

# Hourly Probabilistic Solar Power Forecasts

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UNC CHARLOTTE

*The WILLIAM STATES LEE COLLEGE of ENGINEERING*

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# **Presentation Outline**

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graph TD; A[Presentation Outline] --> B[Overview of Solar Power Forecasting]; A --> C[Hourly Probabilistic Forecasting of Solar Power]
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**Overview of Solar Power  
Forecasting**

**Hourly Probabilistic  
Forecasting of Solar Power**

## Personal Introduction

**Mohamed Abuella**

<https://mohamedabuella.github.io>

An electrical engineer by training, traditionally is interested in Mathematical and Computational Analysis, Modeling and Optimization, and who is recently get passionate in Artificial Intelligence and Data-driven Analytics for Energy a

### **Hobbies and Interests**

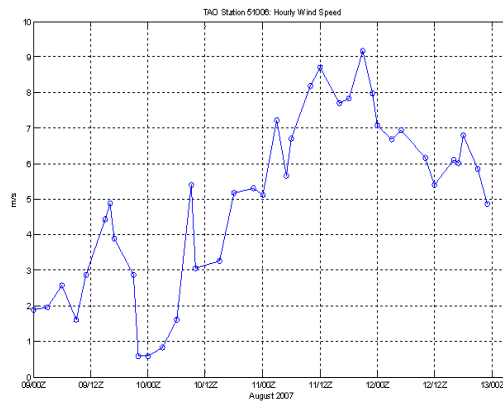
Making Mediterranean Food and Drink, but also try my own out-of-box recipes;  
Stretching, Walking, Running, Driving, Swimming, Diving, ..and hopefully Climbing;  
Wondering around and Discovering New Places, ..find it kind of an adventure;  
Watching, Reading and Sharing Stuff on Internet, useful & dumb things;  
And more often just.. Chilling and Enjoy Doing Nothing!

# Variable Generations (V.G.) Forecasting

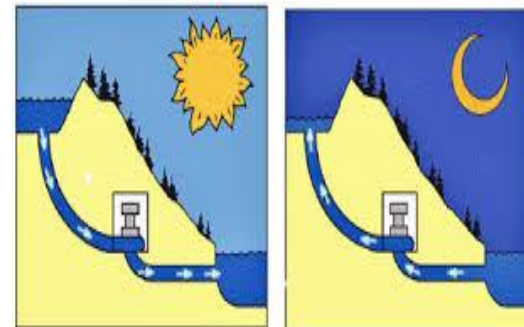
**Why  
Forecast?**

$$P_G = P_D + P_{loss}$$

**Renewables Generations  
(Wind and Solar) are Too  
Variable**



**High Efficiency and  
Large Energy Storage  
Still not Exist**



**Reducing  
Cost  
and Pollution**

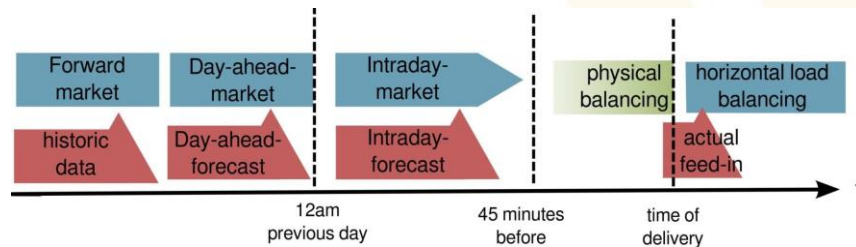


# Variable Generations (V.G.) Forecasting

**Where  
Forecast?**

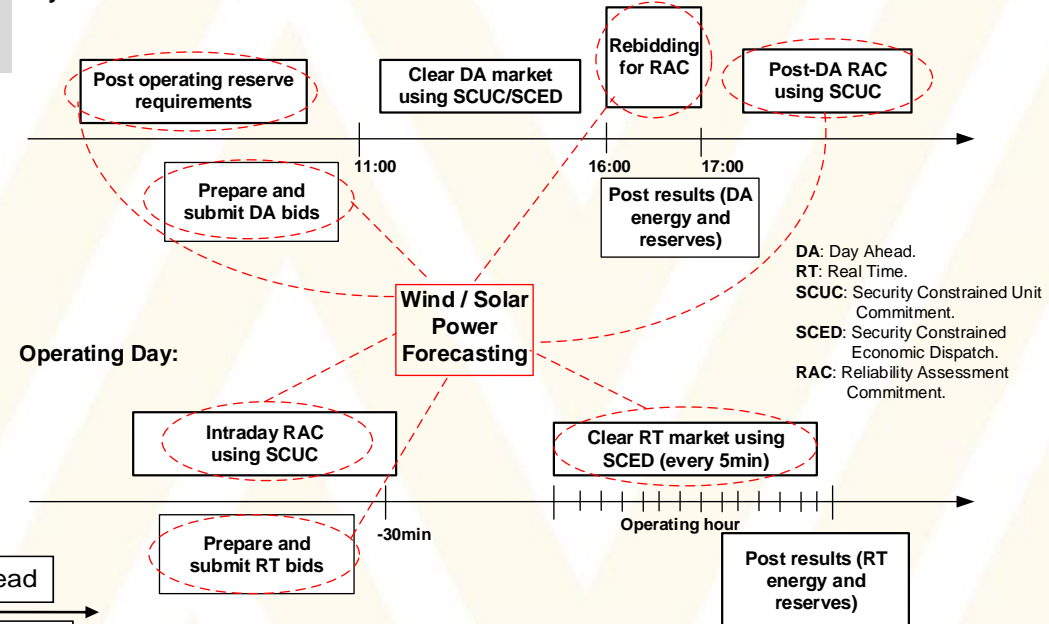
Forecast horizons, forecasting models and the related applications of VG forecasts

## Forecast Horizons



	Intra-hour	Intra-day	Day ahead
<b>Forecasting horizon</b>	15 min to 2 h	1 h to 6 h	1 day to 3 day
<b>Granularity-Time step</b>	30 s to 5 min	hourly	hourly
<b>Related to</b>	Ramping events, variability related to operations	Load following forecasting	Unit commitment, transmission scheduling, day ahead markets

