

بخش اول

تمرین ۴ بخش ۸.۱

a) clauses are a , b and c .

b)

- $$P_a = ((True \vee b) \iff c) \oplus ((False \vee b) \iff c)$$

$$= (True \iff c) \oplus (b \iff c)$$

$$= c \oplus (b \iff c)$$

$$= (c \wedge \neg(b \iff c)) \vee (\neg c \wedge (b \iff c))$$

$$= (c \wedge \neg b \wedge c) \vee (c \wedge b \wedge \neg c) \vee (\neg c \wedge b \wedge c) \vee (\neg c \wedge \neg b \wedge \neg c)$$

$$= (c \wedge \neg b) \vee (\neg c \wedge \neg b)$$

$$= \neg b \wedge (c \vee \neg c)$$

$$= \neg b \wedge True$$

$$= \neg b$$
- $$P_b = \neg a \text{ (similar to } P_a)$$
- $$P_c = ((a \vee b) \iff True) \oplus ((a \vee b) \iff False)$$

$$= (a \vee b) \oplus \neg(a \vee b)$$

$$= True$$

c)

	a	b	c	$(a \vee b) \iff c$	P_a	P_b	P_c
۱	T	T	T	T	F	F	T
۲	T	T	F	F	F	F	T
۳	T	F	T	T	T	F	T
۴	T	F	F	F	T	F	T
۵	F	T	T	T	F	T	T
۶	F	T	F	F	F	T	T
۷	F	F	T	F	T	T	T
۸	F	F	F	T	T	T	T

d)

- GACC pairs for a: (3, 7), (3, 8), (4, 7), (4, 8)
- GACC pairs for b: (5, 7), (5, 8), (6, 7), (6, 8)
- GACC pairs for c: (1, 2), (1, 4), (1, 6), (1, 8), (3, 2), (3, 4), (3, 6), (3, 8),
(5, 2), (5, 4), (5, 6), (5, 8), (8, 2), (7, 4), (7, 6), (7, 8)

e)

- CACC pairs for a: (3, 7), (4, 8)
- CACC pairs for b: (5, 7), (6, 8)
- CACC pairs for c: (1, 2), (1, 4), (1, 6), (3, 2), (3, 4), (3, 6), (5, 2), (5, 4), (5, 6), (7, 8)

f)

- RACC pairs for a: (3, 7), (4, 8)
- RACC pairs for b: (5, 7), (6, 8)
- RACC pairs for c: (1, 2), (3, 4), (5, 6), (7, 8)

بخش دوم

```
a = i < size
b = j < i
c = intervals[i].begin < intervals[j].end
d = intervals[i].end > intervals[j].begin
e = rows[j] >= rows[i]

P = a ∧ b ∧ c ∧ d ∧ e
```

پرسش اول

طبق جدول زیر برای CACC pair ها داریم:

