Linear classifiers: prediction equations

LINEAR CLASSIFIERS IN PYTHON



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Dot Products

```
x = np.arange(3)
x
```

array([0, 1, 2])

```
y = np.arange(3,6)
y
```

array([3, 4, 5])

х*у

array([0, 4, 10])

```
np.sum(x*y)
```

14

x@A

14

• x@y is called the dot product of x and y, and is written $x \cdot y$.

Linear classifier prediction

- raw model output = coefficients \cdot features + intercept
- Linear classifier prediction: compute raw model output, check the sign
 - if positive, predict one class
 - if negative, predict the other class
- This is the same for logistic regression and linear SVM
 - fit is different but predict is the same

How LogisticRegression makes predictions

 $raw model output = coefficients \cdot features + intercept$

```
lr = LogisticRegression()
lr.fit(X,y)
lr.predict(X)[10]
0
lr.predict(X)[20]
```



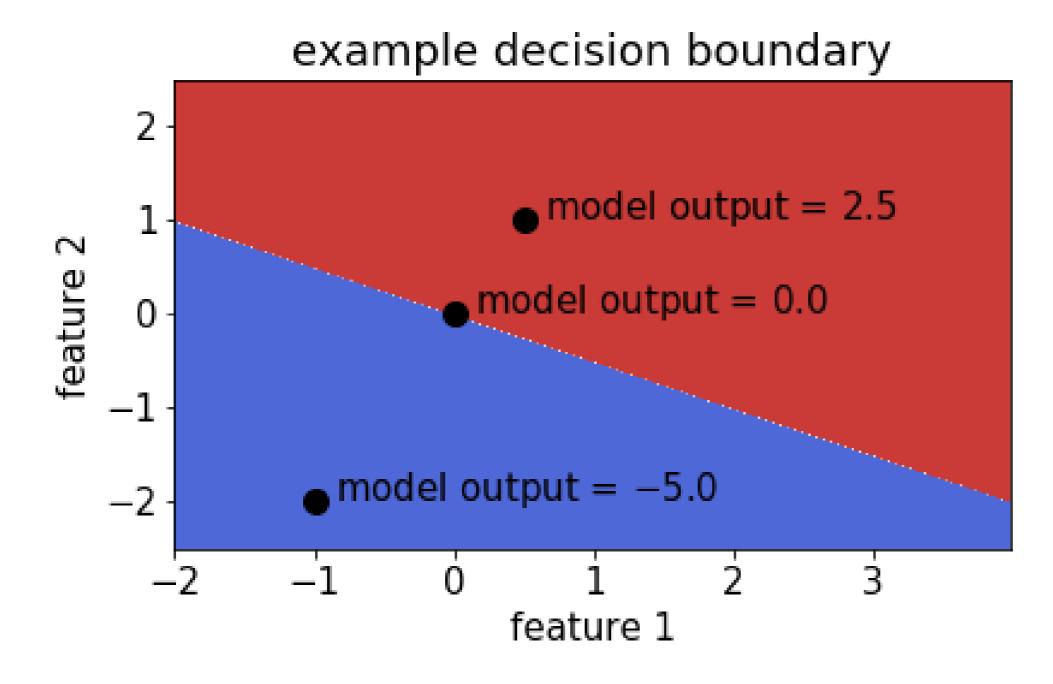
How LogisticRegression makes predictions (cont.)

