Linear Models: Classification

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Data from: [https://www.kaggle.com/datasets/gauravtopre/credit-card-defaulter-prediction (https://www.kaggle.com/datasets/gauravtopre/credit-card-defaulter-prediction)]

Linear classification uses a linear model to find a decision boundry between classes. The model will take a set of inputs and try to find a line that would split up the data into classes as best it can. Linear classification is great because it is simple and easy to undersand and fast with larger data sets. But linear models simplicity is also one of its down falls. It will alawys assume a linear relationship in the input data, even if its not there.

About Logistic Regression and Naive Bayes

I will be using the a logistic regression model and a naive bayes model to try to predict using my choosen data set. The logistic regression is great for this application as it was made to classify a binary response using its set of predicotrs. It is simple and fast to execute as well as a dsicrimitive algorithm, meaning that it directly predict a classification for the new data using its predictors. Its also robust to noise in the data. But it is still only a linear model. It will try to fit the data to the linear relationship its looking for, even if its not there. A problem that I ran into with a data set I tried to use previously, is that the more predictors it has, the longer it takes to do the computational work. I decided to switch data sets previously as the computation time was taking too long.

The naive bayes is a classification model based on Bayes theorem. Naive bayes tends to perform well on smaller data sets than the logistic regression does. While unneeded for this application, it can also be applied to multiclass classification. But naive bayes has a few problems. The first and largest being its assumption that all the predictors are independent of each other, which is not always the case. Naive bayes as tends to have a higher bias than the logistic regression.

Data Exploration

The data set I choose is from Kaggle and it contains data about credit card useage and defaulters in Taiwan in 2005. The goal is to use the data in this set to predict if a given person defaulted on their payments or not. After reading in the csy, I remove an unneeded ID row, as well as four sets of three related columns of payment information in defferent months. I chose to only use the first 2 of 6 months of data for simplicity and to improve the models. The last bit of cleaning is to remove some rows that had invalid values and insignificantly small subsets and then convert some columns to factors.

```
set.seed(1)
credit <- read.csv("creditcard.csv", header = TRUE) # read in csv</pre>
# data cleaning
credit <- credit[, c(-1, -9, -10, -11, -12, -15, -16, -17, -18, -21, -22, -23, -24)] # remove un
needed columns
credit <- subset(credit, credit$education != "0") # remove rows with invalid values</pre>
credit <- subset(credit, credit$education != "Others") # remove rows with this education type as</pre>
its insignificant
credit <- subset(credit, credit$education != "Unknown") # remove rows with this education type a</pre>
s its insignificant
credit <- subset(credit, credit$marriage != "0") # remove rows with invalid values</pre>
credit <- subset(credit, credit$marriage != "Other") # remove rows with this marrage type as its</pre>
insignificant
credit$defaulted <- factor(credit$defaulted)</pre>
credit$sex <- factor(credit$sex)</pre>
credit$education <- factor(credit$education)</pre>
credit$marriage <- factor(credit$marriage)</pre>
```

