

ECEn 631 Structure from Motion

Objectives:

- Learn to estimate camera motion.
- Learn to reconstruct object structure.
- Learn to compute the essential matrix from images taken by one camera from multiple views.

Instructions:

- Use OpenCV to complete this exam.
- Use the same four image sequences, data, and results you got from your previous assignment.
- Download the camera intrinsic and distortion parameters (SFM Camera Parameters.txt) from BYU Learning Suite.
- Download ParallelCube, ParallelReal, TurnedCube, and TurnedReal sequences for this assignment.
- Include your result, images, and discussion for all three tasks in one PDF file.
- Submit your PDF file and source code file(s) in one zip file without the folder or directory.
- Use your first name and last name (e.g., justinsmith.zip) as the file name.
- Login to myBYU and submit your work through BYU Learning Suite online submission.

Task 1: Unknown Intrinsic and Extrinsic Parameters 30 points

Assuming the four image sequences were taken with an unknown camera (intrinsic parameters are not available) and camera motion is unknown (extrinsic parameters are not available), the fundamental matrix F can still be estimated using the 8-point algorithm. Using the estimated F , images can be rectified and disparities can be calculated.

- Use the matching feature points between the first frame (#10) and the last frame (#15) obtained from your previous assignment Task 3 to estimate the fundamental matrix F .
- Use `stereoRectifyUncalibrated()` function to compute the rectification homography matrices (H_1 and H_2) for the first and last frames.
- H_1 and H_2 can then be used to rectify the images. Check Slides# 24 & 25 of Lecture - Calibration & Rectification for details.
- Remember to convert them to R_1 and R_2 ($R_1 = M_1^{-1}H_1M_1$ and $R_2 = M_2^{-1}H_2M_2$) before rectification.
- You need to make a guess on the intrinsic and distortion parameters (Do NOT use the camera parameter file downloaded online).
- The image center (320, 240) is a reasonable estimate for the optical center. In this case, of course $M_1 = M_2$. Pick a reasonable number for f_x and f_y .
- Submit one rectified image pair for each image sequence (total four sequences). Draw a few horizontal lines to show rectification result. Describe what you observe. Include all your answers and images in your PDF file. Submit your code.

Task 2: Known Intrinsic and Unknown Extrinsic Parameters 40 points

With a calibrated camera (intrinsic parameters are available) but unknown camera motion, the object structure can be reconstructed up to an unknown scale factor.

- Use the matching data points from Task 1.
- Now that we know the intrinsic parameters, the data points should be undistorted first using the `undistortPoints()` function before calculating a better fundamental matrix.
- Remember NOT to pass $R1(2)$ and $P1(2)$ to the `undistortPoints()` function and the output points must be converted back to image frame in pixels using $NewPoints.x = OutputPoints.x \times f_x + O_x$ and $OutputPoints.y = NewPoints.y \times f_y + O_y$.
- Use the undistorted matching data points to calculate the fundamental matrix F .
- Calculate the essential matrix E from F using $E = (M_r)^T F M_l$.
- Since we do not know camera motion, E should be normalized so that we don't get confused (see lecture slides).
- Extract R and T between the first view and the last view from E . Remember $E = \hat{T}R$, where \hat{T} is a 3×3 skew-symmetric matrix.
- There will be four sets of R and T solutions. Determine which one is correct.
- Exam the R and T matrices you select and explain what is the estimated camera motion (up to a scale factor).
- Submit your explanation and the R , T , E , and F matrices of all 4 sequences in your PDF file. Submit your code.

Task 3: Known Intrinsic and Extrinsic Parameters 30 points

Assuming that we were able to use a laser range finder to measure the distance from the camera to the 3D scene. Our measurements show that the distance from the camera (at Frame 10) to the closest point on the cube (see ParallelCube and TurnedCube image sequence) is 20 inches. All points on the same vertical corner line have the same distance to the camera (cube is sitting upright).

- Adjust the scale factor until the distance from the camera to the closet point on the cube is roughly 20 inches.
- Use one scale factor (obtained from ParallelCube) for the ParallelCube and ParallelReal sequences.
- Use a different scale factor (obtained from TurnedCube) for the TurnedCube and TurnedReal sequences.
- Explain what you observe how the camera moves (camera motion with actual measurements) in both cases (parallel and turned).
- Select four feature points from the first frame that have their matching points in the second frame and circle them in the first frame (#10) from each sequence and calculate their true 3D information.
- Submit your explanation, image, and data (**the scale factor and T for each sequence**) in your PDF file.
- Submit your code.