers are of equal length, supporting a normal distribution.
- * In the strip plot, the datapoints are not symmetrical about the mean, the concentration of the datapoints are left-skewed, and the spread of the datapoints are uneven.
- \ast In the quantile plot, the curve somewhat resembles a S-shape, but the curve is not symmetrical about the median.
- * In the qqplot, the datapoints stray away from the refernce line.

##

##

##

##

* In the tukey mean-difference qqplot, the datapoints again do not follow the reference line accurately.

Cpue appears to be normally distributed if we analyze the features of all the
visual plots we have generated for cpue.

- * The histogram has a clear symmetrical curve that the super-imposed normal curve is very similar to. The peak is centered.
- * The boxplot is mostly symmetrical about the median, and the wiskers are of equal length, supporting a normal distribution.
- ## * In the strip plot, the datapoints are not symmetrical about the mean, the

 concentration of the datapoints are left-skewed, and the spread of the datapoints

 are uneven.
- ## * In the quantile plot, the curve somewhat resembles a S-shape, but the curve is

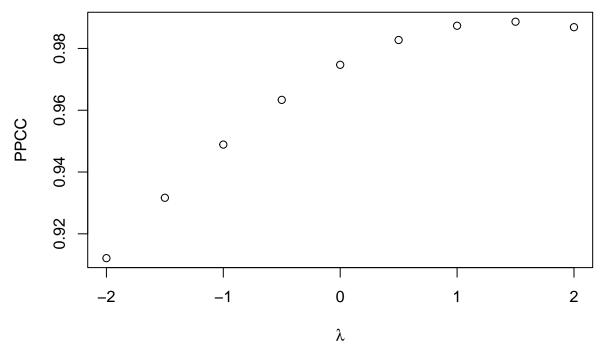
```
##
       not symmetrical about the median.
##
       * In the qqplot, the datapoints stray away from the refernce line.
       * In the tukey mean-difference qqplot, the datapoints again do not follow the
##
##
       reference line accurately.
##
cat("Biomass appears to not be normally distributed if we analyze the features of all the
    visual plots we have generated.
    * The histogram does not have a symmetrical curve and the peak is skewed to the left.
    * The boxplot is symmetrical about the median, however the wiskers are of extremely varying
   length, which does not support normal distribution.
    * In the strip plot, the datapoints are mostly symmetrical about the mean, the
   concentration of the datapoints are most prevalent around the mean, and the
   spread of the datapoints are even on both sides from the mean.
    * In the quantile plot, the curve resembles a S-shape, and the curve is
   symmetrical about the median.
    * In the applot, the datapoints follow the refernce line accurately.
    * In the tukey mean-difference qqplot, the datapoints follow the reference
   line accurately.
    ")
## Biomass appears to not be normally distributed if we analyze the features of all the
##
       visual plots we have generated.
##
       * The histogram does not have a symmetrical curve and the peak is skewed to the left.
##
       * The boxplot is symmetrical about the median, however the wiskers are of extremely varying
##
       length, which does not support normal distribution.
##
       * In the strip plot, the datapoints are mostly symmetrical about the mean, the
##
       concentration of the datapoints are most prevalent around the mean, and the
##
       spread of the datapoints are even on both sides from the mean.
##
       * In the quantile plot, the curve resembles a S-shape, and the curve is
##
       symmetrical about the median.
##
       * In the qqplot, the datapoints follow the refernce line accurately.
       * In the tukey mean-difference qqplot, the datapoints follow the reference
##
##
       line accurately.
##
library(EnvStats)
## Attaching package: 'EnvStats'
## The following objects are masked from 'package:stats':
##
##
       predict, predict.lm
*perform boxcox transformation on cpue for (-2,2) incrementing by .5
box_cpue <- boxcox(halibut$cpue, lambda = seq(-2, 2, by=0.5), plot = TRUE,
                   otpimize = FALSE)
#plot lambda vs PPCC
box_cpue
```

