



Seminar report

# Set Intersection Problem

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# 1 Introduction

The act of *searching* has become so deeply ingrained in the modern society that we tend to take it for granted, not only assuming it normal to have immediate and easily accessible information on the tip of our thumbs, but expecting it: a study from 2004 showed that users were not willing to wait more than ten seconds for a page to load (Nah, 2004). Fast forward twenty years and nowadays even a couple seconds holdup would be unacceptable, thus query retrieval needs to be fast. Blazingly fast in fact, since we need to account for all the delays typical of a gargantuan structure as big as the modern web, and, as the reader probably knows, it is *not* a good idea to rely on memory's performances increasing over time: the smart way to tackle this problem is via research and development of efficient algorithms, and exactly which type should be self-evident from the title of this document. The problem of the set intersection constitutes the backbone of every query resolver in a (web) search engine, since every word in a query is interpreted as a collection of documents' IDs which contains it.

In this survey-style paper we will first explain what searching (i.e., querying) entails, show how a document (e.g., a web page) can be transformed into word tokens which are then further processed into inverted indexes, and, finally, we will see a collection of algorithms that concern themselves with intersecting sets, meaning finding common elements between two or more comparable collections.

## 1.1 How Do We Search?



**Figure 1.1:** From a bag of words to a set of documents

Generally speaking, a query is called a *bag of words*, and finding its result means computing which documents contain all word tokens that are being searched for [1.1]. Let's make an example: word **abiura** is contained in documents number [31, 42, 127], while word **bitonto** is contained in documents number [20, 42, 72].

Thus `query = (abiura,bitonto)` will return the result 42.

Dictionary	Posting List (ASC)	Relevance
abaco	1, 7, 136	0.6, 0.3, 0.8
abiura	31, 42, 127	0.12, 0.5, 0.77
bitonto	20, 42, 72	0.8, 0.1, 0.03

**Figure 1.2:** Table of word tokens

Both The example above [1.2] and all the algorithms we will see in this survey consider the problem of searching as the problem of complete intersection, but modern search engine (e.g., Google) leverage input relevance and filter unneeded outputs to obtain faster and better results. Unfortunately finding information about how they do it is near impossible, since everything is covered by trade secret.

Let's now see what inverted indexes are and how we can obtain them starting from a document corpus.



## 2 Inverted Indexes

Most of the information present in this chapter is thanks to Mahapatra and Biswas "Inverted indexes: Types and techniques" (Mahapatra and Biswas, 2011).

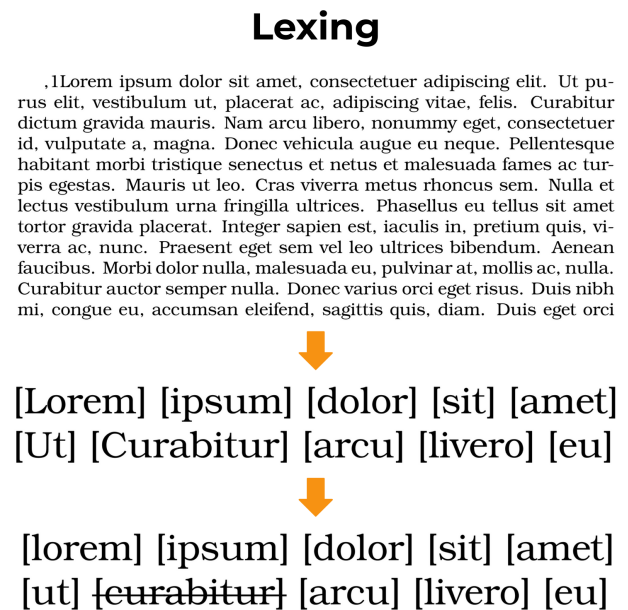
What we will need for the algorithms presented in the rest of this documents are inverted indexes (also called posting lists). To get them we first need to process documents into lists of words (called *word tokens*), then for each token compute a list of IDs that refer to the documents which contain that specific token. Let's see each step in order.

