#### Chapter 8

#### Path Testing

#### Outline

- **Preliminaries**
- Program graphs
- **DD-Paths**
- Test coverage metrics
- Basis path testing
- Essential complexity (from McCabe)

## Code-Based (Structural) Testing

- Complement of/to Specification-based (Functional) Testing
- Based on Implementation
- Powerful mathematical formulation

  - program graph define-use path Program slices
- Basis for Coverage Metrics (a better answer for gaps and redundancies)
- Usually done at the unit level
- Not very helpful to identify test cases
- Extensive commercial tool support

- Paths derived from some graph construct.
- When a test case executes, it traverses a path.
- Huge number of paths implies some simplification is needed.
- Big Problem: infeasible paths.
- Big Question: what kinds of faults are associated with what kinds of paths?
- By itself, path testing can lead to a false sense of security.

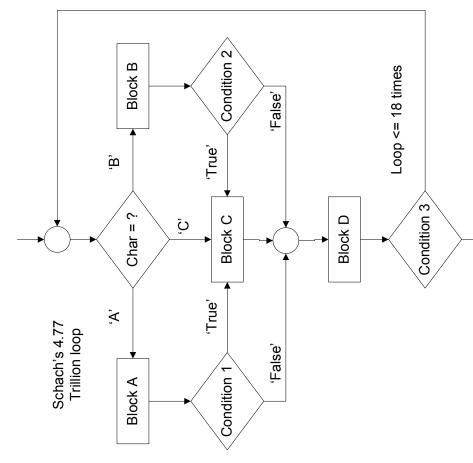
#### Common Objection to Path-Based Testing (Trillions of Paths)

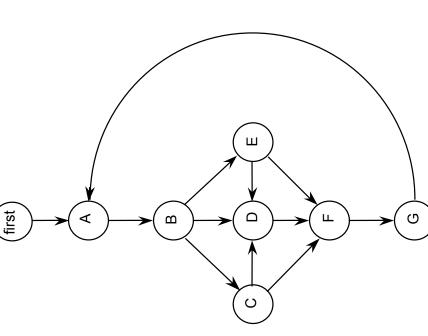
If the loop executes up to 18 times, there are 4.77 Trillion paths. Impossible, or at least, infeasible, to test them all. [Schach]

$$5^0 + 5^1 + 5^2 + ... + 5^{18} = 4,768,371,582,030$$

Stephen R. Schach, Software Engineering, , (2nd edition) Richard D. Irwin, Inc. and Aksen Associates, Inc. 1993

last





- First-A-B-C-F-G-Last
- First-A-B-C-D-F-G-Last First-A-B-D-F-G-A-B-D-F-G-Last
- First-A-B-E-F-G-Last First-A-B-E-D-F-G-Last

These test cases cover

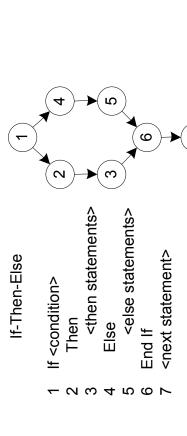
- Every node Every edge
- Normal repeat of the loop Exiting the loop

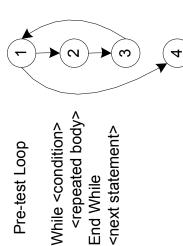
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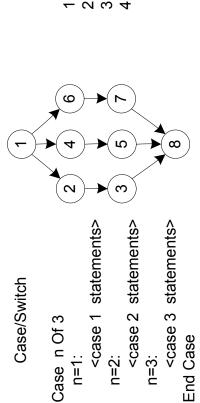
#### Program Graphs

nodes are statement fragments, and edges program graph is a directed graph in which Definition: Given a program written in an imperative programming language, its represent flow of control. (A complete statement is a "default" statement fragment.)

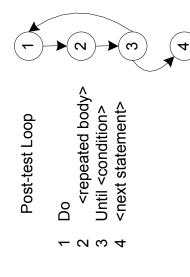
## Programming Constructs





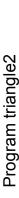


- 0 c 4 c 0 r s



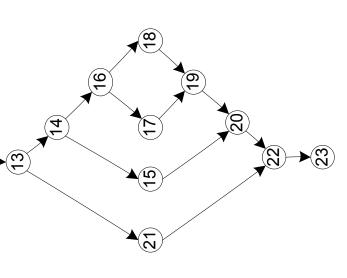
 $4 \rightarrow 6 \rightarrow (7) \rightarrow (8)$ 