Then, I split the data into 80% training and 20% testing data and output the structure and summary of the training data.

```
i <- sample(1:nrow(credit), 0.8 * nrow(credit), replace = FALSE) # split data
train <- credit[i, ] # 80% train</pre>
test <- credit[-i, ] # 20% test
str(train) # structure of training data
```

```
## 'data.frame':
                   23330 obs. of 12 variables:
## $ creditLimit : int 250000 260000 100000 160000 20000 470000 180000 50000 380000 80000
. . .
## $ sex
                    : Factor w/ 2 levels "F", "M": 2 2 1 2 2 2 2 2 1 ...
## $ education
                    : Factor w/ 3 levels "Graduate school",..: 3 3 3 3 3 3 1 2 1 3 ...
                    : Factor w/ 2 levels "Married", "Single": 2 1 1 2 2 2 1 2 1 2 ...
## $ marriage
   $ age
                    : int 26 50 38 59 36 35 32 36 34 26 ...
##
  $ paymentDelaySep: int 0 0 1 0 0 0 -2 2 0 0 ...
##
## $ paymentDelayAug: int 0 0 -1 0 0 0 -2 2 0 0 ...
## $ billTotalSep
                  : int 115497 133208 0 86249 15198 262980 0 2400 106065 47788 ...
## $ billTotalAug : int 114716 122199 199 85764 19590 204078 0 2400 97979 45221 ...
## $ billPaidSep
                    : int 3835 6400 199 5000 5000 10929 0 0 3385 4000 ...
## $ billPaidAug
                    : int 4068 5744 0 4214 2000 4177 0 0 4074 3000 ...
                    : Factor w/ 2 levels "N", "Y": 1 1 1 1 2 1 1 2 1 1 ...
  $ defaulted
```

```
head(train) # first few lines
```

```
##
         creditLimit sex education marriage age paymentDelaySep paymentDelayAug
               250000
                                                26
## 17848
                        M University
                                        Single
## 25079
               260000
                        M University
                                      Married
                                                50
                                                                   0
                                                                                   0
                                      Married
## 4895
               100000
                                                                                   -1
                        F University
                                                38
                                                                   1
## 27506
               160000
                        M University
                                        Single
                                                59
                                                                   0
                                                                                   0
## 13549
                20000
                        M University
                                        Single
                                                36
                                                                   0
                                                                                    0
## 26839
               470000
                        M University
                                        Single 35
                                                                                    0
         billTotalSep billTotalAug billPaidSep billPaidAug defaulted
##
## 17848
                115497
                             114716
                                            3835
                                                         4068
## 25079
                133208
                              122199
                                            6400
                                                         5744
                                                                       N
## 4895
                                 199
                                             199
                                                                       N
                     0
                                                            0
## 27506
                 86249
                              85764
                                            5000
                                                         4214
                                                                       N
## 13549
                 15198
                                                                       Υ
                              19590
                                            5000
                                                         2000
## 26839
                262980
                              204078
                                           10929
                                                         4177
                                                                       N
```

tail(train) # last few lines

```
education marriage age paymentDelaySep
         creditLimit sex
##
               200000
## 25502
                        F Graduate school
                                              Single
                                                      31
                                                                         1
## 13192
               120000
                        F
                                University
                                            Married
                                                                         0
                                                      48
## 26621
                10000
                        Μ
                                University
                                              Single
                                                      23
                                                                        -2
## 26330
               350000
                        F
                                University
                                              Single
                                                      34
                                                                         1
                        F
                               High School
## 23633
               210000
                                              Single 43
                                                                        -1
## 23458
                80000
                        F
                               High School
                                            Married 41
                                                                        -1
##
         paymentDelayAug billTotalSep billTotalAug billPaidSep billPaidAug
## 25502
                                                  896
                                                               896
                        -1
                                      0
## 13192
                        0
                                  78384
                                                77085
                                                              4000
                                                                           3505
## 26621
                        -1
                                    998
                                                  780
                                                               780
                                                                            390
## 26330
                        -1
                                    -20
                                                  630
                                                               650
                                                                              0
## 23633
                        -1
                                   7605
                                                 1170
                                                              1170
                                                                              0
## 23458
                        -1
                                   3526
                                                10129
                                                             10129
                                                                           6100
##
         defaulted
## 25502
## 13192
                  Ν
## 26621
                  Υ
## 26330
## 23633
                  Ν
## 23458
                  N
```

```
summary(train) # summary of data columns
```