$a = (1, 17), b = (1, 9), c = (1, 5), d = (1, 3), e = (1, 2)$

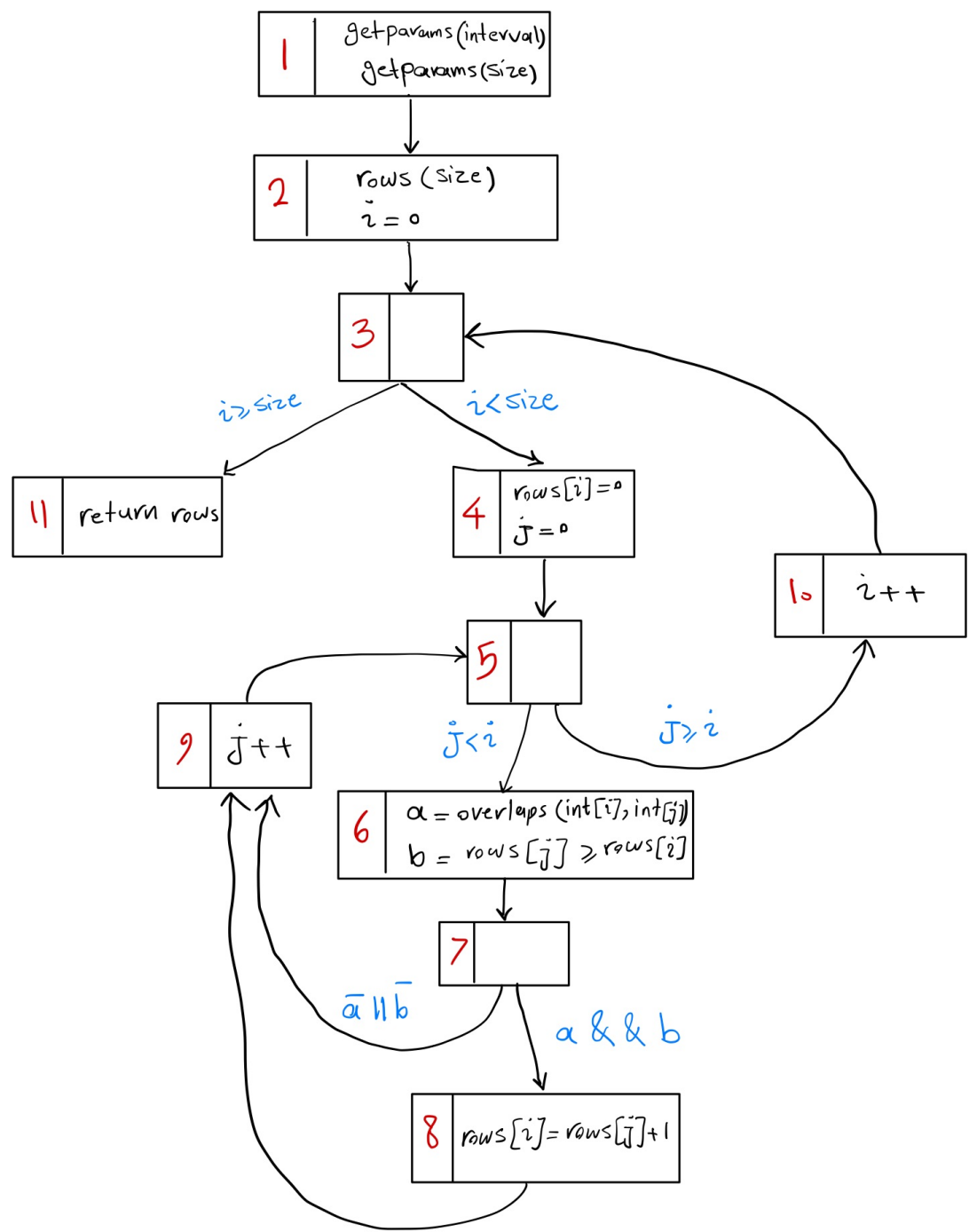
ولی سطر های 9 و 17 infeasible هستند و بنابراین تست $size = 4$ $intervals = \{\{6, 7\}, \{10, 12\}, \{7, 9\}, \{6, 12\}\}$ همه ی سطرهای 1, 2, 3, 5 را پوشش میدهد.

	a	b	c	d	e	$(a \wedge b \wedge c \wedge d \wedge e)$	P_a	P_b	P_c	P_d	P_e
۱	T	T	T	T	T	T	T	T	T	T	T
۲	T	T	T	T	F						T
۳	T	T	T	F	T					T	
۴	T	T	T	F	F						
۵	T	T	F	T	T				T		
۶	T	T	F	T	F						
۷	T	T	F	F	T						
۸	T	T	F	F	F						
۹	T	F	T	T	T			T			
۱۰	T	F	T	T	F						
۱۱	T	F	T	F	T						
۱۲	T	F	T	F	F						
۱۳	T	F	F	T	T						
۱۴	T	F	F	T	F						
۱۵	T	F	F	F	T						
۱۶	T	F	F	F	F						
۱۷	F	T	T	T	T		T				
۱۸	F	T	T	T	F						
۱۹	F	T	T	F	T						
۲۰	F	T	T	F	F						
۲۱	F	T	F	T	T						
۲۲	F	T	F	T	F						
۲۳	F	T	F	F	T						
۲۴	F	T	F	F	F						
۲۵	F	F	T	T	T						
۲۶	F	F	T	T	F						
۲۷	F	F	T	F	T						
۲۸	F	F	T	F	F						
۲۹	F	F	F	T	T						
۳۰	F	F	F	T	F						
۳۱	F	F	F	F	T						
۳۲	F	F	F	F	F						