**In Electricity Markets Operation: You Plan What You Forecast**  
Day Ahead:



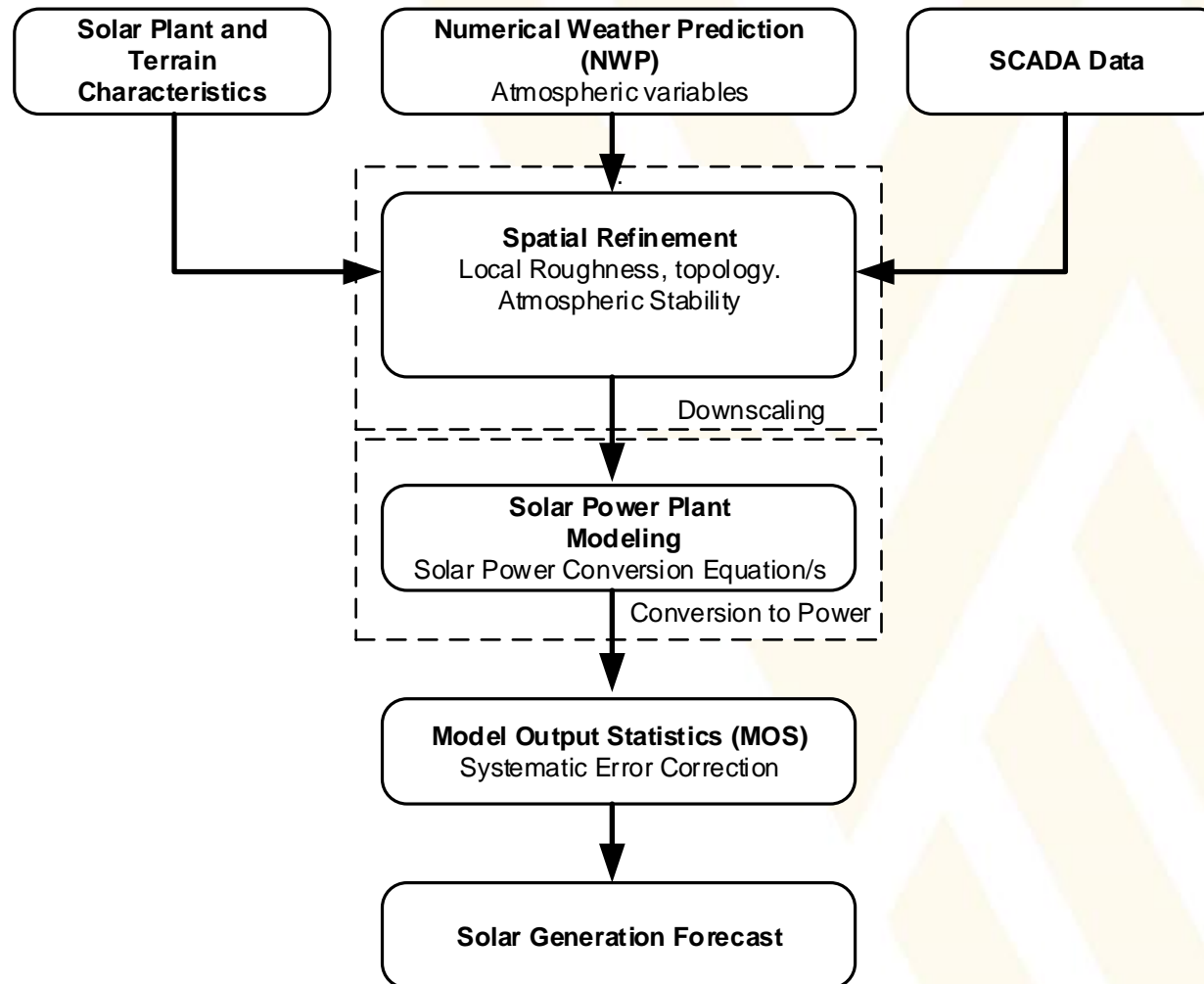
VG forecasting in US. electric utilities and ISO, such as CAISO, ERCOT, MISO, ISO-NE, NYISO,...etc.

Botterud, J. Wang, V. Miranda, and R. J. Bessa, "Wind power forecasting in US electricity markets," The Electricity Journal, vol. 23, no. 3, pp. 71–82, 2010.  
 Elke Lorenz, "Solar Resource Forecasting" International Solar Energy Society (ISES) Webinar, 2016.  
 Voyant, C., Notton, G., Kalogirou, S., Nivet, M. L., Paoli, C., Motte, F., & Fouilloy, A. (2017). Machine learning methods for solar radiation forecasting: A review. *Renewable Energy*, 105, 569-582.