### 2.1 Document Pre-Processing

Documents go through a series of processing steps before being indexed: they get converted into token in the lexing phase, which are then possibly normalized, stemmed or even pruned (removed) entirely.

#### 2.1.1 Lexing

The process of transforming a document into a list of tokens, each of which is a single word, is called *lexing* [2.1]. There often is a maximum length for a single token, as to prevent unbounded index growth in edge cases, and all input is generally first converted into lower-case to normalize it. All non-punctuation characters are added to the list of tokens one by one, and those that exceed a certain size are often pruned (removed from the corpus). It is not entirely clear how Google and other big companies do this step, and it certainly feels strange to think they employ a simple *brute force*, single scan approach, but as mentioned be-



**Figure 2.1:** Lexing: from text to word tokens

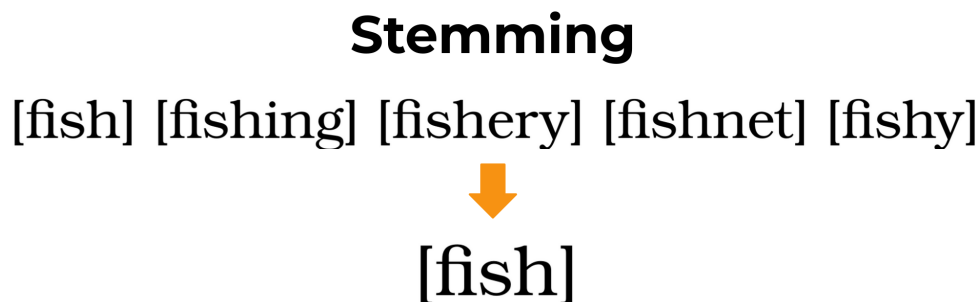
fore it is not easy to find information about it.

All of the above works only with alphabetic languages, ideographic ones (e.g., Chinese) need specialized search techniques.

### 2.1.2 Stemming

We can consider this step deprecated, since nowadays memory, especially for things like text and arrays (which inverted index basically are), is cheap and bountiful.

The idea is to find a sort of *root* (stem) of the words, and indexing that instead. To make an example: fishnet, fishery, fishing, fishy, fishmonger, can all be boiled down to their stem *fish* [2.2].



**Figure 2.2:** Stemming to stem "fish"

In the example above should be clear already that stemming carry some problems: a user searching for "fishnet" is likely not shopping for fishing equipment, thus most modern search engine skip this normalizing step, and most stemming algorithms (most famous of which is Porter's) are complex, full of exceptions and exceptions to the exceptions, while still failing to unite together the correct words. This step basically reduces query precision while providing very little in return.

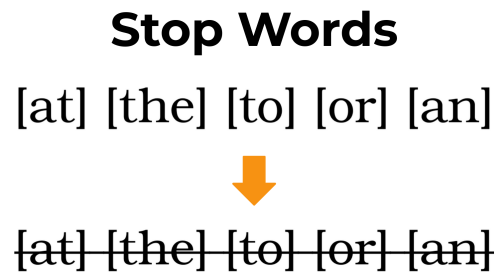
### 2.1.3 Stop Words

*Stop words* are words that work as connectives of sorts, like *and*, *the*, *is*, *of*, *to*, etc.

Their quantity is language dependent (e.g., in English they could be around 500 words) and they are often removed from the corpus which, for normal queries, does not worsen the results while saving space in the index. However in some cases like searching for *to be* or *not to be* stop words are actually essential, and removing them would make the search

fail.

Thankfully they are so common that if saved as differences between consecutive different values, both their document number and word position lists can be compressed to save space. Because of this, the overhead is not as big as one might think, thus modern search engines (like Google) do not seem to remove them from the index, since doing so put them at a competitive advantage at the expense of a slightly bigger index.



