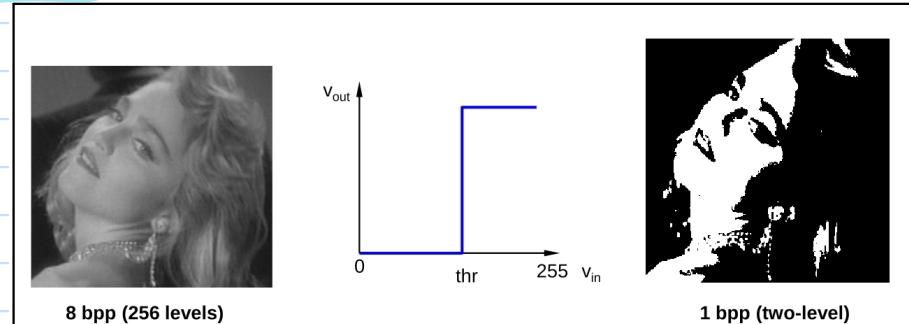


## Digital Halftoning

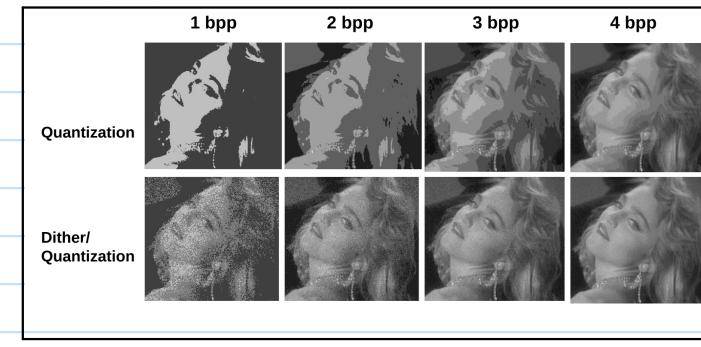
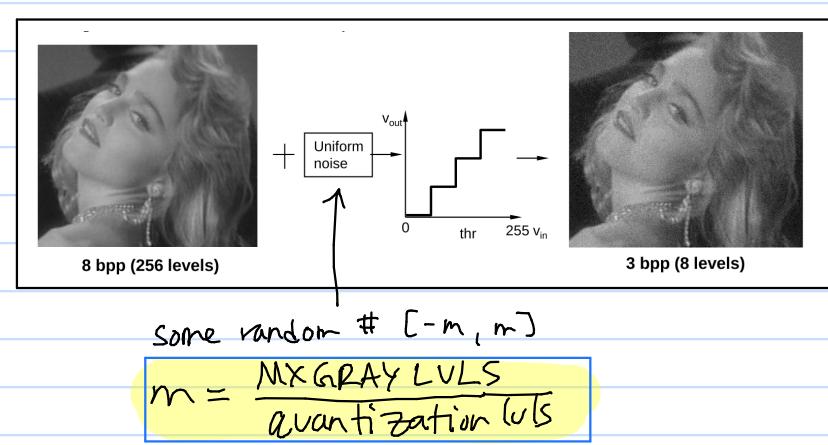
Thresholding: easy way to turn grayscale to binary



↔ loss of info

### Unordered Dither

- add uniformly distributed white noise (dither signal) to input image b4l quantization
- dither hides artifacts



### Ordered Dithering

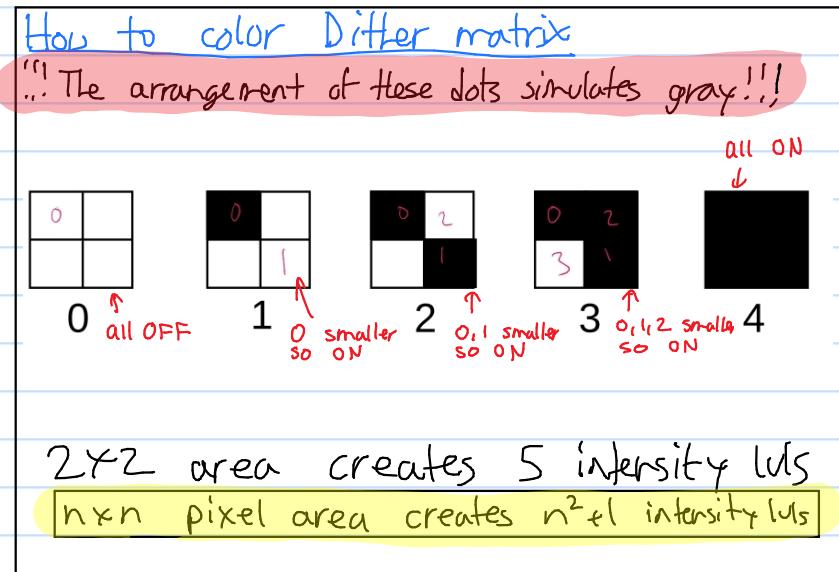
Can simulate gray by some black/white dotting pattern!!!