##

```
## Results of Box-Cox Transformation
##
##
                                      PPCC
  Objective Name:
##
## Data:
                                      halibut$cpue
                                      55
## Sample Size:
##
##
    lambda
                 PPCC
      -2.0 0.9121241
##
      -1.5 0.9316654
      -1.0 0.9488856
##
      -0.5 0.9633503
##
##
       0.0 0.9747060
##
       0.5 0.9827267
##
       1.0 0.9873434
       1.5 0.9886486
##
       2.0 0.9868768
##
```

plot(box_cpue)

Box-Cox Transformation Results: PPCC vs. lambda for halibut\$cpue

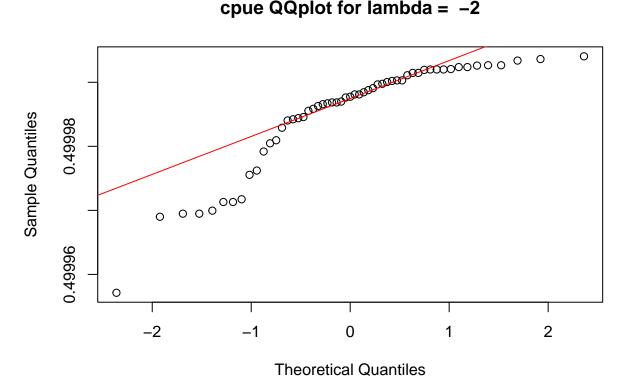


#Retrieve the optimal lambda with the highest PPCC value
cat("From the box_cpue output and plot, it is read that 1.5 produces the highest PPCC
 value. Thus select 1.5 to be the optimal lambda")

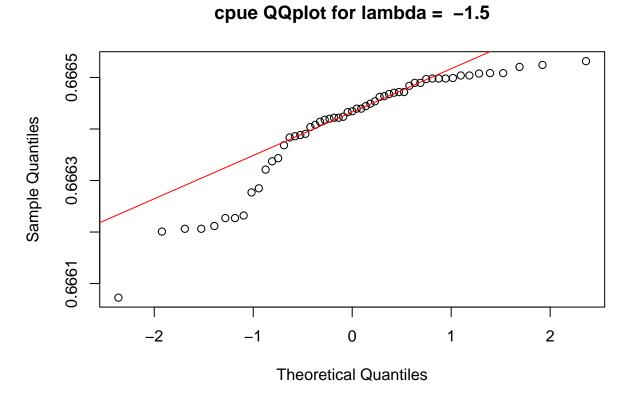
From the box_cpue output and plot, it is read that 1.5 produces the highest PPCC value. Thus select 1.5 to be the optimal lambda

```
#transform cpue with every value of lambda and qqplot every transformation
for(i in seq(-2, 2, by=0.5)){
  cpue_transform <- boxcoxTransform(halibut$cpue, lambda = i)</pre>
  qqnorm(cpue_transform, main=paste("cpue QQplot for lambda = ", i))
  qqline(cpue_transform, col = "red")
}
```

