

Marine Ecological Genetics

02. Hardy-Weinberg equilibrium | computer practical

- Calculate allele and genotype frequencies
- Test for Hardy-Weinberg equilibrium
- Learn to interpret HW test results
- Become familiar with microsatellite data

Martin Helmkamp



Access files for practical

Download files from GitHub:

<https://github.com/mhelmkamp/meg24.git> (Code | Download ZIP)

Alternatively, run git from terminal:

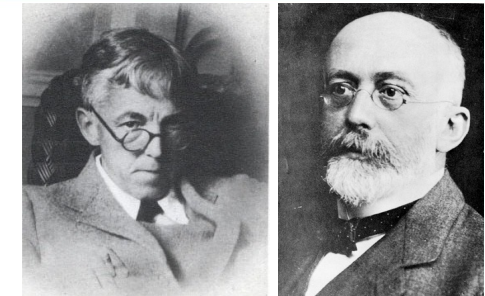
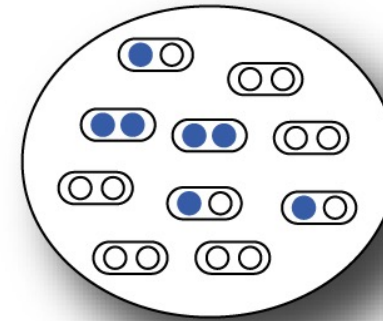
```
git clone https://github.com/mhelmkamp/meg24.git
```

Open R script called **Mar_Ecol_Gen_week2.R** in RStudio

HARDY-WEINBERG (1908)

Godfrey H. Hardy (1877-1947)

Wilhelm Weinberg (1862-1937)