Dither Matrix

$$D^{(2)} = \begin{bmatrix} 0 & 2 \\ 3 & 1 \end{bmatrix} \quad D^{(3)} = \begin{bmatrix} 6 & 8 & 4 \\ 1 & 0 & 3 \\ 5 & 2 & 7 \end{bmatrix}$$

From  $D^2$  and  $D^3$ , can use this Eq to find larger Dithers:

$$D^{(n)} = \begin{bmatrix} 4D^{(n/2)} + D_{00}^{(2)}U^{(n/2)} & 4D^{(n/2)} + D_{01}^{(2)}U^{(n/2)} \\ 4D^{(n/2)} + D_{10}^{(2)}U^{(n/2)} & 4D^{(n/2)} + D_{11}^{(2)}U^{(n/2)} \end{bmatrix}$$



### (1) from 2x2 dither matrix

$$D^{(2)} = \begin{bmatrix} 0 & 2 \\ 3 & 1 \end{bmatrix}$$

### (2) Using Eq to find 4x4 or D<sup>4</sup> Dither Matrix

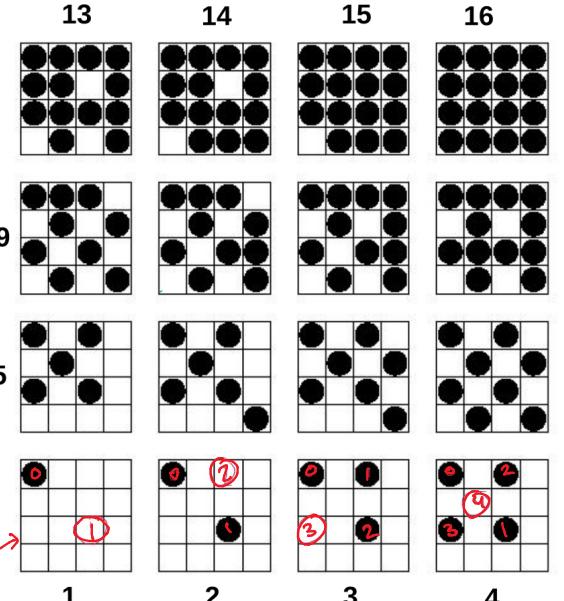
$$U_D^{(n/2)} + D_{00}^{(2)} U^{(n/2)} \rightarrow \begin{bmatrix} 0 & 8 \\ 2 & 4 \end{bmatrix} + 0 \quad U_D^{(n/2)} + D_{10}^{(2)} U^{(n/2)} \rightarrow \begin{bmatrix} 0 & 8 \\ 2 & 4 \end{bmatrix} + 3$$

$$U_D^{(n/2)} + D_{01}^{(2)} U^{(n/2)} \rightarrow \begin{bmatrix} 0 & 8 \\ 2 & 4 \end{bmatrix} + 2$$

$$U_D^{(n/2)} + D_{11}^{(2)} U^{(n/2)} \rightarrow \begin{bmatrix} 0 & 8 \\ 2 & 4 \end{bmatrix} + 1$$

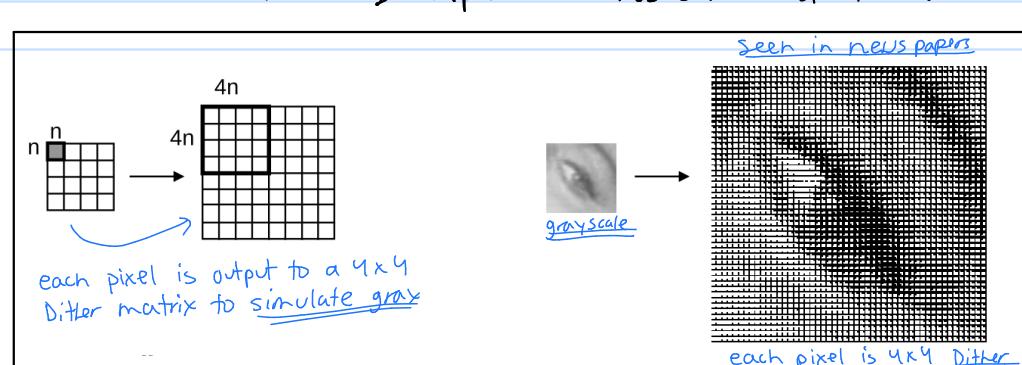
### (3) Make D<sup>4</sup>

$$D^{(4)} = \begin{bmatrix} 0 & 8 & 2 & 10 \\ 12 & 4 & 14 & 6 \\ 3 & 11 & 1 & 9 \\ 15 & 7 & 13 & 5 \end{bmatrix}$$



### Patterning

- let output image > input img
- 1) quantize input [0 ... n<sup>2</sup>] gray lvs
- 2) threshold each pixel against all entries in Dither matrix
  - each pixel → 1x4 block of black/white dots (D<sup>4</sup> matrix)
  - n x n input pixel → 4n x 4n output image
- If a large input area has same constant val → output same val