**Figure 2.3:** Stop words pruning

## 2.2 Inverted Indexes

Now that we have a set of word tokens, we can start building our inverted indexes (or posting lists): documents are often stored as lists of words, but we invert (hence the name) this concept by storing for each word the list of documents that contain it. There are several variants of this data structure, but at minimum you need to store for each word the list of documents that contain that specific word.

We can change the granularity by adding the frequency of the word in the document, which can be useful for query optimization, or by adding the word position in the document, allowing for in-document queries.

Space used by inverted indexes varies wildly in the range of five to one hundred percent (5-100%) of the total size of the document indexed, and this is because implementations come in many different variations: some store word positions and some don't, some aggressively pre-process documents and some don't, some dynamically update themselves and some don't, some use complex and powerful compression methods and some don't, and so on.

Table [2.1] show some sample documents, while table [2.2] shows some examples of inverted indexes, with different levels of granularity.

ID	Contents
1	The only way not to think about money is to have a great deal of it
2	When I was young I thought that money was the most important thing in life; now that I am old I know that it is.
3	A man is usually more careful of money than he is of his principles.

**Table 2.1:** Sample document collection

Word	Doc List	Frequency	Positions
a	1, 3	1:1, 3:1	1:(12), 3:(1)
About	1	1:1	1:(7)
am	2	2:1	2:(19)
Careful	3	3:1	3:(6)
deal	1	1:1	1:(16)
great	1	1:1	1:(13)
have	1	1:1	1:(11)
...	...	...	...
money	1, 2, 3	1:2, 2:1, 3:1	1:(8), 2:(8), 3:(9)
more	3	3:1	3:(5)
...	...	...	...
when	2	2:1	2:(1)

**Table 2.2:** Inverted lists example, most words omitted

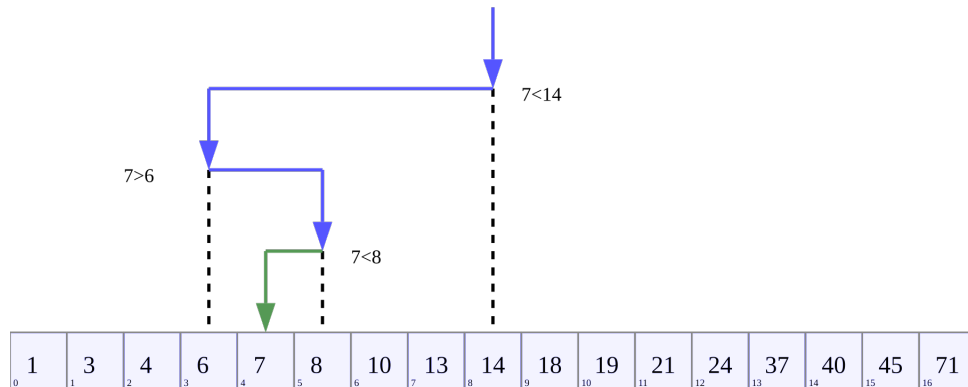
# 3 Intersection Algorithms

In this chapter we are going to see a collection of algorithms to compute the intersection of two **sorted** lists, taken from the chapter six of "Pearl of Algorithm Engineering" by Paolo Ferragina, published by Cambridge University Press (Ferragina, 2023).

We will first look at two of the most commonly used search algorithms, since we cannot intersect without searching.

## 3.1 Search Algorithms

### 3.1.1 Binary Search



**Figure 3.1:** Binary search algorithm, source: [Wikipedia](#)

Binary search, also known as logarithmic search or binary chop, is a search algorithm that finds the position of a target value within a sorted array: it compares the target to the middle element of the array and, if they are not equal, it eliminates half of the search space by discarding either the left or right half, depending on whether the target value is less than or greater than the middle element. This process is repeated by iteratively searching into the remaining sub-array until the target value is found or the search space is empty. The pseudocode for the algorithm can be seen at *Algorithm* [1].