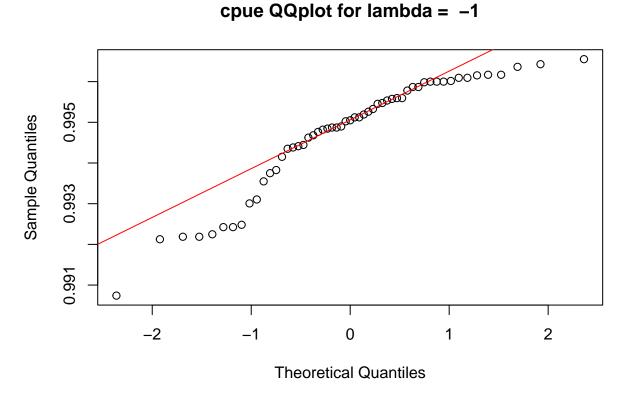
cpue QQplot for lambda = -2



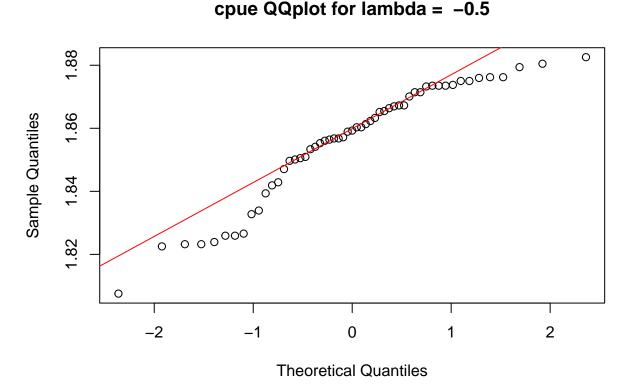
cpue QQplot for lambda = -1.5



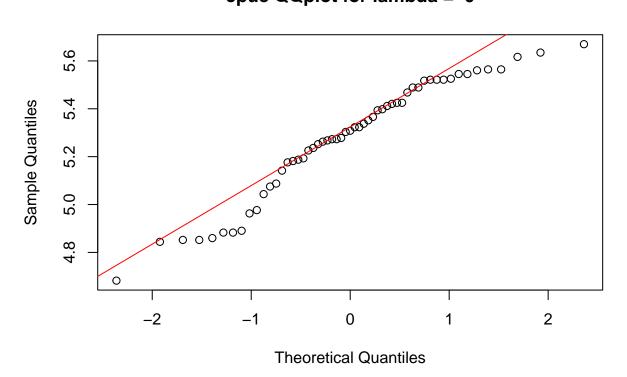
cpue QQplot for lambda = -1



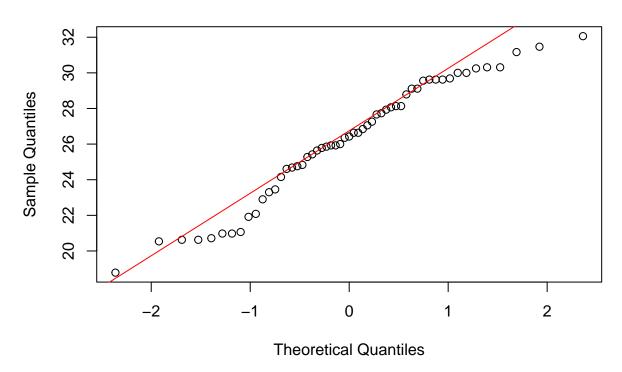
cpue QQplot for lambda = -0.5



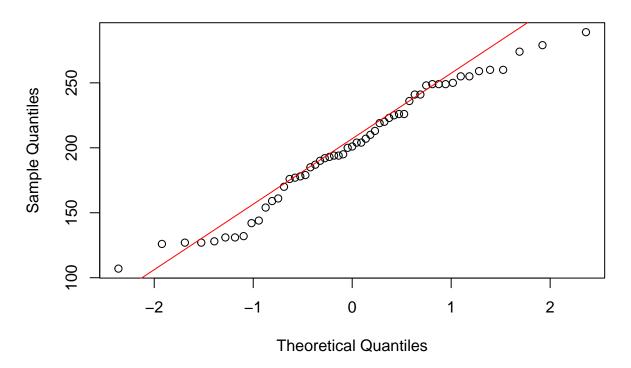
cpue QQplot for lambda = 0



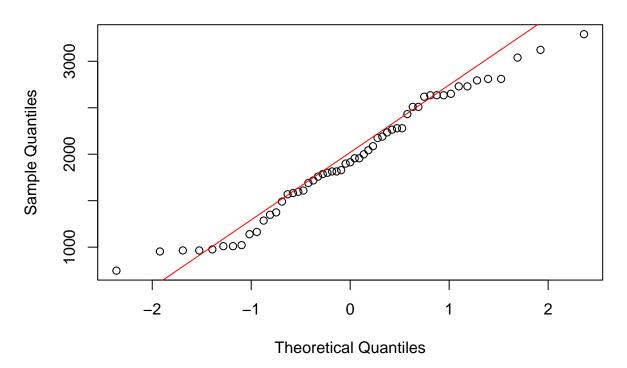
cpue QQplot for lambda = 0.5



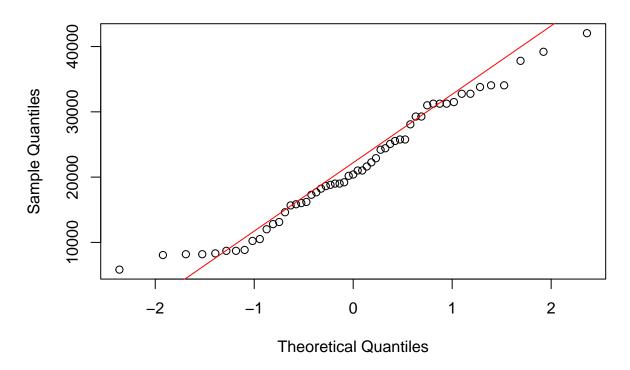
cpue QQplot for lambda = 1



cpue QQplot for lambda = 1.5



cpue QQplot for lambda = 2



```
cat("Based on the results of the lambda vs PPCC plot, and the qqplots of
   all the transformations of cpue for each lambda, lambda=1.5 produced the
   highest value of PPCC, and the plots for the transformations of lambdas 0-2 of
   cpue were very similar, therefore lambda=1.5 with the highest PPCC value
   appears to be the best transformation. A higher PPCC value implies
   a closer match for the transformed data to be normally distributed.")