### Implementation

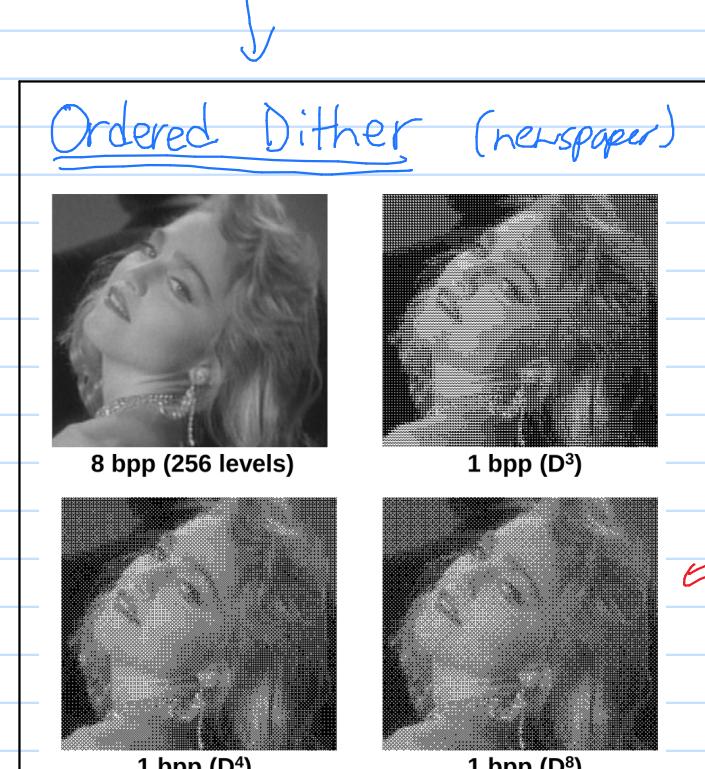
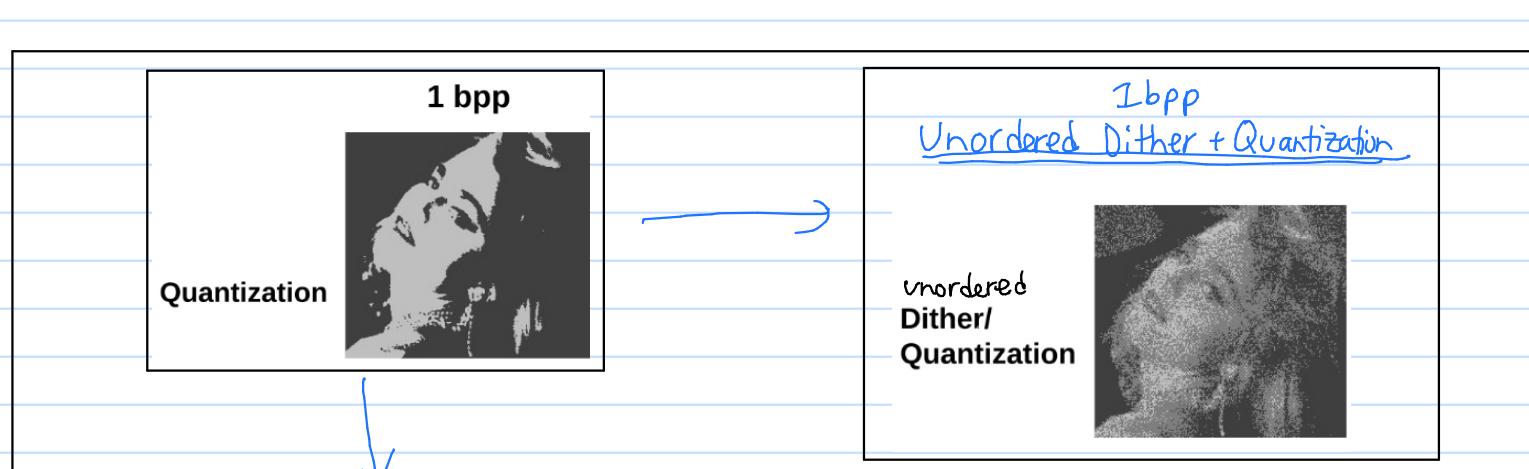
- say input size = output size
- 1) Quantize input image to [0 ... n<sup>2</sup>] gray lvs
- 2) compare Dither matrix with input image

```
for(y=0; y<h; y++) // visit all input rows
  for(x=0; x<w; x++){
    i = x % n; // dither matrix index
    j = y % n; // dither matrix index

    // threshold pixel using dither value Dij(n)
    out[y*w+x] = (in[y*w+x] > Dij(n)) ? 255 : 0;
  }
}
X loop: goes thru each elem in 1st row
Y loop: goes to next row
Y*w = go down each row
bla + x = go to each elem in row
```

h = row length  $\leftarrow Y = \text{row}$   
 w = col length  $\leftarrow X = \text{col}$

