Computing in Science Education (CSE): Integrating a computational perspective in the basic science education

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### People and links

- Hans Petter Langtangen, Computer Science
- Knut Morken, Mathematics
- Anders Malthe Sorensen and Arnt Inge Vistnes, Physics
- Tom Lindstrom, Mathematics
- Oyvind Ryan, Mathematics
- Solveig Kristensen, Dean of Education
- Hanne Solna. Director of studies
- http:

//www.mn.uio.no/english/about/collaboration/cse/

• http:

//www.mn.uio.no/english/about/collaboration/cse/
national-group/computing-in-science-education.pdf

### More links

- Python and our first programming course, first semester course. Excellent new textbook by Hans Petter Langtangen, click here for the textbook or the online version
- Mathematical modelling course, first semester course.
   Textbook by Knut Morken to be published by Springer.
- Mechanics, second semester course. New textbook by Anders Malthe-Sorenssen, in press by Springer, Undergraduate Lecture Notes in Physics
- Computational Physics I, fifth semester course. Textbook to be published by IOP in 2015, with online version.

# Wouldn't it be cool if your mechanics students could reproduce results in a PRL?



Grand challenge project in FYS-MEK1100 (Mechanics), Second Semester: a friction model to be solved as coupled ODEs. And find problems with the article?

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### An important observation and a question

The basic tools for mathematical calculations have changed radically.

How does this influence science education?

- Modern industry and technology is impossible without mathematics and science
- Weather forecasting, product design, film production, materials science, cellular phones, iPad, lunar missions, GPS, furniture production and much more

### Reality

- Students hear about the relevance of the sciences
- But this relevance is hardly visible in school or the first few years at university
- Much emphasis on renewal of the wrapping of science, little on the content

### Principles

### Central aims behind our CSE reform

Algorithmic thinking as a way to

- Enhance instruction based teaching
- Introduce Research based teaching from day one
- Trigger further insights in math and other disciplines (we need a research program to understand if this is the case)
- Validation and verification of scientific results (the PRL example), with the possibility to emphasize ethical aspects as well. Version control is central.

### Research based teaching

### How do we define it?

One possible definition: It is coupled to a direct participation in actual research and builds upon established knowledge and insights about scientific methods.

- It is the standard situation at all universities and takes normally place at the senior undergraduate/graduate level (isn't it too late?)
- It is seldom done in undergraduate courses.
- Taught by a researcher
- The student starts seeing the countour of the scientific approach leading her/him to make new interpretations, develop new insights and understandings that lead to further research.

### Research based education

### What should the education contain?

The standard situation we meet at an almost daily basis:

- Theory+experiment+simulation is almost the norm in research and industry
- To be able to model complex systems with no simple answers on closed form. Solve real problems.
- Emphasis on insight and understanding of fundamental principles and laws in the Sciences.
- Be able to visualize, present, discuss, interpret and come with a critical analysis of the results, and develop a sound ethical attitude to own and other's work.

Our education should reflect this.

### Research based education

### Normal workflow in Science and Engineering

- A problem is properly described using a precise (normal) language.
- It is translated to a mathematical problem using known laws and principles.
- It is solved, normally via numerical similations.
- The solution is visualized and analyzed.
- The solution to the problem is formulated.

People who master these skills bring an important compentence to society.

### Computers and science teaching

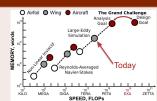
### Education

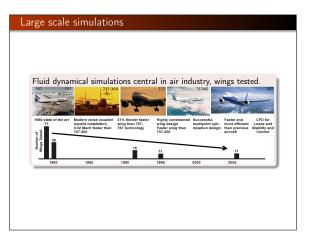
- During the last 25 years there has been considerable focus on technology at all levels in the educational ladder.
- Calculators, text processing, email, digital learning environments etc.
- Much focus on means and technologies, but what about the content, or more importantly, insight into physical systems?