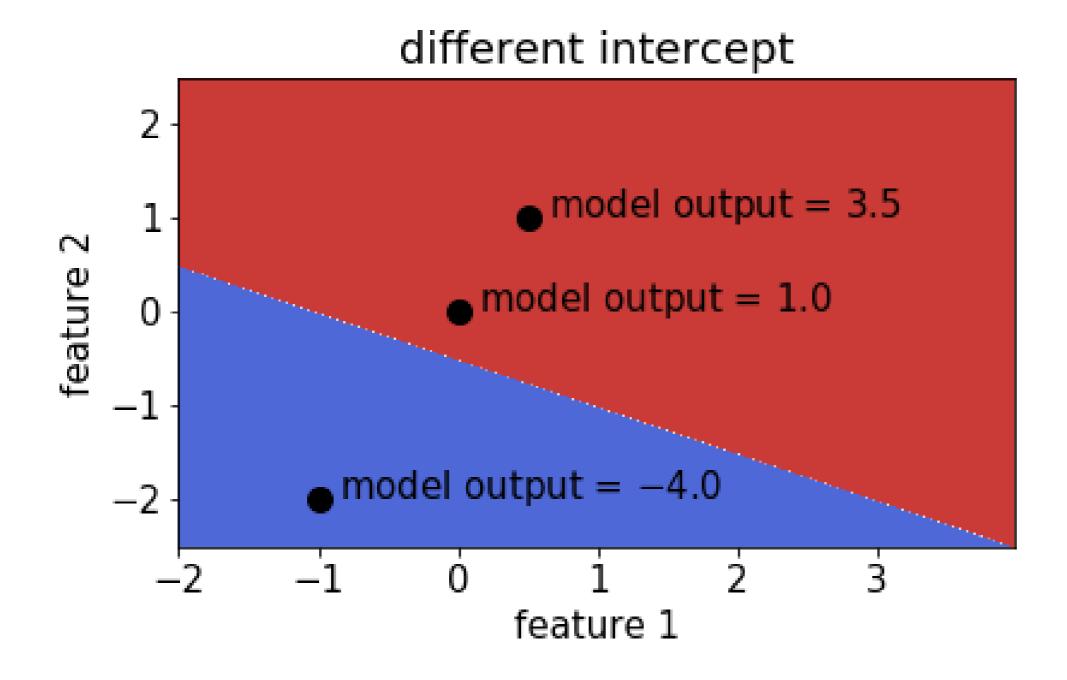
```
lr.coef_ @ X[10] + lr.intercept_ # raw model output
```

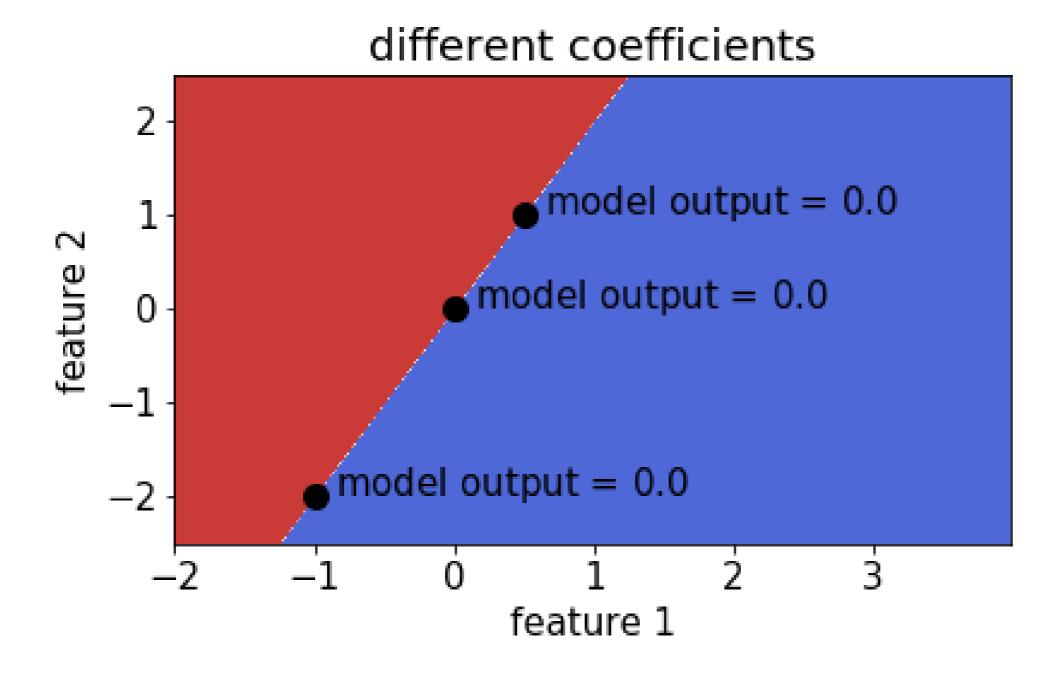
array([-33.78572166])

```
lr.coef_ @ X[20] + lr.intercept_ # raw model output
```

array([0.08050621])







Let's practice!