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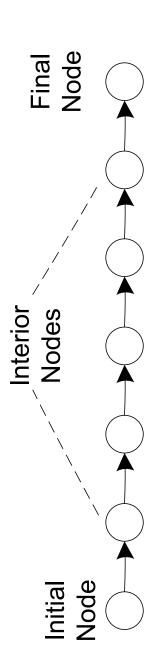
- Dim a,b,c As Integer Dim IsATriangle As Boolean
- Output("Enter 3 integers which are sides of a triangle",
  - Input(a,b,c)

- Output("Side A is ",a)
  Output("Side B is ",b)
  Output("Side C is ",c)
- 9 If (a < b + c) AND (b < a + c) AND (c < a + b)
  - Then IsATriangle = True
- Else IsATriangle = False
  - 12 EndIf
- 4 15 16 7
- 13 If IsATriangle
  14 Then If (a = b) AND (b = c)
  15 Then Output ("Equilateral")
- Else If (a≠b) AND (a≠c) AND (b≠c)
  - Then Output ("Scalene") Else Output ("Isosceles")
- EndIf
- Output("Not a Triangle") 19 20 E 21 Else 22 EndIf 23 End tria
- End triangle2



#### **DD-Paths**

- Originally defined by E. F. Miller (1977?)
- "DD" is short for "decision to decision"
- Original definition was for early (second generation) programming languages
  - Similar to a "chain" in a directed graph
- Bases of interesting test coverage metrics



#### **DD-Paths**

A DD-Path (decision-to-decision) is a chain in a program graph such that

Case 1: it consists of a single node with indeg = 0,

Case 2: it consists of a single node with outdeg = 0,

Case 3: it consists of a single node with indeg ≥ 2 or

outdeg  $\geq 2$ ,

Case 4: it consists of a single node with indeg = 1 and

outdeg = 1,

Case 5: it is a maximal chain of length ≥ 1.



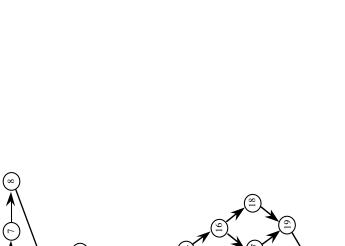
#### **DD-Path Graph**

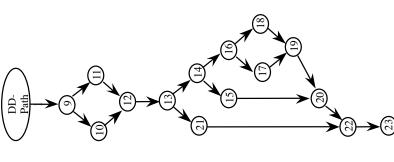
DD-Path graph is the directed graph in which nodes are Given a program written in an imperative language, its DD-Paths of its program graph, and edges represent control flow between successor DD-Paths.

- a form of condensation graph
- 2-connected components are collapsed into an individual node
- single node DD-Paths (corresponding to Cases 1 4) preserve the convention that a statement fragment is in exactly one DD-Path

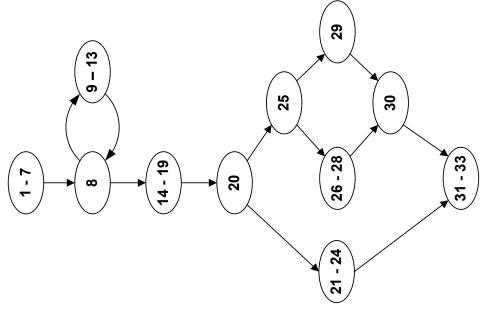
## DD-Path Graph of the Triangle Program

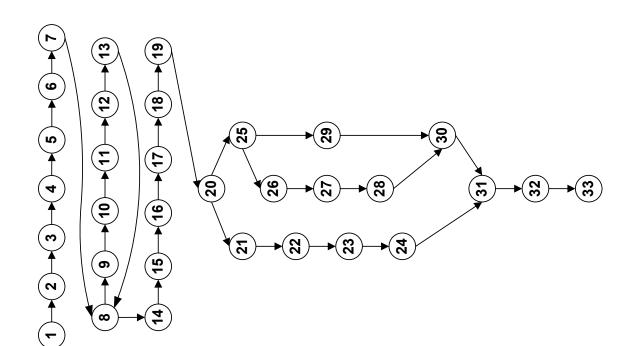
(not much compression because this example is control intensive, with little sequential code.)





#### DD-Path Graph of Commission Problem





### **Exercises and Questions**

- Compute the cyclomatic complexity of
- the commission problem program graph
- the commission problem DD-Path graph
- Are the complexities equal?
- Repeat this for the Triangle Program examples
- What conclusions can you draw?

