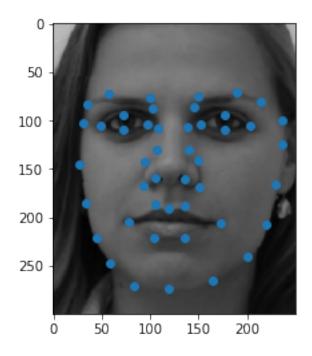
#### ShapeModel

December 5, 2021

```
[12]: import numpy as np
      import glob
      import menpo.io as mio
      import matplotlib.pyplot as plt
      import cv2
[13]: landmarks = sorted(glob.glob("frontalshapes_manuallyannotated_46points/*"))
      faces = sorted(glob.glob("frontalimages_spatiallynormalized*/*"))
      # for face, file in zip(faces, files):
            print(face , file)
      print(type(faces))
      # faces = 200
     <class 'list'>
[14]: len(faces)
[14]: 400
[15]: | test = mio.import_landmark_file(landmarks[0])
      print(landmarks[0])
      img = cv2.imread(faces[0])
      print(test['PTS'].points)
      plt.imshow(img)
      plt.scatter(test['PTS'].points[:,1], test['PTS'].points[:,0])
      # menpo reads the coordinates as ZYX
      # plt.qca().invert_yaxis()
      plt.show()
     frontalshapes_manuallyannotated_46points/100a.pts
     [[159.686 105.447]
      [160.683 135.598]
      [204.476
               77.5498]
      [186.722 105.089]
      [190.508 119.702]
      [187.499 136.291]
```

```
[205.663 172.537]
[220.91
          135.26 ]
[221.072
         104.152 ]
[104.643
           48.8948]
[ 94.3955
         72.6546]
[103.738
           97.1924]
[109.473
           71.9728]
[104.342 152.687]
[ 94.2905 177.701 ]
[105.282 203.153]
[108.826
         177.208 ]
[102.835
           30.3199]
[145.453
           27.0488]
[185.731
           33.5807]
[221.349
           45.09 ]
[247.785
           58.8706]
[270.536
           82.8855]
[274.151
         118.578 ]
[264.663
         164.211 ]
[240.265
         200.355]
[206.831
         219.783 ]
[165.717
         229.271 ]
[124.151 236.5
[ 99.472 236.057 ]
[83.4876 34.3393]
[71.5991 56.7249]
[ 75.731
          99.898]
[86.797 102.897]
[ 86.6024 145.771 ]
[ 74.8597 148.976 ]
[71.1592 189.967]
[ 80.3253 214.813 ]
[107.667 108.521]
[130.173 106.194]
[142.08
           94.5205]
[167.399
          93.2719]
[168.258 150.533]
         150.085 ]
[141.116
[130.609
         139.477 ]
[107.021 138.577]]
```



# 1 Scatter plot of the landmark distribution together with the mean shape

```
[61]: landmarkpoints = []
for points in landmarks:
    landmarkpoints.append(mio.import_landmark_file(points)['PTS'].points)

landmarkpoints = np.array(landmarkpoints)

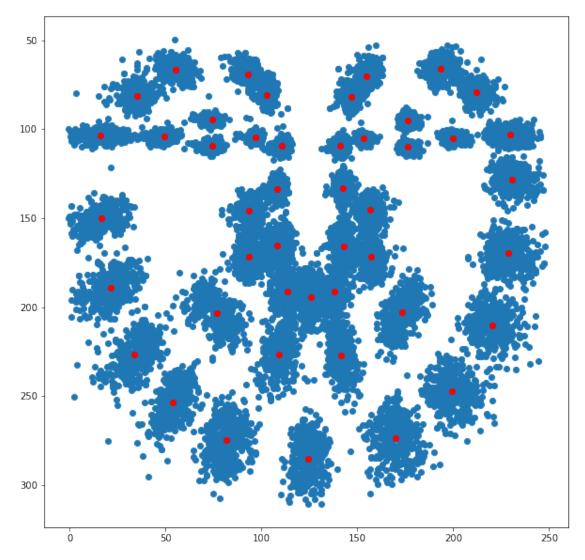
x = landmarkpoints[:,:,1].reshape(-1)
y = landmarkpoints[:,:,0].reshape(-1)

mean = np.zeros([92])

for i in range(46):
    mean[i] = np.mean(landmarkpoints[:,i,1])
    mean[i+46] = np.mean(landmarkpoints[:,i,0])

# print(meany.shape)
# x.shape
# print(landmarkpoints[0])
# print(landmarkpoints[:,:,0])
plt.figure(figsize = (10,10))
```

```
plt.scatter(x, y)
plt.scatter(mean[:46], mean[46:], color = 'r')
plt.gca().invert_yaxis()
plt.show()
```