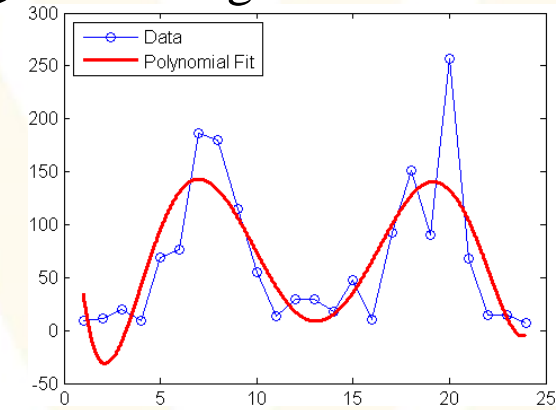


# Solar Power Forecasting

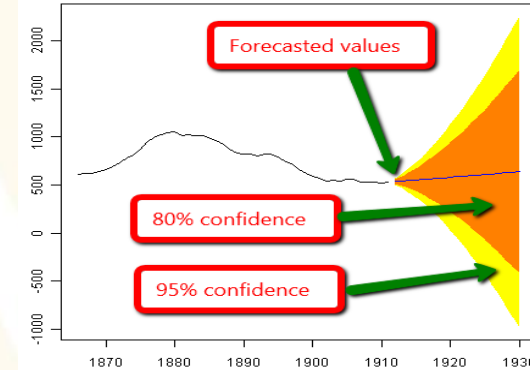
**How  
Forecast?**



## Regression

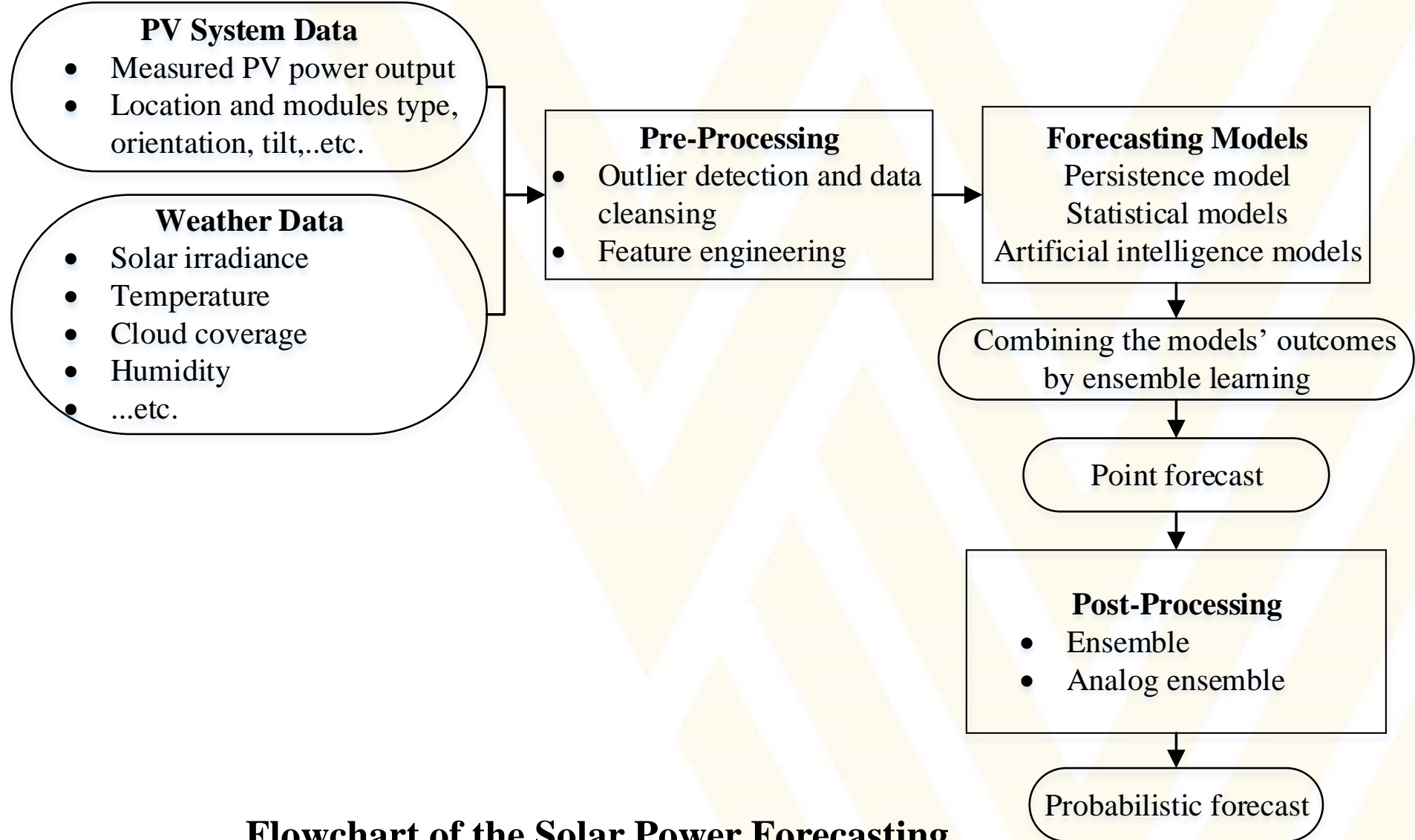


## Extrapolation



**Flowchart of the Combined Approach (Physical and Statistical) of the Solar Power Forecasting**

# Hourly Probabilistic Forecasting of Solar Power



Flowchart of the Solar Power Forecasting

# Hourly Probabilistic Forecasting of Solar Power

## Data Description:

PV solar system is near Canberra, Australia, consisting of 8 panels, its nominal power of (1560W), and panel orientation  $38^\circ$  clockwise from the north, with panel tilt (of  $36^\circ$ ). The historical observed solar power data are normalized to the rated capacity (i.e., 1560W).



Weather predictions are produced by a global numerical weather prediction system, European Centre for Medium-Range Weather Forecasts (ECMWF).

No.	Input Variable, (X)	No.	Input Variable, (X)
1	Cloud Water Content	10	Surface thermal radiation down
2	Cloud Ice Content	11	Top net solar radiation
3	Surface Pressure	12	Total precipitation
4	Relative Humidity	13	Heat Index
5	Cloud Cover	14	Wind Speed
6	10m - U Wind	15	Hours
7	10m - V Wind	16	Months
8	2-m Temperature	17	Days of Month
9	Surface solar radiation down	18	Days of Year

Data partition into training and testing sets

Timeline	Month	Year	Partition
From	April	2012	Training Set
To	May	2013	
From	June	2013	Testing Set
To	May	2014	

<https://crowdanalytix.com/contests/global-energy-forecasting-competition-2014-probabilistic-solar-power-forecasting>

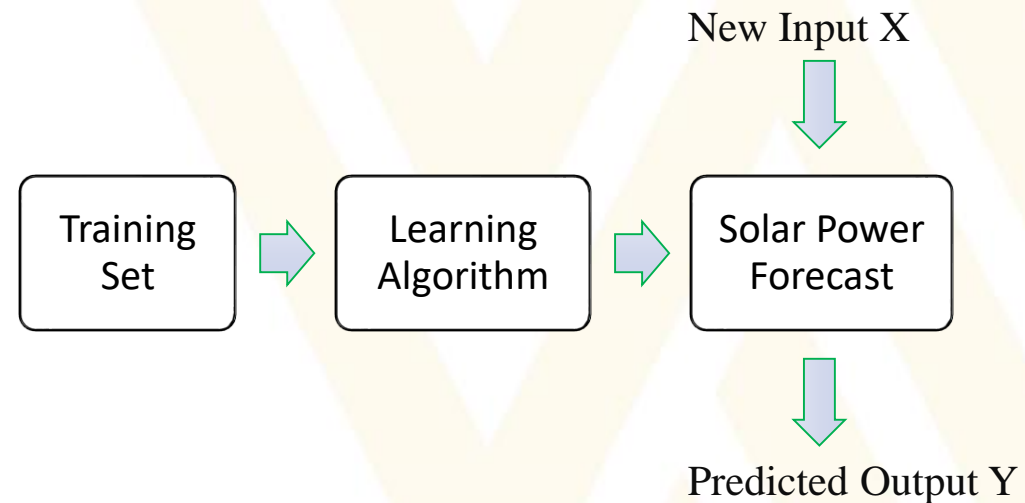
<http://www.ecmwf.int> (European Centre for Medium-Range Weather Forecasts)



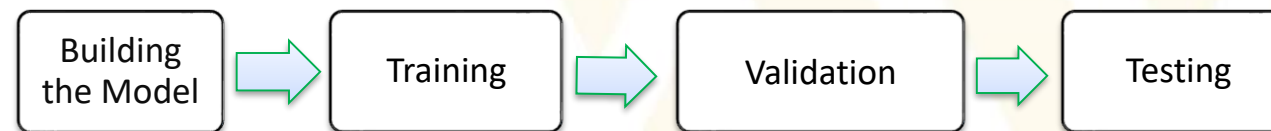
# Forecasting Models

## Parametric and Nonparametric Models

Multiple Linear Regression (**MLR**) Analysis, Artificial Neural Networks (**ANN**), and Support Vector Regression (**SVR**) are deployed for the short-term solar power forecasting.



Flowchart of the forecasting models

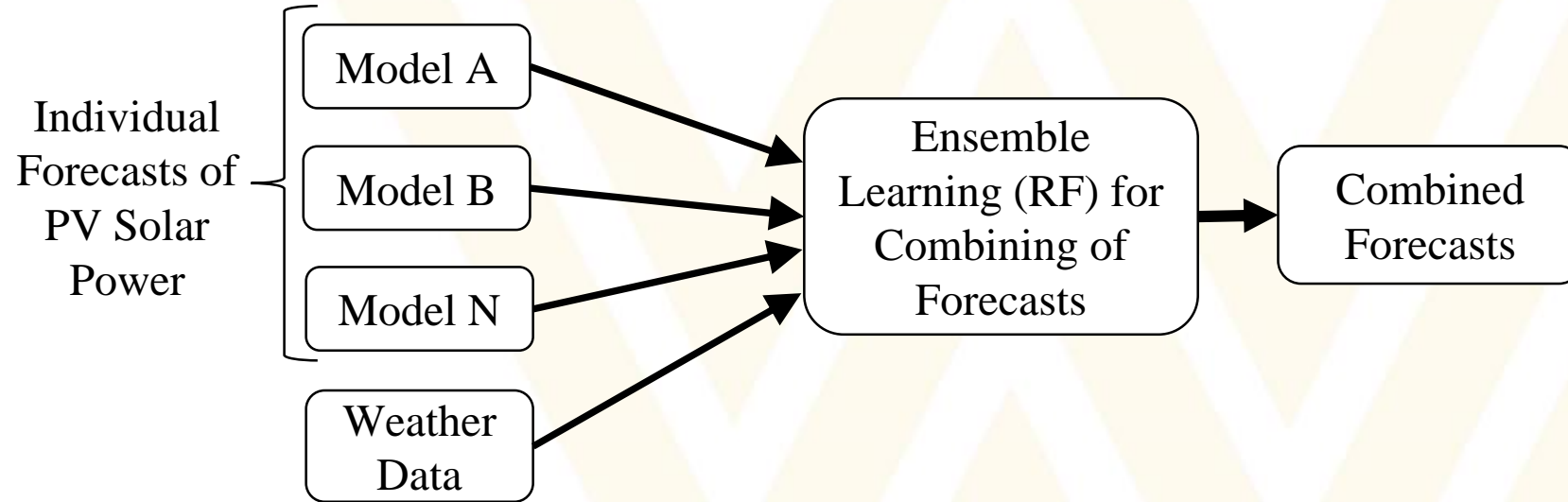


Flowchart of solar forecasting model building steps

T. Hastie, R. Tibshirani, J. Friedman, and others, *The elements of statistical learning*, 2<sup>nd</sup> Edition. Springer-Verlag New York, 2009.