## Code-Based Test Coverage Metrics

- Used to evaluate a given set of test cases
- Often required by
- contract
- U.S. Department of Defense
- company-specific standards
- Elegant way to deal with the gaps and redundancies that are unavoidable with specification-based test cases.
- **B**
- coverage at some defined level may be misleading
- coverage tools are needed



## Code-Based Test Coverage Metrics

(E. F. Miller, 1977 dissertation)

**Every statement** 

**Every DD-Path** 

Every predicate outcome

C<sub>1</sub> coverage + loop coverage C<sub>1</sub> coverage +every pair of dependent **DD-Paths** .. .. .. .. လို လို လို လို

Multiple condition coverage

Every program path that contains up O O ¥:

to k repetitions of a loop (usually k = 2)

"Statistically significant" fraction of

oaths

 $\mathsf{C}_{\mathsf{stat}}$ :

All possible execution paths

# Test Coverage Metrics from Program Graphs

- Every node
- Every edge
- Every chain
- **Every** path
- How do these compare with Miller's coverage metrics?

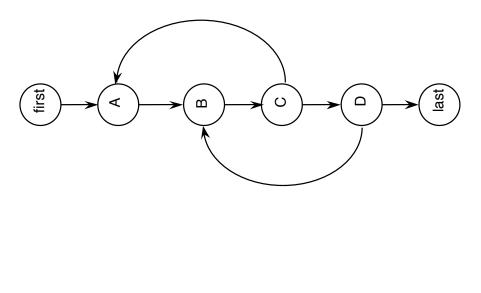


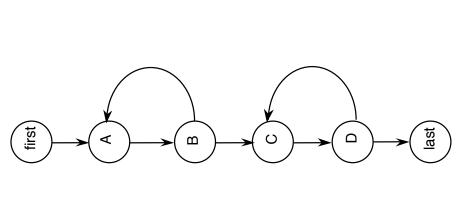
#### **Testing Loops**

traversals: the normal loop traversal and the exit Everything interesting will happen in two loop Huang's Theorem: (Paraphrased) from the loop.

Discuss Huang's Theorem in terms of graph based coverage metrics. Exercise:

first





last)

### Strategy for Loop Testing

- Huang's theorem suggests/assures 2 tests per loop is sufficient. (Judgment required, based on reality of the
- For nested loops:
- Test innermost loop first
- Then "condense" the loop into a single node (as in condensation graph, see Chapter 4)
- Work from innermost to outermost loop
- For concatenated loops: use Huang's Theorem
- For knotted loops: Rewrite! (see McCabe's cyclomatic and essential complexity)



### Multiple Condition Testing

- proposition, i.e., some logical expression of simple Consider the multiple condition as a logical conditions.
- Make the truth table of the logical expression.
- Convert the truth table to a decision table.
- Develop test cases for each rule of the decision table (except the impossible rules, if any).
- Next 3 slides: multiple condition testing for If (a < b + c) AND (b < a + c) AND (c < a + b)Else IsATriangle = False Then IsATriangle = True

#### Truth Table for Triangle Inequality (a<b+c) AND (b<a+c) AND (c<a+b)

| (a <b+c) (b<a+c)="" (c<a+b)<="" and="" td=""><td><b>—</b></td><td>Ш</td><td><b>L</b></td><td>Ш</td><td>Д.</td><td>Ш</td><td>Ь</td><td>Ш</td></b+c)> | <b>—</b> | Ш | <b>L</b> | Ш | Д. | Ш | Ь | Ш |
|---|----------|---|----------|---|----|---|---|---|
| (c <a+b)< td=""><td>⊢</td><td>J</td><td>⊢</td><td>ட</td><td>T</td><td>Ы</td><td>T</td><td>Ь</td></a+b)<>  | ⊢        | J | ⊢        | ட | T  | Ы | T | Ь |
| (b <a+c)< td=""><td><b>—</b></td><td>L</td><td>Ш</td><td>ட</td><td>L</td><td>T</td><td>F</td><td>Н</td></a+c)<>                                     | <b>—</b> | L | Ш        | ட | L  | T | F | Н |
| (a <b+c)< td=""><td>F</td><td>L</td><td>L</td><td>L</td><td>Н</td><td>Ш</td><td>4</td><td>Ш</td></b+c)<>  | F        | L | L        | L | Н  | Ш | 4 | Ш |