Binary search runs in logarithmic time in the worst case, doing  $O(\log n)$  comparisons, where  $n$  is the number of elements in the array, making it much faster than linear search with large arrays thanks to its scaling.

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**Algorithm 1**

Pseudocode for binary search algorithm

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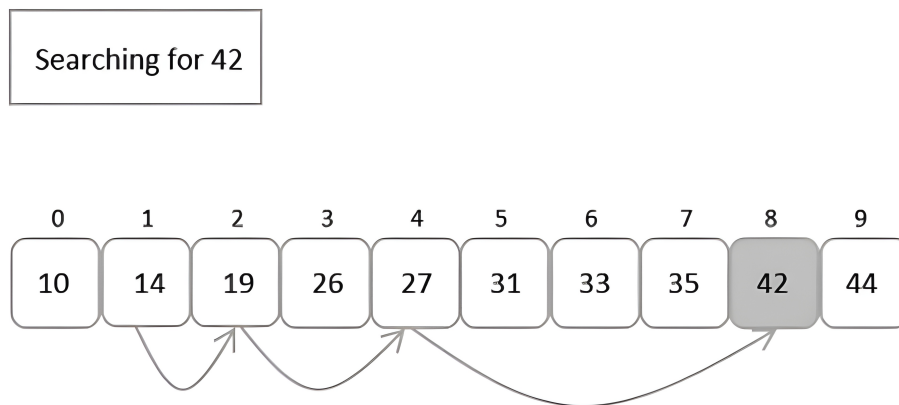
```

1: looking for element key
2: let  $L = 0$  ▷ First half
3: let  $R = n - 1$  ▷ Second half
4: while  $L \leq R$  do
5:    $m = \lfloor (L + R)/2 \rfloor$ 
6:   if  $A[M] < key$  then
7:     let  $L = m + 1$ 
8:   else if  $A[M] > key$  then
9:      $R = m - 1$ 
10:  else
11:    return  $m$  ▷ Found
12:  end if
13: end while
14: return false ▷ Not found

```

---

### 3.1.2 Exponential Search



**Figure 3.2:** Exponential search algorithm, source: [Tutorialspoint](#)

Exponential search, also called doubling or galloping search, is an algorithm for searching sorted, unbounded lists: there are numerous implementations, most common being determining a sub-array into which the **key** may reside in and performing a binary search [3.1.1] within its range.

To be more precise: we go through the list in exponentially increasing steps, with a factor of  $2^k$  such that we first look into `list[0]`, then `list[1]`, then `list[2]`, `list[4]`, `list[8]`, following with *16, 32, 64, 128* and so on until we find a value that is greater than the **key**. Once we find it, we perform a binary search between the previous jump and the current (or the end of the array):  $2^{k-1} \leq \text{key} \leq \min(2^k, n)$ .

The algorithm can be more efficient than binary search, as it runs in  $O(\log i)$  time, where  $i$  is the index of the element being searched for, which could be half if not less than  $n$ .

The pseudocode can be seen at *Algorithm* [2].

---

### Algorithm 2

Pseudocode for exponential search algorithm

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```

1: looking for element key
2: let  $i = 0$ 
3: let  $k = 0$ 
4: while ( $\text{key} > \text{list}[i + 2^k]$  and  $i < n$ ) do
5:      $i = i + 2^k$                                 ▷ Gallop to next step
6:      $k = k + 1$                                 ▷ Increment exponent
7: end while
8: if  $i < n$  then
9:     binary_search(list, key, i, min(i + 2k, n))
10: else
11:     return false                                ▷ Not found
12: end if

```

---

### 3.1.3 Extrapolation and Intrappolation

TODO maybe or maybe not

## 3.2 Intersection Algorithms

### 3.2.1 Brute Force

The first idea that would come to mind when thinking about intersecting two lists is to simply iterate through both of them and check if the elements are equal: this is the *brute force* approach, which is simple but inefficient.

With a time complexity of  $O(m \cdot n)$ , assuming lists sizes  $n$  and  $m$  to be around  $10^6$ , and assuming a modern computer able to do  $10^9$  operations per second, this algorithm would need ten minutes to compute a 2-words query, which is less than ideal.

The (very short) pseudocode can be seen at *Algorithm* [3].

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#### Algorithm 3

Pseudocode for brute force algorithm

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```

1: for all  $i = 0$  to  $n - 1$  do
2:   for all  $j = 0$  to  $m - 1$  do
3:     if  $A[i] == B[j]$  then
4:       add  $A[i]$  to result
5:     end if
6:   end for
7: end for