# Ensemble Forecasts

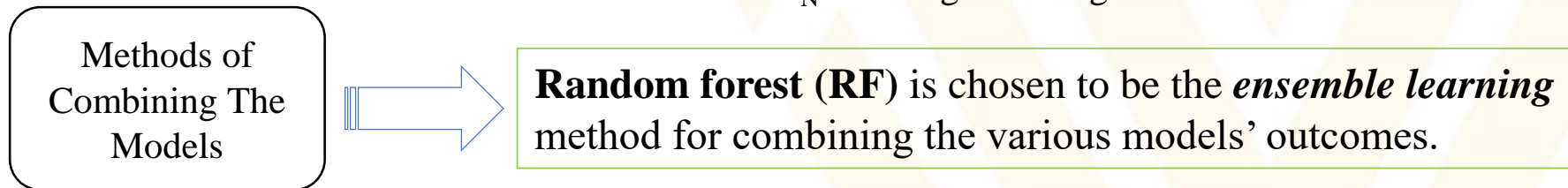
## Combining Various Models



General diagram of combining different models

$$F_{comb} = W_A * M_A + W_B * M_B + W_C * M_C + \dots + W_N * M_N$$

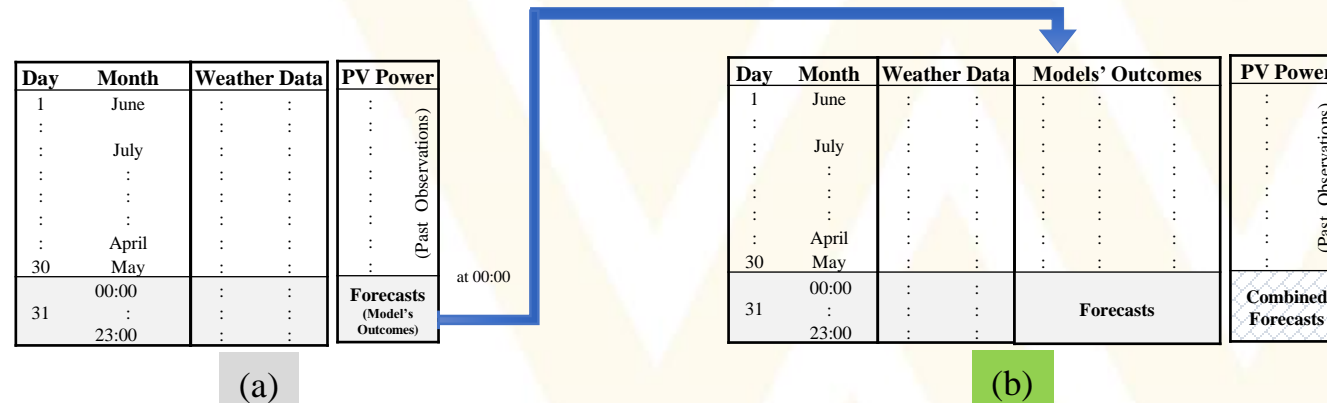
$W_N$  is a weight is assigned to the outcome of a model  $M_N$



T. Hastie, R. Tibshirani, J. Friedman, and others, *The elements of statistical learning*, 2<sup>nd</sup> Edition. Springer-Verlag New York, 2009.

# Ensemble Forecasts

*Persistence model and day-ahead Forecasts from MLR, ANN and SVR*



Producing Different Models' Outcomes

Combining by Radom Forest

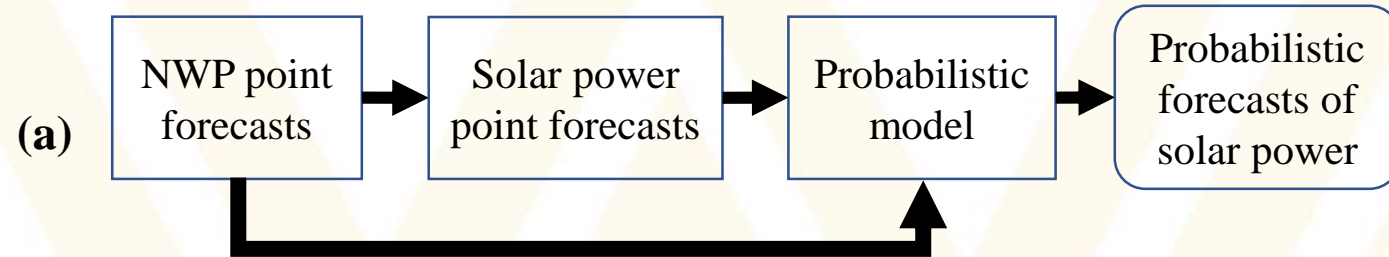
Schematic diagram of producing and ensemble different models' outcomes

*Persistence model,  $F(t) = P(t - \text{horizon})$*

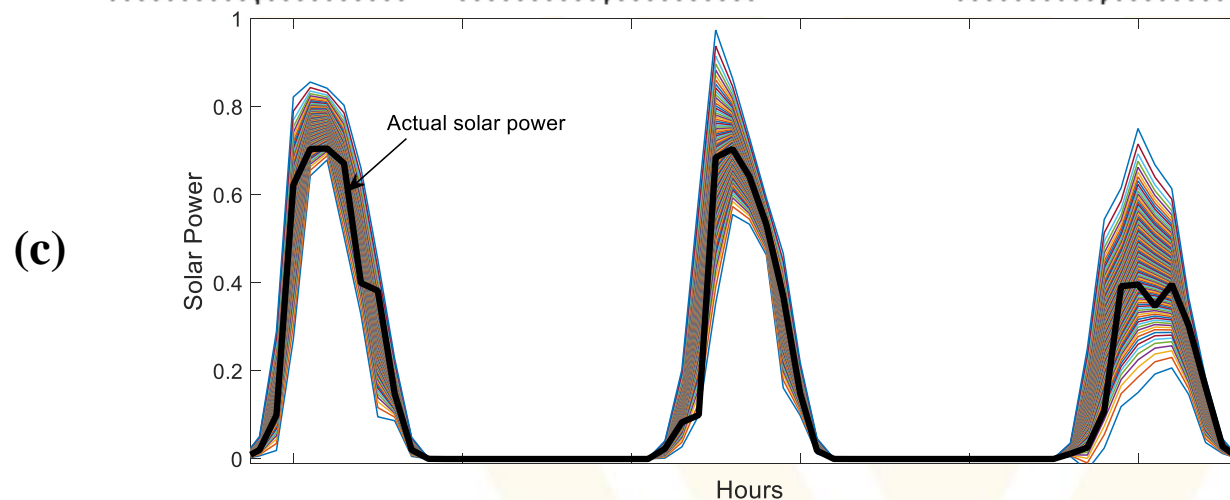
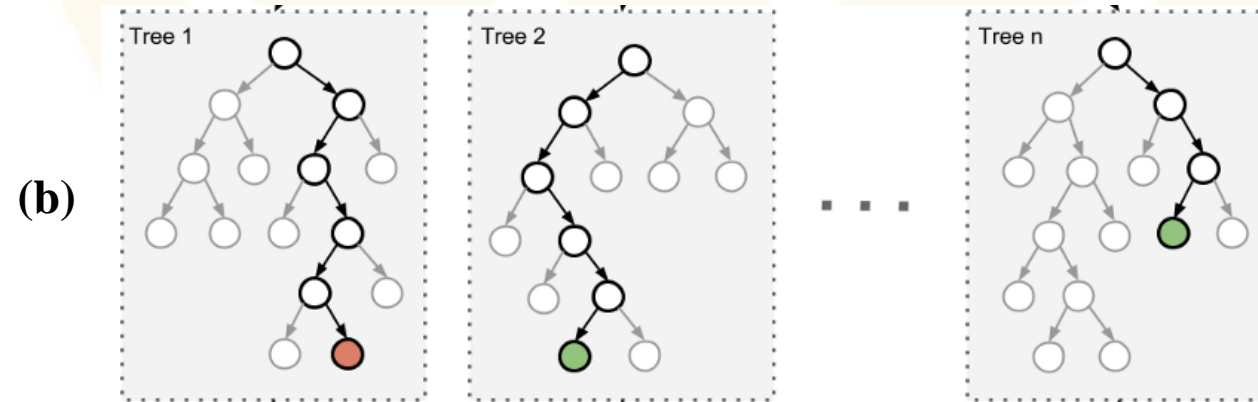
*Here the horizon = 1hour*