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What is a loss function?

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Least squares: the squared loss

• scikit-learn's LinearRegression minimizes a loss:

```
\sum_{i=1}^{n} (\text{true } i \text{th target value} - \text{predicted } i \text{th target value})^2
```

- Minimization is with respect to coefficients or parameters of the model.
- Note that in scikit-learn model.score() isn't necessarily the loss function.

Classification errors: the 0-1 loss

- Squared loss not appropriate for classification problems (more on this later).
- A natural loss for classification problem is the number of errors.
- This is the **0-1 loss**: it's 0 for a correct prediction and 1 for an incorrect prediction.
- But this loss is hard to minimize!

Minimizing a loss

```
from scipy.optimize import minimize
minimize(np.square, 0).x
array([0.])
```

minimize(np.square, 2).x

array([-1.88846401e-08])

Let's practice!

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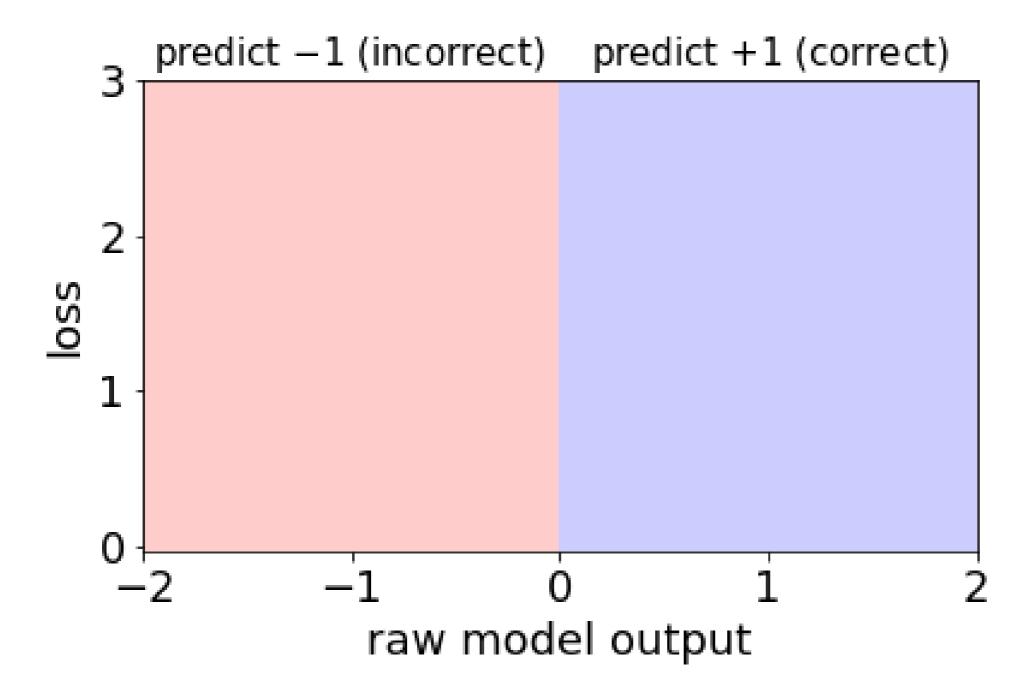
Loss function diagrams