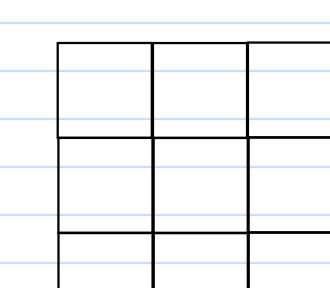
$\boxed{\text{h}}$



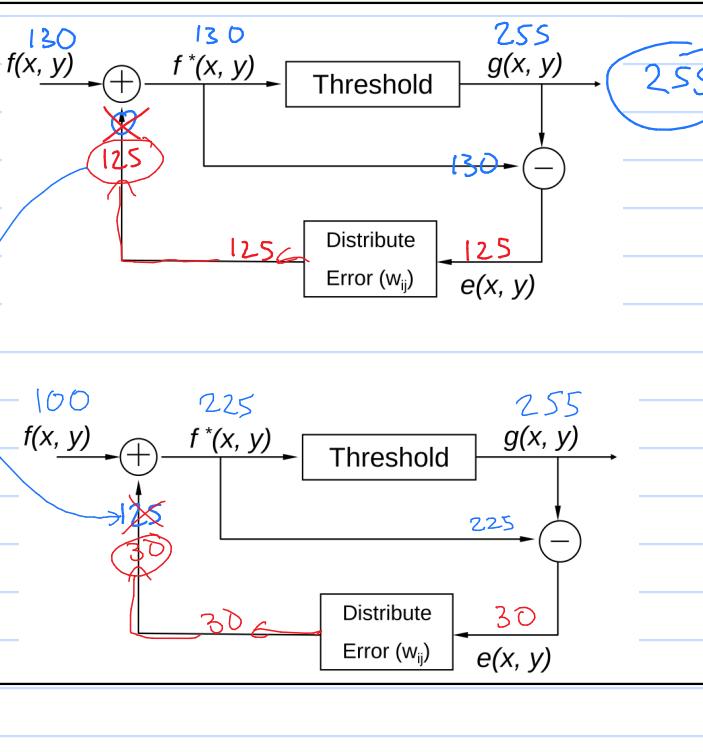
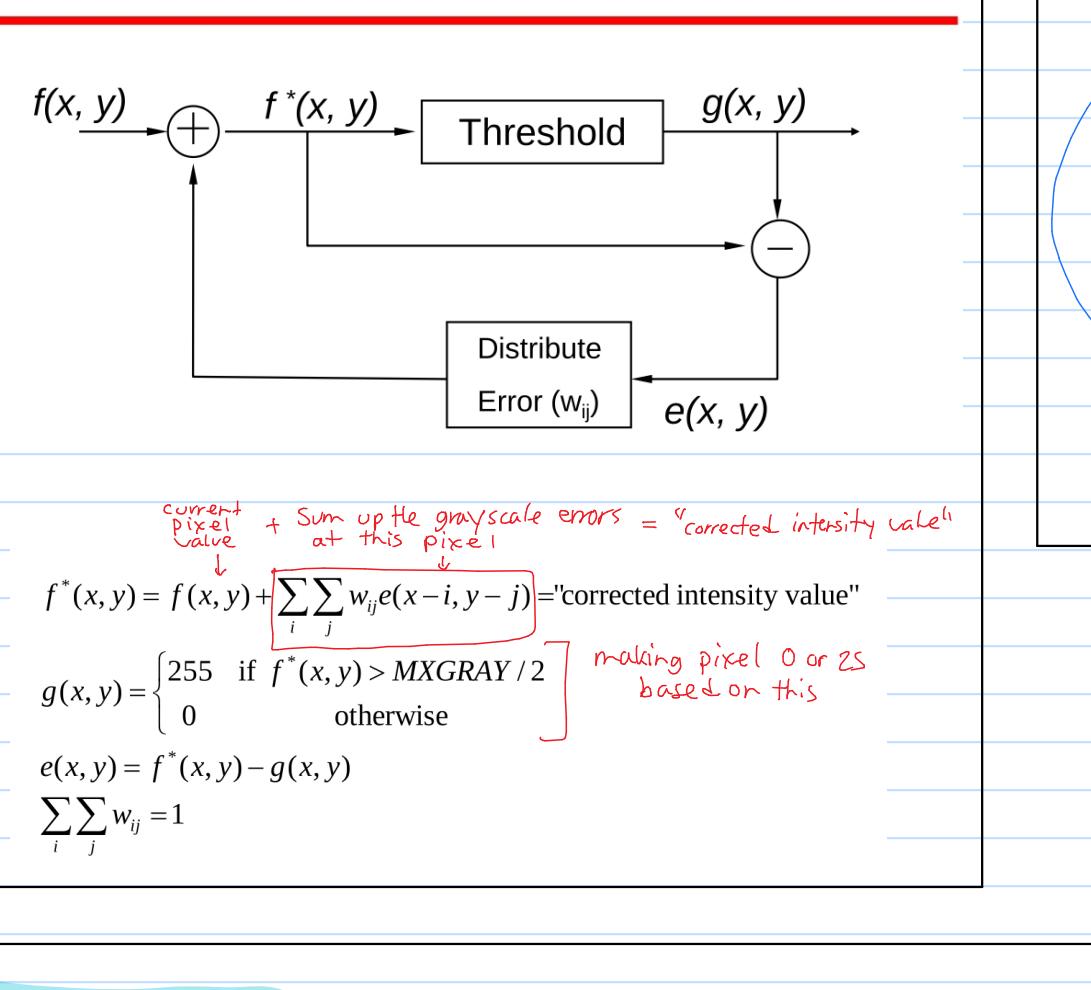
### Error Diffusion