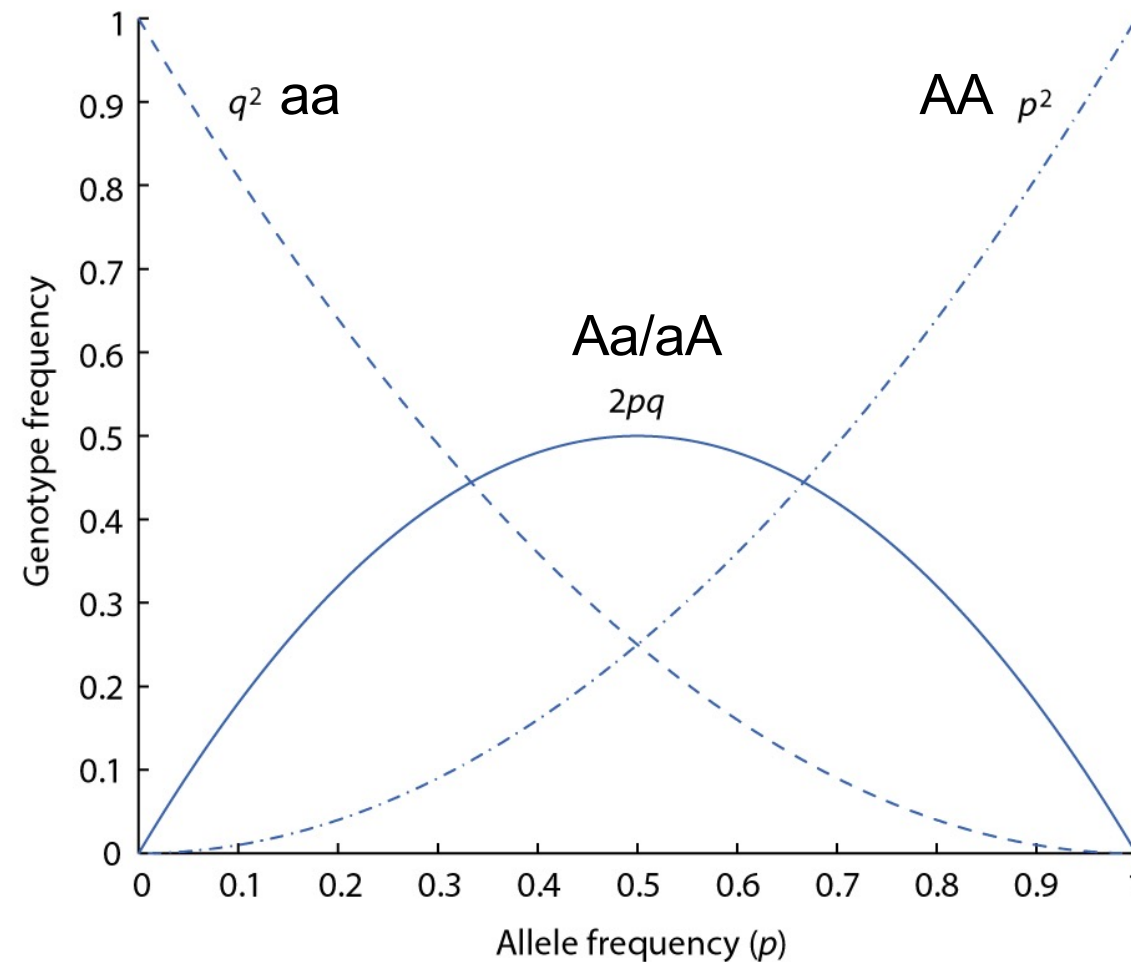


Establish the relationship between allele frequencies and genotype frequencies in a population

$$p^2 + 2pq + q^2 = 1$$

AA Aa/aA aa

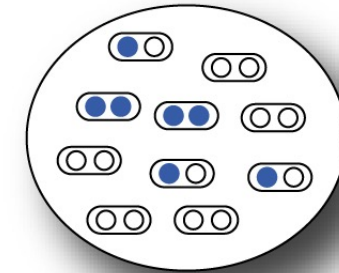
p and q : allele frequencies for a locus with two alleles (A and a)
($p + q = 1$)



A single generation of reproduction will result in a population that meets the expected Hardy-Weinberg frequencies, i.e. is at Hardy-Weinberg (HW) equilibrium

Assuming an “ideal” population, i.e. :

- Diploid organisms
- Sexual reproduction (as opposed to clonal)
- Random mating (as opposed to e.g. assortative) with respect to genotype
- Random union of gametes
- Discrete, non-overlapping generations
- Very large (infinite) population
- No migration
- No population structure
- No natural selection
- Two alleles
- Identical allele frequencies in both sexes

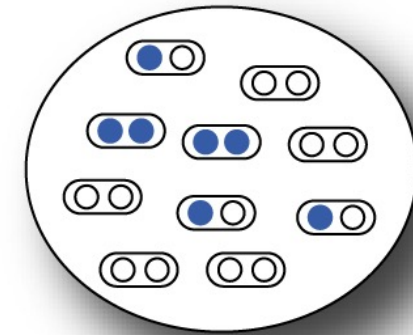


-> Departures from HW equilibrium may indicate:

- Inbreeding
- Assortative mating
- Self-fertilization
- Natural selection
- Population structure
- ...

HETEROZYGOSITY

In one population



H_o = proportion of heterozygote individuals, observed heterozygosity

$H_e = 2pq = 1 - p^2 - q^2$, expected heterozygosity (assuming HW equilibrium)

$$F = \frac{H_e - H_o}{H_e}$$

Fixation index: *proportion by which heterozygosity is reduced or increased relative to the heterozygosity of a population at HW equilibrium with the same allele frequencies.*

Divided by $H_e \rightarrow$ *proportion* (of expected heterozygosity)

Varies between -1 and 1

$F < 0$: heterozygote excess

$F > 0$ heterozygote deficit (homozygote excess)

May be averaged over several loci \rightarrow reduces bias

May be extended to k alleles

Is this population in Hardy-Weinberg equilibrium?