The basic topics (math, chemistry, physics, biology etc) are taught more or less in the same fashion as before, unchanged over several decades!

### Large scale simulations

Fluid dynamical simulations central in air industry. Typical university courses which are taught address the physics of the lower left corner.





### Preliminary summary

### Computations should enter basic science education

- Computation is a fundamental tool to gain new insights and should be included in our elementary teaching.
- Requires development of algorithmic thinking.
- Basic numerical methods should be part of the compulsory
  curriculum
- The students should also learn to develop new numerical methods and adapt to new software tools.
- Requires more training than simple programming in a mathematics course.

### Can we catch many birds with one stone?

- How can we include and integrate an algorithmic (computational) perspective in our basic education?
- Can this enhance the students' understanding of mathematics and science?
- Can it strengthen research based teaching?

### What is needed?

### Programming

A compulsory programming course with a strong mathematical flavour. Should give a solid foundation in programming as a problem solving technique in mathematics. Programming is understanding! The line of thought when solving mathematical problems numerically enhances algorithmic thinking, and thereby the students' understanding of the scientific process.

### Mathematics and numerics

Mathematics is at least as important as before, but should be supplemented with development, analysis, implementation, verification and validation of numerical methods. Science ethics and better understanding of the pedagogical process, almost for free!

### Sciences

Training in modelling and problem solving with numerical methods and visualisation, as well as traditional methods in Science courses, Physics, Chemistry, Biology, Geology, Engineering...

### Implementation

### Crucial ingredients

- Support from governing bodies (now priority 1 of the College of Natural Science at UOslo)
- Cooperation across departmental boundaries
- Willingness by individuals to give priority to teaching reform

Consensus driven approach.

### Implementation in Oslo: The CSE project

### What we do

- Coordinated use of computational exercises and numerical tools in most undergraduate courses.
- Help update the scientific staff's competence on computational aspects and give support (scientific, pedagogical and financial) to those who wish to revise their courses in a computational direction.
- Teachers get good summer students to aid in introducing computational exercises
- Develop courses and exercise modules with a computational perspective, both for students and teachers.
- Basic idea: mixture of mathematics, computation, informatics and topics from the physical sciences.

Interesting outcome: higher focus on teaching and pedagogical issues!!

### Example of bachelor program, astrophysics

Rh semester	AST3210	Choice	Choice
	Radiation I		
5th semester	FY82160	AST2120	AST2210
	Thermodynamics and	The stars	Observational astronom
	statistical physics		
4th semester	FYS2140	Choice	EXPHIL03
3rd semester	Quantum physics		Examen philosophicum
	FYS1120	AST1100	MAT1120
	Electromagnetism	Introduction to astrophysics /	Linear algebra
		GEF1100	
		The climate system	
2nd semester	FYS-MEK1110	MEK1100	MAT1110
	Mechanics	Vector calculus	Calculus and linear
			algebra
1st semester	MAT1100	MAT-INF1100	INF1100
	Calculus	Modelling and	Introduction to
		computations	programming with
			scientific applications
	10 credits	10 credits	10 credits

### Example: Computations from day one

### Differentiation

Three courses the first semester: MAT1100, MAT-INF1100 og INF1100

Definition of the derivative in MAT1100 (Calculus and analysis)

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}.$$

 Algorithms to compute the derivative in MAT-INF1100 (Mathematical modelling with computing)

$$f'(x) = \frac{f(x+h) - f(x-h)}{2h} + O(h^2).$$

Implementation in Python in INF1100

```
def differentiate(f, x, h=1E-5):
    return (f(x+h) - f(x-h))/(2*h)
```