# Probabilistic Forecasts

## Ensemble-based probabilistic forecasts method:



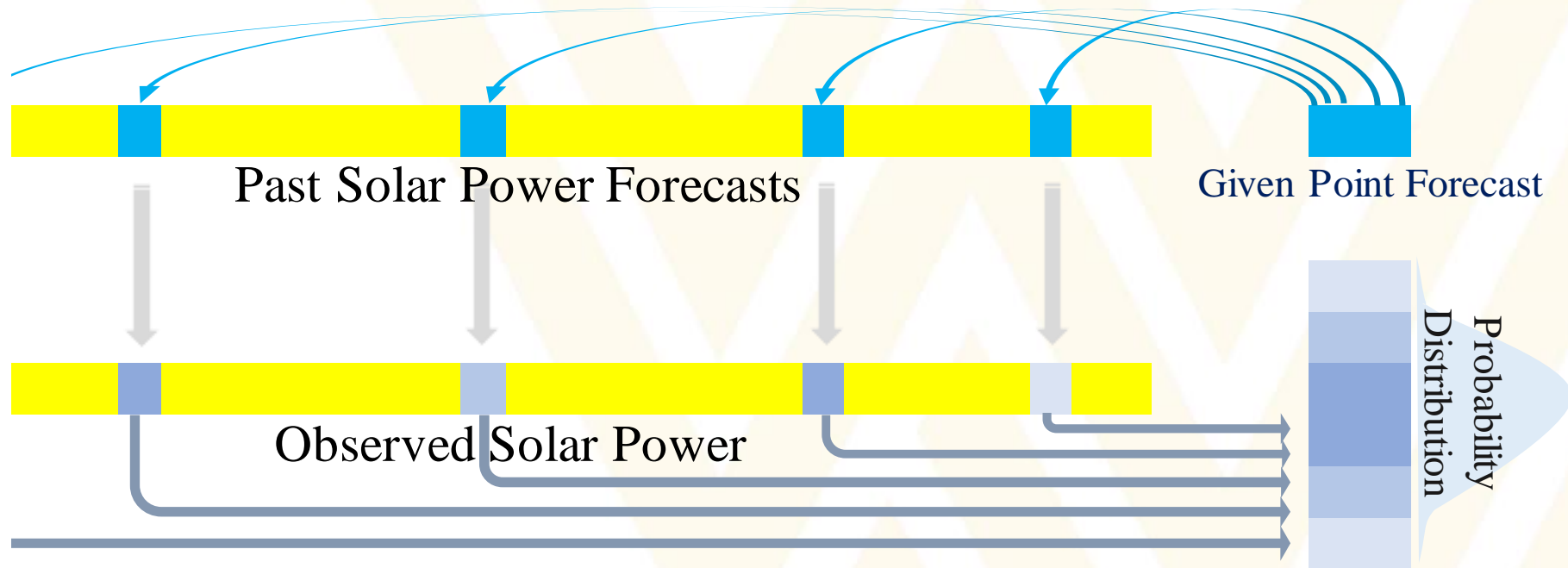
- a) Diagram of ensemble-based probabilistic forecasts,
- b) Splitting mechanism of trees in random forest,
- c) Sample of ensemble-based probabilistic forecasts of solar power of 3 days



$$\hat{f}_{RF} = \frac{1}{B} \sum_{b=1}^B T_b(Hr)$$

## Probabilistic Forecasts

**Analog Ensemble (AnEn) method:**



Schematic diagram of analog ensemble method

$$|F_{\text{Given}}^{Hr} - F_{\text{Past}}^{Hr}| \leq \varepsilon$$

$$\varepsilon = 0.1$$

where  $F_{\text{Given}}^{Hr}$  denotes the given point forecast at an hour  $Hr$ , for which the prediction interval will be estimated,  $F_{\text{Past}}^{Hr}$  the point forecasts at the same hour of the day.

Notice that all values are normalized in the range  $[0, 1]$ .

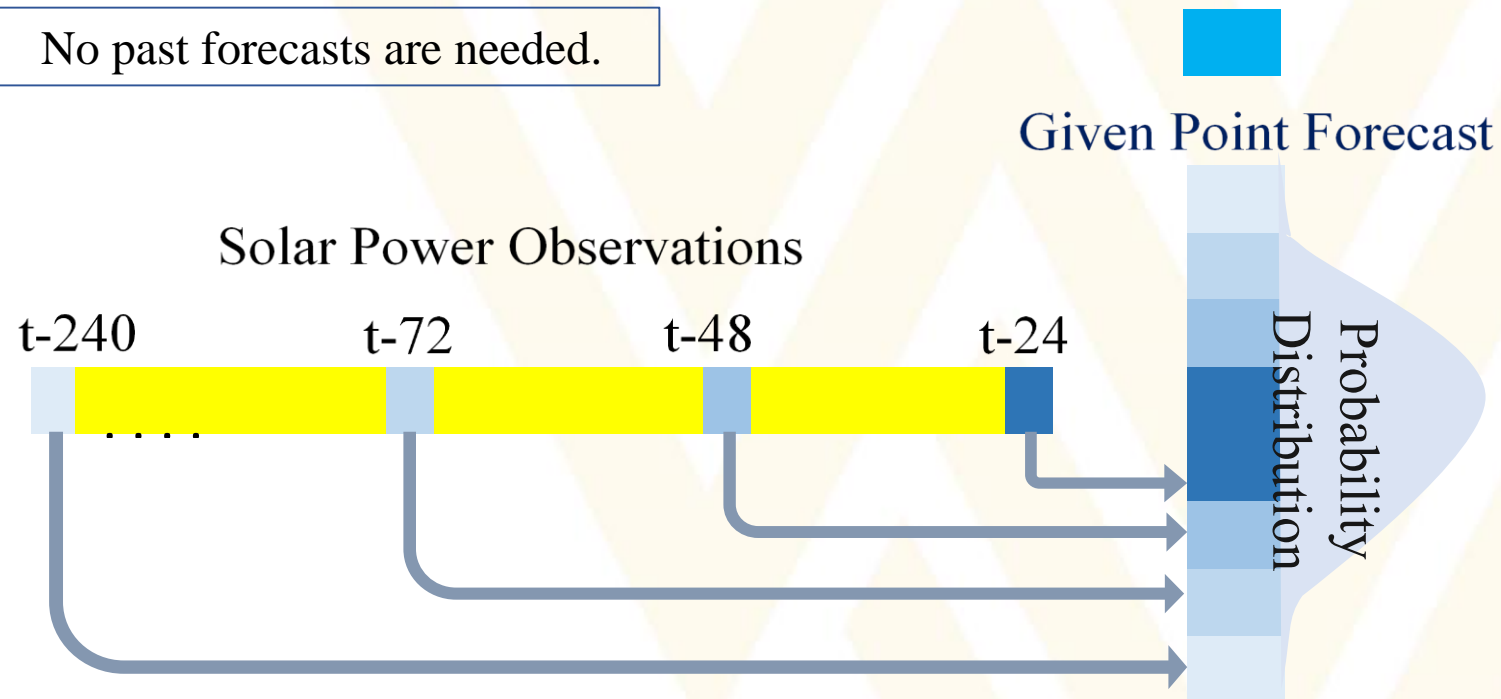
S. Alessandrini, L. Delle Monache, S. Sperati, and G. Cervone, “An analog ensemble for short-term probabilistic solar power forecast,” Appl. Energy, vol. 157, pp. 95–110, 2015.