Exercise 1

Diploid, sexual reproduction, 1 locus, 2 co-dominant alleles (yellow, blue)



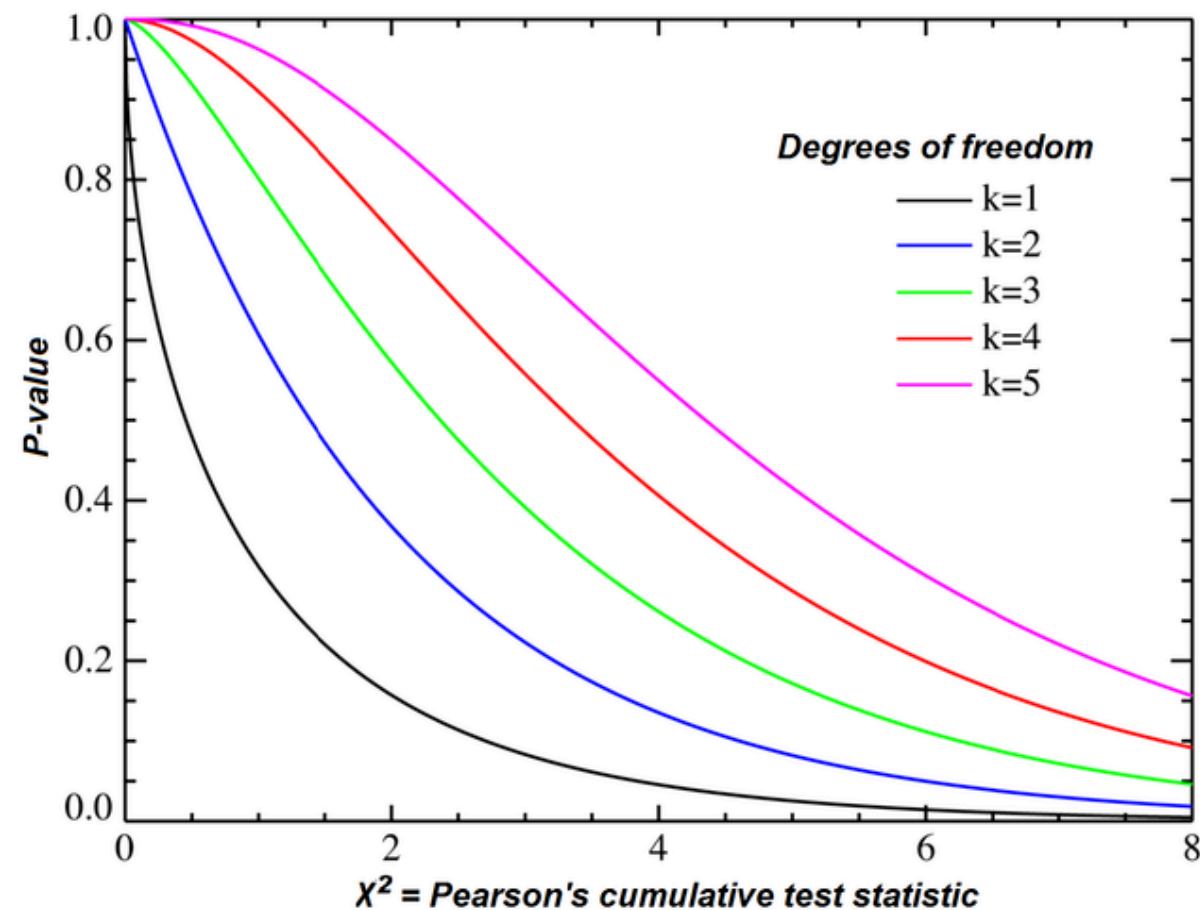
Pearson's chi-squared test

Exercise 1

Chi-square statistic:

$$\chi^2 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i}$$

Chi-square distribution:



Genepop format

Exercises 2/3

yellowblue.txt

Example data
Color
POP
ind01, yy
ind02, yy
ind03, yy
ind04, yy
ind05, yy
ind06, yy
ind07, yb
ind08, bb
ind09, bb
ind10, bb

puella_barbados.txt

Microsatellite genotypes of Hypoplectrus puella from Barbados

g2
gag010
h24
hyp001
hyp015
hyp018
e2
hyp008
hyp016
pam013
POP

Free text

Locus names

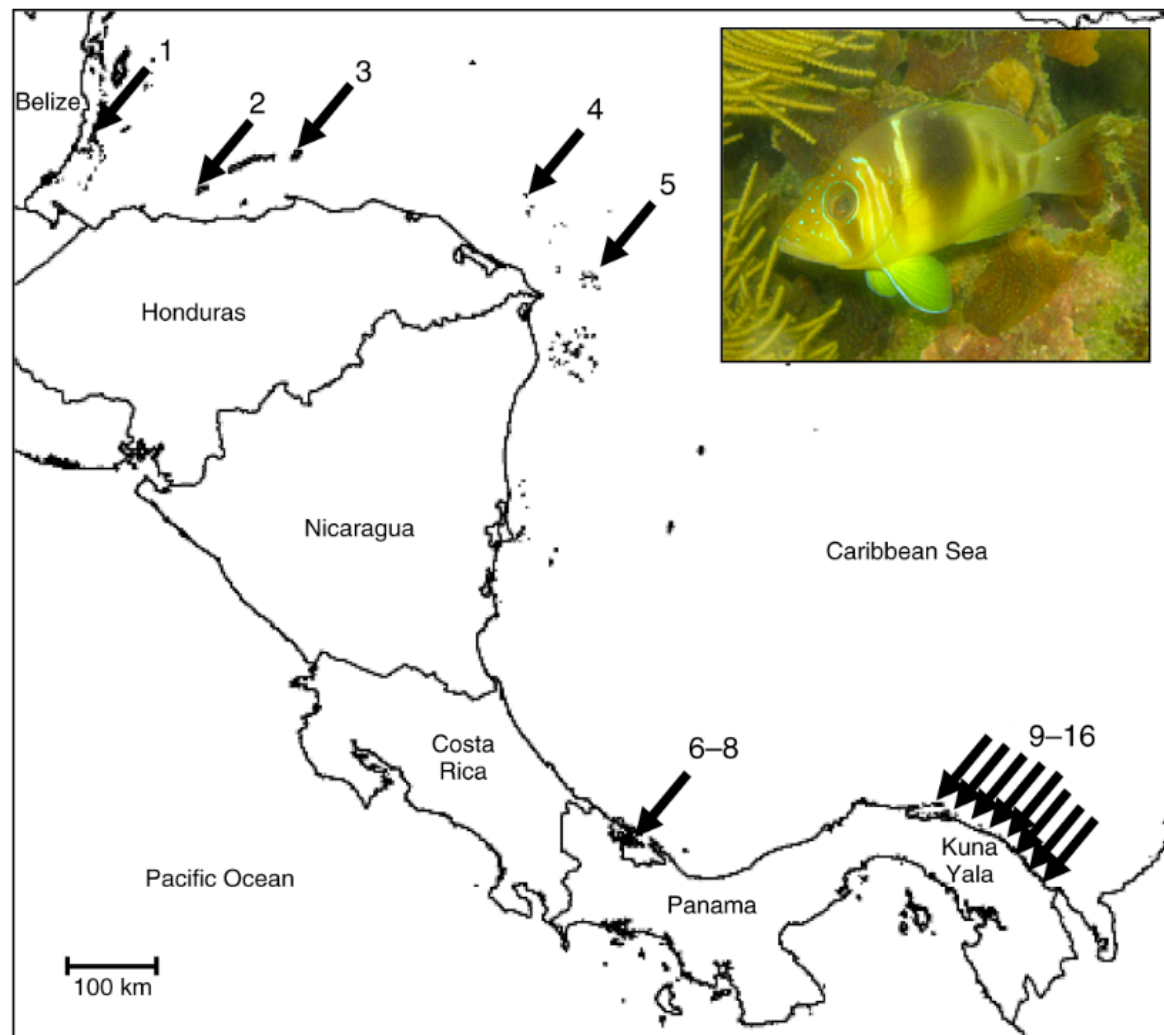
Sample / population

Alleles (000 = missing data)

