# Exponetial function

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#### Abstract

In this article a power serie reprecentation of the exponential function is investergated.

### 1 Introduction

The exponential function normally denoted as:

$$f(x) = e^x \tag{1}$$

The exponential function can be repercented using a power series <sup>1</sup>:

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!} = 1 + x + \frac{x^2}{2} + \frac{x^3}{6} + \frac{x^4}{24} + \cdots$$
 (2)

This reprecentation only uses which only uses multiplications and divisions.

# 2 Implementation

The inplementation is made in C#. The implementation of the power function reprecentation are done in the following way:

```
\begin{array}{c} {\rm static\ double\ ex\,(double\ x)} \{\\ & {\rm if\,(x<0)}\\ & {\rm return\ 1/ex(-x)};\\ {\rm if\,(x>1.0/8)}\\ & {\rm return\ Pow(\,ex\,(x/2)\,,2)};\\ {\rm return\ 1+x*(1+x/2*(1+x/3*(1+x/4*(1+x/5*(1+x/6*(1+x/7*(1+x/8*(1+x/9*(1+x/10)))))))))};\\ \} \end{array}
```

Starting from the top, if the x < 0 the the function call itself but now rewritten using a positive value of x. if x > 1/8 the function the function calls itself but with a smaller agument, wich is x/2, wich gives an better accuricy. To account for halving the agument, the the result from the exponential equation is squared. At last if 0 <= x <= 1/8 then a revritten version of the power function repecentation of the exponential function is called.

 $<sup>^{1} \</sup>verb|https://en.wikipedia.org/wiki/Exponential_function|$ 

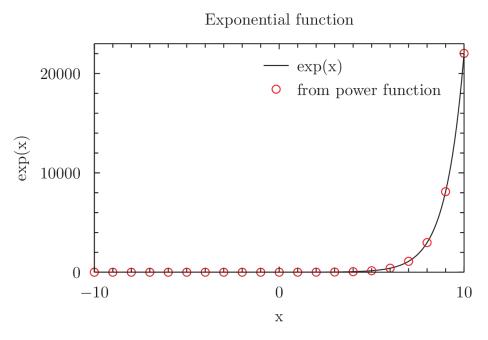


Figure 1: Exponential function plottet togeter with the power funtion reprecentation.

### 3 Results

In figure (??) are plottet trogether with results from the power function reprecentation equation (??).