# Probabilistic Forecasts

## Persistence probabilistic forecasts method:

No past forecasts are needed.



Schematic diagram of analog ensemble method

The 10, 20 and 30 recent observed powers are carried out.

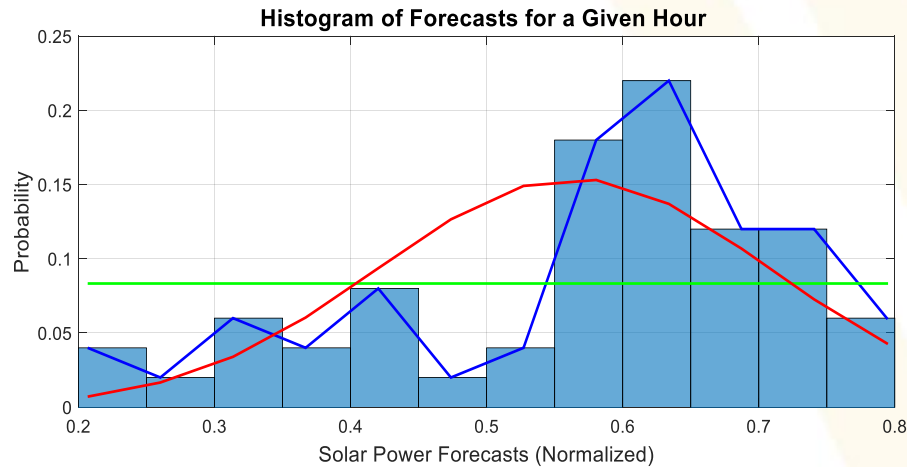
It is found that the recent **10** observed solar powers at the given hour with CDF distribution achieve more accurate persistence probabilistic forecasts.

# Probabilistic Forecasts

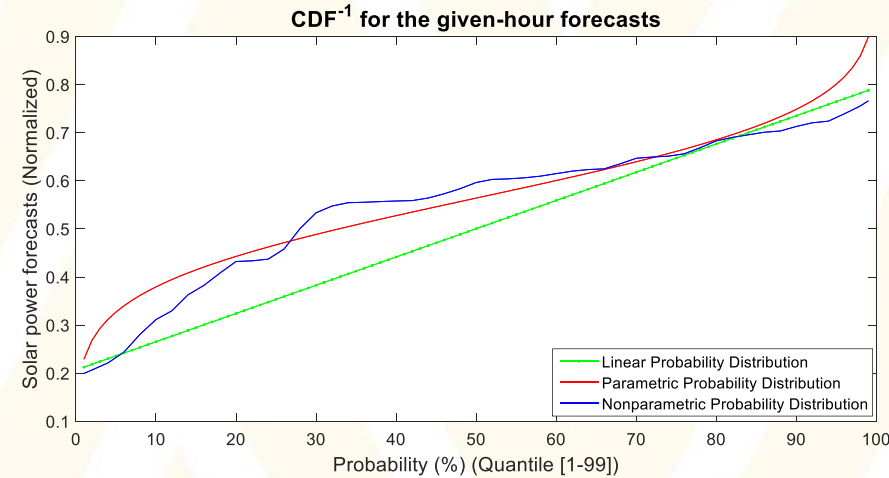
## Probability distributions by the cumulative distribution function (CDF)

→ For example, for a given point forecast at **14:00, June 2<sup>nd</sup> 2013**:

Histogram of the ensemble of RF's outcomes



Different distributions of probability



### Linear CDF

Max  
Min  
to derive CDF

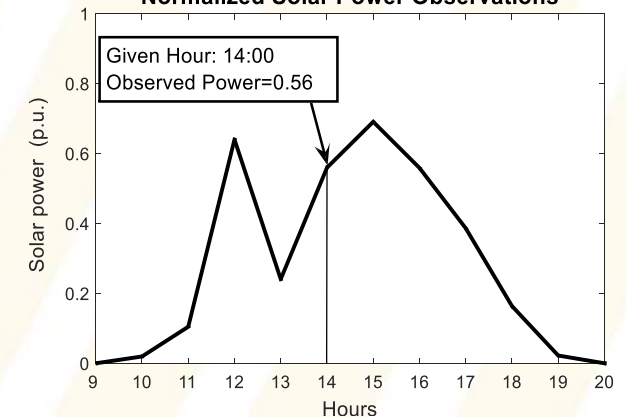
### Parametric normal-distributed CDF

Mean  
Std. dev.  
to derive CDF.

### Nonparametric CDF

No mean  
neither Std. Dev.  
CDF is estimated by  
piecewise  
nonparametric method

Normalized Solar Power Observations



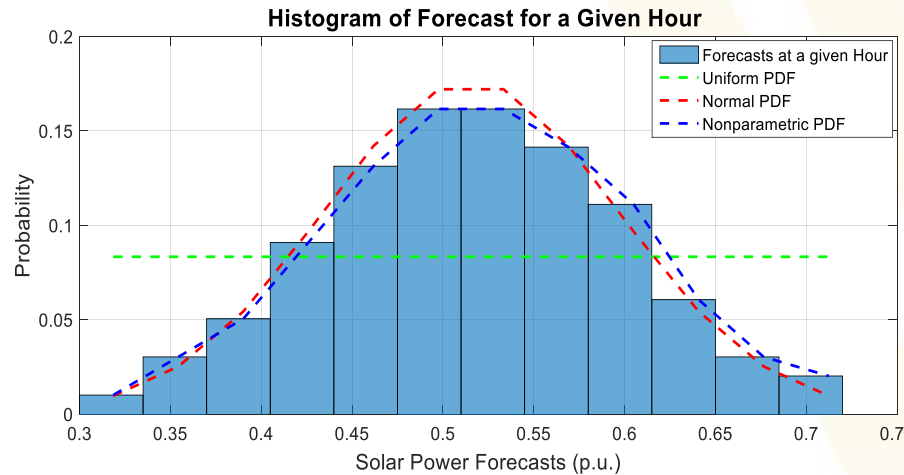
The probabilistic forecasts are estimated by using  $CDF^{-1}$

