$\bigcup_{i=1}^{n}$	VINFORMED SEARCH
	Let's think about how we might find a solution to the word ladder problem using our state machine formulation. IP PRAWS
	TRAIN TRAIN TRAIN TRAIL TRAIL
2	We'll define a search node as a triple (q,g,h) where: - q \in \mathbb{Q} is a state of our state machine - g \in \mathbb{R} is the "cost" of the search node (roughly speaking) - h \in \mathbb{R} is a guess at the "cost" of finding a final state from the current state q. (roughly speaking)

If we have a search node n = < q, g, h >, we will

sometimes use the notation g(n), g(n), h(n) to

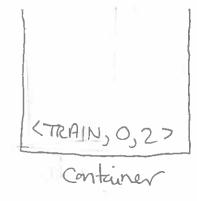
refer to its components.

UNINFORMED	SEARCH
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3) Let's go through a general-purpose search strategy. We'll start by making a search node out of the initial state ("TRAIN"):

Since we haven't done anything yet, we'll say the cost $g(n_0) = 0$. We'll guess that the cost $h(n_0)$ of finding a final state from TRAIN is 2, because only two letters of TRAIN are different than PRAWN

4) We put Pis node into a container.



5) Next, we get a node from the container. There's only one; of course, 60 we get that one:

(6) We now want to look at its "successors".

TRAIN has two neighbors in the state machine:

BRAIN and TRAIL. Each of these states costs I

to reach (assuming the weight of any transition

is I for word ladder). Because BRAIN has 2

letters that are different from PRAWN, we add node

< BRAIN, 1, 2 >

to the container. Because TRAIL has 3 letters that are different from PRAWN, we add node < TRAIL, 1, 3>

to the container.

<TRAIL, 1,3> <BRAIN, 1,27 container

7) Now we just repeat this process, getting a search node from the container, generating search nodes ("successors") for its neighbors, and putting them into the container.

<BRAIN, 1, 27 before

<TRAIN, 2, 27 <TRAIN, 2, 27 <TRAIN, 2, 27 <BRAIN, 1, 27 after

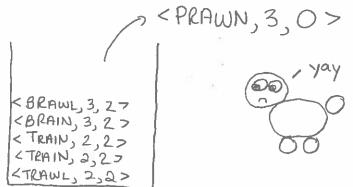
< TRAIN, 2, 2> < TRAIN, 2, 2> < TRAWL, 2, 2>

TRAIN, 2,2> <BRAWN, 2,1> <TRAIN, 2,2> <TRAWL, 2,2> 9fter

< BRAWN, 2, 1> <TRAIN, 2, 27 <TRAIN, 2, 27 <TRAWL, 2, 27 before

<PRAWN, 3, 0 > |
<BRAWL, 3, 27 |
<BRAIN, 3, 27 |
<TRAIN, 2, 27 |
<TRAIN, 2, 27 |
<TRAWL, 2, 27 |
<TRAWL, 2, 27 |
<TRAWL, 2, 27 |
</pre>

18) At some point, we get a final state from the container.



Thus we have found that there exists a solution of cost 3 for our word ladder.

- 9) There are two important details:
 - how do we decide which search node to get from the container?
 - how do we compute the h-value for each search node?
- 10 We'll let the container decide. It will be required to have methods . get () and . put (n), which "get" (and remove) a search node from the container (chosen by the container) and "put" a search node n into the container.

- Mode? We'll assume we have a heuristic function H: Q → R that maps each state to an estimated cost. In our example, H computed the number of letters that were different from PRAWN, so H(BRAWL) = 2 and H(CLAPS) = 4.
- 12) This gives us the following preliminary "master search algorithm":

SEARCH (M = (Q, E, D, qo, F, w), H):

Container = new Container()

container.put (< qo, O, H(qo)>)

repeat:

if container.empty() return oo

n = container.get()

if q(n) e F return q(n)

VISIT (n, container, M, H)

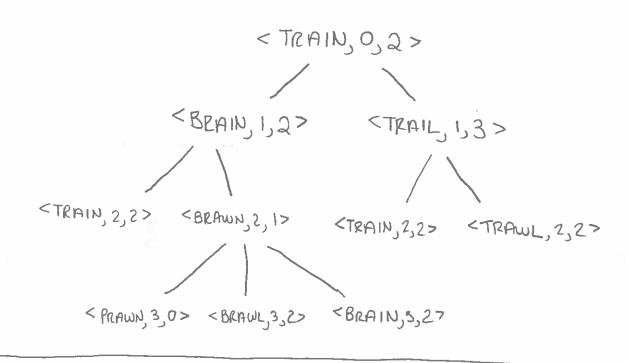
VISIT (n, container, M, H):

for n' in successors M, H (n):

