# Data Mining: Concepts and Techniques

(3<sup>rd</sup> ed.)

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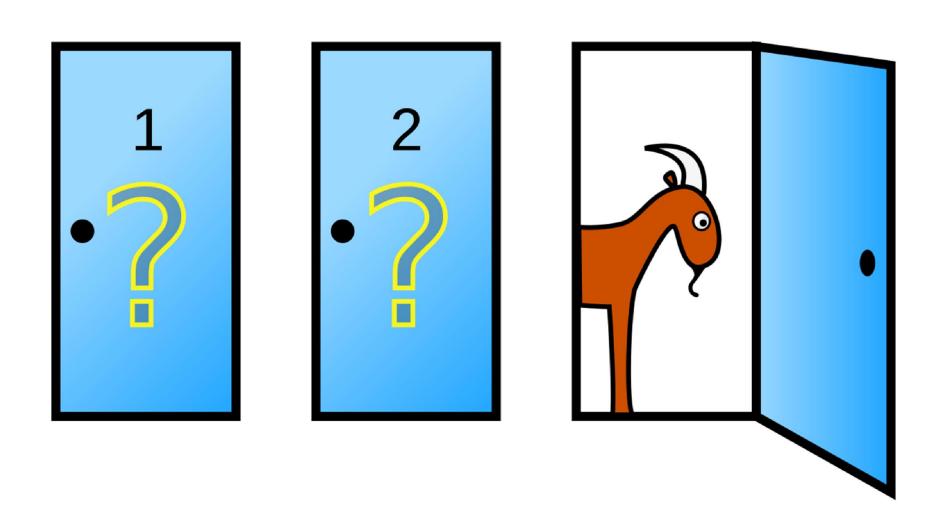
## Chapter 8. Classification - Cont.

Bayes Classification Methods



- Techniques to Improve Classification Accuracy:
   Ensemble Methods
- Summary

# **Monty Hall**



### **Bayesian Classification: Why?**

- A statistical classifier: performs probabilistic prediction, i.e., predicts class membership probabilities
- Foundation: Based on Bayes' Theorem.
- <u>Performance:</u> A simple Bayesian classifier, naïve Bayesian classifier, has comparable performance with decision tree and selected neural network classifiers
- Incremental: Each training example can incrementally increase/decrease the probability that a hypothesis is correct prior knowledge can be combined with observed data
- Standard: Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

### **Bayes' Theorem: Basics**

- Total probability Theorem:  $P(B) = \sum_{i=1}^{M} P(B|A_i)P(A_i)$
- Bayes' Theorem:  $P(H | \mathbf{X}) = \frac{P(\mathbf{X}|H)P(H)}{P(\mathbf{X})} = P(\mathbf{X}|H) \times P(H)/P(\mathbf{X})$ 
  - Let X be a data sample ("evidence"): class label is unknown
  - Let H be a hypothesis that X belongs to class C
  - Classification is to determine P(H|X), (i.e., posteriori probability): the probability that the hypothesis holds given the observed data sample X
  - P(H) (prior probability): the initial probability
    - E.g., X will buy computer, regardless of age, income, ...
  - P(X): probability that sample data is observed
  - P(X|H) (likelihood): the probability of observing the sample X, given that the hypothesis holds
    - E.g., Given that X will buy computer, the prob. that X is 31..40,
       medium income

### Prediction Based on Bayes' Theorem

Given training data X, posteriori probability of a hypothesis H,
 P(H|X), follows the Bayes' theorem

$$P(H | \mathbf{X}) = \frac{P(\mathbf{X}|H)P(H)}{P(\mathbf{X})} = P(\mathbf{X}|H) \times P(H)/P(\mathbf{X})$$

- Informally, this can be viewed as posteriori = likelihood x prior/evidence
- Predicts **X** belongs to  $C_i$  iff the probability  $P(C_i | \mathbf{X})$  is the highest among all the  $P(C_k | \mathbf{X})$  for all the k classes
- Practical difficulty: It requires initial knowledge of many probabilities, involving significant computational cost

#### Classification Is to Derive the Maximum Posteriori

- Let D be a training set of tuples and their associated class labels, and each tuple is represented by an n-D attribute vector  $\mathbf{X} = (\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_n)$
- Suppose there are m classes  $C_1$ ,  $C_2$ , ...,  $C_m$ .
- Classification is to derive the maximum posteriori, i.e., the maximal  $P(C_i | X)$
- This can be derived from Bayes' theorem