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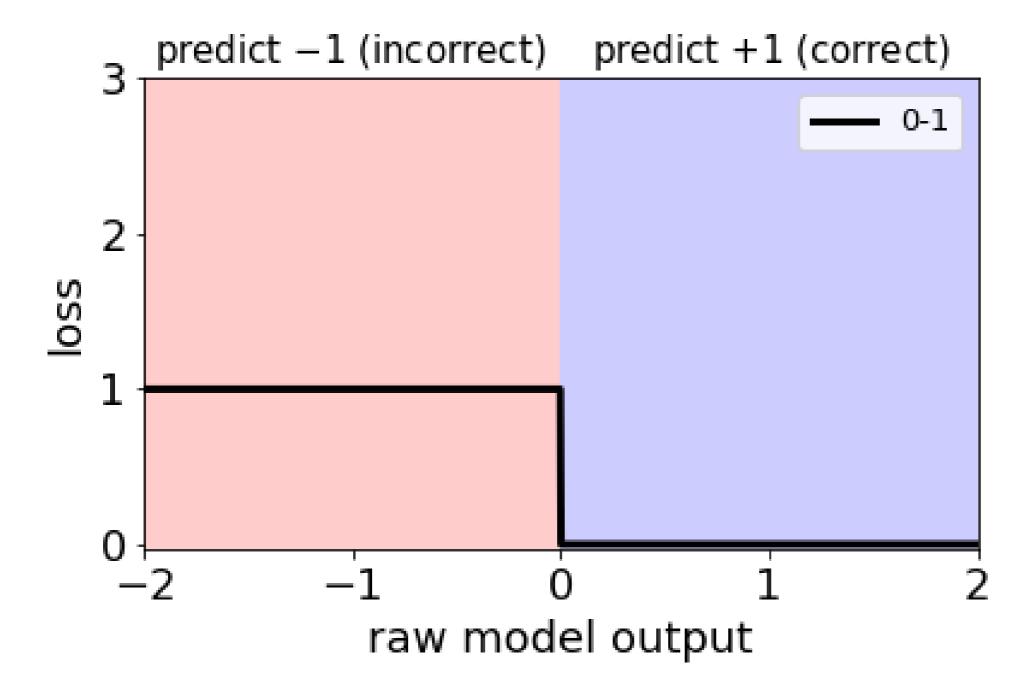


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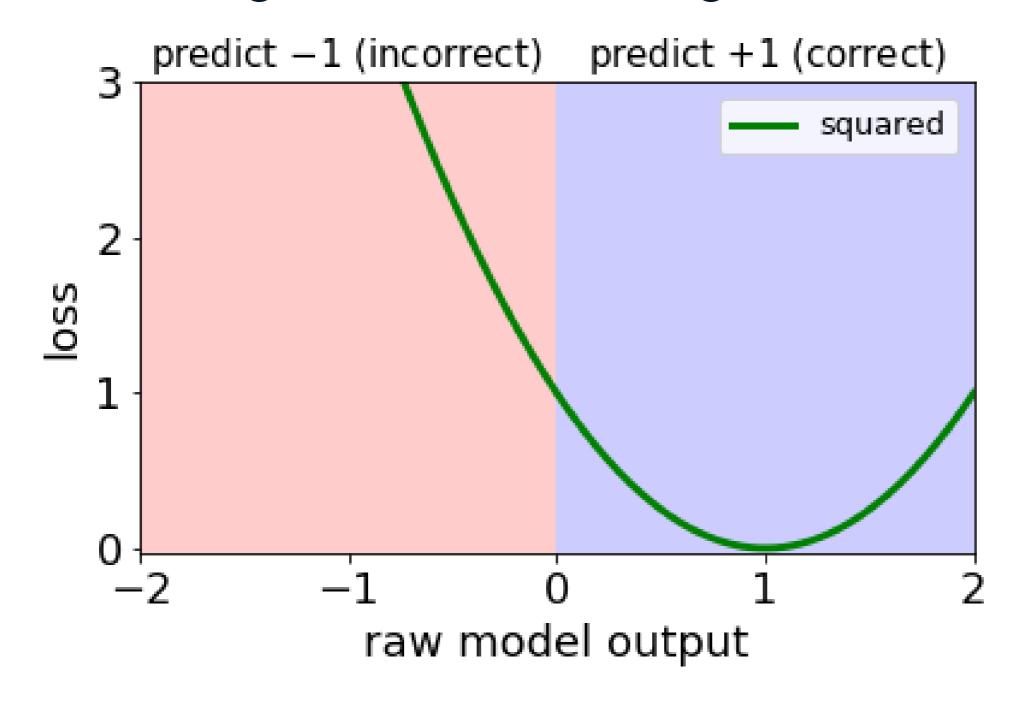