| | | | | | | | | | | | | |
|----------|---------|---|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| barbados | ind#735 | , | 203235 | 121127 | 210248 | 225231 | 126132 | 190192 | 157157 | 236244 | 194220 | 114128 |
| barbados | ind#736 | , | 205217 | 119119 | 204216 | 225229 | 126126 | 190192 | 157165 | 236236 | 216222 | 106144 |
| barbados | ind#737 | , | 203203 | 135147 | 224226 | 233235 | 126136 | 190198 | 157163 | 238250 | 202226 | 126160 |
| barbados | ind#738 | , | 211217 | 119121 | 228230 | 223231 | 126130 | 190190 | 157157 | 240244 | 220226 | 138160 |
| barbados | ind#739 | , | 205225 | 121125 | 208216 | 227231 | 132132 | 192192 | 158159 | 244256 | 192196 | 146146 |
| barbados | ind#740 | , | 217233 | 119121 | 216228 | 227233 | 126126 | 192198 | 157157 | 242256 | 194216 | 000000 |
| barbados | ind#741 | , | 203209 | 000000 | 216222 | 223229 | 126130 | 192198 | 157157 | 234236 | 188226 | 118130 |
| barbados | ind#742 | , | 203215 | 119119 | 222234 | 233233 | 130130 | 190190 | 157157 | 240246 | 182188 | 108126 |
| barbados | ind#743 | , | 203243 | 111121 | 216224 | 231231 | 126126 | 190192 | 157159 | 234249 | 188198 | 118126 |
| barbados | ind#744 | , | 203225 | 121135 | 206232 | 231231 | 126130 | 192198 | 157159 | 240249 | 182222 | 122156 |
| barbados | ind#745 | , | 203211 | 121123 | 224236 | 227231 | 126132 | 192192 | 157163 | 238238 | 182204 | 138148 |
| barbados | ind#746 | , | 227233 | 119123 | 216234 | 227233 | 126130 | 190190 | 157159 | 236245 | 186188 | 124142 |
| barbados | ind#747 | , | 203223 | 133141 | 236240 | 231231 | 126126 | 192198 | 157157 | 234236 | 194204 | 118126 |
| barbados | ind#748 | , | 203217 | 141145 | 222226 | 227235 | 126126 | 190192 | 145157 | 238240 | 182196 | 108108 |
| barbados | ind#749 | , | 205221 | 125147 | 210238 | 223231 | 126132 | 192198 | 157157 | 234234 | 188200 | 106148 |
| barbados | ind#750 | , | 203235 | 123123 | 230234 | 223231 | 126132 | 192198 | 157157 | 236256 | 188214 | 122136 |
| barbados | ind#751 | , | 203211 | 121143 | 212248 | 223229 | 126132 | 190196 | 157159 | 234242 | 214216 | 118128 |
| barbados | ind#752 | , | 213217 | 123169 | 204234 | 223231 | 126134 | 190198 | 157163 | 236248 | 193224 | 142148 |

Barred hamlet (*H. puella*) microsatellite dataset

Exercise 3



Ecology, 90(11), 2009, pp. 3087–3098
© 2009 by the Ecological Society of America

Estimating dispersal from genetic isolation by distance
in a coral reef fish (*Hypoplectrus puella*)

OSCAR PUEBLA,^{1,2,3} ELDREDGE BERMINGHAM,^{1,2} AND FRÉDÉRIC GUICHARD²

- 10 highly variable microsatellite loci
- 854 individuals
- 15 Caribbean locations

Take-home messages

- Testing for HWE can tell us whether a population is behaving like an ideal population or not
- Deviation from HWE indicates that the population is under the influence of genetic, evolutionary or demographic processes
- Tests should be conducted over multiple loci, because not all loci may show the same pattern with respect to HWE (requires correction for multiple tests)
- Microsatellites are a widely used type of marker in population genetics (as well as forensics and other applications)