• whenever we turn a grayscale image to just black or white → we get an error because crashing scales to 0 or 255  
 • To compensate overshoots (255) and undershoots (0) → need to spread error to neighbors

~~Can only make pixels 0 or 255  
 If input pix is 150 → make it white (255)  
 .that excessive brightness ( $\frac{255-150}{8} = 18.75$ ) is an error.  
 .18.75 must be subtracted from neighbors!  
 .why? since I made pixel brighter  
 → make neighbors darker to compensate for excessive brightness~~

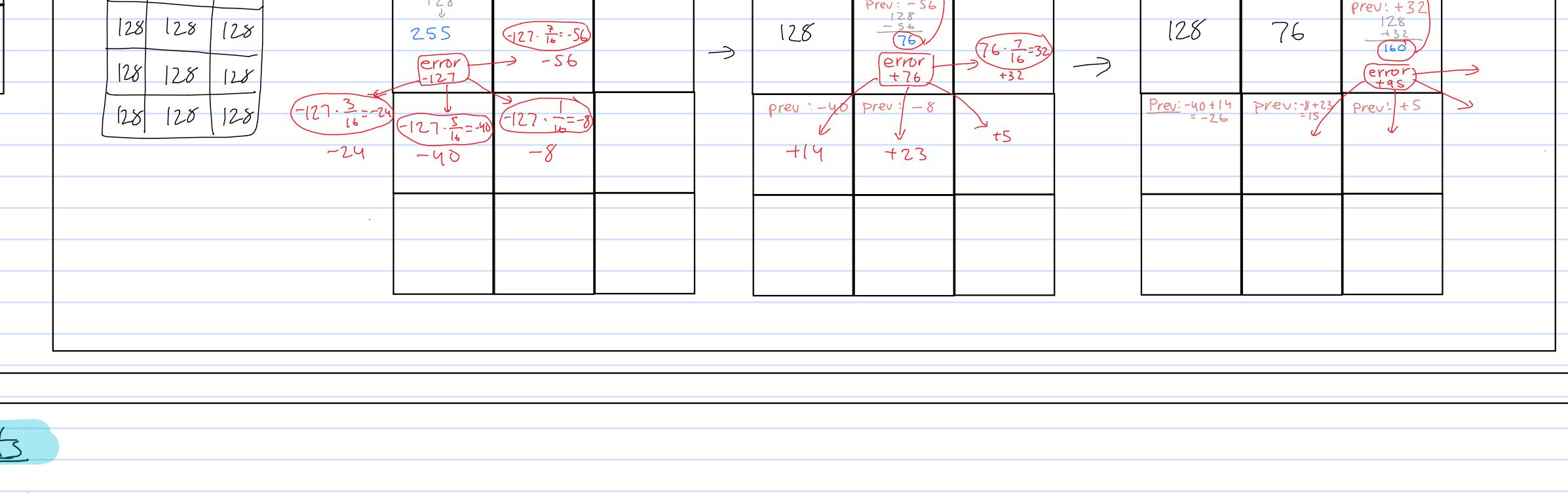


### Floyd-Steinberg Algorithm



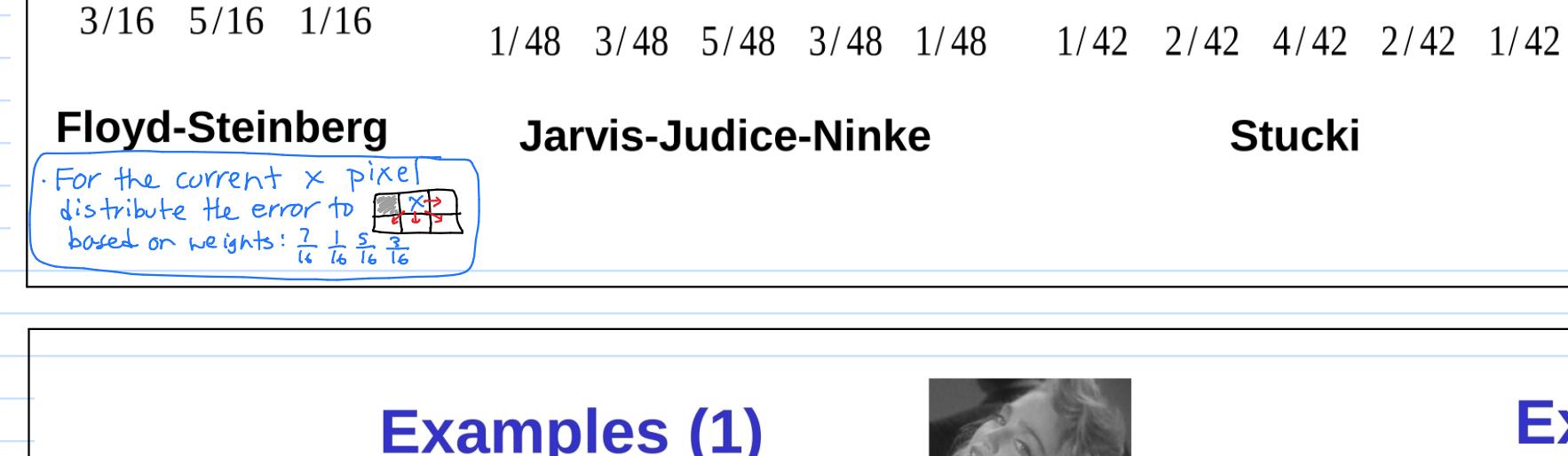
### Floyd-Steinberg

Pass the errors to their boxes



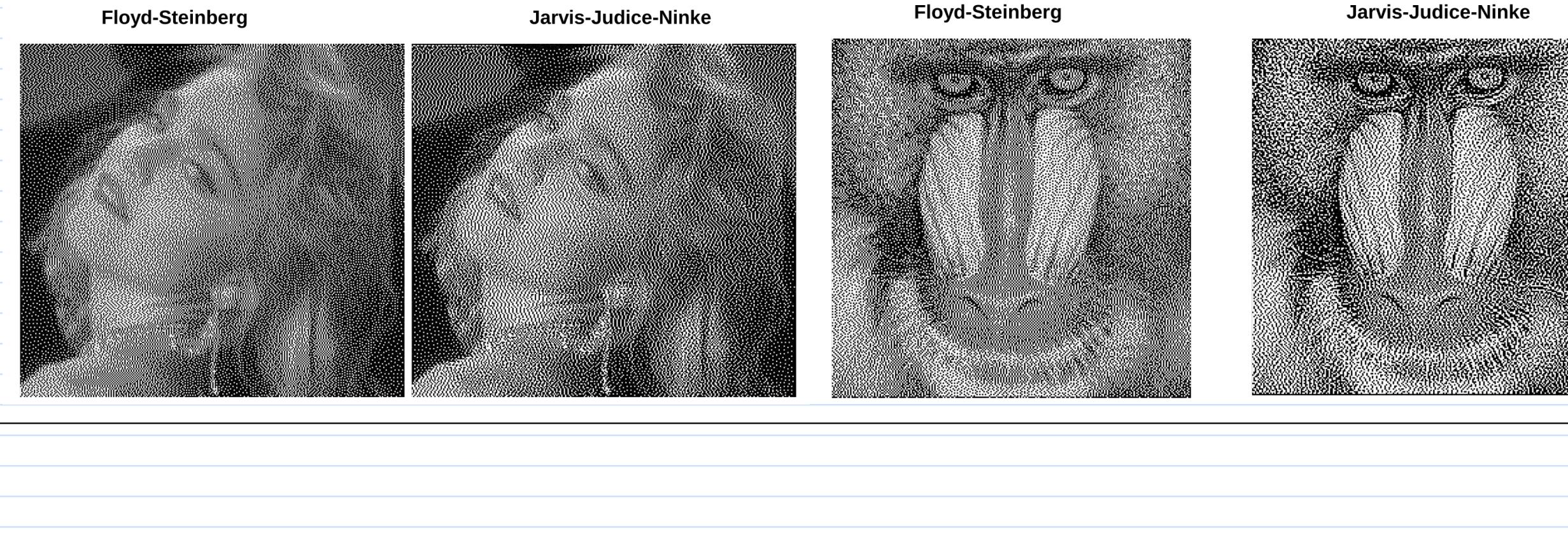
### Error Diffusion Weights

- moves left to right
- sum of all diffused error weights = 1
- larger neighborhood → better results

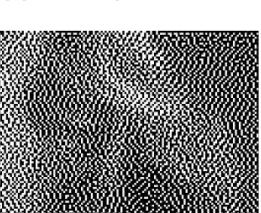