### Example: Computations from day one

### Differentiation and comparison with symbolic expressions

Combined with the possibility of symbolic calculations with *Sympy*, Python offers an environment where students and teachers alike can test many different aspects of mathematics and numerical mathematics, in addition to being able to verify and validate their codes. The following simple example shows how to extend the simple function for computing the numerical derivative with the possibility of obtaining the closed form or analytical expression

```
def differentiate(f, x, h=1E-5, symbolic=False):
   if symbolic:
    in import sympy
        return sympy.lambdify([x], sympy.diff(f, x))
   else:
        return (f(x+h) - f(x-h))/(2*h)
```

### Other Examples

### Integration by Trapezoidal Rule

- Definition of integration in MAT1100 (Calculus and analysis).
- $\bullet$  The algorithm for computing the integral vha the Trapezoidal rule for an interval  $x \in [a,b]$

$$\int_{a}^{b} (f(x)dx \approx \frac{1}{2} [f(a) + 2f(a+h) + \dots + 2f(b-h) + f(b)]$$

- Taught in MAT-INF1100 (Mathematical modelling)
- The algorithm is then implemented in INF1100 (programming course).

### Typical implementation in INF1100

```
Integration by Trapezoidal Rule

from math import exp, log, sin
def Trapez(a,b,f,n):

h = (b-a)/float(n)
0 = 0
x = a
for i in range(1,n,i):
x = x*h
s = s + f(x)
s = 0.5*(f(a)+f(b)) +s
return h*s

def f1(x):
return exp(-x*x)*log(1*x*sin(x))

a = 1; b = 3; n = 1000
result = Trapez(a,b,f1,n)
rint result
```

### Typical implementation in INF1100

### Symbolic calculations and numerical calculations in one code!

Python offers an extremely versatile programming environment, allowing for the inclusion of analytical studies in a numerical program. Here we show another example where *SymPy* is used to evaluate the integral and compute the absolute error with respect to the numerically evaluated one of the integral

```
4 \( \int_0^1 \) \( dx/(1+x^2) = \pi : \)
from math import *
from sympy import *
def Trapez(a,b,f,n):
  \( h = (b-a)/float(n) \)
  \( s = 0 \)
  \( x = a \)
  \( for i \) in range(1,n,i):
  \( x = x + h \)
  \( s = 0.5 * (f(a) + f(b)) \) +s
  \( return h * s \)

# function to compute pi
def function(x):
  \( return 4.0/(1 + x * x) \)
```

a = 0.0: b = 1.0: n = 100

### Integrating numerical mathematics with calculus

The last example shows the potential of combining numerical algorithms with symbolic calculations, allowing thereby students and teachers to

- Validate and verify their algorithms.
- Including concepts like unit testing, one has the possibility to test and validate several or all parts of the code.
- Validation and verification are then included naturally and one can develop a better attitude to what is meant with an ethically sound scientific approach.
- The above example allows the student to also test the mathematical error of the algorithm for the trapezoidal rule by changing the number of integration points. The students get trained from day one to think error analysis.
- With an ipython notebook the students can keep exploring similar examples and turn them in as their own notebooks.

### Error analysis

The following extended version of the trapezoidal rule allows the student to plot the relative error by comparing with the exact result. By increasing to 10<sup>8</sup> points one arrives at a region where numerical errors start to accumulate.

```
from math import log10
import numpy as np
from sympy import Symbol, integrate
import matplotlib.pyplot as plt
# function for the trapezoidal rule
def Trapez(a,b,f,n):
h = (b-a)/float(n)
s = 0
x = a
for i in range(1,n,1):
x = x*h
s = s*f(x)
s = 0.5*f((a)*f(b)) +s
return h*s
function to compute pi
def function(x):
return 4.0/(1*x*x)
# define integration limits
a = 0.0; # find result from sympy
# define x as a symbol to be used by sympy
# define x as a symbol to be used by sympy
```

### Learning outcomes three first semesters

### Knowledge of basic algorithms

- Differential equations: Euler, modified Euler and Runge-Kutta methods (first semester)
- Numerical integration: Trapezoidal and Simpson's rule, multidimensional integrals (first semester)
- Random numbers, random walks, probability distributions and Monte Carlo integration (first semester)
- Linear Algebra and eigenvalue problems: Gaussian elimination, LU-decomposition, SVD, QR, Givens rotations and eigenvalues. Gauss-Seidel. (second and third semester)
- Root finding and interpolation etc. (all three first semesters)
- Processing of sound and images (first semester).