```

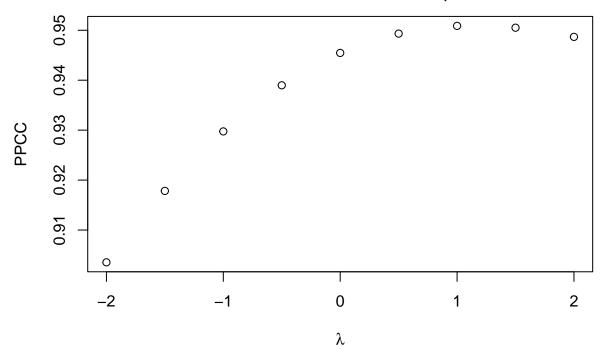
```
## Based on the results of the lambda vs PPCC plot, and the qqplots of
## all the transformations of cpue for each lambda, lambda=1.5 produced the
## highest value of PPCC, and the plots for the transformations of lambdas 0-2 of
## cpue were very similar, therefore lambda=1.5 with the highest PPCC value
## appears to be the best transformation. A higher PPCC value implies
## a closer match for the transformed data to be normally distributed.
```

```
##
## Results of Box-Cox Transformation
## -----
##
##
## Objective Name: PPCC
```

```
##
## Data:
                                      halibut$biomass
##
## Sample Size:
                                      55
##
##
    lambda
                 PPCC
      -2.0 0.9035375
      -1.5 0.9178377
##
##
      -1.0 0.9297465
##
      -0.5 0.9389792
       0.0 0.9454617
       0.5 0.9493274
##
       1.0 0.9508767
##
       1.5 0.9505129
##
       2.0 0.9486756
```

plot(box_bio)