### Jarvis-Judice-Ninke

### Stucki



### Examples (1)



### Examples (2)



### Floyd-Steinberg

### Jarvis-Judice-Ninke

### Floyd-Steinberg

### Jarvis-Judice-Ninke

### Implementation

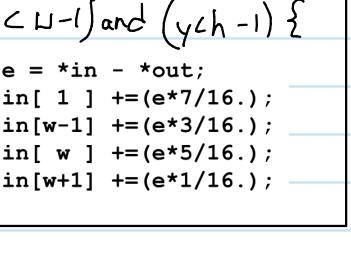
```
the midgray lvl (y) →
thr = MXGRAY / 2;
for(y=0; y<h; y++) {
    for(x=0; x<w; x++) {
        *out = (*in < thr)? BLACK : WHITE; // init threshold value
        ① use LUT
        if(*in > thr) {
            *out = BLACK;
            *out += LUT[(*in - thr) * 16];
        }
        ② error update
        e = *in - *out; // eval error
        in[ 1 ] +=(e*7/16.); // add error to E nbr
        in[w-1] +=(e*3/16.); // add error to SW nbr
        in[ w ] +=(e*5/16.); // add error to S nbr
        in[w+1] +=(e*1/16.); // add error to SE nbr
        ③ increment both pointers
        in++;
        out++;
    }
}
```

$h = \text{height}$ ,  
 $w = \text{width}$

$x = \text{column pixel iteration}$   
 $y = \text{row pixel iteration}$

### Border Issue Fix

Question: How do we deal with edges?