پرسش دوم

با توجه به گراف زیر، مسیری شده به این صورت است:

[1, 2, 3, 4, 5, 10, 3, 4, 5, 6, 7, 9, 5, 10, 3, 4, 5, 6, 7, 9, 5, 6, 7, 9, 5, 10, 3, 4, 5, 6, 7, 8, 9, 5, 6, 7, 9, 5, 6, 7, 9, 5, 10, 3, 11]



مسیرهایی که قرمز شده اند infeasible هستند. مسیرهای سبزرنگ پوشش داده میشوند و سایر مسیرها پوشش داده نمیشوند.

[1, 2, 3, 4, 5, 10, 3, 4, 5, 6, 7, 9, 5, 10, 3, 4, 5, 6, 7, 9, 5, 6, 7, 9, 5, 10, 3, 4, 5, 6, 7, 8, 9, 5, 6, 7, 9, 5, 6, 7, 9, 5, 10, 3, 11]

Variable	DU-pair	DU-path
intervals	(1, 6)	[1, 2, 3, 4, 5, 6]
size	(1, 2)	[1, 2]
	(1, (3, 11))	[1, 2, 3, 11]
	(1, (3, 4))	[1, 2, 3, 4]
rows	(2, 6)	no def-clear path
	(2, 8)	no def-clear path
	(2, 11)	[2, 3, 11]
	(4, 6)	[4, 5, 6]
	(4, 8)	[4, 5, 6, 7, 8]
	(4, 11)	[4, 5, 10, 3, 11]
	(8, 6)	[8, 9, 5, 6]
	(8, 8)	[8, 9, 5, 6, 7, 8]
	(8, 11)	[8, 9, 5, 10, 3, 11]
i	(2, 4)	[2, 3, 4]
	(2, 6)	[2, 3, 4, 5, 6]
	(2, 8)	[2, 3, 4, 5, 6, 7, 8]
	(2, 10)	[2, 3, 4, 5, 10]
	(2, (3, 11))	[2, 3, 11]
	(2, (3, 4))	[2, 3, 4]
	(2, (5, 10))	[2, 3, 4, 5, 10]
	(2, (5, 6))	[2, 3, 4, 5, 6]
	(10, 4)	[10, 3, 4]
	(10, 6)	[10, 3, 4, 5, 6]
	(10, 8)	[10, 3, 4, 5, 6, 7, 8]
	(10, 10)	[10, 3, 4, 5, 10]
	(10, (3, 11))	[10, 3, 11]
	(10, (3, 4))	[10, 3, 4]
	(10, (5, 10))	[10, 3, 4, 5, 10]
	(10, (5, 6))	[10, 3, 4, 5, 6]

Variable	DU-pair	DU-path
j	(4, 6)	[4, 5, 6]
	(4, 8)	[4, 5, 6, 7, 8]
	(4, 9)	[4, 5, 6, 7, 8, 9]
	(4, (5, 10))	[4, 5, 10]
	(4, (5, 6))	[4, 5, 6]
	(9, 6)	[9, 5, 6]
	(9, 8)	[9, 5, 6, 7, 8]
	(9, 9)	[9, 5, 6, 7, 8, 9]
	(9, (5, 10))	[9, 5, 10]
	(9, (5, 6))	[9, 5, 6]
a	(6, (7, 9))	[6, 7, 9]
	(6, (7, 8))	[6, 7, 8]
b	(6, (7, 9))	[6, 7, 9]
	(6, (7, 8))	[6, 7, 8]

(۱)