# Probabilistic Forecasts

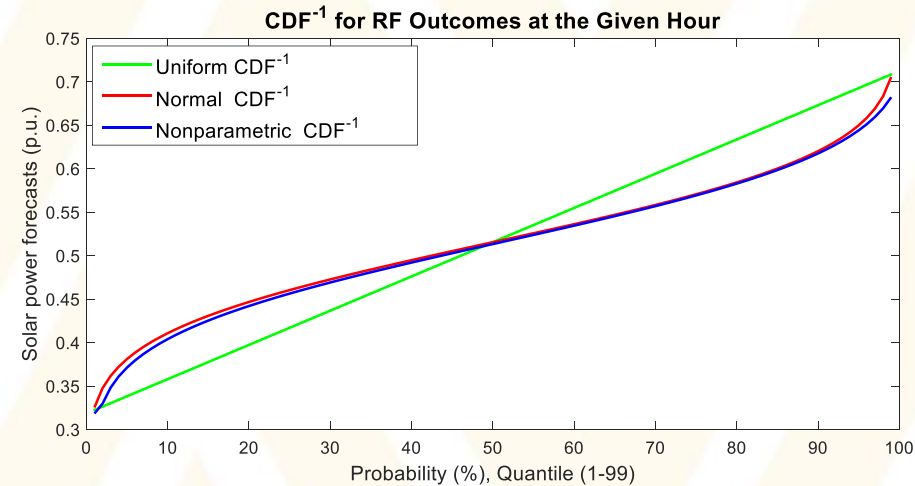
## Probability distributions by the cumulative distribution function (CDF)

→ For example, for a given point forecast at **12:00, May 29<sup>th</sup> 2014**:

Histogram of the ensemble of RF's outcomes



Different distributions of probability



### Linear CDF

Max  
Min  
to derive CDF

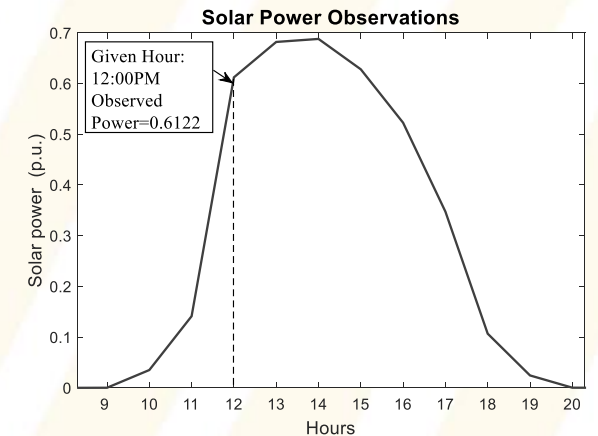
### Parametric normal-distributed CDF

Mean  
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No mean  
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The probabilistic forecasts are estimated by using  $CDF^{-1}$



# Probabilistic Forecasts

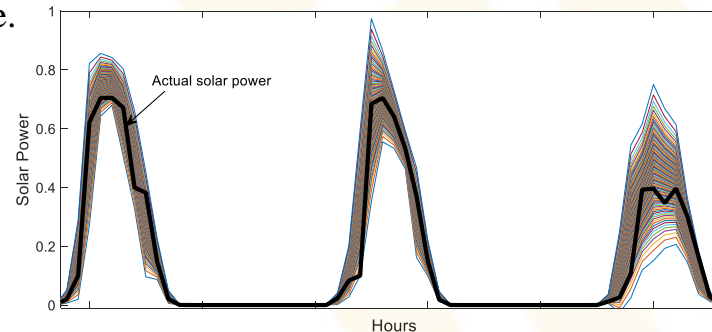
## Evaluation of probabilistic forecasts:

The objective is to determine probabilistic solar forecasts in the form of probabilistic distribution (in quantiles) in incremental time steps through the forecast horizon.

A **Pinball loss function** is used to evaluate the accuracy of the probabilistic forecasts. It is a piecewise linear function which is often used to evaluate the accuracy of quantile forecasts.

$$Pb_q(F, P) = \begin{cases} q(F - P), & \text{if } P \leq F \\ (1 - q)(P - F), & \text{if } P > F \end{cases}$$

where  $Pb_q(F, P)$  is the pinball loss function to the probabilistic forecasts for each hour;  $F$  is the forecasted value at the certain  $q$  quantile of the probabilistic solar power forecasts, and  $P$  is the observed value of the solar power. The quantile  $q$  has discrete values  $q \in [0.01, 0.99]$ . For instance,  $q = 0.9$  means that there is a 90% probability that the observed solar power will be less than the value of the 90<sup>th</sup> quantile.



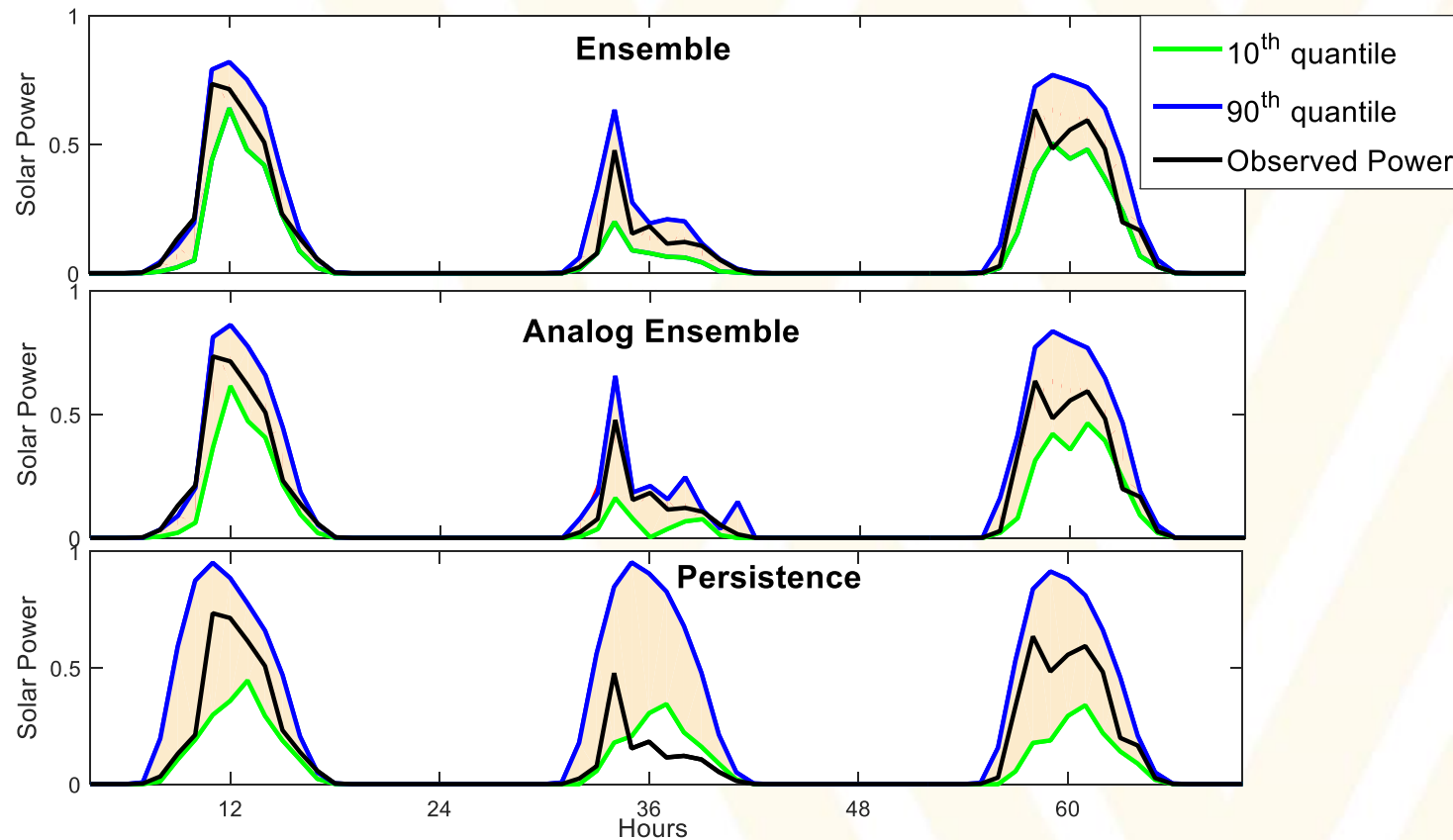
J. M. Morales, A. J. Conejo, H. Madsen, P. Pinson, and M. Zugno, Integrating renewables in electricity markets - Operational problems, vol. 205. Boston, MA: Springer US, 2014.