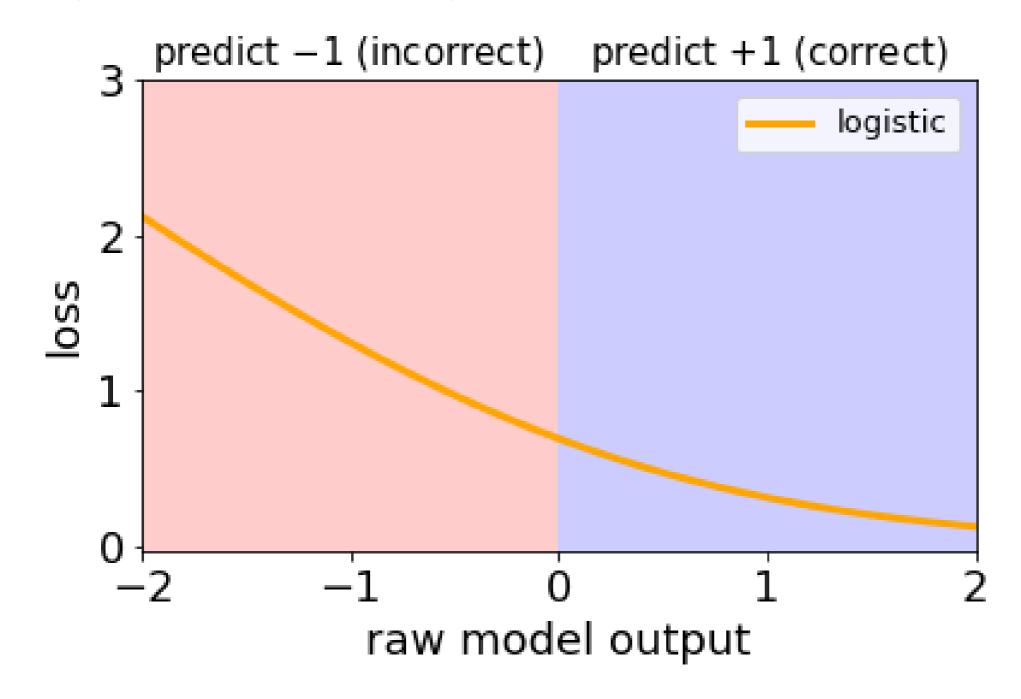
0-1 loss diagram



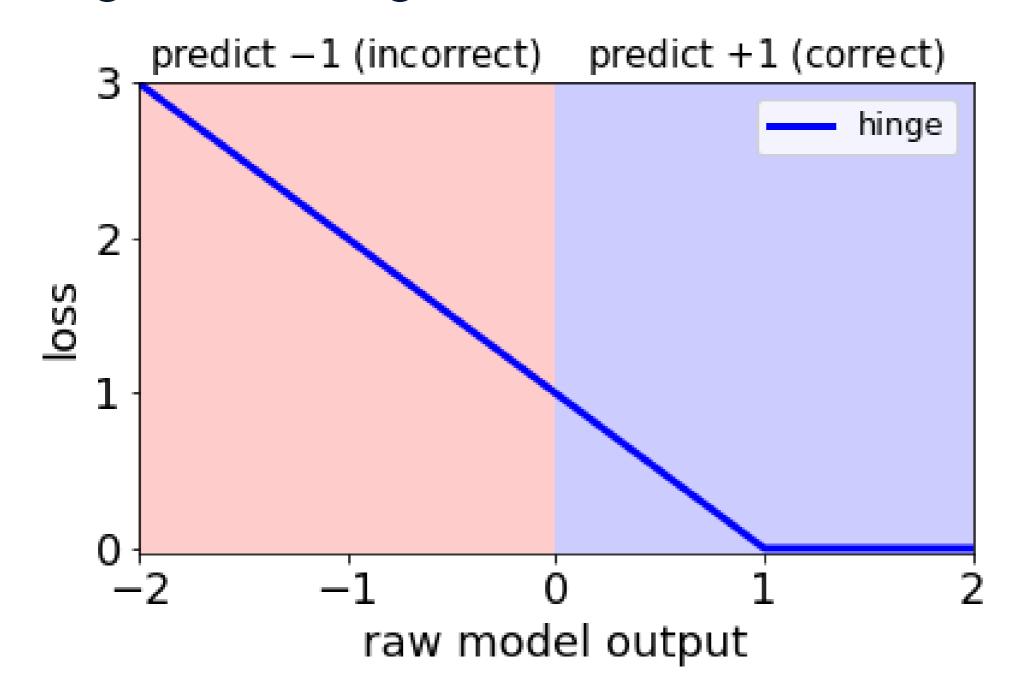
Linear regression loss diagram



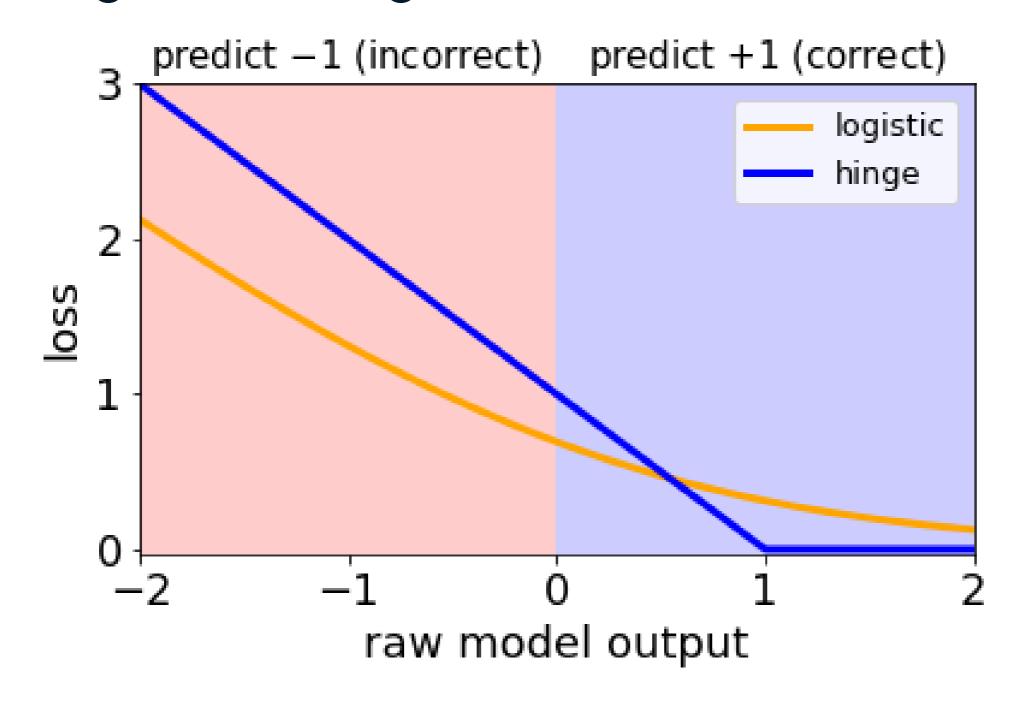
Logistic loss diagram



Hinge loss diagram



Hinge loss diagram



Let's practice!

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