### Decision Table for

(a<b+c) AND (b<a+c) AND (c<a+b)

| Щ   | Щ  | ட   | ×                 |                         |
|---|--|---|-------------------|-------------------------|
| ъ   | Щ  | _   | ×<br>×            |                         |
| ш   | T  | Э   | ×                 |                         |
| Н<br>Н<br>Н<br>Т  | T  | T   |                   | 4                       |
| ⊢   | Ь  | Ь   | X                 |                         |
| T   | ш  | FT  |                   | 3                       |
| ⊢   | T  |   |                   | 2 3                     |
| T   | T  | _   |                   | 1                       |
| c1: a <b+c< td=""><td>c2: b<a+c< td=""><td>c3: c<a+b< td=""><td>a1:<br/>impossible</td><td>a2:Valid test<br/>case #</td></a+b<></td></a+c<></td></b+c<> | c2: b <a+c< td=""><td>c3: c<a+b< td=""><td>a1:<br/>impossible</td><td>a2:Valid test<br/>case #</td></a+b<></td></a+c<> | c3: c <a+b< td=""><td>a1:<br/>impossible</td><td>a2:Valid test<br/>case #</td></a+b<> | a1:<br>impossible | a2:Valid test<br>case # |

(a<b+c) AND (b<a+c) AND (c<a+b)

| expected<br>output | TRUE     | FALSE | FALSE     | FALSE |
|--------------------|----------|-------|-----------|-------|
| С                  | 5        | 6     | 4         | 4     |
| q                  | 4        | 4     | 6         | 3     |
| а                  | 3        | 3     | 3         | 6     |
|                    | all true | c≥a+b | p ≥ a + c | a≥b+c |
| Test               |          | 2     | 3         | 4     |

Note: could add test cases for c = a + b, b = a + c, and a = b + c.  $(4) \rightarrow (5) \rightarrow (6) \rightarrow (7) \rightarrow (8)$ 

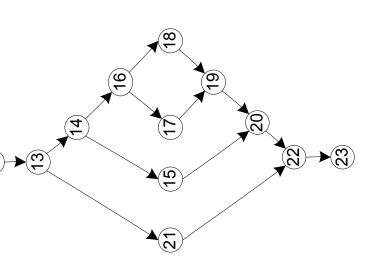
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- Program triangle2
- Dim a,b,c As Integer Dim IsATriangle As Boolean
- Output("Enter 3 integers which are sides of a triangle",
  - Input(a,b,c)

- Output("Side A is ",a)
  Output("Side B is ",b)
  Output("Side C is ",c)
- 9 If (a < b + c) AND (b < a + c) AND (c < a + b)
  - Then IsATriangle = True
- Else IsATriangle = False

- 13 If IsATriangle
  14 Then If (a = b) AND (b = c)
  15 Then Output ("Equilateral")
- Else If (a≠b) AND (a≠c) AND (b≠c)

  - Then Output ("Scalene") Else Output ("Isosceles")
    - EndIf
- Output("Not a Triangle")
- End triangle2



(often correspond to infeasible paths)

- Look at the Triangle Program code and program graph
- If a path traverses node 10 (Then IsATriangle = True), then it must traverse node 14.
- Similarly, if a path traverses node 11 (Else IsATriangle = False), then it must traverse node 21.
- Paths through nodes 10 and 21 are infeasible.
- Similarly for paths through 11 and 14.
- Hence the need for the C<sub>d</sub> coverage metric.

## Test Coverage for Compound Conditions

- Extension of/to Multiple Condition Testing
- Modified Condition Decision Coverage (MCDC)
- Required for "Level A" software by DO-178B
- Three variations\*
- Masking MCDC
- Unique-Cause MCDC
- Unique-Cause + Masking MCDC
- Masking MCDC is
- the weakest of the three, AND
- is recommended for DO-178B compliance

Chilenski, John Joseph, "An Investigation of Three Forms of the Modified Condition Decision Coverage (MCDC) Criterion," DOT/FAA/AR-01/18, April

[http://www.faa.gov/about/office\_org/headquarters\_offices/ang/offices/tc/library/



### Chilenski's Definitions

- Conditions can be either s*imple* or *compound*
- isATriangle is a simple condition
- (a < b + c) AND (b < a + c) is a compound condition
- Conditions are strongly coupled if changing one always changes the other.
- (x = 0) and  $(x \neq 0)$  are strongly coupled in

$$((x = 0) AND a) OR ((x \neq 0) AND b)$$

- Conditions are weakly coupled if changing one may change one but not all of the others.
- All three conditions are weakly coupled in

$$((x = 1) OR (x = 2) OR (x = 3))$$

- "Masking" is based on the Domination Laws
- (x AND false)
- (x OR true)

#### MCDC requires...

- Every statement must be executed at least once,
- Every program entry point and exit point must be invoked at least once,
- All possible outcomes of every control statement are taken at least once,
- Every non-constant Boolean expression has been evaluated to both True and False outcomes,
- Every non-constant condition in a Boolean expression has been evaluated to both True and False outcomes,
- has been shown to independently affect the outcomes Every non-constant condition in a Boolean expression (of the expression).