The students have to code several of these algorithms during the first three semesters.

### Later courses

Later courses should build on this foundation as much as possible.

- In particular, the course should not be too basic! There should be progression in the use of mathematics, numerical methods and programming, as well as science.
- Computational platform: Python, fully object-oriented and allows for seamless integration of c++ and Fortran codes, as well as Matlab-like programming environment. Makes it easy to parallelize codes as well.

### Coordination

 Teachers in other courses need therefore not use much time on numerical tools. Naturally included in other courses.

### FYS-MEK1100 (Mechanics), Second Semester

### Realistic Pendulum

Classical pendulum with damping and external force

$$ml rac{d^2 heta}{dt^2} + 
u rac{d heta}{dt} + mgsin( heta) = Asin(\omega t).$$

Easy to solve numerically without classical simplification, and then visualize the solution. Done in first semester! Same equation for an RLC circuit

$$L\frac{d^2Q}{dt^2} + \frac{Q}{C} + R\frac{dQ}{dt} = V(t).$$

### FYS1120 Electromagnetism, Third Semester

### RLC circuit

Same equation as the pendulum for an RLC circuit

$$L\frac{d^2Q}{dt^2} + \frac{Q}{C} + R\frac{dQ}{dt} = V(t).$$

From the numerics, the students found the optimal parameters for studying experimentally chaos in an RLC circuit. Then they did the experiment.

### More Examples from Physics Courses, 2-5 semester

### Second-fourth semester

- Air resistance in two and three dimensions with quadratic velocity dependence.
- Launching a probe into a tornado
- Rocket launching with realistic parameters, gravity assist
- How to kick a football and model its trajectory.
- Planet motion and position of planets
- Magnetic fields with various geometries based on Biot-Savart's law
- Harmonic oscillations and various forms of electromagnetic
   waves
- Combined effect of different potentials such as the electrostatic potential and the gravitational potential.
- Simple studies of atoms and molecules, and much more

### First computational physics course

### Late: Fifth semester, FYS3150 Computational Physics

The first computational physics course can then be used to summarize many of the gained insights about algorithms, mathematical models, physics etc. And direct the students to more advanced algorithms and applications like

- Monte carlo methods
- Parallelization
- Solving quantum mechanical problems by Variational Monte Carlo or other quantum mechanical methods
- Study phase transitions with for example the Ising and Potts model.
- Molecular dynamics simulations etc etc

### Challenges..

### .. and objections

Standard objection: computations take away the attention from other central topics in 'my course'.

CSE incorporates computations from day one, and courses higher up do not need to spend time on computational topics (technicalities), but can focus on the interesting science applications.

• To help teachers: Developed pedagogical modules which can aid university teachers.

### Challenges and future plans

- The project depends crucially on few individuals.
- Need to get more teachers involved, not only good TAs.
- How to implement a CSE perspective in other programs like Chemistry, Molecular Biology, Biology, Engineering. New courses are being developed.
- Now a national pilot for other universities and regional colleges.

Key issue: modularization of topics and development of a 'technological platform' which glues together different modules

# Which aspects are important for a successful introduction of CSE?

- Early introduction, programming course at beginning of studies linked with math courses and science and engineering courses.
- Crucial to learn proper programming at the beginning.
- Choice of software.
- Textbooks and modularization of topics.
- Resources and expenses.
- Tailor to specific disciplines.
- Organizational matters.

### What about life science/biology? Overarching questions

### Which skills are needed by candidates in biology?

There is new demand for more

- quantitative methods & reasoning
- understanding data and phenomena via models
- creating in silico virtual labs

### Challenge

How to integrate such computing-based activities in the undergraduate programs when the students are *not* interested in mathematics, physics, and programming?