$$P(C_i|\mathbf{X}) = \frac{P(\mathbf{X}|C_i)P(C_i)}{P(\mathbf{X})}$$

Since P(X) is constant for all classes, only

$$P(C_i|\mathbf{X}) = P(\mathbf{X}|C_i)P(C_i)$$

needs to be maximized

### Naïve Bayes Classifier

- A simplified assumption: attributes are conditionally independent (i.e., no dependence relation between attributes):  $P(\mathbf{X}|C_i) = \prod_{l=1}^{n} P(x_k|C_l) = P(x_1|C_l) \times P(x_2|C_l) \times ... \times P(x_n|C_l)$
- This greatly reduces the computation cost: Only counts the class distribution
- If  $A_k$  is categorical,  $P(x_k|C_i)$  is the # of tuples in  $C_i$  having value  $x_k$  for  $A_k$  divided by  $|C_{i,D}|$  (# of tuples of  $C_i$  in D)
- If  $A_k$  is continous-valued,  $P(x_k|C_i)$  is usually computed based on Gaussian distribution with a mean  $\mu$  and standard deviation  $\sigma$

and 
$$P(\mathbf{x}_k | \mathbf{C}_i)$$
 is 
$$g(\mathbf{x}, \mu, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(\mathbf{x} - \mu)^2}{2\sigma^2}}$$
$$P(\mathbf{X} | \mathbf{C}_i) = g(\mathbf{x}_k, \mu_{C_i}, \sigma_{C_i})$$

### Naïve Bayes Classifier: Training Dataset

#### Class:

C1:buys\_computer = 'yes'

C2:buys\_computer = 'no'

Data to be classified:

X = (age <= 30,

Income = medium,

Student = yes

Credit\_rating = Fair)

age	income	<mark>studen</mark> 1	credit_rating	_com
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

### Naïve Bayes Classifier: An Example

- $P(C_i)$ :  $P(buys\_computer = "yes") = 9/14 = 0.643$  $P(buys\_computer = "no") = 5/14 = 0.357$
- Compute P(X | C<sub>i</sub>) for each class

```
P(age = "<=30" | buys_computer = "yes") = 2/9 = 0.222

P(age = "<= 30" | buys_computer = "no") = 3/5 = 0.6

P(income = "medium" | buys_computer = "yes") = 4/9 = 0.444

P(income = "medium" | buys_computer = "no") = 2/5 = 0.4

P(student = "yes" | buys_computer = "yes) = 6/9 = 0.667

P(student = "yes" | buys_computer = "no") = 1/5 = 0.2

P(credit_rating = "fair" | buys_computer = "yes") = 6/9 = 0.667

P(credit_rating = "fair" | buys_computer = "no") = 2/5 = 0.4
```

X = (age <= 30, income = medium, student = yes, credit\_rating = fair)</p>

```
P(X|C_i): P(X|buys\_computer = "yes") = 0.222 x 0.444 x 0.667 x 0.667 = 0.044 
 <math>P(X|buys\_computer = "no") = 0.6 x 0.4 x 0.2 x 0.4 = 0.019
```

 $P(X|C_i)*P(C_i): P(X|buys\_computer = "yes") * P(buys\_computer = "yes") = 0.028$  $P(X|buys\_computer = "no") * P(buys\_computer = "no") = 0.007$ 

Therefore, X belongs to class ("buys\_computer = yes")

### **Avoiding the Zero-Probability Problem**

 Naïve Bayesian prediction requires each conditional prob. be non-zero. Otherwise, the predicted prob. will be zero

$$P(X \mid C_i) = \prod_{k=1}^{n} P(x_k \mid C_i)$$

- Ex. Suppose a dataset with 1000 tuples, income=low (0), income= medium (990), and income = high (10)
- Use Laplacian correction (or Laplacian estimator)
  - Adding 1 to each case

Prob(income = low) = 1/1003

Prob(income = medium) = 991/1003

Prob(income = high) = 11/1003

 The "corrected" prob. estimates are close to their "uncorrected" counterparts

### Naïve Bayes Classifier: Comments

- Advantages
  - Easy to implement
  - Good results obtained in most of the cases
- Disadvantages
  - Assumption: class conditional independence, therefore loss of accuracy
  - Practically, dependencies exist among variables
    - E.g., hospitals: patients: Profile: age, family history, etc.
       Symptoms: fever, cough etc., Disease: lung cancer, diabetes, etc.
    - Dependencies among these cannot be modeled by Naïve Bayes Classifier
- How to deal with these dependencies? Bayesian Belief Networks (Chapter 9)

#### Chapter 8. Classification: Basic Concepts

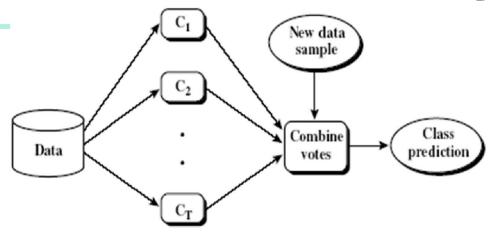
- Bayes Classification Methods
- Techniques to Improve Classification Accuracy:



**Ensemble Methods** 

Summary

### **Ensemble Methods: Increasing the Accuracy**



- Ensemble methods
  - Use a combination of models to increase accuracy
  - Combine a series of k learned models, M<sub>1</sub>, M<sub>2</sub>, ..., M<sub>k</sub>, with the aim of creating an improved model M\*
- Popular ensemble methods
  - Bagging: averaging the prediction over a collection of classifiers
  - Boosting: weighted vote with a collection of classifiers
  - Ensemble: combining a set of heterogeneous classifiers

#### **Bagging: Bootstrap Aggregation**

- Analogy: Diagnosis based on multiple doctors' majority vote
- Training
  - Given a set D of d tuples, at each iteration i, a training set D<sub>i</sub> of d tuples is sampled with replacement from D (i.e., bootstrap)
  - A classifier model M<sub>i</sub> is learned for each training set D<sub>i</sub>
- Classification: classify an unknown sample X
  - Each classifier M<sub>i</sub> returns its class prediction
  - The bagged classifier M\* counts the votes and assigns the class with the most votes to X
- Prediction: can be applied to the prediction of continuous values by taking the average value of each prediction for a given test tuple
- Accuracy
  - Often significantly better than a single classifier derived from D
  - For noise data: not considerably worse, more robust
  - Proved improved accuracy in prediction

#### **Boosting**

- Analogy: Consult several doctors, based on a combination of weighted diagnoses—weight assigned based on the previous diagnosis accuracy
- How boosting works?
  - Weights are assigned to each training tuple
  - A series of k classifiers is iteratively learned
  - After a classifier M<sub>i</sub> is learned, the weights are updated to allow the subsequent classifier, M<sub>i+1</sub>, to pay more attention to the training tuples that were misclassified by M<sub>i</sub>
  - The final M\* combines the votes of each individual classifier, where the weight of each classifier's vote is a function of its accuracy
- Boosting algorithm can be extended for numeric prediction
- Comparing with bagging: Boosting tends to have greater accuracy, but it also risks overfitting the model to misclassified data

### Adaboost (Freund and Schapire, 1997)

- Given a set of d class-labeled tuples,  $(\mathbf{X_1}, \mathbf{y_1}), ..., (\mathbf{X_d}, \mathbf{y_d})$
- Initially, all the weights of tuples are set the same (1/d)
- Generate k classifiers in k rounds. At round i,
  - Tuples from D are sampled (with replacement) to form a training set
     D<sub>i</sub> of the same size
  - Each tuple's chance of being selected is based on its weight
  - A classification model M<sub>i</sub> is derived from D<sub>i</sub>
  - Its error rate is calculated using D<sub>i</sub> as a test set
  - If a tuple is misclassified, its weight is increased, o.w. it is decreased
- Error rate:  $err(X_j)$  is the misclassification error of tuple  $X_j$ . Classifier  $M_i$  error rate is the sum of the weights of the misclassified tuples:

error 
$$(M_i) = \sum_{j=1}^{d} w_j \times err(\mathbf{X_j})$$

The weight of classifier M<sub>i</sub>'s vote is

$$\log \frac{1 - error(M_i)}{error(M_i)}$$

### Random Forest (Breiman 2001)

#### Random Forest:

- Each classifier in the ensemble is a decision tree classifier and is generated using a random selection of attributes at each node to determine the split
- During classification, each tree votes and the most popular class is returned
- Two Methods to construct Random Forest:
  - Forest-RI (random input selection): Randomly select, at each node, F
    attributes as candidates for the split at the node. The CART methodology
    is used to grow the trees to maximum size
  - Forest-RC (random linear combinations): Creates new attributes (or features) that are a linear combination of the existing attributes (reduces the correlation between individual classifiers)
- Comparable in accuracy to Adaboost, but more robust to errors and outliers
- Insensitive to the number of attributes selected for consideration at each split, and faster than bagging or boosting

#### Classification of Class-Imbalanced Data Sets

- Class-imbalance problem: Rare positive example but numerous negative ones, e.g., medical diagnosis, fraud, oil-spill, fault, etc.
- Traditional methods assume a balanced distribution of classes and equal error costs: not suitable for class-imbalanced data
- Typical methods for imbalance data in 2-class classification:
  - Oversampling: re-sampling of data from positive class
  - Under-sampling: randomly eliminate tuples from negative class
  - Threshold-moving: moves the decision threshold, t, so that the rare class tuples are easier to classify, and hence, less chance of costly false negative errors
  - Ensemble techniques: Ensemble multiple classifiers introduced above
- Still difficult for class imbalance problem on multiclass tasks

#### Chapter 8. Classification: Basic Concepts

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# Summary (I)

- Classification is a form of data analysis that extracts models describing important data classes.
- Effective and scalable methods have been developed for decision tree induction, Naive Bayesian classification, and many other classification methods.