#### **MCDC Variations**

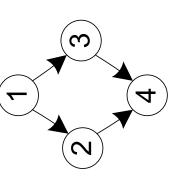
- "Unique-Cause MCDC [requires] a unique cause (toggle a single condition and change the expression result) for all possible (uncoupled) conditions.
- expression result) for all possible (uncoupled) conditions. allowed} for that condition only, i.e., all other (uncoupled) In the case of strongly coupled conditions, masking [is "Unique-Cause + Masking MCDC [requires] a unique cause (toggle a single condition and change the conditions will remain fixed."

### MCDC Variations (continued)

(i.e., all other (uncoupled) conditions will remain fixed." (uncoupled) conditions. In the case of strongly coupled conditions, masking [is allowed] for that condition only coupled and uncoupled. (toggle a single condition and "Masking MCDC allows masking for all conditions, change the expression result) for all possible

#### Example

If (a AND (b OR c))
 Then y = 1
 Else y = 2
 EndIf



Chapter 8 Path Testing

## Decision Table for (a AND (b OR c))

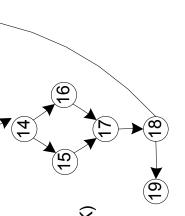
| Conditions     | rule<br>1 | rule<br>2 | rule<br>3 | rule<br>4 | rule<br>5 | rule<br>6 | rule<br>7 | rule<br>8 |
|----------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| а              | T         | ⊥         | ⊢         | ⊢         | Ш         | ш         | F         | Ь         |
| q              | ⊢         | ⊢         | ш         | ш         | <b>—</b>  | ⊢         | Ъ         | ш         |
| 2              | F         | ш         | ⊢         | ш         | <b>—</b>  | ш         | T         | ш         |
| a AND (b OR c) | True      | True      | True      | False     | False     | False     | False     | False     |
| Actions        |           |           |           |           |           |           |           |           |
| y = 1          | ×         | ×         | ×         |           |           | 1         |           | 1         |
| y = 2          |           |           |           | ×         | ×         | ×         | ×         | ×         |

## For MCDC Coverage of (a AND (b OR c))

- Rules 1 and 5 toggle condition a
- Rules 2 and 4 toggle condition b
- Rules 3 and 4 toggle condition c
- cause testing on variable a because it appears in ((a AND b) OR (a AND C)), we cannot do unique If we expand (a AND (b OR c)) to both sub-expressions.

### A NextDate Example

- Dim day, month, year As Integer
- Dim dayOK, monthOK, yearOK As Boolean
- Input(day, month, year)
- Then dayOK = True 1 NextDate Fragment
  2 Dim day, month, year
  3 Dim dayOK, monthOK
  4 Do
  5 Input(day, month, 6 If 0 < day < 32 7 Then dayOK = F
  8 Else dayOK = F
- Else dayOK = False
  - Endlf
- If 0 < month < 13
- Then monthOK = True
- Else monthOK = False
- If 1811 < year < 2013
- Then yearOK = True
- Else yearOK = False
  - EndIf
- 18 Until (dayOK AND monthOK AND yearOK) 19 End Fragment



## Corresponding Decision Table

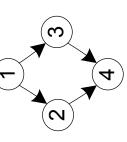
| Conditions          | rule 1   | rule 1 rule 2 | rule 3 | rule 4 | rule 5   | rule 6 | rule 7 | rule 8 |
|---------------------|----------|---------------|--------|--------|----------|--------|--------|--------|
| dayOK               | _        | <b>-</b>      | ⊥      | T      | ш        | Ш      | ш      | ш      |
| monthOK             | _        | <b>-</b>      | Ц      | ш      | <b>—</b> | _      | ш      | ш      |
| YearOK              | <b>—</b> | ш             |        | Н      | <b>-</b> | Ь      | T      | ш      |
| The Until condition | True     | False         | False  | False  | False    | False  | False  | False  |
| Actions             |          |               |        |        |          |        |        |        |
| Leave the loop      | ×        | ı             | 1      |        | ı        | 1      |        | l      |
| Repeat the loop     | I        | ×             | ×      | ×      | ×        | ×      | ×      | ×      |