Box-Cox Transformation Results: PPCC vs. lambda for halibut\$biomass

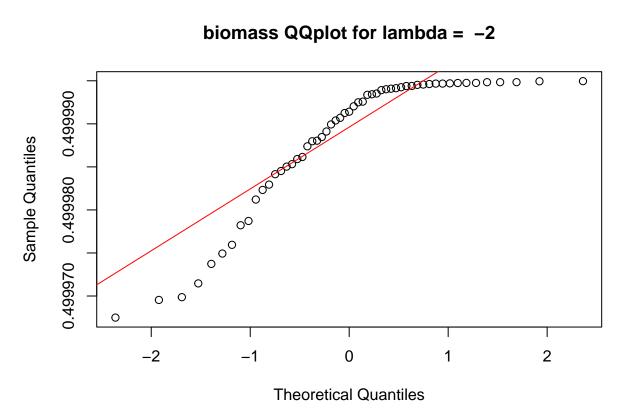


#Retrieve the optimal lambda with the highest PPCC value
cat("From the box_bio output and plot, it is read that 1 produces the highest PPCC
 value. Thus select 1 to be the optimal lambda")

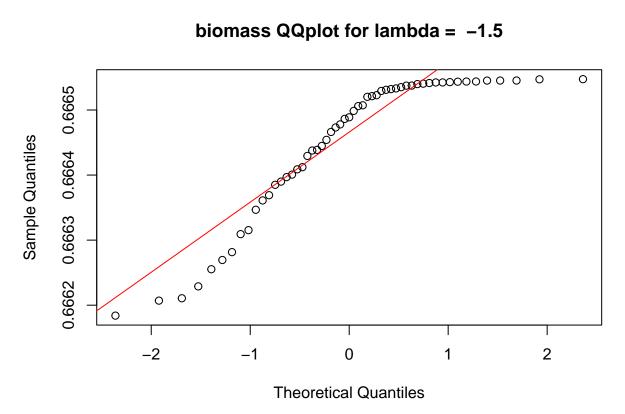
From the box_bio output and plot, it is read that 1 produces the highest PPCC
value. Thus select 1 to be the optimal lambda

```
\hbox{\it\#transform biomass with every value of lambda and $qqplot$ every transformation}
for(i in seq(-2, 2, by=0.5)){
  bio_transform <- boxcoxTransform(halibut$biomass, lambda = i,)</pre>
  qqnorm(bio_transform, main=paste("biomass QQplot for lambda = ", i))
  qqline(bio_transform, col = "red")
```

