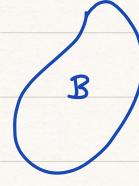
Short review of force 2 momentum object with mass m and velocity \(\times \) \Rightarrow Linear momentum: \(\L = \text{m y} \)

Force:
$$f = \frac{dL}{dt} = \frac{d}{dt} (mv) = m \frac{dv}{dt} = ma$$

Unils of force:
$$[F = \frac{ML}{T^2}]$$
 general boure units

Newton: $N = \frac{kgm}{s^2}$

Mass and Deusity



Volume of a body B:

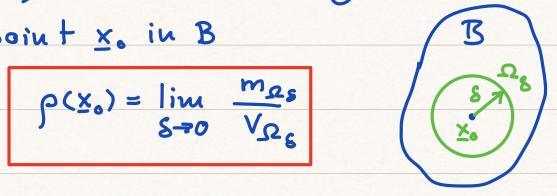
$$V_{\mathbf{B}} = \int_{\mathbf{B}} dV$$

Hars of a body B:

p(x) = mass density field

At any point x. in B

$$\rho(x_0) = \lim_{S \to 0} \frac{m_{\Omega S}}{V_{\Omega S}}$$



Important geometric quantities of a body are:

Center of volume:
$$\underline{x}_{v} = \frac{1}{V_{B}} \int_{B} \underline{x} dV$$

$$\bar{x}^{A} = \frac{\Lambda^{B}}{I} \int_{B} \bar{x} d\Lambda$$

$$\underline{x}_{m} = \frac{1}{m_{B}} \int_{B} \rho \underline{x} \underline{x} dV$$

Note: p = const

$$\underline{x}_{m} = \frac{1}{m^{D}} \int_{D} \underline{x} \, dV = \frac{b}{b} \int_{D} \underline{x} \, dV = \frac{1}{a} \int_{D} \underline{x} \, dV = \underline{x}_{A}$$

Important because resulting forces.

Body Forces

Any force that not due to physical contact is a body force and acts on the entire body.

Example: gravitational body force

⇒ body force field has units of force volume

If a body force acts on a body B the net or resultant body force is:

$$\Gamma_{b}[B] = \int_{B} b(x) dV \quad \text{units of force} \left[\frac{HL}{T^{2}}\right]$$

Resultant force due to Gravity

= ro[B] = SpogdV if g is constant

= g SpodV = mog

Surface/Contact Forces

bodies. Forces along imaginary surfaces within a body are called internal forces while forces along the bounding surface of a body are external.

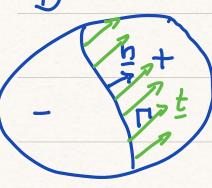
Internal surface forces hold a booky together. External surface forces discribe the interaction

with the environment.

Traction Field

B

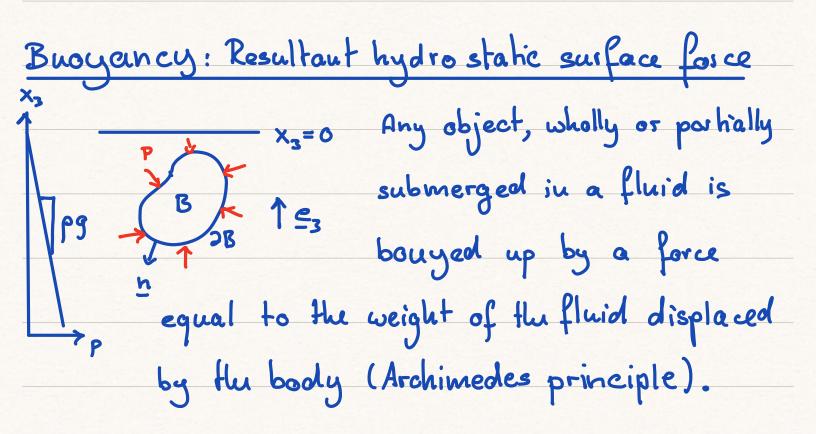
Consider an arbitrary surface



I' in B with unit normal n(x) that defines the positive and negative sides of B.

The force per unit area exerted by material on the pos. side upon material on the neg. side is given by the traction field to for Γ .

The resultant force due to a traction field on
$$\Gamma$$
 is $\Gamma = \int_{\Gamma} t_n(x) dA$



Hydrostatic traction en DB: t=-pn

need to convert this to volume integral

$$\Rightarrow \int_{B} = -\int_{B} p_{1} dA = -\int_{B} \nabla_{p} dV$$
where
$$\nabla_{p} = \nabla(-p_{3}x_{3}) = -p_{3}e_{3} = p_{4}e_{3}$$

where
$$\nabla p = \nabla (-p_3 x_3) = -p_3 = 3 = p_f g$$

Buogancy force is minus the weight of the displaced fluid (Archimedes r)

Hydrostatic force balance

Total resultant force f on

a submerged body in a

gravitational field is the

sum of weight and buoyancy.

$$f = \int_{B} (p_f - p_b) g e_3 dV = (m_f - m_b) g e_3$$

f_c ↓

Pf > Pb: f points up -> body rises (pos. buoyaucy) Pt < Pb : f points down -> body sinho (neg. buoyanay) Pf=Pb:f=0 -> body is neutrally buoyant

Note: The integrated expression assumes g=const. Some demonstrations Harvard Natural Science Lecture Serves