## Test Cases and Coverage

- Decision Coverage: Rule 1 and any of Rules 2 8
- Multiple Condition Coverage: all eight rules are needed
- Modified Condition Decision Coverage:
- rules 1 and 2 toggle yearOK
- rules 1 and 3 toggle monthOK
- rules 1 and 4 toggle dayOK

If (a < b + c) AND (a < b + c) AND (a < b + c)</li>
 Then IsA Triangle = True
 Else IsA Triangle = False

IsA Triangle = False



In the three conditions, there are interesting dependencies that create four impossible rules.

| Conditions          | rule<br>1 | rule<br>2 | rule<br>3 | rule 4 | rule<br>5 | rule<br>6 | rule<br>7 | rue<br>8 |
|---------------------|-----------|-----------|-----------|--------|-----------|-----------|-----------|----------|
| (a < b + c)         | T         | T         | 1         | Т      | ш         | Ъ         | Ъ         | ш        |
| (p < a + c)         | 1         | Т         | ±         | F      | L         | T         | Ь         | Ь        |
| (c < a + b)         | L         | ш         | 1         | F      | L         | д         | T         | Ь        |
| IsATriangle = True  | X         |           |           | _      |           |           |           |          |
| IsATriangle = False |           | X         | ×         | _      | ×         |           |           |          |
| impossible          | _         |           |           | X      |           | ×         | ×         | ×        |

## Two Strategies of MCDC Testing

- Rewrite the code as a decision table
- algebraically simplify
- watch for impossible rules
- eliminate masking when possible
- Rewrite the code as nested If logic
- (see example of the Triangle Program fragment on the next slide)

- Decision Coverage: Rule 1 and Rule 2. (also, rules 1 and 3, or rules 1 and 5.
- Rules 4, 6, 7, and 8 are impossible.
- Condition Coverage
- rules 1 and 2 toggle (c < a + b)</li>
- rules 1 and 3 toggle (b < a + c)
- rules 1 and 5 toggle (a < b + c)
- Modified Condition Decision Coverage:
- rules 1 and 2 toggle (c < a + b)
- rules 1 and 3 toggle (b < a + c)
- rules 1 and 5 toggle (a < b + c)

## Code-Based Testing Strategy

- Start with a set of test cases generated by an "appropriate" (depends on the nature of the program) specification-based test method.
- Look at code to determine appropriate test coverage metric.
- Loops?
- Compound conditions?
- Dependencies?
- If appropriate coverage is attained, fine.
- Otherwise, add test cases to attain the intended test coverage.



### Test Coverage Tools

- Commercial test coverage tools use "instrumented" source code.
- New code added to the code being tested
- Designed to "observe" a level of test coverage
- When a set of test cases is run on the instrumented code, the designed test coverage is ascertained.
- Strictly speaking, running test cases in instrumented code is not sufficient
- Safety critical applications require tests to be run on actual (delivered, non-instrumented) code.
- Usually addressed by mandated testing standards.



(values of array DDpathTraversed are set to 1 when corresponding instrumented code is executed.)

```
DDpathTraversed(1) = 1
```

- Output("Enter 3 integers which are sides of a triangle")
- Input(a,b,c)
- Output("Side A is ",a)
- Output("Side B is ",b)
  Output("Side C is ",c)
- Step 2: Is A Triangle?

DDpathTraversed(2) = 
$$1$$

- If (a < b + c) AND (b < a + c) AND (c < a + b)Then DDpathTraversed(3) = 1

11. Else DDpathTraversed(4) = 1

lsATriangle = False

### Instrumentation Exercise

- record how many times a set of test cases traverses the How could you instrument the Triangle Program to individual DD-Paths?
- Is this useful information?

- Proposed by Thomas McCabe in 1982
- Math background
- a Vector Space has a set of independent vectors called basis vectors
- every element in a vector space can be expressed as a linear combination of the basis vectors
- Example: Euclidean 3-space has three basis vectors
- (1, 0, 0) in the x direction
- (0, 1, 0) in the y direction
- (0, 0, 1) in the z direction
- The Hope: If a program graph can be thought of as a vector space, there should be a set of basis vectors. Testing them tests many other paths.



## (McCabe) Basis Path Testing

- in math, a basis "spans" an entire space, such that everything in the space can be derived from the basis elements.
- the cyclomatic number of a strongly connected directed graph is the number of linearly independent cycles.
- given a program graph, we can always add an edge from the sink node to the source node to create a strongly connected graph. (assuming single entry, single exit)
- computing V(G) = e n + p from the modified program graph yields the number of independent paths that must be tested.
- since all other program execution paths are linear combinations of the basis path, it is necessary to test the basis paths. (Some say this is sufficient; but that is problematic.)
- the next few slides follow McCabe's original example.