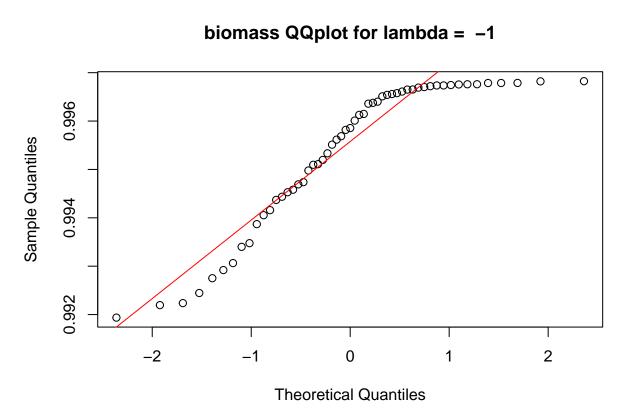
biomass QQplot for lambda = -2



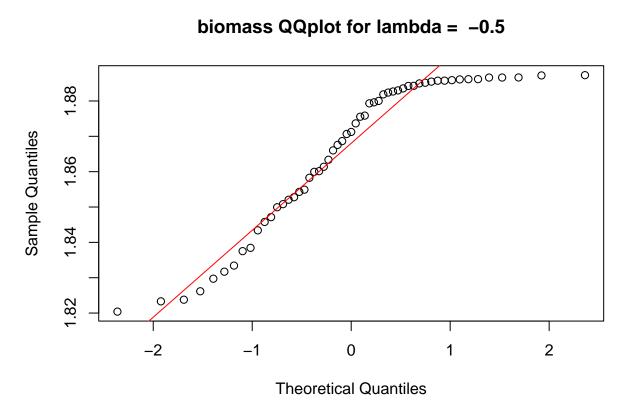
biomass QQplot for lambda = -1.5



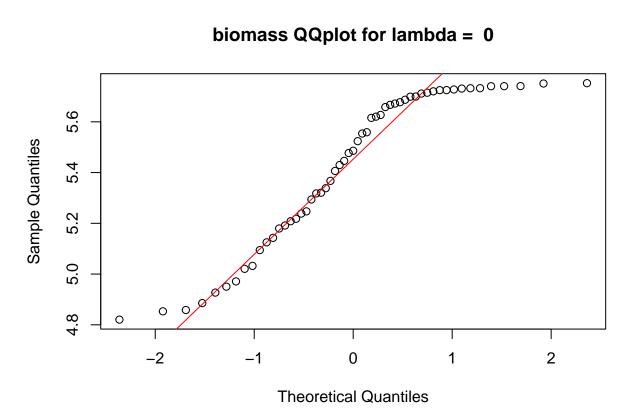
biomass QQplot for lambda = -1

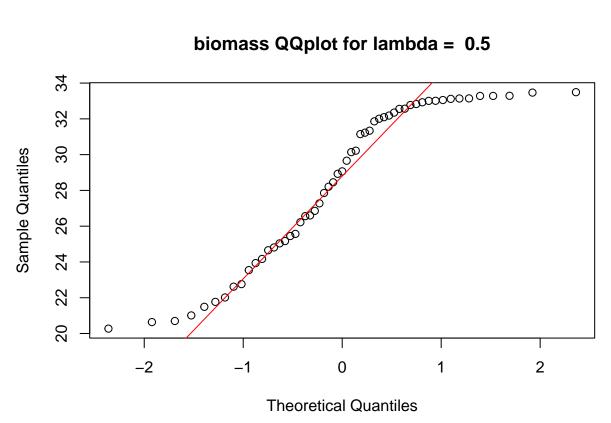


biomass QQplot for lambda = -0.5

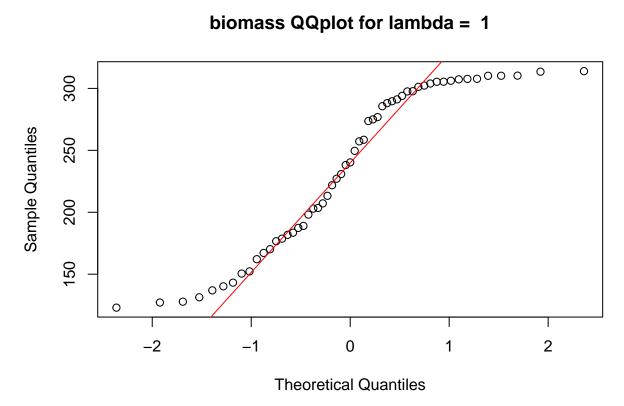


biomass QQplot for lambda = 0

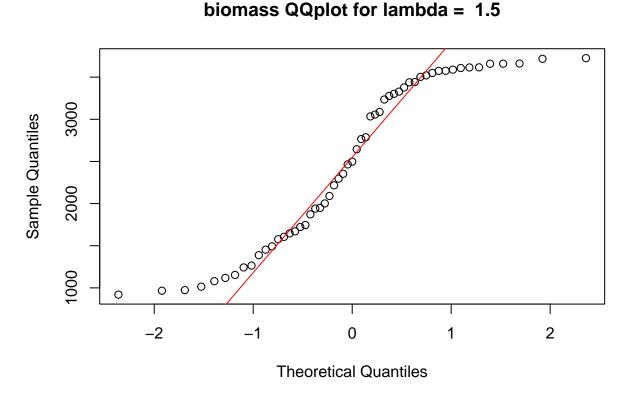




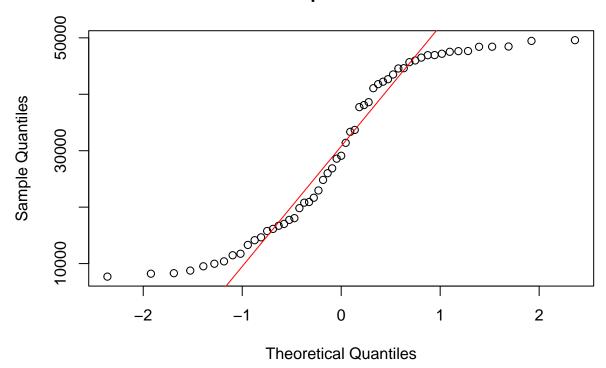
biomass QQplot for lambda = 1



biomass QQplot for lambda = 1.5



biomass QQplot for lambda = 2



cat("Based on the results of the lambda vs PPCC plot, and the qqplots of
 all the transformations of biomass for each lambda, lambda=1 produced the
 highest value of PPCC, and the plots for transformations of lambdas 0-2 of biomass
 were very similar, therefore lambda=1 with the highest PPCC value appears to be
 the best transformation. A higher PPCC value implies a closer match for
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```
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```

```
# #3 - Use the function stat.desc() of R (install the relevant R package as necessary) and obtain
# the output of page 57 of the Exploring Data, Exploring Assumptions, Graphs.pdf for
# the variables CPUE and biomass. Provide the definition/formula for each of the statistic
# computed in this output. (These formulas, for the most part, are available in Millard and
# Neerchal book. You should be able to look up the index and find the formula.) Draw
# conclusions on the normality (or lack of) of the variables.

#install.packages("pastecs")
library(pastecs)
statdesc <- stat.desc(cbind(halibut$cpue, halibut$biomass), basic = FALSE, norm = TRUE)</pre>
```

colnames(statdesc) <- c("cpue", "biomass") statdesc</pre>

```
##
                                  biomass
                       cpue
                202.0000000 2.412600e+02
## median
                201.9272727 2.364964e+02
## mean
## SE.mean
                  6.2541490 8.716848e+00