### How to teach computing in biology?

Do we need to still follow the tradition and teach mathematics, physics, computations, chemistry, etc. in separate discipline-specific courses?

- Uninteresting to first study tools when you want to study biology
- Little understanding of what the tools are good for
- Minor utilization of tools later in biology

### It's time for new thinking:

- Just-in-time teaching: teach tools when needed
- Teach tools in the context of biology
- Emphasize development of intuition and understanding
- Base learning of the students' own explorations in biology projects
- Integrate lab work with computing tools

### The pedagogical framework

### Aim: Develop intuition about the scientific method

- Method: case-based learning
- Coherent problem solving *in biology* by integrating mathematics, programming, physics/chemistry, ...
- Starting point: data from lab or field experiments
- Visualize data
- Derive computational models directly from mathematical/intuitive reasoning
- Program model(s), fit parameters, compare with data
- Develop intuition and understanding based on
  - the principles behind the model
  - exploration of the model ("what if")
  - · prediction of new experiments

### Example 1: ecoli lab experiment

Observations of no of bacteria vs time in seconds, stored in Excel and written to a CVS file:

0,100 600,140 1200,250 1800,360 2400,480 3000,820 3600,1300 4200,1700 4800,2900

6000,7000

### Visualize data

- Meet a text editor and a terminal window
- Very basic Unix

### First program:

t = [0, 600, 1200, 1800, 2400, 3000, 3600, 4200, 4800, 5400, 6000]
N = [100, 140, 250, 360, 480, 820, 1300, 1700, 2900, 3900, 7000]
import matplotlib.pyplot as plt
plt.plot(t, N, 'ro')
plt.xlabel('t [s]')
plt.ylabe('N')
plt.show()

### Concepts must be introduced implicitly in a structured way

### Warning

- Always identify new concepts
- Train new concepts in simplified ("trivial") problems

### Concepts in the previous example:

- Lists or arrays of numbers
- Plotting commands
- Curve = function of time

### Notice

The concept of a continuous function N(t) is not necessary, just straight lines between discrete points on a curve.

# import numpy as np data = np.loaduxt('ecoli.csv', delimiter=',') print data # look at the format t = data[:,1] import matplotlib.pyplot as plt plt.plot(t, N, 'rev)' plt.xlabel('t [s]') plt.ylabel('N') plt.show() Typical pattern: The population grows faster and faster. Why? Is there an underlying (general) mechanism?

### Lab journal

Use IPython notebook as lab journal.

## How can we reason about the process?

- Cells divide after T seconds on average (one generation)
- ② 2N celles divide into twice as many new cells  $\Delta N$  in a time interval  $\Delta t$  as N cells would:  $\Delta N \propto N$
- **②** N cells result in twice as many new individuals  $\Delta N$  in time  $2\Delta t$  as in time  $\Delta t$ :  $\Delta N \propto \Delta t$
- Same proportionality wrt death (repeat reasoning)
- **9** Proposed model:  $\Delta N = b\Delta tN d\Delta tN$  for some unknown constants b (births) and d (deaths)
- **1** Describe evolution in discrete time:  $t_n = n\Delta t$
- **Q** Program-friendly notation: N at  $t_n$  is  $N^n$
- Math model:  $N^{n+1} = N^n + r\Delta t N$  (with r = b d)