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     // for (int i = 0; i < size; i++) {
12     for (int i = 0; i < size - 1; i++) {
13         rows[i] = 0;
14         for (int j = 0; j < i; j++) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }

```

(۲)

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     // for (int i = 0; i < size; i++) {
12     for (int i = 0; i < size + 1; i++) {
13         rows[i] = 0;
14         for (int j = 0; j < i; j++) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }

```

(۳)

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     // for (int i = 0; i < size; i++) {
12     for (int i = 0; i < size; i += 2) {
13         rows[i] = 0;
14         for (int j = 0; j < i; j++) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }

```

(۴)

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         // rows[i] = 0;
13         rows[i] = rows[i-1];
14         for (int j = 0; j < i; j++) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }

```

(5)

```
4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         rows[i] = 0;
13         // for (int j = 0; j < i; j++) {
14         for (int j = 0; j != i; j++) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }
```

(6)

```
8 struct interval {
9     int begin;
10    int end;
11 };
12
13 vector<int> layout(vector<interval> intervals, int size) {
14     vector<int> rows(size);
15     for (int i = 0; i < size; i++) {
16         rows[i] = 0;
17         for (int j = 0; j < i; j++) {
18             // if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
19             if ((intervals[i].begin <= intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
20                 rows[i] = rows[j] + 1;
21             }
22         }
23     }
24 }
```

(7)

```
4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         rows[i] = 0;
13         for (int j = 0; j < i; j++) {
14             // if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
15             if ((intervals[i].begin < intervals[j].end) || (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }
```

(8)

```
4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         rows[i] = 0;
13         for (int j = 0; j < i; j++) {
14             // if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] > rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }
```

(۹)

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         rows[i] = 0;
13         for (int j = 0; j < i; j++) {
14             // if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
15             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] < rows[i]) {
16                 rows[i] = rows[j] + 1;
17             }
18         }
19     }
20 }

```

(۱۰

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         rows[i] = 0;
13         for (int j = 0; j < i; j++) {
14             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
15                 // rows[i] = rows[j] + 1;
16                 rows[i] = rows[j] - 1;
17             }
18         }
19     }
20 }

```

(۱۱

```

4 struct interval {
5     int begin;
6     int end;
7 };
8
9 vector<int> layout(vector<interval> intervals, int size) {
10     vector<int> rows(size);
11     for (int i = 0; i < size; i++) {
12         rows[i] = 0;
13         for (int j = 0; j < i; j++) {
14             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
15                 // rows[i] = rows[j] + 1;
16                 rows[i] = rows[i] + 1;
17             }
18         }
19     }
20 }

```

(۱۲

```

8 struct interval {
9     int begin;
10    int end;
11 };
12
13 vector<int> layout(vector<interval> intervals, int size) {
14     vector<int> rows(size);
15     for (int i = 0; i < size; i++) {
16         rows[i] = 0;
17         for (int j = 0; j < i; j++) {
18             if ((intervals[i].begin < intervals[j].end) && (intervals[i].end > intervals[j].begin) && rows[j] >= rows[i]) {
19                 rows[i] = rows[j] + 1;
20                 // immediate runtime failure if reached.
21                 bomb();
22             }
23         }
24     }

```

پرسش پنجم

بله mutant شماره‌ی پنجم redundant است.

- $intervals = \{\}, size = 0 \rightarrow 2,$
- $intervals = \{\{8, 9\}\}, size = 1 \rightarrow 1, 4$
- $intervals = \{\{8, 9\}, \{10, 11\}\}, size = 2 \rightarrow 3, 7,$
- $intervals = \{\{8, 10\}, \{9, 11\}, \{8, 11\}\}, size = 3 \rightarrow 8, 9, 10, 11, 12$

بله هر چه تعداد mutant هایی که زنده میمانند بیشتر باشند، نشان دهنده‌ی ضعف بیشتر مجموعه تست کیس ها می باشد. همانطور که میدانیم mutant شماره پنج redundant است و mutant شماره شش توسط هیچ یک از تست های بالا کشته نمیشود. و تست زیر آن را میکشد:

$$intervals = \{\{8, 9\}, \{9, 10\}\}, size = 2$$