```

---

### 3.2.2 Bunny Race

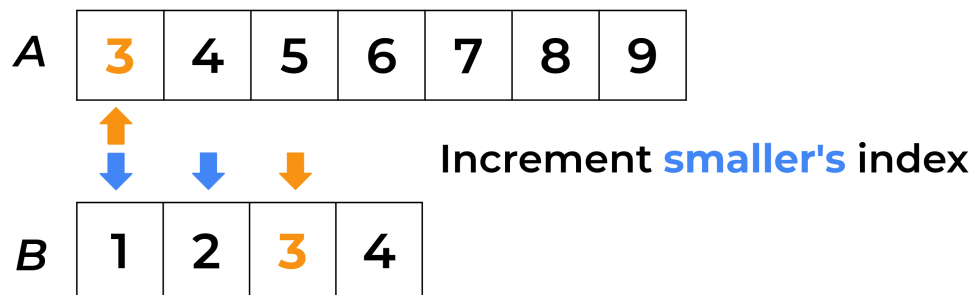


Figure 3.3: Bunny race algorithm



This approach, often called merge-based, is simple, elegant and fast: the main idea is to have two indices pointing at the two list running after each other by comparing elements each time and incrementing the index pointing at the smallest one (or incrementing both if they are equal).

To clarify: lets say we have two lists,  $A$  and  $B$ , of size  $n$  and  $m$  respectively. We start with two pointers,  $i$  and  $j$ , both set to zero.

We compare the elements at these indices,  $A[i]$  and  $B[j]$ : if they are equal, we add the element to the result and increment both pointers.

If  $A[i] < B[j]$ , we increment  $i$ , while if  $A[i] > B[j]$ , we increment  $j$ .

This process continues until one of the pointers reaches the end of its respective list.

The correctness can be proven inductively, exploiting the following observation: if  $A[i] < B[j]$  then  $A[i]$  is smaller than all elements following  $B[j]$  in  $B$  since its ordered, so  $A[i] \notin B$ .

The other case is symmetric.

In regards to time complexity, we just need to note that at each step the algorithm executes one comparison and advances at least one iterator, thus, given that  $n = |A|$  and  $m = |B|$ , the algorithm runs in no more than  $O(n + m)$  time.

This time complexity is significantly better than the *brute force* [3] approach, since it can compute a 2-word query in  $10^{-3}$  seconds.

The pseudocode can be seen at *Algorithm* [4].

In the case that  $n = \Theta(m)$  this algorithm is optimal, because we need to process the smallest set, thus  $\Omega(\min(n, m))$  is an obvious lower bound. Moreover, this procedure is also optimal in the disk model since it takes  $O\left(\frac{n}{B}\right)$  I/Os.

In the case that  $n \ll m$  the classic *binary search* can be helpful since we can design an algorithm that search in  $A$  for each elements of  $B$  in  $O(m \log n)$  time, which is better than  $O(n + m)$  when  $m = o\left(\frac{n}{\log n}\right)$ .