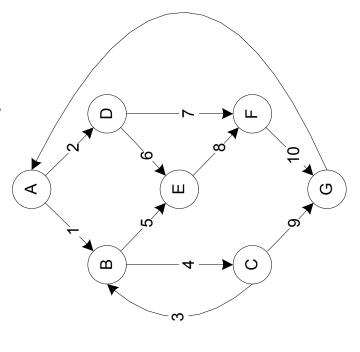


### McCabe's Example

Original Graph McCabe's

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Connected Graph Derived, Strongly



Ω

$$V(G) = 10 - 7 + 2(1)$$
  
= 5

$$V(G) = 11 - 7 + 1$$
  
= 5

## **McCabe's Baseline Method**

- Pick a "baseline" path that corresponds to normal execution. (The baseline should have as many decisions as possible.)
- another alternative) and continue as much of the baseline To get succeeding basis paths, retrace the baseline until you reach a decision node. "Flip" the decision (take as possible.
- Repeat this until all decisions have been flipped. When you reach V(G) basis paths, you're done.
- If there aren't enough decisions in the first baseline path, find a second baseline and repeat steps 2 and 3.

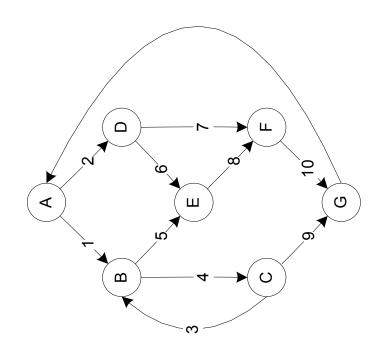
Following this algorithm, we get basis paths for McCabe's example.



# McCabe's Example (with numbered edges)

### Resulting basis paths

p1: A, B, C, G Flip decision at C p2: A, B, C, B, C, G Flip decision at B p3: A, B, E, F, G Flip decision at A p4: A, D, E, F, G Flip decision at D First baseline path p5: A, D, F, G



### Path/Edge Incidence

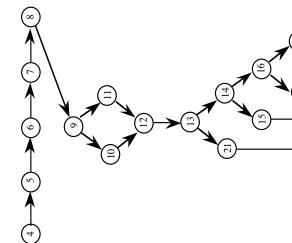
| Path / Edges                | e1 | e2 | 63 | 64 | e5 | 99 | e7 | 68 | 69 | e10 |
|-----------------------------|----|----|----|----|----|----|----|----|----|-----|
| p1: A, B, C, G              | _  | 0  | 0  | _  | 0  | 0  | 0  | 0  | _  | 0   |
| p2: A, B, C, B, C, G        | _  | 0  | -  | 2  | 0  | 0  | 0  | 0  | _  | 0   |
| p3: A, B, E, F, G           | _  | 0  | 0  | 0  | _  | 0  | 0  | _  | 0  | _   |
| p4: A, D, E, F, G           | 0  | _  | 0  | 0  | 0  | _  | 0  | _  | 0  | _   |
| p5: A, D, F, G              | 0  | _  | 0  | 0  | 0  | 0  | _  | 0  | 0  | _   |
| ex1: A, B, C, B, E, F, G    | _  | 0  | ~  | _  | _  | 0  | 0  | _  | 0  | _   |
| ex2: A, B, C, B, C, B, C, G | _  | 0  | 2  | က  | 0  | 0  | 0  | 0  | _  | 0   |

Sample paths as linear combinations of basis paths ex1 = p2 + p3 - p1 ex2 = 2p2 - p1

- What is the significance of a path as a linear combination of basis paths?
- What do the coefficients mean? What does a minus sign mean?
- In the path ex2 = 2p2 p1 should a tester run path p2 twice, and then not do path p1 the next time? This is theory run amok.
- Is there any guarantee that basis paths are feasible?
- Is there any guarantee that basis paths will exercise interesting dependencies?

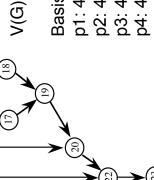


# McCabe Basis Paths in the Triangle Program



There are 8 topologically possible paths. 4 are feasible, and 4 are infeasible.

Exercise: Is every basis path feasible?



