Exponetial function

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Abstract

In this article a power serie reprecentation of the exponential function is investergated.

1 Introduction

The exponential function normally denoted as:

$$f(x) = e^x \tag{1}$$

The exponential function can be repercented using a power series ¹:

$$e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!} = 1 + x + \frac{x^2}{2} + \frac{x^3}{6} + \frac{x^4}{24} + \cdots$$
 (2)

This reprecentation only uses which only uses multiplications and divisions.

2 Implementation

The inplementation is made in c#. The implementation of the power function reprecentation are done in the following way:

```
static double ex(double x){  if(x<0) \\ return \ 1/ex(-x); \\ if(x>1.0/8) \\ return \ Pow(ex(x/2),2); \\ return \ 1+x*(1+x/2*(1+x/3*(1+x/4*(1+x/5*(1+x/6*(1+x/7*(1+x/8*(1+x/9*(1+x/10))))))))); \\ \}
```

Starting from the top, if the x < 0 the the function call itself but now rewritten using a positive value of x. if x > 1/8 the function the function calls itself but with a smaller agument, wich is x/2, wich gives an better accuricy. To account for halving the agument, the the result from the exponential equation is squared. At last if 0 <= x <= 1/8 then a revritten version of the power function repecentation of the exponential function is called.

 $^{^{1} \}verb|https://en.wikipedia.org/wiki/Exponential_function|$

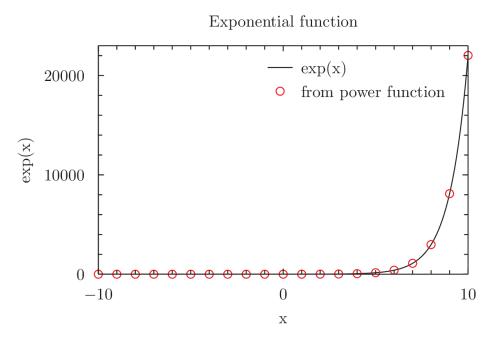


Figure 1: Exponential function plottet togeter with the power funtion reprecentation.

3 Results

In figure (1) are plottet trogether with results from the power function reprecentation equation (2).