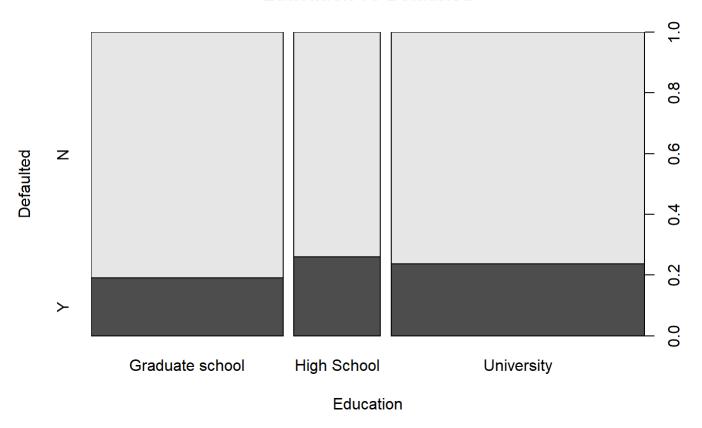
```
##
     creditLimit
                                           education
                       sex
                                                             marriage
                                 Graduate school: 8428
           : 10000
##
    Min.
                       F:14183
                                                          Married:10759
##
    1st Qu.:
              50000
                      M: 9147
                                 High School
                                                 : 3795
                                                          Single :12571
                                 University
##
    Median : 140000
                                                 :11107
           : 168031
##
    Mean
    3rd Qu.: 240000
##
##
    Max.
           :1000000
                     paymentDelaySep
##
                                        paymentDelayAug
                                                            billTotalSep
         age
                                                :-2.0000
                                                                  :-165580
##
    Min.
           :21.00
                    Min.
                            :-2.00000
                                        Min.
                                                           Min.
##
    1st Qu.:28.00
                    1st Qu.:-1.00000
                                        1st Qu.:-1.0000
                                                           1st Qu.:
                                                                      3510
    Median :34.00
                    Median : 0.00000
                                        Median : 0.0000
##
                                                           Median :
                                                                     22316
##
    Mean
           :35.36
                    Mean
                            :-0.01547
                                        Mean
                                                :-0.1293
                                                           Mean
                                                                  :
                                                                     50870
    3rd Qu.:41.00
                                        3rd Qu.: 0.0000
##
                     3rd Qu.: 0.00000
                                                           3rd Qu.:
                                                                     66503
##
    Max.
           :79.00
                    Max.
                            : 8.00000
                                        Max.
                                                : 8.0000
                                                           Max.
                                                                  : 964511
     billTotalAug
                       billPaidSep
                                          billPaidAug
                                                              defaulted
##
   Min.
           :-69777
                     Min.
                             :
                                         Min.
                                                              N:18105
##
                                   0.0
                                                        0.0
##
    1st Ou.: 2975
                      1st Ou.:
                                 961.2
                                         1st Ou.:
                                                      788.2
                                                              Y: 5225
##
    Median : 21066
                     Median : 2100.0
                                         Median :
                                                     2009.0
          : 48917
##
    Mean
                             : 5580.3
                                                     5742.1
                     Mean
                                         Mean
    3rd Qu.: 63327
                      3rd Qu.: 5005.0
##
                                         3rd Qu.:
                                                     5000.0
##
    Max.
           :983931
                     Max.
                             :505000.0
                                         Max.
                                                 :1227082.0
```

Graphs

This first graph shows that education level does have an effect on if someone defaults on their payment. The amount of poeple who defaulted that went to grad school is less than the amount of people that went to university is less than the amount of people that only went to high schoool.

```
plot(train$defaulted ~ train$education, xlab = "Education", ylab = "Defaulted", main = "Educatio
n vs Defaulted")
```

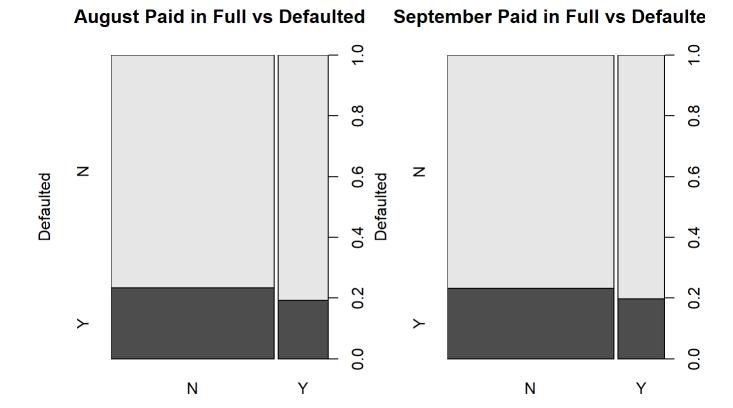
Education vs Defaulted



These next two graphs are showing that in both months there are less people who paid their bill in full and defaulted than those that didnt pay their bill in full and defaulted.

```
par(mfrow = c(1, 2)) # output graphs in 2x1
plot(factor(ifelse(train$billPaidAug >= train$billTotalAug, "Y", "N")), train$defaulted, xlab =
"Paid bill in full", ylab = "Defaulted", main = "August Paid in Full vs Defaulted")
plot(factor(ifelse(train$billPaidSep >= train$billTotalSep, "Y", "N")), train$defaulted, xlab =
"Paid bill in full", ylab = "Defaulted", main = "September Paid in Full vs Defaulted")
```