## CI.mean.0.95 12.5388139 1.747623e+01
            2151.2909091 4.179089e+03
## std.dev
               46.3820106 6.464588e+01
                 0.2296966 2.733483e-01
## coef.var
## skewness
                -0.1648767 -2.789871e-01
## skew.2SE
                 -0.2562250 -4.335570e-01
## kurtosis
                 -0.9698153 -1.452879e+00
                 -0.7654336 -1.146695e+00
## kurt.2SE
                  0.9676733 8.908189e-01
## normtest.W
## normtest.p
                  0.1445546 1.211366e-04
```

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Skewness =
$$\frac{n}{(n-1)(n-2)} \sum_{i=1}^{n} \left(\frac{x_i - \bar{x}}{s}\right)^3$$

cat("Skew.2SE is skewness divided by 2 times its standard error.")

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$$Skew.2SE = \frac{Skewness}{(2)(SE)}$$

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cat("kurt.2SE is kurtosis divided by 2 times its standard error.")

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cat("We can draw conclusions about the normality of cpue and biomass from their skewness and kurtosis statistics.

cpue has a skewness of -0.1648767 and a kurtosis of -0.9698153, which shows that the skewness is not very far from normality (no skew = 0), and the kurtosis is not far from 0 (normality), and implies that the tails are light. Thus we can say that there is a high probability of cpue being normally distributed. biomass has a skewness of -.2789871 and a kurtosis of -1.452879. This also shows that there is a slight left-skew for biomass and the skew is close to normality(0). The kurtosis is also not extremely far from 0, but less than -1 or greater than 1 indicates tail behavior that does not match normal distribution. Therefore we can say that biomass is less likely to be normally distributed than cpue, and is more likely to not be normally distributed.

```
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## can say that biomass is less likely to be normally distributed than cpue, and is
## more likely to not be normally distributed.
```

")