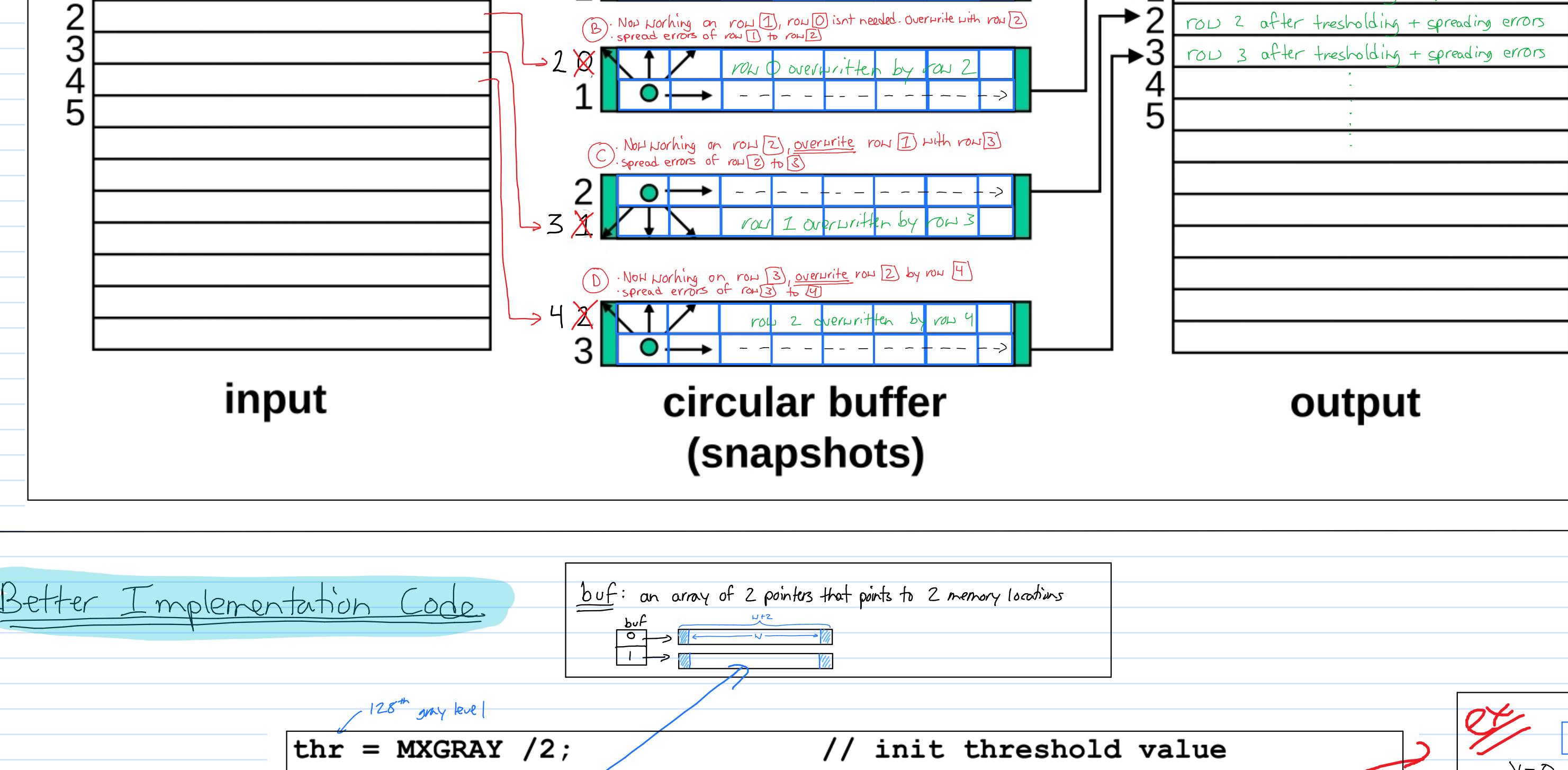


Troubles: 1) errors can be deposited beyond image border (true for all neighborhood operations...)

2) the depositing of errors can force grayvals to go out of [0, 255] range

Solutions: a) Before you deposit errors, do a if statement: handles start treatment  
 b) find image with extra rows and cols  
 c) handle extra memory  
 • use 16-bit precision (short) for pixel values outside dataset  
 Solution: use Circular buffer to significantly reduce memory req.