**Algorithm 4**

Pseudocode for bunny race algorithm

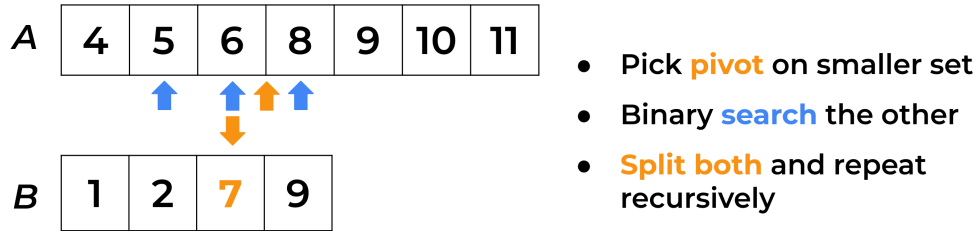
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```

1: let  $i = 0$ 
2: let  $j = 0$ 
3: while  $i < n$  and  $j < m$  do
4:   if  $A[i] < B[j]$  then
5:      $i = i + 1$  ▷ Increment first
6:   else if  $A[i] > B[j]$  then
7:      $j = j + 1$  ▷ Increment second
8:   else
9:     add  $A[i]$  to result ▷ Found
10:     $i = i + 1$  ▷ Increment both
11:     $j = j + 1$ 
12:   end if
13: end while

```

---

**3.2.3 Divide and Search****Figure 3.4:** Divide and search algorithm

Also called *mutual partitioning*, this approach adopt a classic algorithmic paradigm, namely *divide and conquer*, famously used to design the *quick sort* algorithm (which can be visualized [here](#)).

Let us assume  $m = |B| \leq n = |A|$ . We select the median element of  $B$ ,  $b_{m/2}$ , as a *pivot* and search for it in the longer sequence  $A$  using the *binary search* [3.1.1] algorithm.

Two cases may occur:

- i. *pivot* is one of the elements fo the intersection;
- ii.  $b_{m/2} \notin A$ , e.g,  $A[j] < b_{m/2} < A[j + 1]$ .

In both cases the algorithm proceeds *recursively* by calling itself on the two sub-lists in which each list ( $A$  and  $B$ ) has been split according to the *pivot* element, thus computing the following intersections:

- $A[1, j] \cap B[1, \frac{m}{2} - 1]$
- $A[j + 1, n] \cap B[\frac{m}{2} + 1, m]$ .

In simpler terms: we pick the middle element of the smaller list, search for it in the bigger list, split both lists and repeat the process recursively on the remaining sub-lists, then again, then again, then again, until we reach the base case where each list is of size one. The pseudocode of the algorithm can be seen at *Algorithm* [5].

Correctness follows, while for evaluating time complexity we need to identify the worst case.

Let us start with the case where *pivot* falls outside  $A$ , meaning that one of the two parts is empty and thus the corresponding half of  $B$  can be ignored. So, one *binary search* [3.1.1] over  $A$ , costing  $O(\log n)$  time, has discarded half of  $B$ .

If this keeps occurring in all recursive calls, the total number of them will be  $O(\log m)$ , which leads us to a time complexity of  $O(\log m \log n)$ .

On the other hand, if we have both balanced partitions so that  $b_{m/2}$  not only falls inside  $A$  but coincides with the median element  $a_{n/2}$ , the time complexity can be expressed via the recurrence relation  $T(n, m) = O(\log n) + 2T(\frac{n}{2}, \frac{m}{2})$ , with the base case  $T(n, m) = O(1)$  whenever  $n, m \leq 1$ .

This recurrence has the solution  $T(n, m) = O(m(1 + \log \frac{n}{m}))$  for each  $m \leq n$ , which is an optimal time complexity in the comparison model.

That being said, despite its optimal time complexity, the mutual-partitioning paradigm is heavily based on recursive calls and binary searching, and both paradigms offer poor performance in a disk-based setting when sequences are long hence requiring a large number of both dynamic memory allocations (recursive calls) and random memory access (*binary search* steps).

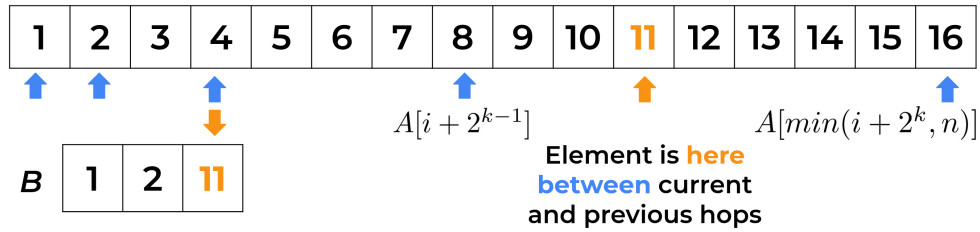
**Algorithm 5**

Pseudocode for divide and search algorithm

- 
- ```