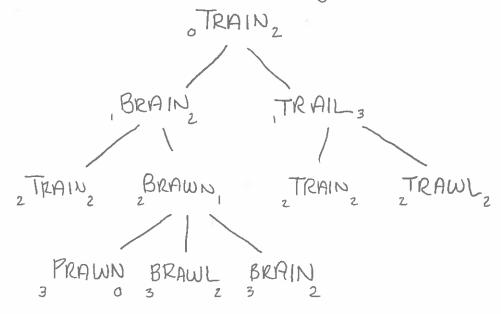
container. put (n')

where successors M, H (<q,g,h) = } <q',g+w(q,o,g'), H(q') > | o ∈ Σ, (q,o,q') ∈ []'

13) This repeated process of "visiting" nodes and generating their successors can be visualized with a tree where the vertices are search nodes, and the children of a search node are its successors:



(14) To make this a little easier to write, let's write Search node < 9,9,h > as 39h when we write the tree:



15) Each search node corresponds to a search path of State machine M (see the handout STATE SPACES, 6).

For instance, a BRAWN, corresponds to the search path (TRAIN, IB, BRAIN), (BRAIN, 4W, BRAWN)>.

The g-value of a search node is the cost of that search path, e.g.

$$g(BRAIN_2) = g(oTRAIN_2) + w(TRAIN_1B_BRAIN)$$

$$= 0 + 1$$

$$g(BRAWN_1) = g(BRAIN_2) + w(BRAIN_1AW_1B_RAWN)$$

$$= g(oTRAIN_2) + w(TRAIN_1B_BRAIN) + w(BRAIN_1AW_1BRAWN)$$

$$= g(oTRAIN_2) + w(TRAIN_1B_BRAIN) + w(BRAIN_1AW_1BRAWN)$$

$$= 0 + 1 + 1$$

16) 13 the q-value of a search node is a final state, then lits search path is a solution to our search problem. We call these goal nodes.

In other words, we want to find a goal node with minimum g-value.

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17)	When	dis	scussing	search	trees,	Some	additional	terms
	may	be	useful.		ч.		additional	

The search depth of a search node is its depth in the tree:

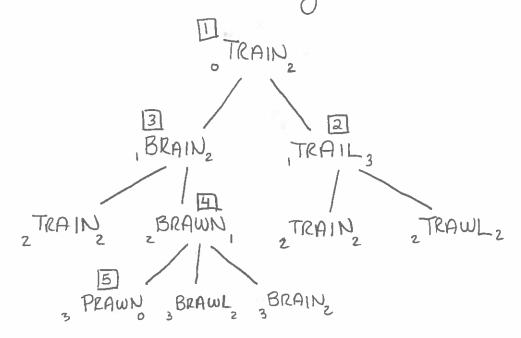
TRAIN Colepth O

BRAIN TRAIL Colepth 1

TRAIN BRAWN, Colepth 2

Another way to define search depth is the length of its search path.

18) In our first example, the container visited search nodes in a rather arbitrary order.



19 Let's consider the behavior of SEARCH Using different containers.

Suppose that we use a queve. Queve's are "first in, first act", so we get the following behavior:

1 Container

put < TRAIN, 0,2> 1 < TRAIN, 0,23

get < TRAIN, 0,2>

put (< BRAIN, 1,2> 1 < BRAIN, 1,2> < TRAIL, 1,3> (< TRAIL, 1,3> 1)

get < BRAIN, 1, 27

< TRAIL, 1, 3>

put & < BRAWN, 2, 17

< TRAIL, 1, 3> < BRAWN, 2,1> < TRAIN, 2,2>

< TRAIN, 2,2>

< BRAWN, 2, 1 > < TRAIN, 2, 2 >

get <TRAIL, 1,3>

< BRAWN, 2, 1 > < TRAIN, 2, 2 > < TRAWL, 2, 2 > < TRAIN, 2, 2>

Put > < TEAWL, 2,27 / < TEAIN, 2,27

< TRAIN, 2, 2>< TRAWL, 2, 2>< TRAIN, 2, 2>

get < BRAWN, 2, 1>

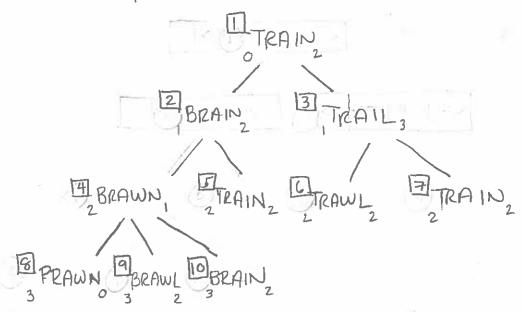
Put { < PRAWN, 3,0>

etc.