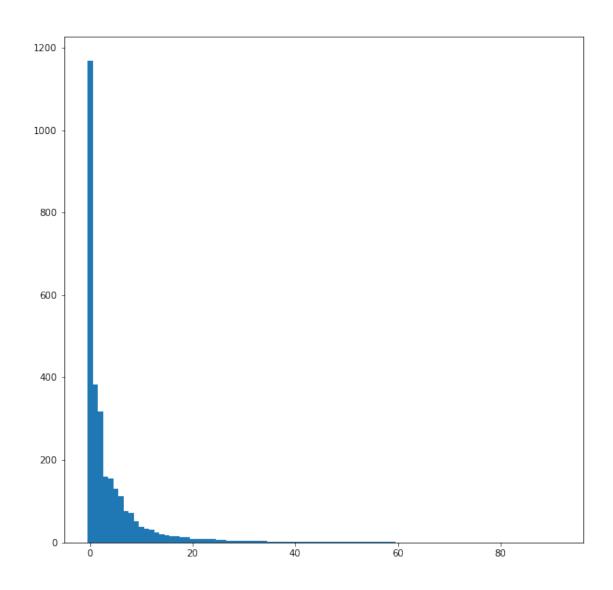
## 2 Histogram of eigenvalues as obtained from the SVD of the data covariance matrix

```
[62]: print(landmarkpoints.shape)
X = landmarkpoints.reshape(400,-1)
print(X.shape)

(400, 46, 2)
```

```
[63]: # print(X.shape)
      CovarMatrix = np.cov(X.T)
      CovarMatrix.shape
[63]: (92, 92)
[64]: U,S,VT = np.linalg.svd(CovarMatrix)
      eigval, eigenvec = np.linalg.eig(CovarMatrix)
      # eigenval = np.vstack([np.arange(0,46,1), eigval])
      # eigval
      print(eigval.shape)
      print(eigenvec.shape)
     (92,)
     (92, 92)
[65]: print(S.shape)
      xlabel = np.arange(0,92, 1)
      print("Using eig function:\n", eigval[:10])
      print("\nUsing SVD function:\n",S.T[:10])
     (92,)
     Using eig function:
      [1167.9764863
                      382.55719475 318.43578404 160.3621351
                                                                 154.87818493
       129.79082387 111.62111697
                                    77.10411958
                                                  71.91281368
                                                                 51.92322807]
     Using SVD function:
                      382.55719475 318.43578404 160.3621351
                                                                 154.87818493
      [1167.9764863
       129.79082387 111.62111697
                                    77.10411958
                                                  71.91281368
                                                                 51.92322807]
[66]: plt.figure(figsize=(10,10))
      plt.bar(xlabel,S,width=1)
      plt.show()
```

(400, 92)



#### 3 Synthetic face shapes by varying the main modes of variation

```
[113]: var = eigenvec[:,1]*25+ mean
  var2 = eigenvec[:,5]*25 + mean
  var3 = eigenvec[:,20]*25 + mean

print(test.shape)
  fig, axs = plt.subplots(1, 3, figsize=(15,5))

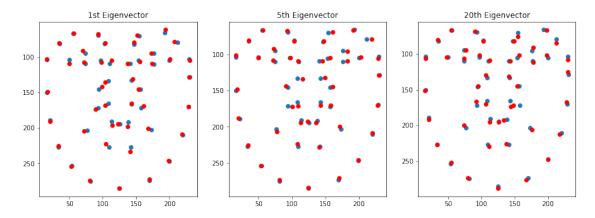
axs[0].set_title('1st Eigenvector')
  axs[0].scatter(mean[:46], mean[46:])
  axs[0].scatter(var[:46], var[46:], color='r')
  axs[0].invert_yaxis()
```

```
axs[1].set_title('5th Eigenvector')
axs[1].scatter(mean[:46], mean[46:])
axs[1].scatter(var2[:46], var2[46:], color='r')
axs[1].invert_yaxis()

axs[2].set_title('20th Eigenvector')
axs[2].scatter(mean[:46], mean[46:])
axs[2].scatter(var3[:46], var3[46:], color='r')
axs[2].invert_yaxis()

# plt.scatter(test2[:46], test2[46:], color='g')
plt.show()
```

(92,)



### [114]: print(eigval.shape)

(92,)

# Exaggerated face shapes by varying the main modes of variation beyond the plausible range of variance

```
[115]: exag = eigenvec[:,1]*eigval[1]*2+ mean
    exag2 = eigenvec[:,5]*eigval[2]*2 + mean
    exag3 = eigenvec[:,20]*eigval[3]*2 + mean

print(test.shape)
    fig, axs = plt.subplots(1, 3, figsize=(15,5))

axs[0].set_title('1st Eigenvector')
    axs[0].scatter(mean[:46], mean[46:])
    axs[0].scatter(exag[:46], exag[46:], color='r')
```

```
axs[0].invert_yaxis()
axs[1].set_title('5th Eigenvector')
axs[1].scatter(mean[:46], mean[46:])
axs[1].scatter(exag2[:46], exag2[46:], color='r')
axs[1].invert_yaxis()

axs[2].set_title('20th Eigenvector')
axs[2].scatter(mean[:46], mean[46:])
axs[2].scatter(exag3[:46], exag3[46:], color='r')
axs[2].invert_yaxis()

# plt.scatter(test2[:46], test2[46:], color='g')
plt.show()
```

#### (92,)