1: Let  $m = |B| \leq n = |A|$ 
2: Pick pivot  $p = b_{\lfloor m/2 \rfloor}$ 
3: Binary search for  $p$  in  $A$  ▷ Say  $a_j \leq p < a_{j+1}$ 
4: Divide and search on  $A[1, j] \cap B[1, \frac{m}{2} - 1]$ 
5: if  $p = a_j$  then
6:   Add  $p$  to result
7: end if
8: Divide and search on  $A[j + 1, n] \cap B[\frac{m}{2} + 1, m]$ 

```
- 

**3.2.4 Doubling Search****Figure 3.5:** Doubling search algorithm

Also called *exponential search* or *galloping search*, this paradigm is more or less what we presented in the search algorithm *exponential search* [3.1.2]: assuming  $m = |B| \leq n = |A|$ , we search of each element  $b_j$  of  $B$  into  $A$  by jumping through it with exponentially bigger steps that increase by a factor of  $2^k$ , meaning that we compare  $b_j$  with  $A[0]$ ,  $A[1]$ ,  $A[2]$ ,  $A[4]$ ,  $A[8]$ ,  $A[16]$ ,  $A[32]$ , and so on, until we find that either  $b_j < A[i + 2^k]$  for some  $k$ , or we have jumped out of the array since  $i + 2^k > n$ .

Then we perform a *binary search* [3.1.1] for  $b_j$  between  $A[i + 2^{k-1}]$  and  $A[\min(i + 2^k, n)]$ .  $A[0, i + 2^{k-1}]$  will be discarded from the subsequent searches.

The pseudocode of the algorithm can be seen at *Algorithm* [6], which is a bit different from the one we saw in *exponential search* section [3.1.2], so it can be seen as an extra resource. Both works very similarly.

Correctness is again immediate, while deriving time complexity will require some reasoning: we denote with  $\Delta_i$  the size of the sub-array of  $A$  where  $b_j$  could be found. We then say that:

- $b_j \geq i + 2^{k-1}$  i.e. previous step
- $b_j < \min(i + 2^k, n)$  i.e. current step or end of  $A$

We can therefore write  $2^{k-1} \leq i - (i-1)$  where  $i$  and  $(i-1)$  are current and previous step respectively, and combining this inequality with  $\Delta_i$  we get  $\Delta_i \leq 2^{k-1} \leq i - (i-1)$ .

At this point we can estimate the total length of search sub-arrays of  $A$ :  $\sum_{i=1}^m \Delta_i \leq \sum_{i=1}^m (i - (i-1)) \leq n$ , because the latter is a telescopic sum in which consecutive terms cancel out.

For every  $i$ , the algorithm executes  $O(1 + \log \Delta_i)$  steps, thus summing for  $i = 1, 2, \dots, m$  (since  $m = |B|$ ) we get a total time complexity of  $\sum_{i=1}^m O(1 + \log \Delta_i) = O(\sum_{i=1}^m (1 + \log \Delta_i)) = O(m + m \log \sum_{i=1}^m \frac{\Delta_i}{m}) = O(m(1 + \log \frac{n}{m}))$ .

This is the same time complexity we got from the *divide and search* [5] algorithm, except with an iterative paradigm, which thus does not require dynamic memory allocation. Moreover, it calls the *binary search* [3.1.1] on a sub-array of  $A$  needing less disk accesses. Unfortunately, it falls short with very large lists, since galloping through them may require moving them in chunks back and forth from memory. It would thus be ideal to *compress* in some way the vector  $A$ .

---

### Algorithm 6

Pseudocode for doubling search algorithm

---