Circular Buffer: to fix padding excessive memory issue by only using 2 arrays and constantly overwriting the used pixel row with new row

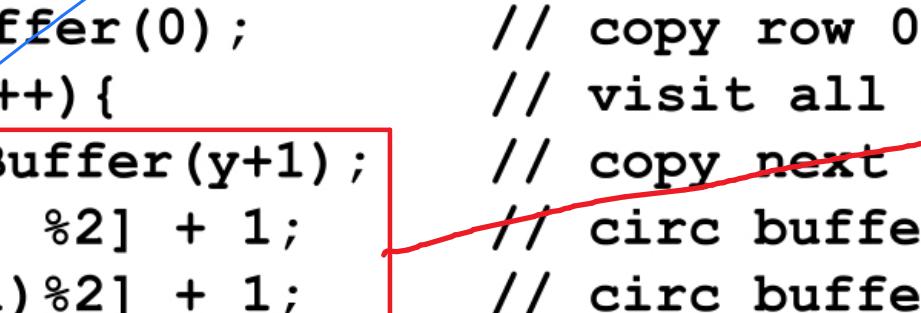


median, convolve

use this

assure buffer not over 32

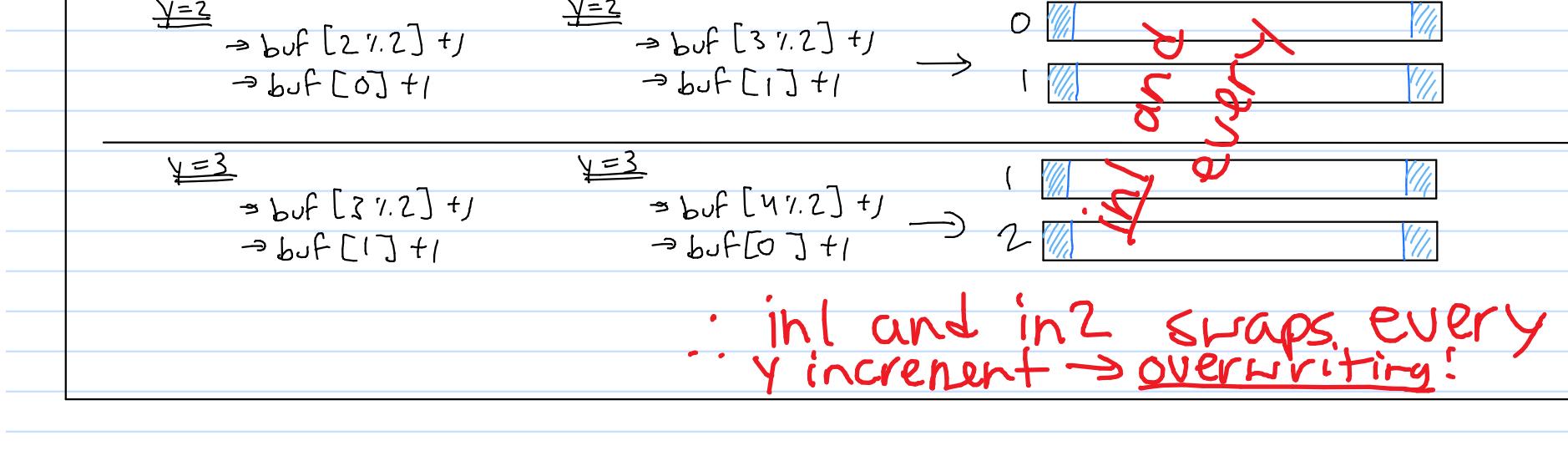
### (better) Better Implementation Code



```
Copy row 0 to circular buffer
if I iterate by rows (no more rows and col)
    (copy next row to buffer
    ) input pixel to start with
buf[0] returns same memory address
buf[1] is the 1st pixel of that row
The buf[y+1] and buf[(y+1)+2] also swaps
```

```
thr = MXGRAY / 2;
copyRowToCircBuffer(0); // copy row 0 to circular buffer
for(y=0; y<h; y++){
    // visit all input rows
    copyRowToCircBuffer(y+1); // copy next row to circ buffer
    in1 = buf[ y % 2 ] + 1; // circ buffer ptr; skip over pad
    in2 = buf[ (y+1)%2 ] + 1; // circ buffer ptr; skip over pad
    for(x=0; x<w; x++) { // visit all input cols
        *out = (*in1 < thr)? BLACK : WHITE; // threshold
        e = *in1 - *out; // eval error
        in1[ 1 ] +=(e*7/16.); // add error to E nbr
        in2[-1] +=(e*3/16.); // add error to SW nbr
        in2[ 0 ] +=(e*5/16.); // add error to S nbr
        in2[ 1 ] +=(e*1/16.); // add error to SE nbr
        in1++; in2++;
        out++; // advance circ buffer ptrs
    }
}
```

Y1,2 and (Y+1),Y-2 → Circular → saves space



∴ in1 and in2 swaps every y increment → overwriting!

part of code for convolution

```
float sum
for y=0 to yCh y++
    for x=0 to xCh x++
        sum=0
        weight = pKernel
        int ih
```

for convolve.c pp

NW = yCh

hh = xCh

create circular buffer

size

int buf[NW\*hh];

buf set to 0 somehow (use new)

then delete them later