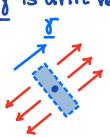
Simple states of stress

I) Hydrostatic stress

II) Uniaxial stress

$$\bar{\varsigma} = \varrho \, \bar{\lambda} \bar{\omega} \bar{\lambda} \Rightarrow \bar{\Gamma}^{\mu} = \bar{\varsigma} \bar{u} = \varrho \, (\bar{\lambda} \cdot \bar{u}) \bar{\lambda}$$

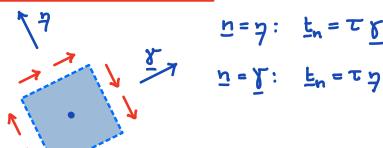


(y is unit vector) Traction is always parallel to y and vanishes on surfaces with normal perpendicular to y.

6 >0: pure tension

à <0: pure compression

$$\vec{\xi} = \mathcal{L} \left(\vec{\lambda} \otimes \vec{\lambda} + \vec{\lambda} \otimes \vec{L} \right) \Rightarrow \vec{\Gamma}^{\mu} = \vec{e} \vec{\nu} = \mathcal{L} (\vec{\lambda} \cdot \vec{\nu}) \vec{L} + \mathcal{L} (\vec{\lambda} \cdot \vec{\nu}) \vec{\lambda}$$



IV, Plane stress

If there exists a pair of orthogonal vectors of and of such that the matrix representation of 5 in the frame { \$, 7, \ \ x \ x \ z } is of the form

$$\begin{bmatrix} \mathbf{S} \end{bmatrix} = \begin{pmatrix} \mathbf{S}_{11} & \mathbf{S}_{12} & \mathbf{0} \\ \mathbf{S}_{21} & \mathbf{S}_{22} & \mathbf{0} \\ \mathbf{S} & \mathbf{0} & \mathbf{0} \end{pmatrix}$$

then a state of plane stress exists.

The pressure $p = -\frac{1}{3} \operatorname{tr}(\S) = -\frac{1}{3}(s_1 + s_2 + s_3)$ can be interpreted as the mean normal traction. The spherical stress is the part of \S that changed the volume of the body. Note that p > 0 corresponds to compression.

The deviatoric stress is the part of of that changing the shape of abody without changing its volume. By definition trop=0.

Principal invariants of 5:

I, (5) = tr 5 = 0

$$J_{2}(\vec{\xi}) = -I_{2}(\vec{\xi}_{D}) = \frac{1}{2} \vec{\xi}_{D} : \vec{\xi}_{D}$$

 $J_3(\underline{\epsilon}) = I_3(\underline{\epsilon}_D) = \det \underline{\epsilon}_D$

The invariants J_2 and J_3 of the deviatoric stress on are used to formulate yield functions in theory of plasticity.