Paid bill in full



Logistic Regression Model

Paid bill in full

Now, I create a binomial logistic regression model using the training data where I am training it to predict if a given person defaulted on their payment. As shown in the summary, the range of the min and max of the deviance residuals is small which is good for thid model. R seems very confident that the best predictor is the paymentDelaySep and to a lessser degree paymentDelayAug based on the reported z and p values. But overall, most of the predictors are significant. Interestingly, the dummy variables for the high school and university predictors are not reported as significant by R. Finally, the residual deviance is lower than the null deviance which does show that the model is at least improved over just the intercept with no predictors.

```
logModel <- glm(defaulted ~ ., data = train, family = "binomial") # create Logistic regression m</pre>
odel
summary(logModel)
```

```
##
## Call:
## glm(formula = defaulted ~ ., family = "binomial", data = train)
##
## Deviance Residuals:
##
      Min
                10 Median
                                  3Q
                                          Max
##
  -3.1167 -0.7006 -0.5505 -0.2979
                                       3.8271
##
## Coefficients:
##
                         Estimate Std. Error z value Pr(>|z|)
                       -1.172e+00 9.280e-02 -12.624 < 2e-16 ***
## (Intercept)
## creditLimit
                       -9.390e-07 1.713e-07 -5.483 4.19e-08 ***
## sexM
                        1.114e-01 3.464e-02 3.215 0.001306 **
## educationHigh School -6.635e-02 5.339e-02 -1.243 0.213929
## educationUniversity -6.729e-02 3.987e-02 -1.688 0.091440 .
## marriageSingle
                       -1.765e-01 3.880e-02 -4.549 5.39e-06 ***
## age
                        7.083e-03 2.108e-03 3.360 0.000779 ***
                        5.839e-01 1.965e-02 29.711 < 2e-16 ***
## paymentDelaySep
                        1.640e-01 1.744e-02 9.400 < 2e-16 ***
## paymentDelayAug
## billTotalSep
                       -7.444e-06 1.292e-06 -5.763 8.28e-09 ***
## billTotalAug
                        6.082e-06 1.341e-06 4.534 5.79e-06 ***
## billPaidSep
                       -1.607e-05 2.632e-06 -6.105 1.03e-09 ***
                       -1.169e-05 2.383e-06 -4.905 9.34e-07 ***
## billPaidAug
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 24817 on 23329 degrees of freedom
## Residual deviance: 21890 on 23317 degrees of freedom
## AIC: 21916
##
## Number of Fisher Scoring iterations: 6
```

Naive Bayes Model

Next, I create a naive bayes model using the e1071 library. The first notable data in the model's output is the Apriori probabilties. These are what the model thinks the overall probabilties that a given person will have defaulted or not. Next is the conditional probabilities, where each group is what the model thinks the probability that a person would default given each column of data.

```
library(e1071) # import lib for naive bayes
bayesModel <- naiveBayes(defaulted ~ ., data = train) # create naive bayes model
bayesModel
```

```
##
## Naive Bayes Classifier for Discrete Predictors
##
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
##
## A-priori probabilities:
## Y
##
                     Υ
           Ν
## 0.7760394 0.2239606
##
## Conditional probabilities:
      creditLimit
##
## Y
           [,1]
                  [,2]
     N 178948.1 131947
##
##
    Y 130204.3 115571
##
##
      sex
## Y
               F
                         Μ
    N 0.6179508 0.3820492
##
##
     Y 0.5732057 0.4267943
##
##
      education
## Y
       Graduate school High School University
##
     Ν
             0.3766363
                         0.1552610 0.4681027
##
     Υ
             0.3079426
                         0.1883254 0.5037321
##
##
      marriage
                  Single
## Y
        Married
##
     N 0.452306 0.547694
##
     Y 0.491866 0.508134
##
##
      age
## Y
           [,1]
                    [,2]
##
     N 35.26407 9.002781
     Y 35.67254 9.649452
##
##
##
      paymentDelaySep
## Y
             [,1]
                       [,2]
##
     N -0.2104391 0.9472449
##
     Y 0.6600957 1.3919982
##
##
      paymentDelayAug
## Y
             [,1]
                     [,2]
##
     N -0.2989229 1.035447
     Y 0.4583732 1.513543
##
##
##
      billTotalSep
## Y
           [,1]
                    [,2]
##
     N 51733.21 73193.86
##
     Y 47879.87 73460.41
##
```

```
##
      billTotalAug
## Y
           [,1]
                     [,2]
##
     N 49552.02 70811.78
##
     Y 46714.99 71446.26
##
      billPaidSep
##
## Y
           [,1]
                      [,2]
##
     N 6232.587 16998.128
##
     Y 3319.910 9145.588
##
##
      billPaidAug
## Y
                     [,2]
           [,1]
##
     N 6460.940 21015.84
     Y 3251.403 11054.06
##
```