### The first simple program

Let us solve the difference equation in as simple way as possible, just to train some programming:  $r=1.5,~N^0=1,~\Delta t=0.5$  import numpy as np  $\begin{array}{l} t=np.1 \\ \text{inspace}(0,~10,~21) & \text{\# 20 intervals in [0,~10]} \\ \text{dt}=t[1]-t[0] \\ \text{N}=np.zeros(t.size) \\ \\ \text{N[0]}=1 \\ \text{r}=0.5 \\ \end{array}$  for n in range(0, N.size-1, 1):  $\begin{array}{l} N[n+1]=N[n]+r\text{-dt-N[n]} \\ \text{print-N[d]}=N[n]+r\text{-dt-N[n]} \\ \text{print-N[d]}=N[n]+1;~N[n+1]) \end{array}$ 

```
The output

N[1]=1.2
N[2]=1.6
N[3]=2.0
N[4]=2.1
N[5]=3.1
N[6]=3.1
N[6]=3.8
N[7]=4.8
N[9]=7.5
N[10]=9.3
N[11]=11.6
N[12]=14.6
N[13]=18.2
N[14]=22.7
N[15]=28.4
N[16]=35.5
N[17]=44.4
N[18]=55.5
N[19]=69.4
N[20]=86.7
```

### Parameter estimation

- We do not know r
- How can we estimate r from data?

We can use the difference equation with the experimental data

$$N^{n+1} = N^n + r\Delta t N^n$$

Say  $N^{n+1}$  and  $N^n$  are known from data, solve wrt r:

$$r = \frac{N^{n+1} - N^n}{N^n \Delta t}$$

Use experimental data in the fraction, say  $t_1=600$ ,  $t_2=1200$ ,  $N^1=140$ ,  $N^2=250$ : r=0.0013.

### More sophisticated methods

Can do a nonlinear least squares parameter fit, but that is too advanced at this stage.

# import numpy as np # Estimate r data = np.loadtxt('ecoli.csv', delimiter=',') t\_e = data[:,0] N\_e = data[:,0] N\_e = data[:,1] i = 2 # Data point (i,i+1) used to estimate r r = (N\_e[i+1] - N\_e[i])/(N\_e[i]\*(t\_e[i+1] - t\_e[i])) print 'Estimated r=',5:' % r # Can experiment with r values and see if the model can # match the data better T = 1200 # cell can divide after T sec t\_max = 5\*T # 5 generations in experiment t = np.linspace(0, t\_max, 1000) dt = t[1] - t[0] N = np.zeros(t.size) N[0] = 100 for n in range(0, len(t)-1, 1): N[n+1] = N[n] + r\*dt\*N[n] import matplotlib.pyplot as plt plt.plot(t, N, 'r-', t\_e, N\_e, 'bo') plt.xlabel('time [s]'); plt.ylabel('N') plt.legend(['model', 'experiment'], loc='upper left') plt.legend(['model', 'experiment'], loc='upper left') plt.legend(['model', 'experiment'], loc='upper left') plt.show()

### Discuss the nature of such a model

- Write up all the biological factors that influence the population size of bacteria
- Understand that all such effects are merged into one parameter r
- Understand that the reasoning must be the same whether we have bacteria, animals or humans - this is a generic model! (even the interest rate in a bank follows the same model)

### Discuss the limitations of such a model

- How many bacteria in the lab after one month?
- Growth is restricted by environmental resources!
- Fix the model (logistic growth)
- Is the logistic model appropriate for a lab experiment?
- Find data to support the logistic model (it's a *very* simple model)

### The pedagogical template (to be iterated!)

- Start with a real biological problem
- Be careful with too many new concepts
- Workflow:
  - data
  - visualization
  - patterns
  - modeling (discrete)
  - programming
  - testing
  - parameter estimation (difficult)
  - validation
  - prediction
- Make many small exercises that train the new concepts
- Repeat the case in a way that makes a complete understanding

# Do we get better students? Molecular dynamics visualization by two MSc students

### Summary

- Make our research visible in early undergraduate courses, enhance research based teaching
- Possibility to focus more on understanding and increased insight.
- Impetus for broad cooperation in teaching.
- Strengthening of instruction based teaching (expensive and time-consuming).
- Give our candidates a broader and more up-to-date education with a problem-based orientation, often requested by potential employers.
- And perhaps the most important issue: does this enhance the student's insight in the Sciences?