```

1: Let  $m = |B| \leq n = |A|$ 
2: Let  $i = 0$ 
3: for all  $j = 0$  to  $m - 1$  do
4:   Let  $k = 0$ 
5:   while  $B[j] > A[i + 2^k]$  and  $i + 2^k \leq n$  do
6:      $k = k + 1$  ▷ Increment exponent
7:   end while
8:    $i' = \text{binary search into } A[i + 2^{k-1} + 1, \min(i + 2^k), n]$ 
9:   if  $a_{i'} = b_j$  then
10:    Add  $b_j$  to result
11:   end if
12:    $i = i'$  ▷ Update  $i$  to the last position
13: end for

```

---

### 3.2.5 Two-Level Storage Approach

Since most of the time we can consider physical memory as divided in two, namely cache and RAM, engineers took advantage of this by adopting a two-level storage approach: the main idea is to preprocess a collection of lists, logically partitioning each of them into blocks of size  $L$  (final block may be shorter), and copying the first element of each block into an auxiliary sequence. Then, merge them and compute the intersection: elements of block  $merged\_list[i + 1]$  will be contained (if present) in block  $merged\_list[i]$ .

Lets see a simplified implementation where we preprocess only the longer sequence: say we have two lists such that  $m = |B| \leq n = |A|$ , we then divide  $A$  in  $\lceil \frac{n}{L} \rceil$  blocks of size  $L$  and we save the first element of each block, called *guides*, in a new list  $A'$ , effectively compressing the original list.

We then use the *merge procedure* (which can be seen [here](#)) to merge  $A'$  and  $B$  into a new list  $Merged$ , which will contain each *guide* of  $A$  and all elements of  $B$  interspersed between them. The list is, of course, sorted.

Now we can find the elements of  $B$  in the respective preceding *guide* of  $A$ . Lets clarify, we have:

- $Merged[k] = A'[i]$
- $Merged[k + 1 \dots k + 1 + \alpha] = B[j \dots j + \alpha]$
- $Merged[k + \alpha + 2] = A'[i + 1]$

Thus the elements of  $B$ ,  $b_j \dots b_{j+\alpha}$  can all be found in the block of *guide*  $A'[i]$ .

Regarding time complexity, creating the list of *guides* takes linear time over the size of  $A$ . We then apply the *merge procedure* to fuse together  $A'$  and  $B$  in  $O\left(\frac{n}{L} + m\right)$  time, and finally we search for  $b_j \dots b_{j+\alpha}$  in the block of *guide*  $A'[i]$  using the *bunny race* [3.2.2] algorithm in time  $O(|A_i| + |B_j|) = O(L + |B_j|)$  where  $|A_i|$  is the size of the block of  $A'[i]$ , and  $|B_j| = |B[j \dots j + \alpha]|$ .

This algorithm is executed over all non-empty pairs  $(A_i, B_j)$ , which are no more than  $m$  since  $B = \cup_j B_j$ , thus the total time taken by this step is  $O(Lm + m)$ .

Summing up the time complexity of all steps we get that the algorithm has:

- $O\left(\frac{n}{L} + mL\right)$  Time complexity
- $O\left(\frac{n}{LB} + \frac{mL}{B} + m\right)$  I/Os

Where  $B$  is the disk-page size of the two-level memory model.

## 4 Discussion



## 5 Conclusions

# Bibliography

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## Appendix A Sample Appendix

You can add one or more appendices to your thesis.