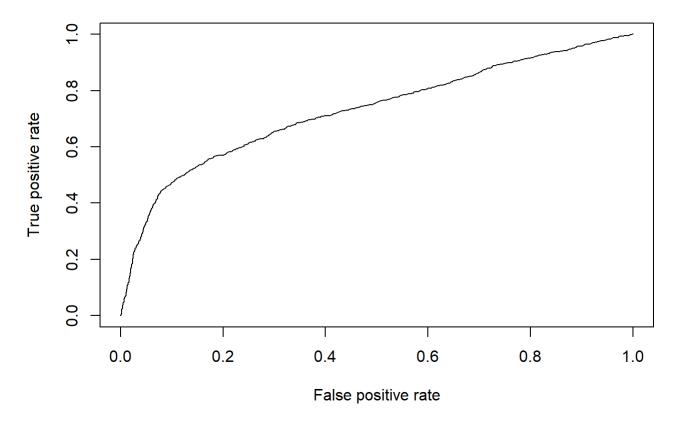
Evaluation of Models on Test Set

In evaluating the logistic regression model, it performs pretty well. R reports an accuracy of 0.8092 which is higher than I expected. But looking closer at the confusion matrix and statistics, there are a lot of false positive. This is further shown by the fact that the specificity is quite low. The Kappa value is also on the low end of 0.2815 which is not great but good enough. Looking at the ROC graph, the model clearly a little lackcing as the slope of the line does go up significantly in the beginning, indicating a good true positive rate, but it does not ever flatten out. Ideally the true positive rate would be as close to 1 as possible and the false positive rate would be close to 0. The reported AUC is also repoted to be at least better than randomly guessing, with a 0.7293 chance to correctly distinguish between if someone did default or not.

```
library(ROCR)
library(caret)
## Loading required package: ggplot2
## Loading required package: lattice
# logistic regession
predLog <- ifelse(predict(logModel, newdata = test, type = "response") > 0.5, "Y", "N")
confusionMatrix(as.factor(predLog), reference = test$defaulted)
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                 Ν
##
            N 4399 968
##
            Y 145 321
##
                  Accuracy : 0.8092
##
                    95% CI: (0.7989, 0.8192)
##
       No Information Rate: 0.779
##
       P-Value [Acc > NIR] : 8.915e-09
##
##
                     Kappa: 0.2815
##
##
##
   Mcnemar's Test P-Value : < 2.2e-16
##
               Sensitivity: 0.9681
##
##
               Specificity: 0.2490
            Pos Pred Value: 0.8196
##
            Neg Pred Value : 0.6888
##
##
                Prevalence : 0.7790
##
            Detection Rate : 0.7542
      Detection Prevalence : 0.9201
##
##
         Balanced Accuracy: 0.6086
##
          'Positive' Class : N
##
##
```

```
plot(performance(prediction(predict(logModel, newdata = test, type = "response"), test$defaulte
d), measure = "tpr", x.measure = "fpr"))
```



```
print(paste("AUC:", performance(prediction(predict(logModel, newdata = test, type = "response"),
test$defaulted), measure = "auc")@y.values[[1]]))
## [1] "AUC: 0.729258234628874"
```

Now, in evaluating the naive bayes model, its clear that it does not perform as well as the logistic regression model. While the naive bayes model does not have as many false positives as the logistic regression model, it does have more overall incorrect classifications than teh logistic model. This is furth shown by its accuracy being a bit lower at about 0.7876.

```
# naive bayes
predBayes <- predict(bayesModel, newdata = test, type = "class")</pre>
predBayes_raw <- predict(bayesModel, newdata = test, type = "raw")</pre>
table(predBayes, test$defaulted)
```

```
##
## predBayes
##
            N 3947
                    642
##
               597
                    647
```

```
print(paste("Accuracy:", mean(predBayes == test$defaulted)))
```

[1] "Accuracy: 0.787587862163552"