V(G) = 23 - 20 + 2(1) = 5

Basis Path Set B1

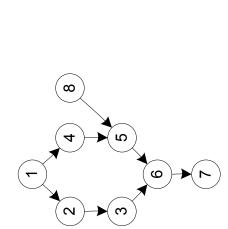
p1: 4, 5, 6, 7, 8, 9, 10, 12, 13, 14, 16, 18, 19, 20, 22, 23 (mainline) p2: 4, 5, 6, 7, 8, 9, 11, 12, 13, 14, 16, 18, 19, 20, 22, 23 (flipped at 9) p3: 4, 5, 6, 7, 8, 9, 11, 12, 13, 21, 22, 23 (flipped at 13) p4: 4, 5, 6, 7, 8, 9, 11, 12, 13, 14, 15, 20, 22, 23 (flipped at 14) p5: 4, 5, 6, 7, 8, 9, 11, 12, 13, 14, 16, 17, 19, 20, 22, 23 (flipped at 16)

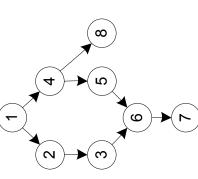
### **Essential Complexity**

- McCabe's notion of Essential Complexity deals with the extent to which a program violates the precepts of Structured Programming.
- To find Essential Complexity of a program graph,
- Identify a group of source statements that corresponds to one of the basic Structured Programming constructs.
- Condense that group of statements into a separate node (with a new name)
- Continue until no more Structured Programming constructs can be
- The Essential Complexity of the original program is the cyclomatic complexity of the resulting program graph.
- The essential complexity of a Structured Program is 1.
- Violations of the precepts of Structured Programming increase the essential complexity.



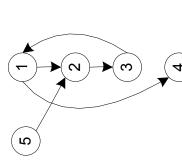


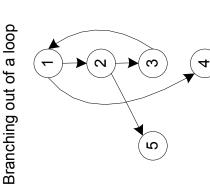




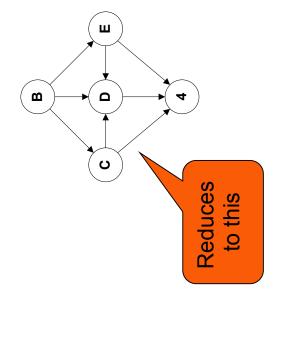


Branching into a loop

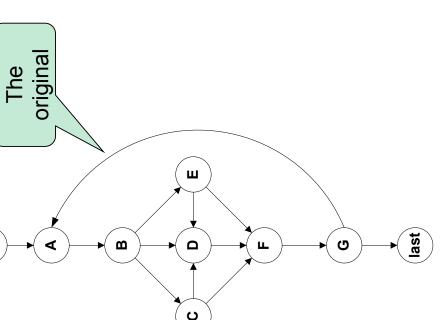




Essential Complexity of Schach's Program Graph



V(G) = 8 - 5 + 2(1)= 5 Essential complexity is 5



#### senes

- Linear combinations of execution paths are counter-intuitive. What does 2p2 - p1 really mean?
- How does the baseline method guarantee feasible basis paths?
- Given a set of feasible basis paths, is this a sufficient test?

#### Advantages

- McCabe's approach does address both gaps and redundancies.
- Essential complexity leads to better programming practices.
- constructs increase cyclomatic complexity, and violations cannot McCabe proved that violations of the structured programming occur singly. ı



# Conclusions For Code-Based Testing

- Excellent supplement (complement?) to specificationbased testing because..
- highlights gaps and redundancies
- supports a useful range of test coverage metrics
- Test coverage metrics help manage the testing process.
- Tool support is widely available.
- Not much help for identifying test cases.
- Satisfaction of a test coverage metric does not guarantee the absence of faults.



addition, the following criteria must hold for all vectors x, y, and z  $\in$  V, scalar multiplication) must be defined for elements in the set. In For a set V to be a vector space, two operations (addition and and for all scalars k, I, 0, and 1:

if x,  $y \in V$ , the vector  $x + y \in V$ .

$$x + y = y + x$$

$$(x + y) + z = x + (y + z).$$

1. there is a vector 
$$0 \in V$$
 such that  $x + 0 = x$ .

For any 
$$x \in V$$
, there is a vector  $-x \in V$  such that  $x + (-x) = 0$ .

for any 
$$x \in V$$
, the vector  $kx \in V$ , where  $k$  is a scalar constant.

$$y$$
.  $k(x + y) = kx + ky$ .

1. 
$$(k + 1)x = kx + 1x$$
.  
 $k(1x) = (k1)x$ .

$$K(|X) = (K|)X.$$