CORNAL, J, Z/

KBRAIN, 3,2>

20) If we lock at the search tree, this is the order in which states are processed



We first visit all search nodes at depth O(i.e. TRAIN2), then all search nodes at depth I (i.e. BRAIN2 and TRAIL3), then all search nodes at depth 2, etc.

This instantiation of the master Schech algorithm is called breadth-first search (BFS).

UN	INFORMED	SEARCH
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(a) BFS will find the optimal solution for word ladder because of the following property: if node n_1 is visited before node n_2 , then depth $(n_1) \leq depth (n_2)$

Because depth(n) is equal to its cost g(n) for word ladder, we know that the first goal node in we visit has minimal cost g(n).

Suppose otherwise, that there's a better goal node n' such that g(n') < g(n). Thus depth(n') < depth(n), so n' is visited by BFS before n — CONTRADICTION

BFS will not necessarily find the optimal solution for state machines with non-uniform weights, like:

Seattle Base

Seattle

Boise

Boise

Seattle

Oakland

Dakland

Eureka o

How might we adjust the container so that it finds the optimal solution even for state machines with non-uniform weights? Instead of having a policy of "first in, first out", we could instead prioritize getting search nodes of lowest g-value (corresponding to search paths of lowest cost):

Container put Seathle Seattle get . Seattle. put (3 Portland o 13 Portlando 10 Baise. Lio Boiseo get 3 Portlando 10 Boise o put Siz Oaklando 10 Boiseo 13 Oaklando 16 Eurekao Lie Eureka. get 10 Boise o 13 Oaklando 16 Eurekao put) 18 Oaklando 13 Oaklando 16 Eurekao 18 Oaklando 20 Seattles (20 Seather get 13 Oaklando 16 Eureka 18 Oaklando 20 Seather Put) 15 Eurekao 16 Eureka. 18 Oaklando 20 Seattle. 15 Eureka. 21 Boise. (al Boiseo get 15 Eureka 1 10 Eureka 18 Oaklando 20 Seattles 21 Boises

A queve that gets the next node based on some function of the node (like its g-value) is called a priority queve. The instantiation of the master SERRCH algorithm whose container is a priority queve prioritized by g-value is called Uniform Cost Search (UCS).

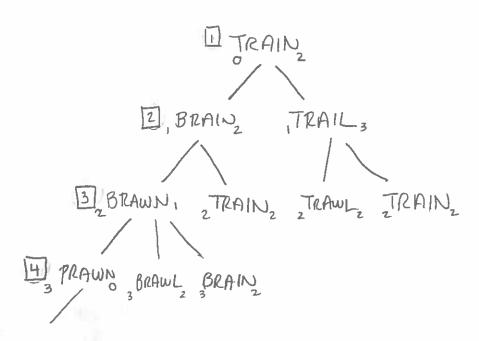
Well if the bonching of the Uniform Cost factor is finite.

UCS is guaranteed to find the optimal solution for any state machine because of the following property: if node n_1 is visited before node n_2 , then $g(n_1) \leq g(n_2)$

25) We could alternatively use a stack as our container. Stacks are "last in, first out," so we get the following behavior:

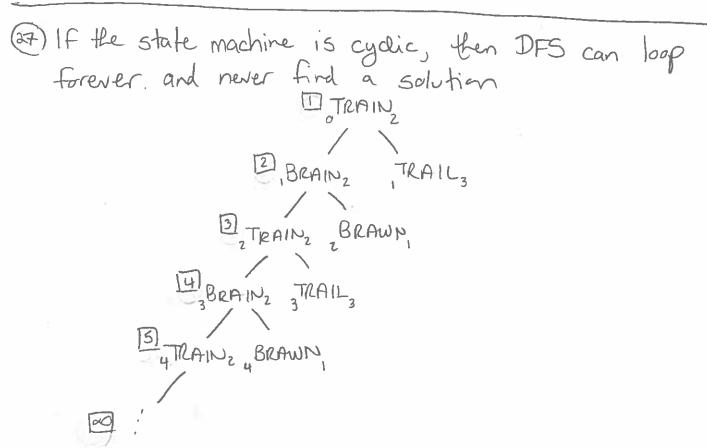
```
Confouner
put <TEAIN,0,27
                         \ <TRAIN_0, 2>
get <TRAIN, 0, 2>
put {< BRAIN, 1, 27
                         . < BRAIN, 1, 2> < TRAIL, 1, 3>
     (< TRAIL, 1,3>
get < BRAIN, 1, 2>
                          <TRAIL, 1,3>
put ( < BRAWN, Z, 1>
                         1 < BRAWN, 2, 17 < TRAIN, 2, 27 < TRAIL, 1, 3>
     < TRAIN, 2,2>
get < BRAWN, 2, 1>
                         1<TRAIN, 2, 2><TRAIL, 1, 3>
put (<PRAWN, 3,0>
                           < PRAWN, 3,0 > < BRAWL, 3,2> < BRAIN, 3,2> < TRAIN, 2,2 > < TRAIL, 1,3:
      < BRAWL, 3, 27
< BRAIN, 3, 27
get <PRAWN, 3,0>
                            etc.
```

26) This time, if we look at the search tree we process states in a different order:

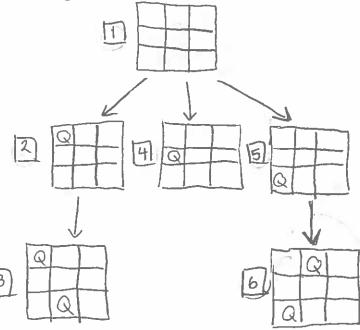


We dive headlong down a single path until we reach a final state or a dead-end (a state with no transition). If we hit a dead-end, we backtrack to the closest unvisited "cousin".

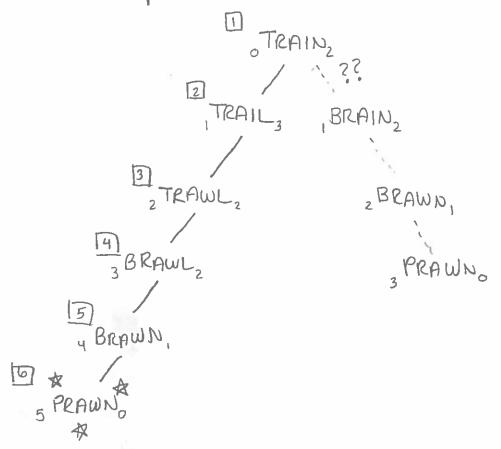
This instantiation of the moster SEARCH algorithm is called depth-first search (DFS)



(38) However it will terminate eventually if the state machine is acyclic (and finite state).

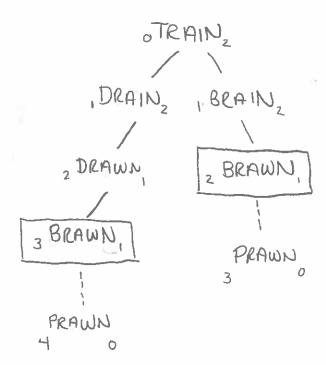


(29) But DFS is not guaranteed (even with uniform weights) to find an optimal solution:



(30) Here's a techniques:	summary of 5	o-called "uninformed search"
V	container	finds optimal solution?
BFS	queve	yes (with uniform weights)
DF5	Stack	no
UCS	priority queue prioritized by g-value	yes .

(31) One optimization of the master SEARCH algorithm is to record states that have already been processed. The observation is: no matter how we reached a particular search node, the optimal search path from its state to a final state is the same as any other search node with the same state:



32) So if we don't find a goal node after visiting the state once, it won't help to visit it again.

(33) This suggests a slightly more sophisticated version of master SEARCH algorithm, which "memoizes" (records) the states it has already visited:

MEMOIZED SEARCH (M=(Q, E, D, go, F, w), H): container = new Container () container. put (< 90, 0, H(90)>) Visited = {3 repeat: if container. empty () return 00 n = container. get() if q(n) EF return g(n) VISIT (n, container, [visited], M, H) VISIT (n, container, visited, M, H): if n & visited: visited add (n) for n' in successors M, H (n):

container put (n')

We do, however, need to be a bit careful with this optimization, as it may affect optimality of certain algorithms (as we will see). However, the optimality of BFS and UCS are unaffected by this optimization.