## Results and Evaluation

Pinball loss function (Pb):

$$Pb_q(F, P) = \begin{cases} q(F - P), & \text{if } P \leq F \\ (1 - q)(P - F), & \text{if } P > F \end{cases}$$

The lower Pinball (Pb) is, the more accurate probabilistic forecasts are.



Graphs of the probabilistic forecasts of the three methods for three days



## Results and Evaluation

Pinball loss function (Pb):

$$Pb_q(F, P) = \begin{cases} q(F - P), & \text{if } P \leq F \\ (1 - q)(P - F), & \text{if } P > F \end{cases}$$

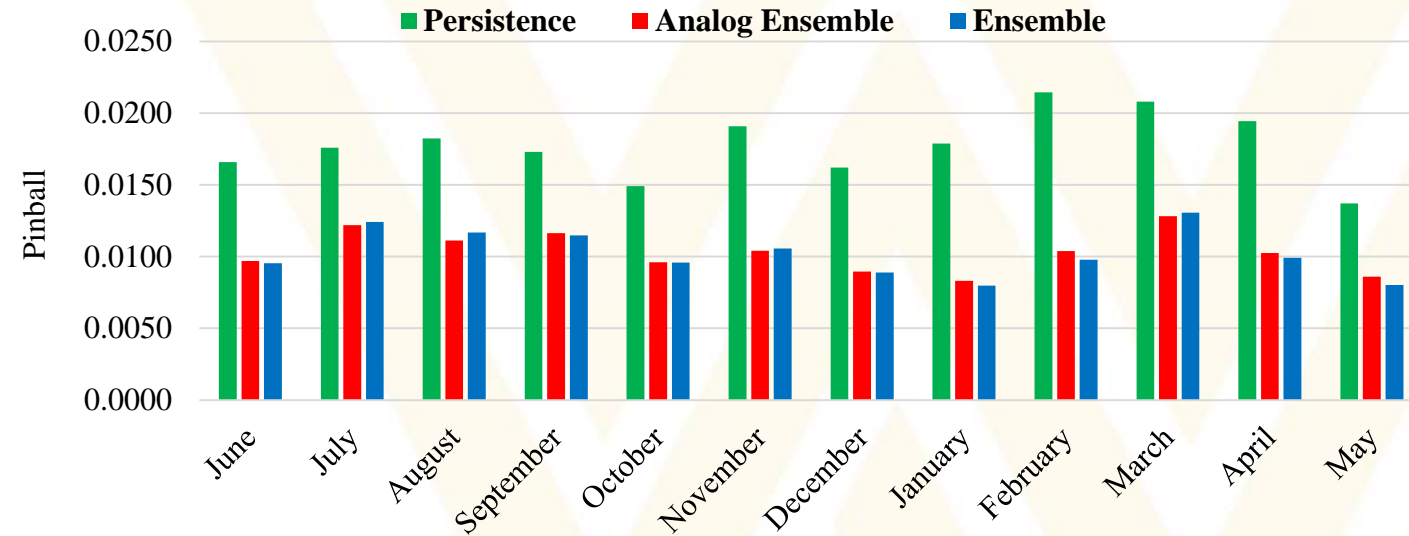
The lower Pinball (Pb) is, the more accurate probabilistic forecasts are.

Month	Pinball (Pb)			Improvement of Ensemble Over	
	Persistence	Analog Ensemble	Ensemble	Persistence	Analog Ensemble
June	0.0166	0.0097	0.0095	42%	2%
July	0.0176	0.0122	0.0124	29%	-2%
August	0.0182	0.0111	0.0117	36%	-5%
September	0.0173	0.0116	0.0115	34%	1%
October	0.0149	0.0096	0.0096	36%	0%
November	0.0191	0.0104	0.0106	45%	-2%
December	0.0162	0.0090	0.0089	45%	1%
January	0.0179	0.0083	0.0080	55%	4%
February	0.0215	0.0104	0.0098	54%	6%
March	0.0208	0.0128	0.0131	37%	-2%
April	0.0194	0.0103	0.0099	49%	3%
May	0.0137	0.0086	0.0080	42%	7%
<b>Average Pb.</b>	<b>0.0178</b>	<b>0.0103</b>	<b>0.0102</b>	<b>42%</b>	<b>1%</b>

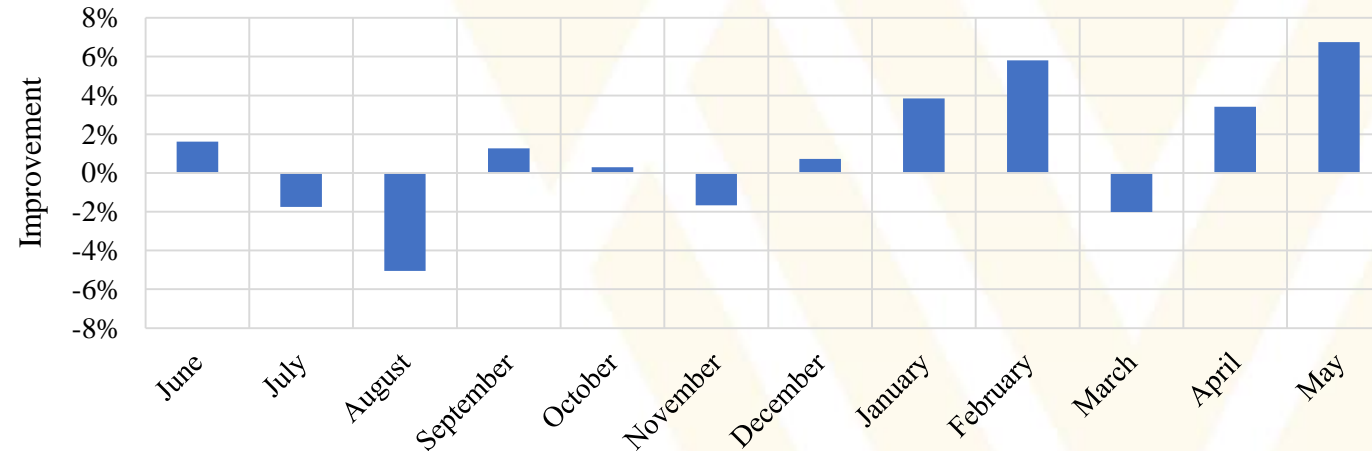
Monthly Pinball of the probabilistic forecasts of the three methods

# Results and Evaluation

## Probabilistic Forecasts



## The Improvements of Ensemble over Analog Ensemble



## Conclusions

- ✓ The probabilistic forecasting are quantifying the uncertainty associated with point forecasts.
- ✓ Combining the forecasts of various models leads to accurate point and probabilistic forecasts.
- ✓ Throughout the complete year, the ensemble based-probabilistic forecasts are more accurate than the analog ensemble and persistence probabilistic forecasts.
- ✓ The random forest is a powerful ensemble learning method.
- ✓ The CDF with the assumption of a normal distribution is better than the linear distribution to produce the probabilistic forecasts.
- ✓ The nonparametric estimation of CDF without the normality assumption yields a small improvement ( $P_b=0.0100$  vs.  $P_b=0.0102$  with a normality assumption of CDF).
- ✓ With additional historical data, the forecasting performance could be improved.

# Thanks for Your Listening

## Any Question?

**Mohamed Abuella**

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